

Dear Anonymous Referee #1,

Thank you very much for your comments. I modified the manuscript as follows:

– RC: *Please comment and discuss on followings to clarify the implementation of the resolved gust approach in an incompressible solver:*

5 1. RC: *Loss-free transport of gust velocity through the flow field may require the free-stream velocity update not only on inflow boundary but on other far boundaries (top and sides) as well, or actually whole domain if necessary. How are the slip-condition velocities (or freestream conditions changing on these far boundaries? Gust model is changing inflow velocity i.e., freestream, and inflow velocity will effect all boundaries. Please clarify.* AC: The velocities on the slip-walls changes in the same way as the velocities in the whole domain. Due to the way, the implementation is performed in THETA, this happens without any user-interaction or additional user-implementation. A hint is given in section 4.1, page 7, line 18

10 2. RC: *And no-slip condition on the bottom boundary will result in somehow development of a Boundary Layer (BL) in the unsteady solution. Is there any development and effect of this BL on the tower and rotor, or flow field? Please clarify.* AC: Yes, I should have mentioned that the developing boundary layer has no effect on the HAWT performance because it remains below 1m in the entire flow domain. I will add a comment in section 5.1, page 9, line 25.

15 – RC: *Discussing clearly all the assumptions and difficulties encountered in such expensive unsteady computations will be helpful for future studies.* AC: I added the following sentences to the conclusion (section 6, page 18) "The assumptions, which are made in the paper can be summarized as

- 20 1. the wind speed is constant in height and time (except gust velocity)
 2. the gust velocity is constant in height
 3. the gust transport velocity is equal to speed of sound which is infinite
 4. the boundary conditions of the flow domain are chosen to prevent the flow from escaping sideways.

25 The disadvantage of the resolved-gust approach clearly is the requirement of fine time steps and fine grids upstream of the geometry in question which increases the computational costs. The infinite speed of sound and its direct relation to the gust transport velocity is ambivalent. It leads to an inaccurate reproduction of the wind turbine wake transport on the one hand, while on the other hand, the response of the rotor loading to the gust velocity is immediately obtained. Clear advantages fo the resolved-gust approach are numerical stability and no artificial oscillations. Finally, the resolved-gust approach can be applied to any completed wind turbine U-RANS computation to obtain more insight of the wind turbine characteristics." Please also referre to the response to Referee #2, last point.

- 30 – Furthermore, I found some typos which were corrected.
 – I deleted the sentence "The floor is defined as viscous wall." on page 6 as the information was given repeatedly in the paragraph.

Dear Dear Anonymous Referee #2,

thank you very much for your hints to improve the revised version of my paper. I updated the manuscript as follows:

- RC: *The paper has been improved since the original review, there are though a few points I would suggest to address before the final acceptance.* AC: Thank you
- 5 – RC: *Page 4, line 20: 'low dissipation' is mentioned twice.* AC: Please read carefully. It is low dissipation low dispersion
- RC: *Grid resolution: The comment for the coarse grid still stands, the NREL Phase-VI investigation do not feature any grid dependency study. The fact that the results agree well with measured value do not guarantee grid independence. Additionally, the differencing scheme test in the referred paper is done at high AOA where cancelling errors might obscure the question. Comparing directly the C_p distributions, there are clear visual differences.* AC: Yes, a true grid
10 independence study has not been performed, yet. In the referenced paper, the high AOA has been chosen because it was the only test case that showed differences between the measurement and computation. In attached flow regions, even the result which were obtained with the first order upwind scheme matched the experiment perfectly (not shown in the referenced paper). Hence, the only possibility to show a difference between the schemes was in the partly separated flow
15 region where a the difference between the second and third order schemes were small. I propose to add the performance of a grid independency study of the test case to the to-do-list in the conclusion of the paper (section 9, page 19, line 2).
- RC: *Is the reference used for FAST correct, I would imagine that an older one exists?* AC: I updated the reference to an older version of 2013 even though I am using a the latest FAST version which includes the updates of 2015.
- RC: *Page 6: I do not think that a standard engineering viscous wall resolved condition will allow you to model atmospheric rough wall flow with roughness length 0.1 m and larger. Here typically Monin-Obukhov theory must be used.* AC: I think that there is a small misunderstanding. Monin-Obukhov theory is used for non-neutral conditions and if the
20 atmospheric boundary layer is actually resolved. I rather envisaged prescribing the neutral atmospheric boundary layer by logarithmic profiles than having a RANs solver resolving atmospheric flows. I reformulated the sentence on page 6 to clarify my point.
- RC: *Page 8, line 12: 't the computational time'. I would suggest to say: 't is the physical time simulated'* AC: Yes you
25 are right. Thank you for the hint.
- RC: *Page 12: There are basically no description on the turbine setup in the FAST model, is this based on the reference manual including airfoil data and more of Jonkman. Is the model including a Dynamic Inflow model, dynamic stall model So even though we see good comparisons, we do not know what we are comparing against.* AC: Of course it
30 is as much of Jonkman and the reference manual as possible. Everything that is not is already mentioned in section 2.2. I added the above information together with the parameter choices that you explicitly asked for to section 2.2.
- RC: *Why are there no thrust force shown for the FAST simulations in Figure 5?* AC: As the thrust does not add anything new to the discussion it is omitted to display it to keep a clear appearance of the figure.
- RC: *Page 14: It seems that the skin-friction (C_f) shown is basically the absolute value of the skin friction. I would suggest showing the C_f with a sign, easily indicating where separation is present. Additionally, the scaling of both the
35 C_p and C_f are not optimal for visual inspection.* AC: Yes, it is the absolute value of the skin-friction coefficient vector because in the present case no component of the 3D vector has had a dominant part that could be shown. Inversely, neglecting components of the C_f vector would have led to misunderstandings in the results interpretation. The same holds for showing all components next to each other in both separate or the same plots. It would have become a mess in presentation. Thus, in my opinion the best way is to show the absolute friction force coefficient.
40 The differences between the scaling of figures 8 to 10 results from the very different magnitudes in both c_p and c_f . For all other issues about scaling, I would be glad if the reviewer would share his/her ideas more precisely.

- RC: *Page 18: Line 25: I would suggest removing the word ‘perfect’ and ‘exactly’* AC: I changed perfect to ‘very well’ and exactly to ‘very close’.
- 5 – RC: *Page 18: It would maybe also be appropriate to discuss whether the gain in details over the engineering modelling is worth the additional computational effort.* AC: Well, it is a three-stage process whereof the presented URANS computation is one of multiple contributions to the first stage. In the first stage, it is aimed for gaining more detailed knowledge about the behaviour of wind turbines during extreme gust events. This needs further computations of different modelling approaches and test conditions. In a second step, the engineering models can be adjusted to better predict the wind turbine behaviour during the design process. Consequently, the potential of weight reduction (and thus costs) and same reliability in wind turbine designs can be shown. I added this argument at the very end of my conclusion (section 6, page 10 19). Please also refer to the response to Referee #1, last point.
- Furthermore, I found some typos which were corrected.
- I deleted the sentence "The floor is defined as viscous wall." on page 6 as the information was given repeatedly in the paragraph.

Simulation of transient gusts on the NREL5 MW wind turbine using the U-RANS-solver THETA

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Abstract. A procedure to propagate longitudinal transient gusts through a flow field by using the resolved-gust approach is implemented in the U-RANS solver THETA. Both, the gust strike of a $1 - \cos()$ -gust and an extreme operating gust following the IEC 61400-1 standard are investigated on the generic NREL 5 MW wind turbine at rated operating conditions. The impact of both gusts on pressure distributions, rotor thrust, rotor torque, and flow states on the blade are examined and quantified. The flow states on the rotor blade before the gust strike, at maximum and minimum gust velocity are compared. An increased blade loading is detectable in the pressure coefficients and integrated blade loads. The friction force coefficients indicate the dynamic separation and re-attachment of the flow during the gust. Moreover, a validation of the method is performed by comparing the rotor torque during the extreme operating gust to results of FAST rotor code.

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1 Introduction

The origins of applying Computational Fluid Dynamics (CFD) to wind turbine rotors date back to the 1990th when ? applied EllipSys3D to a wind turbine. ? solved the Reynolds Averaged Navier-Stokes (RANS) equations and applied the Menter SST $k - \omega$ -turbulence model to a full scale wind turbine. In 2002 the National Renewable Energy Laboratory (NREL) performed an Unsteady Aerodynamic Experiment (UAE) (?) which has long been the reference for several CFD computations. For example, ? presented a Detached Eddy Simulation (DES) on the NREL UAE phase VI blade to demonstrate the capabilities of predicting flow separation. ? developed a delayed DES to investigate whether the simulation approach could be improved. Furthermore, the experiment has been widely used for U-RANS solver validation for example by ??????.
? developed the generic NREL 5 MW wind turbine. Through its open access documentation, the NREL 5 MW wind turbine is established as reference and validation test case for single- and multi physic test cases. For example, ? focused on the prediction of aerodynamic features of the wind turbine. Furthermore, they investigated the impact of fences on the flow separation in the inboard region. Full aero-elastic computations were performed by ? for an isolated rotor and ? respecting also the tower

and nacelle. ? and ? modelled the aerodynamics with an U-RANS method and the structure with shell elements. The structure properties represented the material properties of the blade. The resulting aerodynamic characteristics and blade tip deflections were good when compared to the NREL 5 MW documentation and FAST.

In the past years, the growing computer power enabled the geometry resolved simulation of wind turbines including the sites with Computational Fluid Dynamics (CFD). Studies have been performed for example by ? or ? who used an Unsteady Reynolds-Averaged Navier Stokes (U-RANS) solver to perform according studies. Moreover, hybrid Large Eddy Simulation(LES)-RANS approaches are implemented to analyse the behaviour of wind turbines in a complex terrain as for example presented by ? who also considered the unsteady atmospheric inflow conditions.

The challenges of correctly predicting uncertainty of the fluctuating wind loads is a research field on its own. For example, ? or ? investigated wind fields to better understand the shape of wind gusts. ? argued that a detailed understanding of wind fields is not necessary. Matthäus et al. rather respected unknowns of all parts of the wind turbine life cycle as for example changes in the blade shape due to production tolerances, ageing, or the wind field and summarized them in uncertainty parameters to estimate the effective power outcome and rotor loads. ? proved that turbulent wind fields are not distributed Gaussian as assumed in the International Electrotechnical Commission Standard (?). A similar conclusion was drawn by ? who investigated whether the 50 year loads as defined in the ? adequately fulfil their purpose by applying different approaches of probability prediction to the generic NREL 5 MW turbine using the FAST rotor code.

The aerodynamic interferences between the unsteady wind conditions and wind turbines are of major importance for the prediction of fatigue loads and the annual power production. Therefore, it is part of the certification computation for each wind turbine. Nevertheless, the detailed investigation of isolated effects as the 50 year Extreme Operating Gust (EOG) on the flow of a wind turbine using high fidelity methods as CFD is rare even though the blade loads resulting from the extreme load cases are dimensioning load cases. In the case of vertical axis wind turbines ? analysed the power loss of a wind turbine subjected to a sinusoidal fluctuation in wind speed. However, compared to the EOG amplitudes were small. Horizontal axis wind turbines which are hit by an EOG as defined in the ? were presented by ?. The wind turbine under consideration was the NREL phase VI rotor with a wind speed of 7 m/s using the panel code AeroSIM+. The impact of the gust was then evaluated in terms of rotor thrust, torque and wake development. Preceding this study, ? examined the flap moment of wind turbine blades which were subjected to a gust with extreme raise, using the wind turbine design tool Bladed. Bladed is an aero-elastic software by Garrad Hassan for the industrial design and certification of wind turbines (?). Other examples of aero-elastic simulation tools for wind turbine design are HAWC2 (?) or FAST (?) which all include at least a blade element momentum (BEM) method to represent the aerodynamics, a multi-body dynamics formulation to represent the structure, and an algorithm for rotational speed control. All three of them provide a possibility to compute EOG cases fully-multidisciplinary on the basis of linearized aerodynamic and structure models.

Even though the literature on gust simulations on wind turbines is rare, some research has been conducted in the field of aerospace science. ? and ? presented two approaches which are implemented in the U-RANS solver TAU (?) to apply vertical gusts on airplanes: the velocity-disturbance approach and the resolved-gust approach. The velocity-disturbance approach adds the gust velocity to the surface of the investigated geometry. It enables the analysis of the resulting forces on the geometry

surface but prevents the feedback of the structure response on the flow field and the gust shape. The resolved-gust approach overcomes the disadvantages of the one-way interaction in the velocity disturbance approach by propagating the gust through the flow field with the speed of sound. But it ignores that the gust transport-velocity usually differs from the speed of sound. The validity of both implementations was demonstrated by the time history of the position of the centre of gravity, pitch angles and load factors necessary for keeping the flight path of an aircraft constant.

In the so-called field approach ? added the gust velocity to the grid velocity of the computational grid to all cells with

$$x \leq u \cdot t \tag{1}$$

wherein x is the coordinate in flow direction, u the gust transport velocity and t the physical time. This approach allows the definition of a gust transport-velocity and the analysis of the two-way interaction between gust, structure, and wake. Nevertheless, it requires a severe manipulation of the velocity field regardless of the flow solution that is produced by the wind turbine. The simulation of unsteady inflow conditions of wind turbines in CFD implies several challenges: The simulation of a wind turbine including the tower is, itself, an in-stationary problem which needs the computation of several rotations to obtain a periodic solution. Superposed by sheared inflow profiles and in-stationary (stochastic) inflow conditions, periodicity can never be gained because the same flow state never occurs twice. Moreover, a computation in which the rotor motion is adapted to the actual rotor forces using a strong coupling approach as proposed by ? should be included in the computation. By using strong coupling between the U-RANS solver Fluent and a pitch control algorithm for the rotor-motion Sobotta has been able to implement a simulation-procedure of turbine start-up. ? performed the computation of an emergency shut-down of a turbine by using the incompressible U-RANS solver EllypSys3D and by neglecting the tower throughout the aerodynamic computations. Additionally, ? considered the rotor mass and inertia by coupling of the U-RANS solver with the aeroelastic code HAWC2. The validation of the resolved-gust approach in the DLR U-RANS solver THETA (??) is presented herein. To reduce the complexity of the problem and emphasize the quality of the resolved gust approach, the NREL 5 MW wind turbine is chosen to operate in shear-free conditions. Moreover, the possible interferences with the structure response and speed controllers are reduced by using infinite rotor mass and inertia. Speed control algorithms are also neglected. As gust, a $1 - \cos()$ shaped gust which lasts about 7 s and the EOG following the ? standard are chosen. As results rotor thrust and rotor torque, pressure distributions, friction force coefficients and the wake-vortex transport are evaluated. The rotor torque during the EOG is validated against FAST.

2 Numerical methods

2.1 Flow solver THETA

DLR's flow solver THETA is a finite volume method which solves the incompressible Navier-Stokes (NS) equation on unstructured grids. The grids can contain a mix of tetrahedrons, prisms, pyramids and hexagons. The transport equations are formulated on dual cells, which are constructed around each point of the primary grid. Therefore, the method is cell-centred with respect to the dual grid. The transport equations are solved sequentially and implicitly. The Poisson equation which links

velocity and pressure is either solved by the SIMPLE algorithm for stationary problems or the projection method for unsteady simulations. With the projection method the momentum equations are first solved with an approximated pressure field. The pressure field then is corrected with a Poisson equation to fulfil continuity. Pressure stabilization is used to avoid spurious oscillations caused by the collocated variable arrangement.

5 The technique of overlapping grids (Chimera) is used to couple fixed and moving grid blocks. The method was developed by ? for structured grids or ? for unstructured grids for the application in incompressible flow problems. It has been implemented to THETA by ?. The interpolation between the different blocks at interior boundaries is integrated in the system of linear equations on all grid levels of the multi-grid solver leading to an implicit formulation across the blocks. This procedure was identified to be crucial for achieving fast convergence of the Poisson equation.

10 Implicit time-discretization schemes of first order (implicit Euler) or second order (Crank Nicolson, BDF) are implemented. The temporal schemes are global time stepping schemes. A variety of schemes from first order upwind up to second order linear or quadratic upwind or a central scheme and the low dissipation, low dispersion scheme (?) are implemented. Throughout this study, the second order central scheme is used.

The THETA code provides a user interface for setting complex initial and boundary conditions using the related C functions.

15 This guarantees a high flexibility on the definition of boundary conditions and a straightforward modelling of very specific test cases. For example, the functions enable the prescription of gusts at the inflow boundary condition which are then propagated through the flow field. Moreover, all physical models are separated from the basis code. Therefore, new physical models can be implemented without modification of the base code.

For turbulence modelling the commonly used Spalart-Allmaras, $k - \epsilon$, $k - \omega$ or Menter-SST models are available. Since the
20 early U-RANS computations of wind turbines the Menter-SST turbulence model is used (?) for wind turbine applications. Recently, ? confirmed this finding during the THETA validation by comparing the results of common one- and two equation turbulence models to the NREL UAE phase VI experiment. Hence, the Menter-SST turbulence model is applied throughout the present study. Moreover, according to the studies in ? a time step of $\delta t = 0.006887052s$ which is equivalent to a rotor advance of $\Psi = 0.5^\circ$ per time step is chosen. As time stepping scheme, the Eulerian implicit scheme for the temporal discretization is
25 chosen. To ensure convergence in every time step, a residual of less than 10^{-5} has to be reached. Moreover, the solver has to perform at least 20 iterations per time step in all equations. Due to efficiency reasons, the maximum number of iterations per time step has been limited to 100.

2.2 FAST

The comprehensive rotor code FAST (~~Sprague et al., 2015~~) (?) is a modular software framework for computer aided engineering (CAE) of wind turbines. FAST provides a coupling procedure to compute time-dependent multi-physics relevant for wind
30 turbine design. By the means of different modules, FAST is able to respect different physical models and turbine components in the computations. The aerodynamics are represented by a blade element momentum method (BEM) which is based on profile polars for drag, lift and momentum.

In the present case, - most parameters remained on the default of NREL's v8.16.00a version for both FAST and the NREL

5 MW wind turbine. Few parameters had to be adjusted. As there are: the variable-speed control has been turned off to ensure a constant rotational speed as in the U-RANS computation. The blade stiffness has been increased to the order of 10^{29} Nm² per blade element to obtain a stiff blade. To ensure a shear-free inflow profile, the constant wind profile type without dynamic inflow model was selected. In FAST, the EOG started after the computation of 8 s. The analytical inflow profile was included
5 as x -velocity in the IECWind file. The other wind directions were equal to 0.

3 Geometry

3.1 NREL 5 MW wind turbine

The NREL 5 MW turbine (?) is a three bladed wind turbine with a rotor radius of 63.0 m and a hub height of 90 m. The rotor has a cut-in wind speed of $v_{ci} = 3$ m/s and a rated wind speed of $v_{rated} = 11.4$ m/s. Cut-in and rated rotational speeds are
10 $\omega_{ci} = 41.4^\circ/\text{s}$ and $\omega_{rated} = 72.6^\circ/\text{s}$, respectively. The blades are pre-coned and the rotor plane is tilted about $\beta = 5.0^\circ$ and not yawed. Along the non-linearly twisted blade 7 different open-access profiles are used.

Due to the narrow gap between rotor and nacelle a valid chimera overlap-region could not be achieved in that region. Thus the nacelle of the NREL 5 MW turbine is neglected while the tower is respected. This approach leads to an error in the flow prediction behind the rotor hub but is supposed to have no impact on the blade loads.

15 The gust simulation is based on the rated wind speed $v_{rated} = 11.4$ m/s. Air density of $\rho = 1.225$ kg/m³ and the kinematic viscosity of $\nu = 1.82 \cdot 10^{-5}$ m²/s is used. To isolate the gust impact of the rotor loads, a shear-free velocity profile is considered throughout the computation.

3.2 Grid characteristics

The computational grid consists of 3 parts. The first part contains the three rotor blades, stubs and the rotor hub. On the
20 blade surface, a structured grid with 156×189 elements in span-wise and chord-wise direction was generated. The boundary layer mesh of the blades consists of 49 hexagon layers in an O-O-topology. The height of the wall-next cell is $\delta = 3 \cdot 10^{-6}$ m along the entire blade, ensuring $y^+ \leq 1$. Figure 1a) and b) give an impression of the chord-wise and span-wise grid resolution, respectively.

The second part of the grid has the shape of a disk and contains the entire rotor. The disk measures $D = 166.7$ m in diameter
25 and has a depth of 26.7 m. It is filled with tetrahedrons with an edge length between 0.002 m and 0.9 m. The entire disk is used as chimera child grid for the overlapping grid technique and contains approximately $11.63 \cdot 10^6$ points.

The chimera parent grid has the dimensions of $504 \times 504 \times 1512$ m³ in width, height, and length. It contains a boundary layer grid of the floor, the tower, and a refined grid region to resolve the rotor wake up to $3R$ downstream.

The 54 prism layers, used to resolve the boundary layer of the viscous floor, have a total height of $H = 5$ m with a wall-next
30 cell height of $\delta = 3 \cdot 10^{-5}$ m. ~~The floor is defined as viscous wall.~~ This meshing strategy enables the comparison of future gust computations that include analytically defined velocity-profiles of neutral atmospheric boundary layer flows. The tower

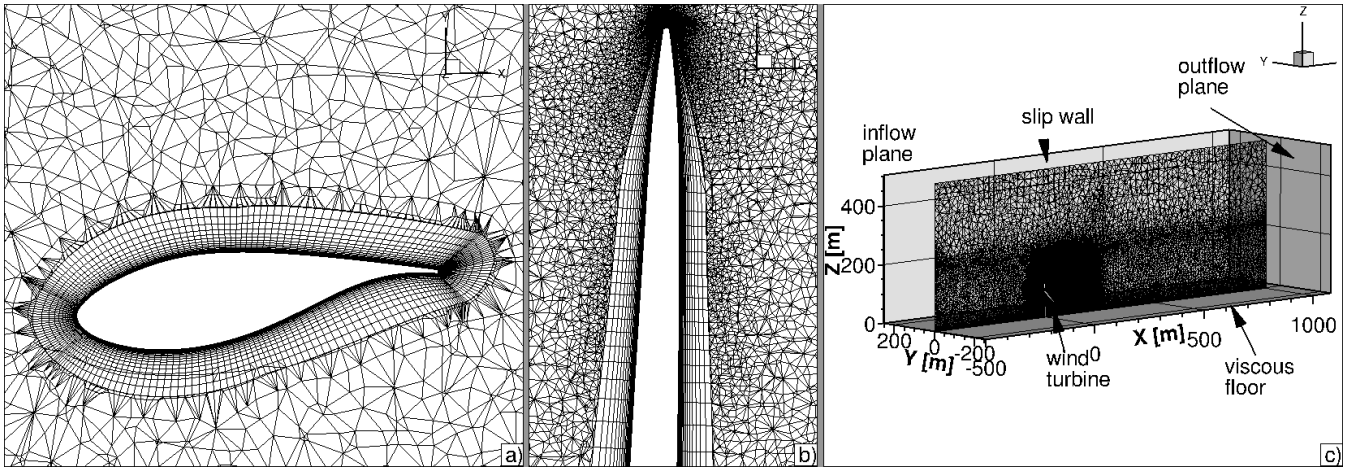


Figure 1. Computational grid setup; a) Chord wise distribution; b) span wise distribution in blade tip region; c) Cut through the flow field and boundary conditions

surface-grid is meshed structured in a height below 5 m with 54 point in height and 180 points in radial direction. Above 5 m, a triangulated unstructured grid is generated with the maximum edge length of 0.55 m. As the tower surface is modelled as slip-wall, tetrahedrons are built directly on the tower surface.

In the chimera parent grid, the edge length of the cells continuously grow from very small in the rotor-tower and wake region to rather large close to the farfield boundaries. The entire chimera parent grid contains approximately $13.25 \cdot 10^6$ points.

In figure 1c) the entire chimera setup is displayed and the boundary conditions are indicated. The upwind and downwind boundaries are defined as inflow and outflow respectively. At the inflow boundary surface, the turbulence quantities and inflow velocities are prescribed. Later, also the gust profile is introduced in this boundary. The floor is defined as viscous wall. The surfaces on top, left and right of the flow domain are defined as slip wall.

10 4 Gust modelling

4.1 The resolved-gust approach

The procedure of applying the gust to the flow field starts by computing the flow field around the wind turbine until the flow field and the global rotor loads have become periodic. For the NREL 5 MW turbine in the given setup 9 revolutions are required. Then, the inflow velocity on the inflow boundary is modified according to the velocity change described in section 4.2 or 4.3.

15 The computation is continued so that the gust is propagated through the flow field. In the approach by ? and ? using TAU (?) to solve the compressible RANS equations, the gust is transported with the speed of sound. In their approach, as well as in the present paper, the computation has been run at least until the gust has entirely passed the geometry in question but can be

continued as long as wished by the user.

The restrictions to ensure a loss-free transport of the gust velocity on the resolved-gust approach named by ? or ? are

- a fine grid upstream of the geometry in question
- a fine time step.

- 5 As THETA is an incompressible solver, the speed of sound is infinite. In addition to the strong implicit formulation and the choice of boundary conditions that prevent the flow from escaping sideways, this leads to a spread of the gust velocity through the flow field instantaneously. If the same gust velocity is added to the constant inflow condition in every point in the inflow plane and the boundary conditions are chosen as specified in section 3.2, the transport of the gust velocity will be loss-free and instantaneous through the entire domain and on the farfield boundaries. Hence, the restrictions by ? and ? concerning the
- 10 grid resolutions are obsolete while a fine time step is required to ensure numerical stability.

To analyse the resolved gust approach in the incompressible U-RANS solver THETA, the inflow velocity profile is shear-free and the gust velocity remains independent of the height above ground.

4.2 Cosines gust

The $1 - \cos()$ gust is modelled in analogy to the EASA certification standard (?) as

$$15 \quad u(t) = u_g \left(1 - \cos\left(\frac{8\pi}{H}\right) \right) \quad (2)$$

with $u(t)$ and u_g as the time dependent velocity and the gust velocity, respectively and H as gust gradient. In the work presented, H is chosen to generate a non-compressed sinusoidal gust

$$H = \frac{8\pi}{t - T_S} \quad (3)$$

- wherein t represents the actual physical time and T_S is the time at which the gust starts. Inserting equation 3 in equation 2 the
- 20 following definition of the gust results:

$$u(t) = \begin{cases} u_g(1 - \cos(t - T_S)) & \text{if } T_S \leq t < T_S + T_g \\ u & \text{if } t \leq T_S \text{ or } t \geq T_S + T_g \end{cases} \quad (4)$$

- Wherein T_g is the duration time of the gust. The gust velocity u_g is defined as +0.25 m/s representing a gust and -0.25 m/s representing a sudden calm. In both cases, the maximum change in wind speed is 0.5 m/s or 4.4 % at rated wind speed of the NREL 5 MW turbine. The turbulence intensity of the $1 - \cos()$ -gust is 2.5 % which is in the order of the atmospheric turbulence
- 25 intensity that ? found in a field measurement campaign on a horizontal wind turbine. The resulting gust profile of the present study is displayed in figure 2.

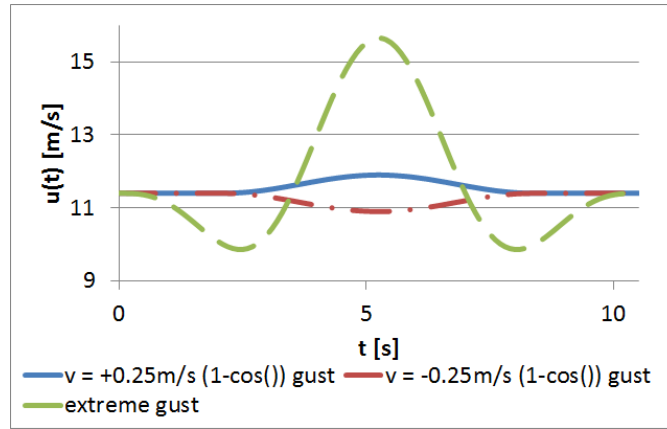


Figure 2. Inflow velocity in dependence of physical time t

4.3 Extreme operating gust

The time dependent velocity change of the EOG is modelled following the ? standard.

$$u(z, t) = u(z) - 0.37 \cdot u_g \sin\left(\frac{3\pi \cdot t}{T_g}\right) \cdot \left(1 - \cos\left(\frac{2\pi \cdot t}{T_g}\right)\right). \quad (5)$$

Wherein $T_g = 10.5$ s is the characteristic time as defined in the ?, t the physical time simulated, $u(z)$ the velocity profile depending on the height and u_g the gust velocity. The latter is defined as

$$u_g = 3.3 \left(\frac{\sigma_1}{1 + 0.1 \left(\frac{D}{\lambda_1}\right)} \right) \quad (6)$$

and is 5.74 m/s in the given case. In equation 4, $\sigma_1 = 0.11 \cdot v_{hub}$ is the standard turbulence deviation, $\lambda_1 = 42$ m the turbulence scale parameter and D the rotor diameter. u_{hub} represents the velocity at hub height. The velocity u_{e1} is the average over 10 minutes with a recurrence period of 1 year. It is defined as

$$u_{e1} = 1.12 \cdot u_{ref} \left(\frac{z}{z_{hub}} \right)^{0.11} \quad (7)$$

with the reference velocity $v_{ref} = 50$ m/s. It is defined in the ? standard for a wind turbine of the wind class A1. In a shear-free inflow, the inflow velocity is constant with height and thus $u(z)$ reduces to u and $u(z, t)$ to $u(t)$. By additionally entering equation 7 in equation 5 one obtains the final gust definition

$$u(t) = u - 0.37 \cdot u_g \sin\left(\frac{3\pi \cdot t}{T_g}\right) \cdot \left(1 - \cos\left(\frac{2\pi \cdot t}{T_g}\right)\right). \quad (8)$$

15 The resulting gust profiles of the EOG in comparison to the moderate $1 - \cos()$ -gust is visualized in figure 2.

5 Results

5.1 Constant inflow conditions

As described in section 4.1 a periodic flow field with periodic rotor loads is mandatory as starting conditions for computing gusts that act on wind turbines. The resulting time history of rotor thrust F_x and rotor torque M_x for constant inflow conditions over revolution 6 to 10 are displayed in figures 3 and 4 with the red line. In both figures the periodic behaviour of a periodic flow field is visible as well as the typical $3/rev$ -characteristic of a rotor-tower configuration of the wind turbine. By averaging rotor thrust F_x and torque M_x about 4 revolutions, one obtains 738.9 N and 4.15 MNm, respectively. Compared to the reference of ? at rated conditions the values deviate about approximately -3.77% and -0.98% , respectively. ? achieved a rotor thrust of 786 kN and a torque of 4.4 MNm in their studies with the compressible U-RANS solver TAU for the stiff-bladed NREL 5 MW turbine.

The agreement between the U-RANS computations performed with THETA, TAU and the reference documentation of the NREL 5 MW wind turbine (?) is excellent. Thus, the numerical setup is validated successfully.

Between $\Psi = 3060^\circ$ and $\Psi = 3240^\circ$, in the 8^{th} revolution, high-frequency oscillations occur in the THETA computation. In the specific time step, the Poisson equation for pressure correction has not converged in the maximum number of iterations. Nevertheless, the interference subsides in the following rotor rotations and is sufficiently small. Thus, the reason for this oscillations is of minor importance in the context of this paper.

If the wind turbine operates in uniform flow conditions, a $3/rev$ -characteristic is found in both F_x and M_x , which is caused by the tower blockage effect. Moreover, the constant amplitudes around a steady mean value of both, F_x and M_x indicate that the flow field has converged. The converged state includes the boundary layer that developed on the viscous floor of the flow domain. Over the length of the entire flow domain, the boundary layer achieved a thickness of approximately 1m at the end of the flow domain. This is far below the rotor area and does not affect the rotor characteristics or wake development during the computation. Hence, the gust as defined in equation 4 or 8 is applied in the next step.

5.2 Cosines gust

The impact of the $1 - \cos()$ -gust on rotor thrust F_x and rotor torque M_x during the gust is evaluated by comparison to uniform inflow conditions. F_x and M_x are displayed in figure 3 and 4, respectively. Therein, the period between 30 s and 50 s is displayed while the gust operates between $T_S = 37$ s and $T_S + T_g = 44$ s. Thus, it lasts approximately 1.5 rotor revolutions. As expected, the gust velocity spreads over the entire field immediately and also affects rotor thrust and rotor torque instantaneously. In the case of gust and calm no hysteresis effect is found as rotor thrust and rotor torque recover immediately after the gust. This is visible in both figures 3 and 4 as the curve of constant inflow conditions is matched right after 44 s. The symmetric response of rotor thrust and rotor torque to the gust is caused by the modelling assumptions of a stiff blade and a missing speed control algorithm.

During the gust, F_x and M_x follow the modification of the inflow condition. Hence, for a positive gust velocity u_g (equation 4) rotor loads increase in a $1 - \cos()$ -shape while they decrease in the same manner for a negative gust velocity. Additionally,

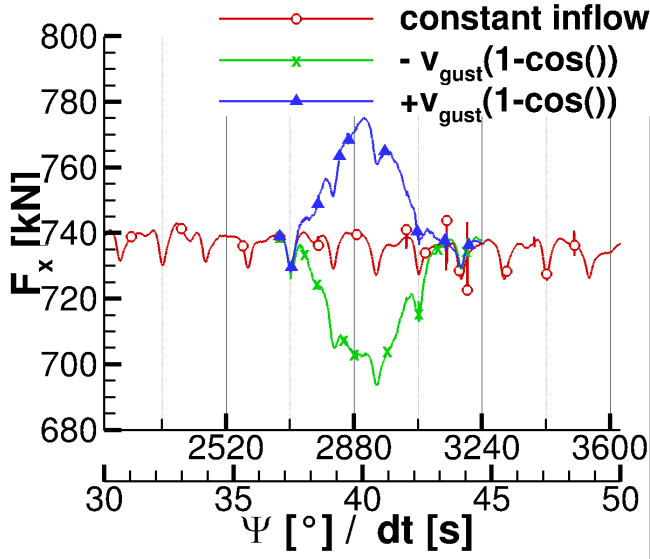


Figure 3. Rotor thrust F_x during the gust

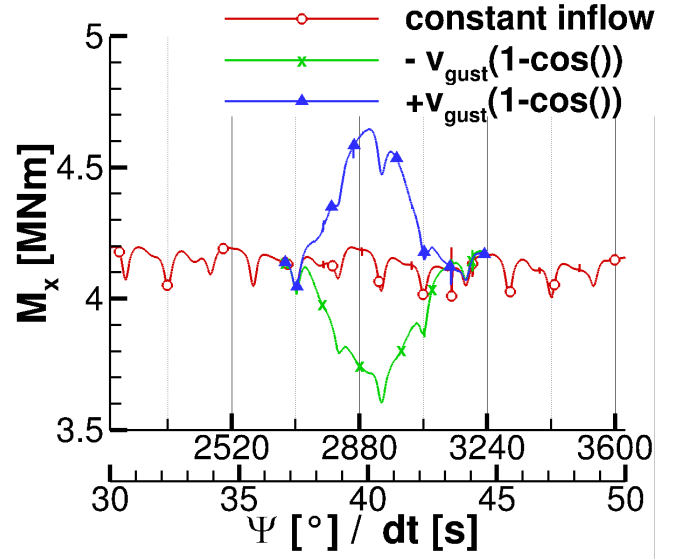


Figure 4. Rotor torque M_x during the gust

the tower blockage effect is superposed on the blade loads and remains detectable in the blade load development. In the case of $u_g = +0.25$ m/s, the tower blockage effect reduces the time that the rotor experiences maximum loads as is visible at approximately $t = 41$ s. A sharp drop in both, rotor thrust and rotor torque, is visible. This drop is due to the tower blockage effect and would have appeared at a different instance of the gust if the rotor position at the gust starting time was different. Nevertheless, during the calm with $u_g = -0.25$ m/s the tower blockage leads to an additional decrease in rotor thrust and rotor torque at $t = 41$ s. The rapid changes in rotor thrust and rotor torque indicate the fast load changes on the blade which increase fatigue loads.

Table 1 lists the relative differences in F_x and M_x during the gust, computed by equation 9. In equation 9 the subscript *max* indicates the extreme rotor loads and the over-line the averaged rotor loads under constant inflow conditions of section 5.1

$$\begin{aligned} \delta F_x &= 100 \cdot \left(\frac{\overline{F_{max}}}{\overline{F_x}} - 1 \right) \\ \delta M_x &= 100 \cdot \left(\frac{\overline{M_{max}}}{\overline{M_x}} - 1 \right). \end{aligned} \quad (9)$$

Additionally, the relative difference in the averaged blade load is computed by first integrating rotor thrust and rotor torque during the gust excitation and then computing equation 9. The result of the gust peak load is listed in table 1 while the integrated loads are contained by table 2.

In both tables it can be seen that a reduction of the wind speed due to a calm or the increase of the wind speed with the same amplitude leads to very similar absolute changes in rotor thrust and rotor torque. By comparing the values of table 1 and 2 it is also found that the absolute peak loads are 2.3 times larger than the averaged loads. Thus, the use of maximum loads during a 10 min-interval is inevitable for a computation of equivalent fatigue loads while averaging the loads is not appropriate.

Table 1. Gust induced peak loads on the rotor during the $1 - \cos()$ -gust in relation to the constant blade load

	δF_x [%]	δM_x [%]
$u_g = +0.25$ m/s	+5.6	+12.9
$u_g = -0.25$ m/s	-5.6	-12.4

Table 2. Averaged rotor loads during the $1 - \cos()$ -gust in relation to the constant blade load

	$\overline{\delta F_x}$ [%]	$\overline{\delta M_x}$ [%]
$u_g = +0.25$ m/s	+2.4	+5.7
$u_g = -0.25$ m/s	-2.1	-4.6

It is also important to note that the rotor loads return to the values of constant inflow conditions right after the gust ended. This indicates that there are neither reflections nor numerical oscillations in the flow field which lower the numerical accuracy. In summary, the behaviour of rotor thrust F_x and rotor torque M_x is as expected. The increased wind speed causes higher thrust and momentum and vice versa while the amplitude is identical for the increase and decrease in wind speed.

- 5 By considering blade deflections and changes to the rotational speed in future aero-elastic computations, the resulting rotor torque and rotor thrust will change.

5.3 Extreme operating gust

Figure 5 presents rotor thrust F_x and rotor torque M_x during the EOG excitation in comparison to the constant inflow conditions. Moreover, the rotor torque that is computed by FAST for a stiff blade and constant rotational speed is displayed. The EOG lasts about 10.5 s or 2 rotor revolutions. In comparison to the rotor loading during the $1 - \cos()$ -gust (section 5.2) the tower blockage effect becomes negligible. Hence, the starting position of the rotor is less important for the computation of maximum loads. This is also seen in the FAST result. By comparing the rotor torque during the gust of THETA to the one of FAST it is found that both values coincide exactly before $t = 43.5$ s and after $t = 46.5$ s. Between this two time stamps, FAST predicts significantly higher loads than THETA. Moreover, the EOG load at the maximum gust velocity is increased in comparison to THETA. The differences result from the flow characteristics of the blade. THETA predicts large areas of flow separation as response to accelerated velocity after $t = 43.5$ s. The flow reattaches over most of the blade after $t = 46.5$ s when the velocity slowed down sufficiently. It is most likely that the profile polars that the BEM of FAST relies on is not able to reproduce the instationary flow behaviour of the given case.

The maximum velocity u_{max} during the gust is about 15.65 m/s and the minimum velocity u_{min} is 9.94 m/s which are 137 % and 87 % of the values at rated wind speed. The changes in rotor thrust and rotor torque, computed by equation 9, are given in table 3. It is shown that the rotor torque is decreased by 36 % during the calm that precedes or follows the velocity maximum and increased about 100 % during the gust peak. The changes in rotor thrust are smaller even though the amplitudes of load

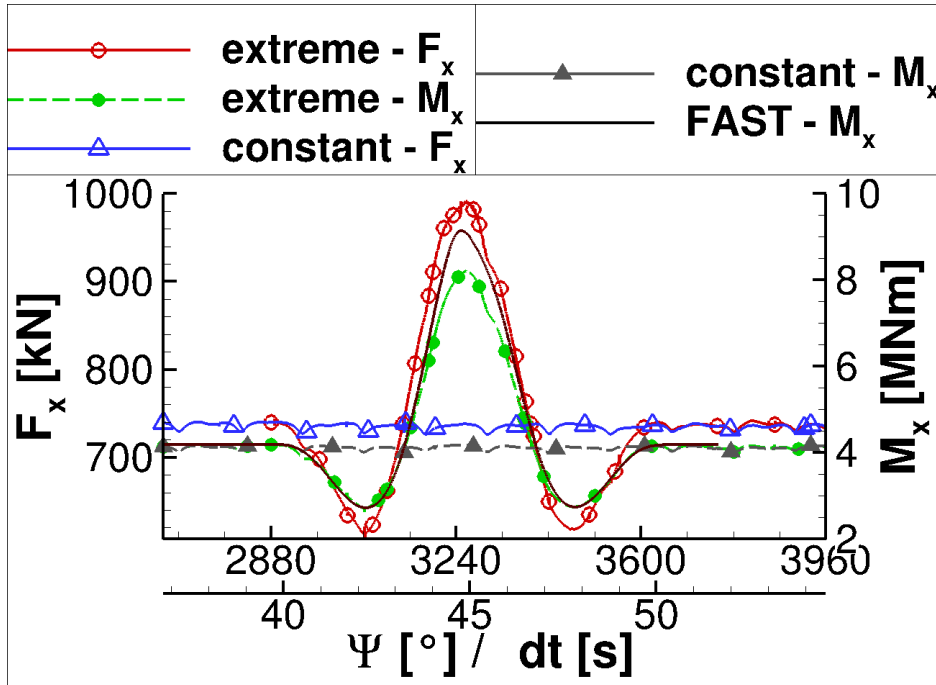


Figure 5. Rotor thrust F_x and torque M_x during the gust

Table 3. Gust induced peak load during the EOG on rotor in relation to the constant blade load

	δu [%]	δF_x [%]	δM_x [%]
$u_g(min)$	-13	-17.3	-36.0
$u_g(max)$	+37	+35.0	+100.2

change are significant as well.

To analyse the flow state on the blade during the gust two instances have been chosen: after $t_{min} = 2.5s + T_S = 42$ s (minimum gust velocity) and $t_{max} = 5.6s + T_S = 45$ s (maximum gust velocity). Figure 6a) and b), respectively, display the rotor positions in the instances investigated. In both figures blade number 1 is coloured in black. At t_{min} , when the gust is at its minimum velocity, blade number 1 is right in front of the tower and additionally experiences the tower blockage effect. Conversely, at t_{max} , when the gust is at its maximum velocity, blade number 1 is in free stream conditions while the flow on blade number 3 enters the tower blockage region. The impact of the tower blockage during the constant inflow conditions at t_{min} and t_{max} is visible in the radial distribution of rotor thrust and rotor torque (figure 7).

In accordance to figure 5 the overall rotor loading is reduced when the blade experiences minimum gust velocity. Conversely, a significant increase in rotor loading is observed when the blade experiences the maximum gust velocity. At all times, the rotor thrust is reduced only slightly by the tower blockage effect. Moreover, only the inboard part of the rotor appears to be

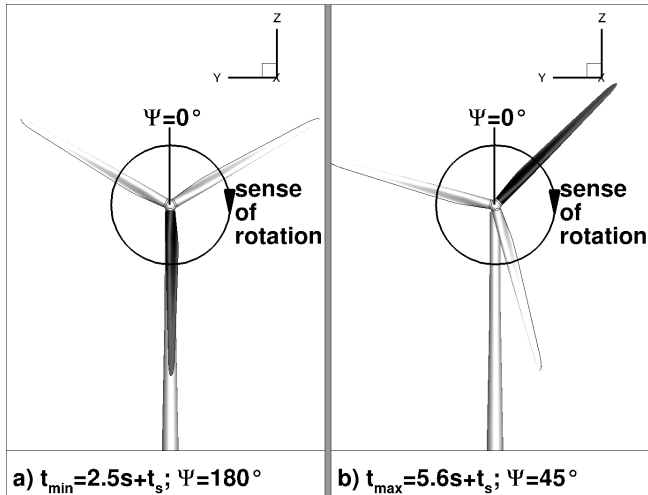


Figure 6. Rotor position at minimum (left) and maximum (right) gust velocity; Black blade is blade number 1

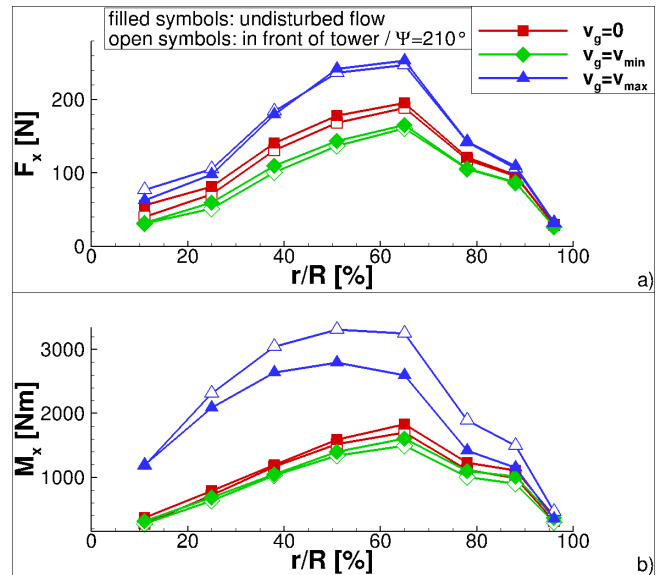


Figure 7. Span-wise distribution of a) rotor thrust and b) rotor torque for different azimuth positions at constant inflow and during the gust

affected by the tower blockage. Contrariwise, the rotor torque is affected by the tower blockage in the outer part of the rotor. Besides, the tower blockage effect generally has only small impact on the rotor torque at wind velocities smaller than rated wind speed. With the maximum gust velocity, the blade at $\Psi = 210^\circ$ experiences a strong tower blockage effect that reduces the rotor torque up to 29% (radial section $r/R = 65\%$). The reason is the different separation behaviour at the trailing edge of the blade which are investigated through pressure coefficient distributions and friction force coefficients at three radial sections: an inboard section at $r/R = 10\%$, a mid-section $r/R = 50\%$ and an outboard section at $r/R = 90\%$. They are displayed in figure 8, 9 and 10, respectively.

In all three figures the pressure is displayed in the upper half and is normalized with the vector sum of the tip speed and the constant inflow velocity. For a meaningful comparison to constant inflow conditions, it was ensured that the investigated sections result from blades at the same azimuth positions.

A noticeable difference in c_p at minimum gust velocity is found in all sections (figures 8a), 9a), and 10a)) when compared to the constant inflow conditions. The decrease in the stagnation point of c_p to lower values at t_{min} is higher than that of the tower blockage effect while otherwise the pressure distributions keep the general shape. Conversely the difference between constant inflow conditions and the maximum gust is significantly higher. The maximum c_p increased about 58% at the blade tip. Moreover, the shape of the pressure distribution changes over the entire blade. This is visible especially in the mid- and outboard blade sections (figures 9a) and 10a)). In both sections, the pressure increases rapidly in the rear half of the upper blade surface and even reaches positive values in the last 20% of the profile. This behaviour is a first indication of a separation

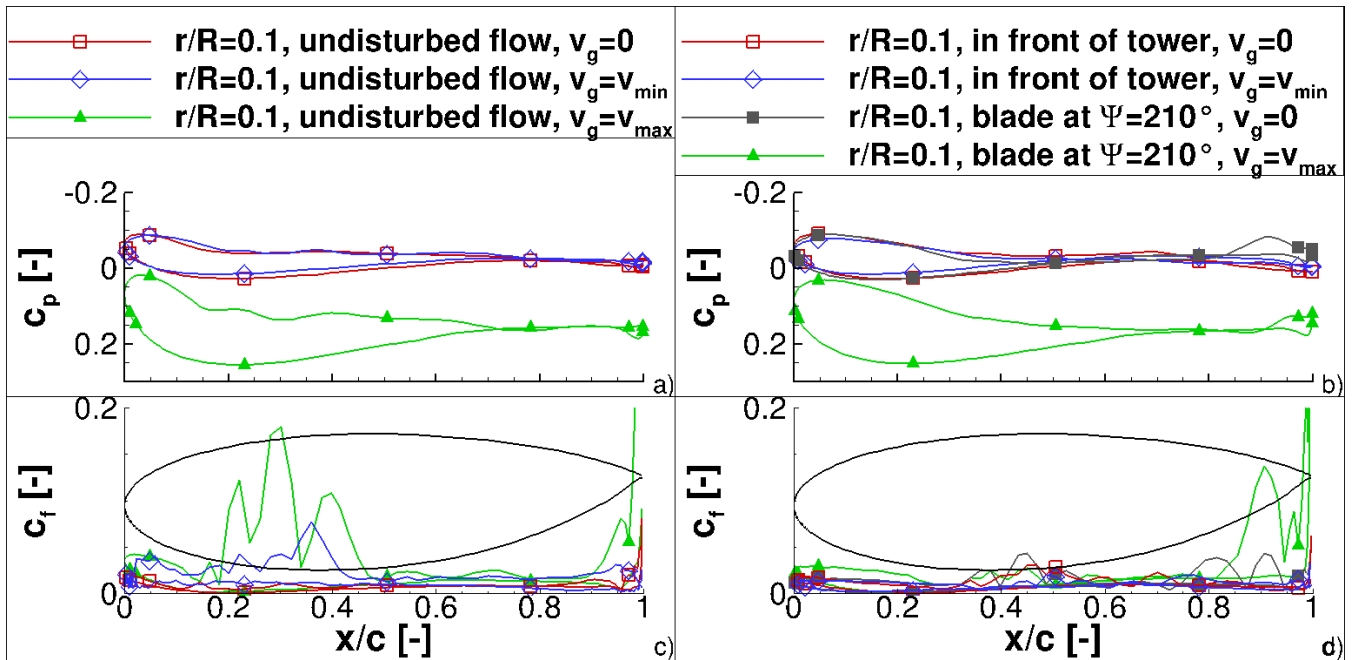


Figure 8. Pressure distribution of blade at inboard section; a,c) undisturbed flow; b,d) with tower blockage; a,b) pressure distribution, c,d) friction force coefficient

region and reversed flow around the trailing edge.

The friction coefficients on the blade sections in undisturbed flow are displayed in figures 8c), 9c), and 10c). In all sections, strong fluctuations are visible at the trailing edge which result from the truncated geometry at $x/c = 1$. The friction force coefficient c_f in the inboard section (figure 8c)) shows large differences between all considered time instances. The oscillations around $x/c = 50\%$ at constant inflow conditions indicate a small separation region with otherwise attached flow. At minimum gust velocity the overall friction force level is increased around the leading edge and the separation region has shifted upward and is between $x/c = 20\%$ and $x/c = 40\%$. At the maximum gust velocity, the friction force is increased and the oscillations between $x/c = 20\%$ and $x/c = 50\%$ indicate a larger separation region on the upper blade surface. The friction force coefficient indicates that separation in the blade inboard section is present during the entire rotor rotation. It is triggered through the close cylindrical blade root and amplified with higher inflow velocities.

Conversely to the inboard section, changes in separation at the mid-section appear due to the gust only. In figure 9c) the friction force level is decreased at minimum gust velocity and the curve is very smooth. At maximum gust velocity, small oscillations appear around $x/c = 90\%$, indicating separation in that region. By increasing the rotor radius, the behaviour is enforced. At the outboard section (figure 10c)), the local maximum in c_f in the last 20% of the profile almost reaches the level of the leading edge at t_{max} .

The same analysis is performed for the blade that is situated right in front of the tower or at $\Psi = 210^\circ$. For the pressure

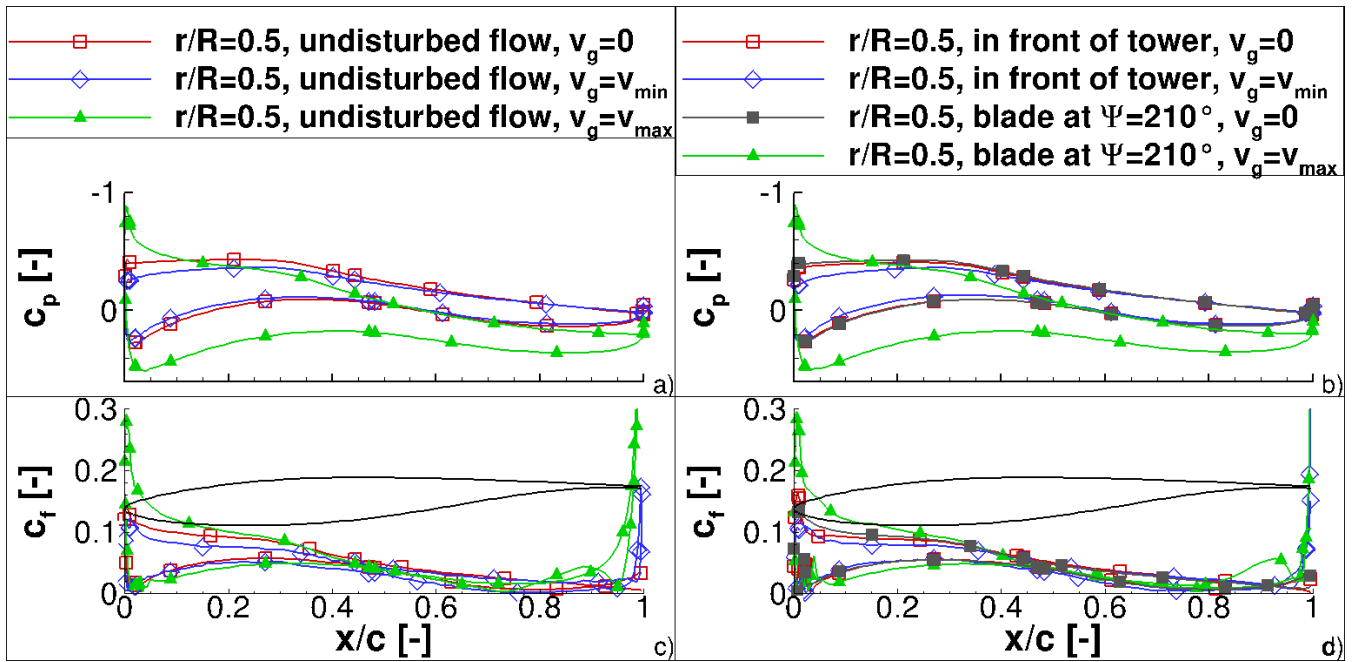


Figure 9. Pressure distribution of blade at mid section; a,c) undisturbed flow; b,d) with tower blockage; a,b) pressure distribution, c,d) friction force coefficient

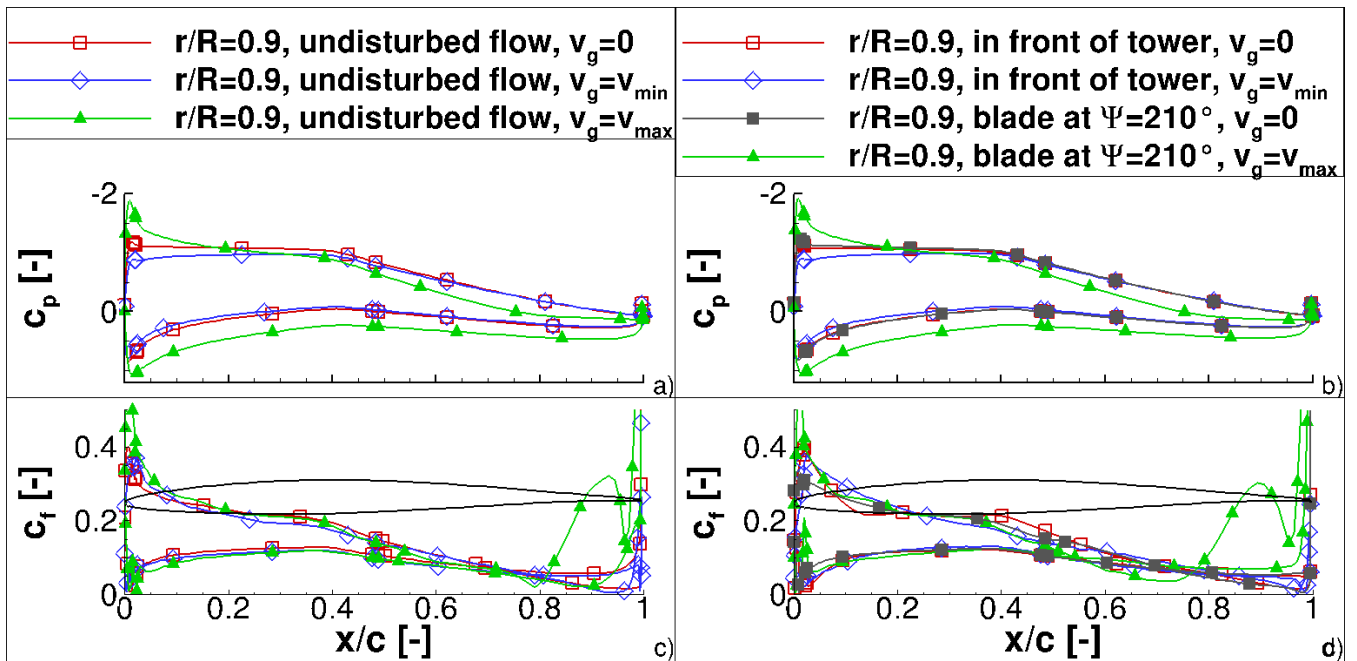


Figure 10. Pressure distribution of blade at outboard section; a,c) undisturbed flow; b,d) with tower blockage; a,b) pressure distribution, c,d) friction force coefficient

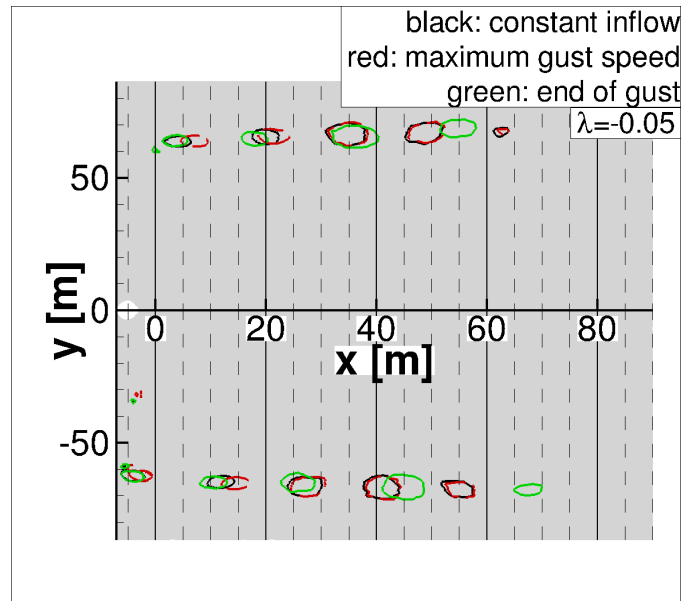


Figure 11. Tip vortex transportation in vertical plane through rotor centre

distributions (figures 8b), 9b), 10b)) the same effects as described for the blades in undisturbed flow are found. The only difference is that due to the tower blockage the overall pressure level is decreased about 1 %. This enforces the observation from the rotor thrust and rotor torque time histories in figure 5 and 7. Namely, the tower blockage effect is small compared to the EOG operating loads. Conversely, the characteristics of friction forces (figures 8d), 9d), and 10d)) in the inboard and outboard sections differ from those of the blades in undisturbed flow. In the inboard section in figure 8d), the oscillations in c_f reduce to a minimum while the overall friction force level remains constant. Only at maximum gust velocity, the oscillations around the trailing edge appear. Thus, the tower seems to suppress separation and it takes some time until the separation state is fully recovered. The friction force coefficient in the mid-section behaves similar to the inboard section with the difference that the entire separation region is larger (figure 9d)). In the outboard section in figure 10d), the friction force is increased significantly due to the maximum gust velocity. By comparing the friction coefficients of the blades in undisturbed flow and in the tower blockage region, it is found that the separation on the suction side of the blade covers a larger area in the rear part of the blade. The separation induces a larger profile thickness which results to different induced angle of attack and thus reduced momentum.

Finally, the transport of the tip vortices is investigated. It has to be understood as indication whether the velocity transport in the field works as expected but the tip-vortex transport has only small meaning on the transient rotor loading during the gust. Besides, the velocity in the field changes gradually because of the infinite speed of sound in the entire flow domain. Thus, the vortices that are shed from the blade at a given wind speed are not transported with their specific gust transport velocity. Contrariwise, all existing vortices experience identical changes in the gust transport velocity. Thus, the geometrical distance between existing vortices remains constant.

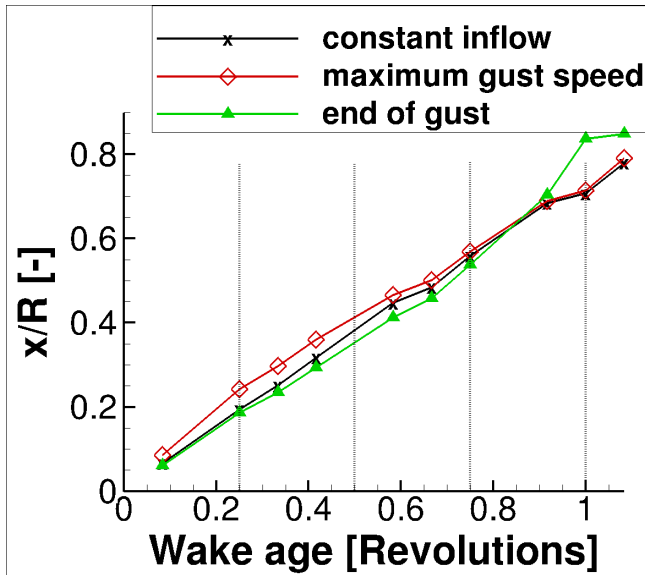


Figure 12. Tip vortex transportation in main flow direction in dependency of the wake age at three time instances during the gust

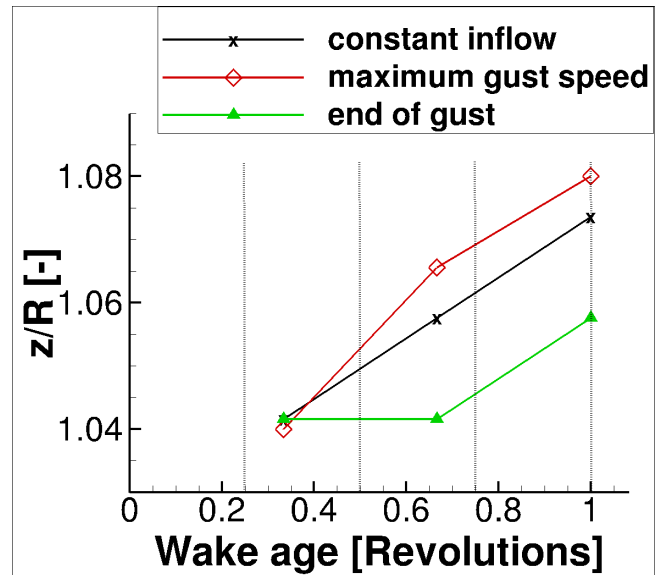


Figure 13. Tip vortex transportation vertical to main flow direction in dependency of the wake age at three time instances during the gust

In figure 11 three instances of the flow field are compared. In all three instances, the rotor is at $\Psi = 0^\circ$ positions. The vortices are made visible with the λ_2 criterion (?). The black lines are extracted during constant inflow, the red lines are extracted shortly before t_{max} and the green ones at the end of the gust. By comparing the vortex transport at the beginning of the gust (black curve) and at the end of the gust (green curve), a compression and stretching of the distance between the vortices is found. The vortex transport in dependency of the vortex age is further discussed through figures 12 and 13. They compare the transport of the vortex in dependency of the vortex age parallel and orthogonal to the flow direction, respectively. As long as the inflow velocity is constant, the vortex transport is approximately $0.23 \cdot r/R$ parallel to the flow direction and $0.16 \cdot r/R$ orthogonal to the flow direction in a $1/3$ -revolution interval. At maximum gust velocity, the constant distance between the vortices is lost. The vortices older than one revolution experienced constant inflow conditions. Thus the inter-vortex distance is constant. The vortices between 0.25 and 1 revolutions were shed during the reduced wind speed. Hence the distance parallel to the flow direction is reduced. As the downstream wake-transport decreases the orthogonal transport increases. The vortices younger than 0.25 revolutions experienced the high wind speed. Thus, the distance between the vortices parallel to the flow direction increases and the orthogonal transport decreases. At the end of the gust, reversed behaviour of the vortex transport is observed. The vortices between 0.75 and 1 revolution were generated while the wind speed slowed down. Thus, the distance between the vortices parallel to the wind direction is increased while the orthogonal transport is decreased. Vortices up to an age of 0.75 revolutions have a decreased distance parallel to the wind direction while an increased distance orthogonal to the wind direction.

The aerodynamic characteristics, rotor thrust and rotor torque of course depend on the assumption of stiff rotor blades and constant rotational speed. If the rotor had finite mass and inertia or a speed control algorithm had been applied, the rotor loading during the gust would have been reduced significantly. Moreover, the symmetry of the rotor loading decreases as soon as the structure dynamics are taken into account.

5 6 Conclusions

The study presented the validation of the resolved-gust approach that was implemented in the U-RANS-solver THETA. As test case, the generic 5 MW wind turbine was computed, operating under a $1 - \cos()$ -gust and an extreme operating gust as defined in the IEC standard. The gust has been introduced with the resolved-gust-approach (??) by introducing the changing velocity at the inflow boundary conditions. The gust velocity was then transported loss-free through the field with infinite speed of sound.

10 The assumptions, which are made in the paper can be summarized as

1. the wind speed is constant in height and time (except gust velocity)
2. the gust velocity is constant in height
3. the gust transport velocity is equal to speed of sound which is infinite
4. the boundary conditions of the flow domain are chosen to prevent the flow from escaping sideways.

15 The disadvantage of the resolved-gust approach clearly is the requirement of fine time steps and fine grids upstream of the geometry in question which increases the computational costs. The infinite speed of sound and its direct relation to the gust transport velocity has to be regarded in its ambivalent effects. It leads to an inaccurate reproduction of the wind turbine wake transport on the one hand, while on the other hand, the response of the rotor loading to the gust velocity is immediately obtained. Clear advantages for the resolved-gust approach are numerical stability and no artificial oscillations. Finally, the resolved-gust
20 approach can be applied to any completed wind turbine U-RANS computation to obtain more insight of the wind turbine characteristics.

The results represented the effects that are expected during the in-stationary inflow condition in combination with the given boundary conditions very well. Rotor thrust and rotor torque follow the gust shape very close. An analysis of the time history of rotor thrust and rotor torque during the gust show an increased rotor loading of about 100 % compared to constant inflow.

25 Pressure distributions and friction force coefficients reveal that the flow on the rotor blades at maximum gust velocity is separated and thus highly in-stationary. Moreover, the effect of accelerating wind speeds was found in the rotor wake as the distance between the vortices is stretched and compressed according to the changes of the wind speed.

The comparison of the results with the aero-elastic software FAST showed a very good agreement of rotor thrust and rotor torque during the EOG. Thus, it is a valid and accurate method to predict wind turbine loads during an EOG. Nevertheless, a

30 complete validation is not possible at this state as a gust experiment for a wind turbine is not available. The first mandatory step for further research on the gust simulation with U-RANS is to perform a grid-independence and time-step study with

the resolved gust approach. Based on that results, a gust transport velocity with other than infinite speed of sound have to be achieved. This may either be realized by adjustments of the resolved-gust approach, by implementing the field approach of, for example, ?, or the velocity disturbance approach of ?. A third possibility would be to introduce the fluctuating gust velocities obtained from LES computations which themselves fulfil the continuity conditions. Only then, the procedures of gust computation for wind turbines in THETA are prepared to be extended to respect atmospheric boundary layer flows or for aero-elastic analysis. ~~Only then, the procedures of gust computations for wind turbines in THETA are prepared to be extended to respect atmospheric boundary layer flows or for aero-elastic analysis. The method would then enable to gain enhanced knowledge on the flow development and load distribution on rotor loads during gust excitations. The then ready-to-use method is supposed to supply a tool for gaining more detailed knowledge about the wind turbine behaviour during extreme gust events, in a first step. In a second step, this knowledge can be used to adjust engineering models which are used during the design process. It has to be clearly understood that the resolved-gust approach in a U-RANS computation can and will not replace engineering models at this stage. Consequently, the potential of weight reduction (and thus cost-reduction) and increased reliability in wind turbine designs are the (very-) long-term objectives.~~

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Data availability. Availability of NREL 5 MW data from NREL reports; no other data available.

Competing interests. The author declares that she has no conflict of interest.