# Interactive comment on "Modal dynamics of structures with bladed isotropic rotors and its complexity for 2-bladed rotors" by Morten Hartvig Hansen 

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Thanks for the many good comments and questions. I have answered them below and I have also uploaded a PDF with a latexdiff of the original submission and the suggested final submission.
${ }^{*}$ ) First, I think the article is a bit verbosely written at some parts. Some sentences are too long and it would be easier for the reader if sentences are shorter. For example, the last sentences in the abstract has over 60 words. From a readability point of view this is too much. There are other examples in the article where readability could be improved (for example, first sentence in 4.4. is also rather long). I think going over it one more time focusing on that will help.

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I agree and I have made changes to the abstract and gone through the manuscript with that in mind.
*) First sentence on page 2: Here the author could be more precise. For readers not fully familiar with the transformation of the modes onto the fixed frame it would be helpful pointing out that each SET of modes of the individual blades (e.g., flapwise, edgewise, etc) is transferred to symmetric, (anti-symmetric), regressive and progressive modes.

I agree and I have changed the sentence to: "The rotor modes of the 3-bladed isotropic rotor consist of a symmetric mode and two whirling modes for each blade mode (e.g. edgewise/flapwise bending and torsion). In the whirling modes, the order of blade vibration describes a backward (regressive) and a forward (progressive) whirling direction relative to the rotor rotation."
*) End of section 2.1 a bit more physical insight could be given on the individual meaning of the matrices to guide the reader through the derivations a bit better.
I recognize that a newcomer to structural modelling of rotary systems Section 2.1 may be a mouthful, but due to space issues I have shortened the section to an absolute minimum.
*) It is probably worth having on or two sentences on the Largrangian modelling approach, which will help starting section 2.1 from a readability point of view.
I originally had half a page more on the Lagrange equation and its linearization, but I shortened the text due to space issues. Instead I included a reference to a text book on the matter.
*) The Model Assurance Criterion at the end of Section 3.2 could be explained shortly or referenced.

I have added a reference to Allemang, R. J. (2003). The modal assurance criterion Twenty years of use and abuse. Sound and Vibration, 37(8), 14-23.
${ }^{*}$ ) To be honest it took me quite some time to understand figure 5-15. Specifically I got confused with the numbering of the modes 2-12 and how they relate to diagram 4. I think it is not straightforward to the reader that if the modal amplitude in on mode is the highest, it gets named after that mode and ends up as name tag in Figure 4. Probably a table would help here.

I totally agree and I have removed the reference to mode numbers, which did not make sense.
*) How is the mentioned naming decided on, as some modes change their highest contribution in the periodic eigen-vector (as in Figure 8).
Yes, the modes may have mode shape cross-overs as for the symmetric flap and FW flap in Figures 8 and 9. I have changed the introduction of this procedure to "The naming of the modes shown in Figure 4 is deduced from the harmonic components that dominate the periodic mode shapes observed in Figures 5-15 across a large part of the rotor speed range".
*) Can the scaling factor of 10 for the drive train be physically be motivated?
The scaling of tower top translations and drivetrain rotation angles is done to highly these components which can be considerably smaller than the blade deflections. I have changed the related text to "The generator rotation and shaft torsion angles are multiplied by 10 for better scaling of these small angles compared to blade deflections. Scaling of the tower translations are also applied to show weak couplings for some modes."
*) The author mentions a threshold of $10 \%$ when a component of the eigenvector is plotted/considered or not. However this might change with rotor speed. How is this handled?
I have changed the text introducing the threshold to: "Only amplitudes higher than 10 \% of the overall maximum amplitude across all rotor speeds are plotted."
${ }^{*}$ ) In the result section I do not understand why actually $\mathrm{N}=3$ has chosen for the three bladed rotor if the 3rd harmonics seems to be close to 0 anyway. Further, for the 2 bladed rotor the decrease is linear (in the log scale), so it is not immediately obvious why $\mathrm{N}=7$ is chosen and not 9 or 5 or something else. I really like the figure and the discussion in 4.3. as it explains why the Coleman works that well for a three bladed rotor (dominance of the $\mathrm{N}=1$ term).

You are right. I have tried to mathematically prove that the third harmonic terms of the system matrix of an isotropic 3-bladed rotor are identical zero, but it requires that one looks deeply into the generic nature of the second order matrices (mass, gyro and stiffness). I will leave it open for later work or let others prove it.

I have truncated the Fourier series of the system matrix for the 2-bladed turbine at $\mathrm{N}=7$ after looking at the modal solutions for other N values. I have not included this convergence study in the manuscript due to space issues. There are no significant improvement for $\mathrm{N}=9$, but $\mathrm{N}=5$ there is a small change in modal solutions.
*) Figure 16 and Line 11 on p 26: "The tower fore-aft mode in Figure 16 couples again with $1 / \mathrm{rev}$ asymmetric rotor modes: : :." Shouldn't that be a coupling of DoFs, as a mode per definition is decoupled (orthogonal) from all the other modes?!
You are right. I have changed the sentence to "The tower fore-aft mode in Figure 16 couples again with $\$ \backslash \mathrm{pm} \$ 1 / \mathrm{rev}$ asymmetric rotor motion as for the 3-bladed turbine" and looked for similar issues in the manuscript.
*) I really enjoyed reading section 4.6. Probably a bit more weight can be put on this outcome as I think it is a major contribution and handles some misunderstandings in common literature.
I agree. I am planning to submit a paper only on the difference of two and three bladed turbines in the near future. This paper is meant as an introduction of the theories.
*) From my experience (and from the results in the paper) the Coleman transformation
works pretty well when the rotors are isotropic, so it would be interesting to see - and add value to the approach - what happens if applied to higher level of anti-isomorphic characteristics for a 3-bladed rotor, for example on the blades (however this might be future work).

I agree, but I will leave that important topic for the next paper.
*) Typos: Page 3, Line 10: I think it should be "can be used to decompose" instead of "decomposed" Page 9, Line 2: "with more than two" instead of "mode than two"

Thanks. I have made the corrections.

Please also note the supplement to this comment:
http://www.wind-energ-sci-discuss.net/wes-2016-27/wes-2016-27-AC2-
supplement.pdf
Interactive comment on Wind Energ. Sci. Discuss., doi:10.5194/wes-2016-27, 2016.

