Interactive comment on “Adaptive stratified importance sampling: hybridization of extrapolation and importance sampling Monte Carlo methods for estimation of wind turbine extreme loads” by Peter Graf et al.

Anonymous Referee #2

Received and published: 28 August 2017

General comments

The authors have presented a very interesting idea for efficiently improving the estimates of 50-year extreme loads for wind turbines. Most attractive about the method is its overall simplicity, using the well known concept of importance sampling and deriving a simple gradient for the variance of the extrapolation estimate that can be used to add the required number of additional samples for each wind bin, in order to reduce the variance of the estimate to an acceptable level. With a few exceptions, to be noted below, the presentation of both background details and the method is clearly written. The results seem to show that the method works quite well, without having to run the optimization for a prohibitively long time. However, there is one aspect of the setup of the problem that obscures the true meaning of the results, again to be expanded on below. Unless this can be clarified, interpretation of the results is difficult. As a preliminary demonstration of the approach, and assuming they hold up to scrutiny, these results are promising and the method could be of use both in conventional assessments of the 50-year extreme load and also in other settings like reliability assessments. It is also nice to see that the authors are open and critical about the overall power of the method and they make some interesting points about the limits of the current analysis framework and suggestions for other ways to improve extreme value analysis for wind turbines.

Specific comments

Introduction:

On page 2, lines 14-15 you write: "... reliable extrapolation of nonlinear physics under uncertain forcing is extremely problematic, especially without knowledge of the form (e.g. quadratic) of the nonlinearity." This is certainly true, but an equally important reason why the specific type of long-term extrapolation usually done for the evaluation of 50-year extreme loads is problematic is precisely the large differences in timescale between the data and the extrapolated estimate. This impacts the problem in many ways, certainly also through the nonlinearity you mention, but in a more practical sense this large difference in timescales means that any uncertainty in the data is necessarily magnified by the extrapolation. Small errors in the short term data set could potentially lead a designer to significantly over- or underestimate the long-term extreme loads. Later in the paper you show that there can be a large variance in the extrapolation, which is in turn reduced by your proposed method, so this overall point should be mentioned here.

Section 2.2, Extrapolation:
On page 4, line 2 you write: “In this paper we use a 3 parameter Weibull distribution.” Why this distribution? This choice may be seemingly irrelevant, but some reason for the choice would be instructive for the reader. One might wonder, for example, if this is indeed the distribution that overall gives the best fit for your data and is therefore the easiest to use for illustrating the method. Certainly, the Gumbel distribution, for instance, can be easier to work with (since it has only 2 parameters), so it seems there must be some motivation for choosing the Weibull. For reasons of clarity and reproducibility, it would also be of interest to know what method you used to fit the distributions to your data. Maximum likelihood estimation perhaps? Please state this.

On page 4, line 29 you write: “To gather peaks, we take the maximum of each 1 minute segment in our simulations.” Yet, you already stated on lines 17-20: “Finally, there is the length of time between independent peaks...” values as low as 4 seconds have been justified in previous studies (Ragan and Manuel, 2008), and 10 seconds seems to be more than adequate.” So why this choice of 1 minute separations? Based on what you write later in the paper it seems to be motivated by a desire to only use the largest peaks, hence using smaller separations would yield maxima that might not give a good description of the extreme behavior of the system. If this is the case, or if there is some other motivation, it would be instructive to have it stated clearly here. To be very precise, given that one wants a number of peaks that exactly divides the total simulation length, why not a 30 second separation, which would give twice the number of maxima and hence more data per simulation with which to fit the distributions while maintaining 3 times the required separation to maintain independence of the peaks?

Section 3.2, ASIS as stochastic optimization:
As a more general point, it is clear from the fact that the variance is what is being minimized, as well as studying equation (21) and from the algorithm summary on page 10, that the procedure is only ever going to add samples to the various bins, never remove samples. However, viewed as a more general optimization problem, an unattentive reader could believe that such an algorithm might in fact reduce the number of samples in a bin. Perhaps this “uni-directionality” of the algorithm should be stated more clearly to avoid any possible confusion over what its purpose is.

On page 10, lines 11-12 you write: “Also, the $N_i$ need to be integers, which is accomplished by rounding. The resulting error is likely subsumed into the general convergence of the stochastic optimization procedure.” This statement needs a more convincing justification. For a k-dimensional optimization problem, which for a discrete solution set induces a k-dimensional lattice of discrete points, it is not immediately clear that a local minimum in the continuous case is also a local minimum in the discrete case. That is, when going from some continuous set of $N_i$ (a point in $k$-space) to a discrete set of $N_i$ (a point on the $k$-lattice) by rounding each $N_i$ to the nearest integer, the corresponding function value is not necessarily lower than at neighboring points on the lattice. If such a correspondence between minima in continuous and discrete space can be established for this particular case, it needs to be justified by specific arguments or at least by reference to another work.

On page 10, line 18 you write: “In fact we have to decide some number of “large peaks” we will use to evolve $N$.” Why? Presumably you already have all the information from the extrapolation that has already been performed before estimating the gradient. So why must the gradient only be estimated from some limited number of large peaks? The motivation for this is certainly not clear from the text.

Section 4, Results:
To demonstrate the method, you set up a problem where you seek the ideal number of peaks, $M_{pks}$, to use for the fitting. However, it is unclear how this variable relates to the extrapolation procedure already described. Initially, you have used 10 maxima, 1 per minute of simulation time, for each wind speed bin. Is it this number of 10 maxima which is now a variable? If so, how is this actually accommodated in the extrapolation? For example, in Figure 2 you show the extrapolation for many different values of $M_{pks}$. 
How do you get the additional peaks? Do you perform another T minutes of simulation corresponding to the number of additional peaks needed? Or do you decrease the separation time between maxima and hence extract more maxima from the simulation data you already have? If the former, do you perform specifically the required amount of simulation time for each case or do you perform enough simulations for all the different values of \( M_{pk} \) you have used and then simply use the 5, 10, 20, 40 etc largest peaks from this expanded set of potential maxima? These different ways of solving the problem have very different statistics and therefore different implications for the extrapolation itself. Using the largest 20 maxima from 160 minutes of simulation time is very different from using 20 maxima from 20 minutes, which is very different from using the 20 largest maxima from 10 minutes and so on. In fact, depending on which of these approaches is used, it is not clear whether the results are truly meaningful. Nor is it clear how the number of maxima used might or might not interact with the number of samples in each bin as dictated by the ASIS optimization procedure.

More details about the optimization are needed in order to ensure that the results are clear and reproducible. For example, the criteria for termination of the algorithm are unclear.

**Technical corrections**

- Section 2.2, page 4, line 2: "In this paper we use a 3 parameter Wiebull distribution." Should be "Weibull"
- Section 3.1, page 8, equation (12): \( Y(x) \) should be \( Y(x_i) \)
- Section 3.1, page 8, lines 14-15: "Here we denote the dataset as \( \{Y_{i,k}\} \) where \( i \) indexes over wind speed bins and \( k \) indexes over the peaks we have extracted at that wind speed." This repeats almost exactly information already given in Section 2.2, page 3, lines 30-31. Consider removing (since we are already aware of the notation) or rephrasing.
- Section 4, page 11, Figure 2, caption: "... (a lower values... " should be "value"

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