



Improving mid-altitude mesoscale wind speed forecasts using LiDAR-based observation nudging for Airborne Wind Energy Systems

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Abstract. Airborne wind energy systems (AWES) aim to operate at altitudes above conventional wind turbines where reliable high resolution wind data is scarce. Wind LiDAR measurements and mesoscale models both have their advantages and disadvantages when assessing the wind resource at such heights. This article investigates whether assimilating measurements into the mesoscale WRF model using observation nudging generates a more accurate, complete data set. The impact of continuous observation nudging at multiple altitudes on simulated wind conditions is compared to an unnudged reference run and to the LiDAR measurements themselves. We compare the impact on wind speed and direction for individual days, average diurnal variability and long term statistics. Finally, wind speed data is used to estimate optimal traction power and operating altitudes of AWES. Observation nudging improves the overall accuracy of WRF. Close to the surface the impact of nudging is limited as effects of the air-surface interaction dominate, but becomes more prominent at mid-altitudes and decreases towards high altitudes. The wind speed probability distribution shows a multi-modality caused by changing atmospheric stability conditions. Based on a simplified AWES model the most probable optimal altitude will be around 400 m. Such systems will benefit from dynamically adjusting their operating altitude.

Keywords: Airborne Wind Energy, Mid-Altitude Wind Measurement, Onshore Wind, Weather Research and Forecasting Model, Observation Nudging, Statistic Wind Conditions



1 Introduction

The prospects of higher energy potential and more consistent strong winds and less turbulence in comparison to near surface winds sparked the interest in mid-altitude, here defined as heights above 100 m and below 1500 m, wind energy systems. Airborne Wind Energy System (AWES) are a novel renewable energy source that harvest stronger winds at altitudes which are unreachable by current wind turbines, at potentially much reduced capital cost (Lunney et al., 2017; Fagiano and Milanese, 2012). For practical and economical reasons we focus on resource assessment within the lower part of the atmosphere, an altitude range spanned by the highly-variable boundary layer. Unlike conventional wind energy which has converged to a single concept with three blades and a conical tower, several different AWES designs are under investigation by numerous companies and research institutes worldwide (Cherubini et al., 2015). Various concepts from ring shaped aerostats, to rigid wings and soft kites with different sizes, rated power and altitude ranges compete for entry into the marketplace. Since this technology is still in an early stage, none are commercially available.

Developers and operators of large conventional wind turbines, AWES and drones require accurate wind data to estimate power and mechanical loads. They currently rely on oversimplified approximations such as the logarithmic wind profile (Optis et al., 2016) or coarsely resolved reanalysis data sets (Archer and Caldeira, 2009) as the applicability of conventional spectral wind models (Burton, 2011) have not been verified for these altitudes.

Recent advancements in wind Light Detection and Ranging (LiDAR) technology enable high resolution measurements in higher altitudes. This measurement technique however suffers from reduced data availability with increasing altitude caused by a decrease in aerosol density which is needed for the backscattering of the LiDAR signal (Peña et al., 2015). The expensive and time consuming nature of LiDAR measurements motivates the usage of Numerical Weather Prediction (NWP) models such as the mesoscale model Weather Research and Forecasting (WRF) as an adequate tool to assess synoptic characteristics of the Atmospheric Boundary Layer (ABL) (Al-Yahyai et al., 2010). These models typically have a spatial resolution that ranges from one kilometer to tens of kilometers and a temporal resolution in the order of minutes. Sub-gridscale high frequency variations to resolved quantities are parameterized. No mid-altitude measurement device can reliably gather long term, high frequency data. However, LiDAR estimated Turbulence Intensities (TI) correlate with sonic turbulence measurements for lower altitudes (Sathe et al., 2011). As such the here presented TI estimates only present a rough estimate and will be complemented with high resolution Large Eddy Simulations (LES) data presented in future work.

This work is a continuation of a previous investigation of mid-altitude wind LiDAR measurements (Sommerfeld et al.). The measurements used in these studies were gathered as part of the *OnKites II* project at the Fraunhofer Institute for Wind Energy Systems (IWES) with the goal of evaluating the potential of AWES. This paper makes use of various statistical tools to describe the relationship between the mesoscale WRF model and LiDAR measurements to determine the impact of wind speed observation nudging (Mylonas-Dirdiris et al., 2012).

Section 2 describes the measurement campaign. Section 3 introduces the mesoscale model and observation nudging methodology used in this article. Section 4 quantifies the impact of observation nudging and summarizes the statistical differences



between WRF and LiDAR. Results are applied to estimate optimal operating altitude and power based on a simplified AWES model in section 4.7. Section 5 concludes the article with an outlook and motivation for future work.

2 Measurement Campaign

The LiDAR data used in this study were collected between September 1st, 2015 and February 29th, 2016 at the ‘Pritzwalk Sommersberg’ airport (Coordinates: Lat: 53° 10’ 47.00"N, Lon: 12° 11’ 20.98"E) in Northern Germany (see white X in figure 1). The area surrounding the airport mostly consists of flat agricultural land with the town of Pritzwalk to the South. A *Galion4000* single beam pulsed wind LiDAR from SgurrEnergy was used. Wind speed data were collected using the Doppler beam swinging (DBS) method which averaged multiple line of sight measurements at constant elevation angle and four azimuth angles to calculate the 10 minute mean wind speed at 40 range gates up to an altitude of about 1100 m. The resulting wind speed is inherently spatially and temporally averaged. At an altitude of 1100 m the radius of the averaging disc defined by the four azimuth positions with 90° increments is about 585 m. For the reconstruction of 10 minute mean wind speed it is thus assumed that the wind vector does not change over this area, a valid assumption for these heights over flat terrain.

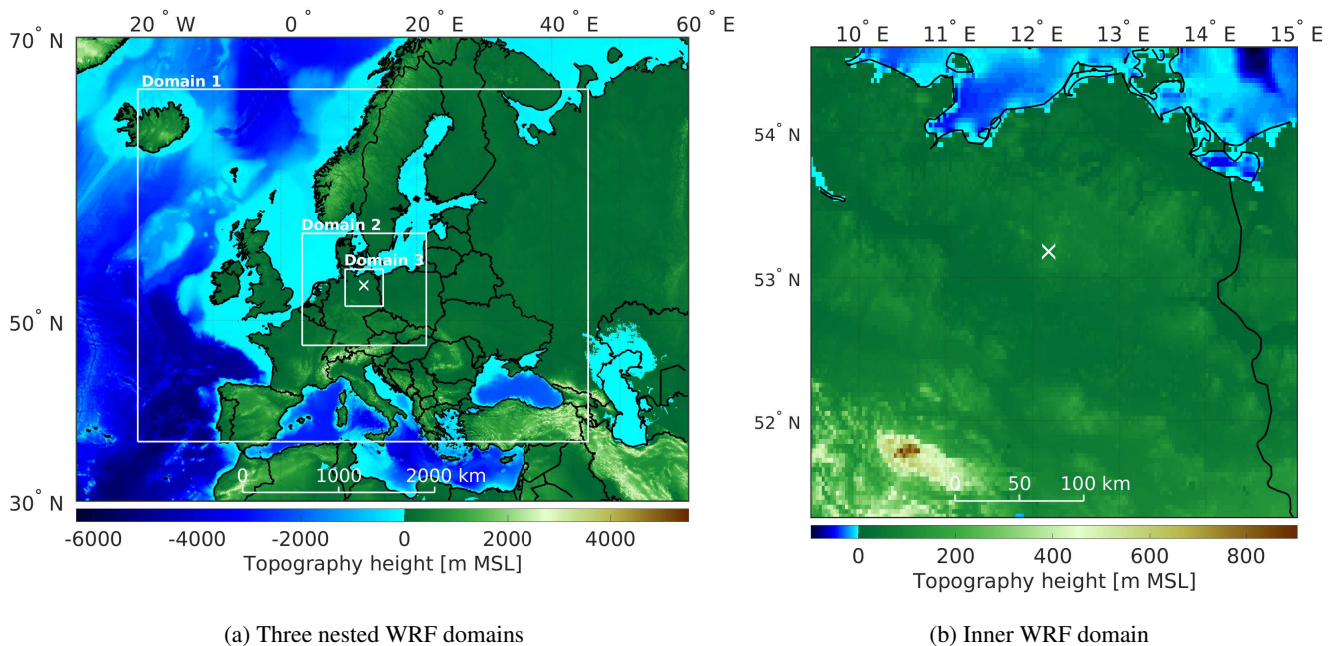


Figure 1. Topography map of all three WRF model domains (a) and a magnification of the innermost domain (b) with the LiDAR measurement site marked by a white X.

LiDAR data availability highly depends on the aerosol content of the air as the wind speed is calculated based on the backscatter of the emitted laser beam. Most aerosols originate from the surface and are transported aloft. Particle density decreases with height and drops to almost zero within the free atmosphere above the ABL (Matthias and Bösenberg, 2002).



Data quality quantified by the Carrier-to-Noise Ratio (CNR) dropped on average by approximately 5 dB over the course of 1000 m. As a result, data availability dropped from about 81% at 100 m and about 24% at 1000 m (Sommerfeld et al.). Low data availability caused by weather effects (e.g. strong precipitation) further emphasize the importance of simulations for mid-altitude wind resource assessment as no measurement technique with sufficient spatial and temporal resolution is available at this point.

Unstable and stable stratifications were identified by partitioning the data based on the sign of WRF calculated sensible Surface Heat Flux (SHF). These two atmospheric conditions lead to bi-modal wind speed probability distributions aloft which is not adequately represented by a single Weibull distribution fit. Mid-altitude wind speeds are better represented by the weighted sum of two wind speed Probability Density Function (PDF) fits conditioned by the sign of SHF.

3 Mesoscale Modeling Framework

To complement the 6 months LiDAR data set two WRF (v. 3.6.1) simulations using the Advanced Research Weather Research and Forecasting (ARW) model (Skamarock and Klemp, 2008) were carried out. The ‘baseline run’ (hereafter referred to as *NoOBS*) is a 12 month study of the area around the measurement location (see figure 1) from the 1st of September 2015 used to derive annual statistics. LiDAR measurements (Sommerfeld et al.) (see section 2) were incorporated into the six months test model between September 2015 and February 2016 using *OBSGRID* (Wang et al.) (hereon after referred to as *OBS*). This methodology uses the difference between model and measurements to calculate a non-physical forcing term that gradually nudges the model towards the observation (Stauffer et al., 1991; Deng et al., 2007). Each simulation is composed of three nested domains with 27-, 9- and 3-km grid spacing and grid dimensions of 120×120 elements at 60 η -pressure heights. Differences between the simulation runs (see section 3.1) are compared within the innermost domain of the simulation. Output data was stored in 10 minute intervals. Figure 1 shows the topography map of the simulation. Initial and boundary conditions of both simulations are based on the *ERA-Interim* (Dee et al., 2011) reanalysis data set by the European Centre for Medium-Range Weather Forecasts (ECMWF) which consists of 6 hourly atmospheric fields with a spatial resolution of roughly 80 km horizontally and 60 η levels. Turbulent Kinetic Energy closure within the ABL was achieved by using the Mellor Yamada Nakanishi Niino (MYNN) 2.5 scheme which predicts sub-grid Turbulent Kinetic Energy (TKE) as a prognostic variable (Nakanishi and Niino, 2004; Lee and Lundquist, 2017). In addition to observation nudging (see subsection 3.1) analysis nudging was performed on every domain of each simulation where each grid point is nudged towards a time-interpolated value from analyses of synoptic observations (Stauffer et al., 1991). Within the Planetary Boundary Layer (PBL) of the inner domain analysis nudging was switched off (see nudging settings in table A1 in the appendix). All simulations were run on the *EDDY* (Carl von Ossietzky Universität Oldenburg, 2018) High-Performance Computing clusters at the University of Oldenburg. Table 1 summarizes the WRF domain size.



Table 1. Resolution and grid size of WRF domains

Name	domain size [km x km]	grid spacing [km x km]	temporal resolution [sec]
Domain 1	3240x3240	27 x 27	90
Domain 2	1080x1080	9 x 9	30
Domain 3	360x360	3x 3	30

3.1 Observation Nudging

Observation nudging also referred to as ‘dynamic analysis’ is a form of Four-Dimensional Data Assimilation (FDDA) where each grid point within the radius of influence and time window is nudged towards observations using a weighted average of differences between model (q_m interpolated at the observation location) and observations (q_0) (Dudhia, 2012; Reen, 2016).

- 5 In this study horizontal wind speed U and direction Φ were nudged towards measurements with a time interval of six hours between an altitude of 66 m and 1100 m, in order to not overly constrain the simulation. The non-physical forcing term is implemented in form of prognostic equations (Deng et al., 2007):

$$\frac{\partial q\mu}{\partial t}(x, y, z, t) = F_q(x, y, z, t) + \mu G_q \frac{\sum_{i=1}^N W_q^2(i, x, y, z, t) [q_0(i) - q_m(x_i, y_i, z_i, t)]}{\sum_{i=1}^N W_q(i, x, y, z, t)} \quad (1)$$

- q refers to the quantity that is nudged, μ is the dry hydrostatic pressure, $F_q(x, y, z, t)$ is the physical tendency term of q , G_q is the nudging strength of q , N is the total number of assimilated observations, i is the index of the current observation, W_q is the weighting function based temporal and spatial separation between grid cell and observation (Dudhia, 2012). Four weighting functions G_q , $W_t(x, y, z, t)$, $W_z(x, y, z, t)$ and $W_{xy}(x, y, z, t)$ describe the temporal and spatial nudging strength. Values used in this study can be found in the appendix (table A1). The inverse of G_q (here about $1/6e^{-4}s \approx 46$ min) can be interpreted as a nudging time scale as it dictates how quickly the model approaches the observation.

- 15 W_{xy} and W_z define the spatial nudging weight while the temporal weighting function W_t defines the duration and weighting strength in time. W_t ramps from 0 to 1 and back to 0 (Reen, 2016). The nudging time window and the time between implemented observations was chosen to be 6 hours so that the implemented observations don’t overlap each other. This ensures all time steps are nudged while not excessively limiting the model.

- 20 Vertical influence was set very small so that observations only affect their own η level (Dudhia, 2012). The horizontal weighting factor W_{xy} (see equation: 2 is calculated based on the radius of influence R and the distance between the observation



and the grid location D . We used the ‘Cressman scheme’ as the horizontal nudging weighting function with a radius of influence of $R = 180$ km, thereby containing the whole inner domain.

$$w_{xy} = \begin{cases} \frac{R^2 - D^2}{R^2 + D^2} & 0 \leq D \leq R \\ 0 & else \end{cases} \quad (2)$$

4 Results

- 5 It is important to keep the difference in temporal and spatial resolution between LiDAR measurements and WRF simulation in mind. Furthermore, data availability highly influences the ability to nudge the simulation (see section 2) and compare wind speed statistics.

To quantify the local effect of observation nudging, we investigate the cell closest to the LiDAR measurement location and compare measured and modeled horizontal wind speeds U and direction. Additionally we investigate several sections
 10 at different locations and altitudes within the inner domain to quantify the spatial and temporal impact of single location observation nudging on the entire domain. Vector values of each WRF cell are calculated on the faces of each cell, linearly interpolated to the cell center and rotated from the grid projection to earth coordinate system.

4.1 Impact of nudging on wind statistics

Figure 2 shows the scatter plots of measured and simulated horizontal wind speed at various altitudes for times at which
 15 LiDAR data is available. The continuous line represents the linear regression of the data (regression coefficient is displayed in the legend) while the dotted line shows an ideal correlation. The color of the scatter points corresponds to the occurrence probability. Multiple wind speed clusters caused by stratification can be identified. While there is a trend towards higher wind speeds with increasing altitude, low wind speeds (< 8 m/s) still occur at high altitudes. Both simulations overpredict horizontal wind speeds at low-altitudes which is a known problem of WRF and could be attributed to the model not resolving sub-grid
 20 scale roughness elements properly (e.g. modeling strongly simplified parameterization of forests and/or cities) or flaws in the planetary boundary layer model which lead to overly geostrophic winds over land (Mass and Ovens, 2011). Observation nudging improves the overall correlation with measurements as surface influence decays. Both models approach similar values at higher altitudes which could be caused by the lack of observations due to reduced data availability or is indicative of WRF generally being better at modeling more geostrophic winds.

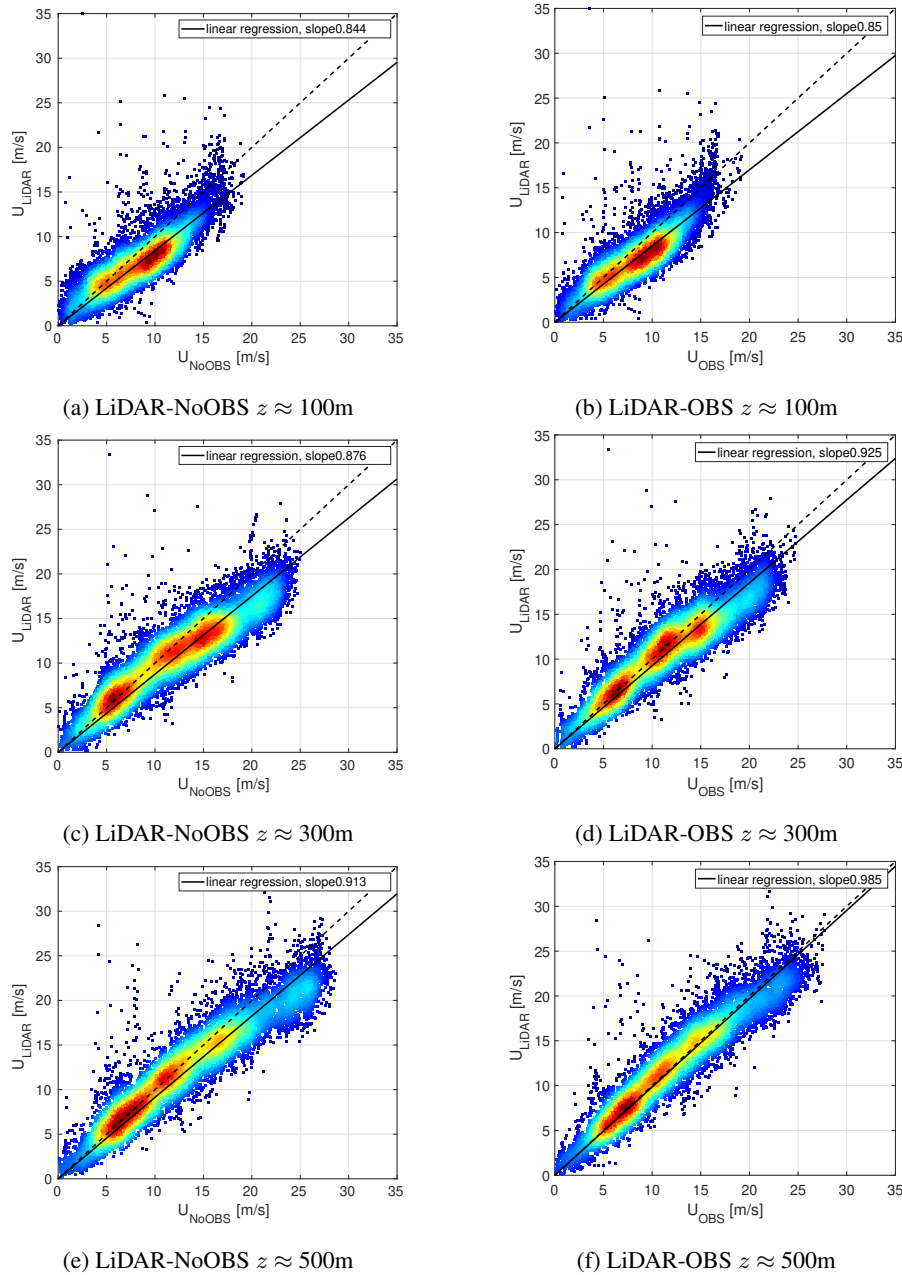


Figure 2. Linear Regression of LiDAR-measured wind speeds against NoOBS-modeled (WRF ‘baseline run’ without observation nudging) wind speeds (left side) and OBS-modeled (‘test run’ with obsgrid observation nudging) wind speeds (right side), at 100 m (a-b), 300 m (c-d), 500 m (e-f)

The statistical analysis of the absolute difference between the WRF simulated quantities and the LiDAR observations ($\Delta U = U_{WRF} - U_{LiDAR}$; $\Delta \Phi = \Phi_{WRF} - \Phi_{LiDAR}$) is shown in figure 3 in form of a box plot. The circle corresponds to the median,



the colored box indicate the 25 % and 75 % percentile and the whiskers to both sides mark ± 2.7 times standard deviation (σ). Outliers beyond $\pm 2.7\sigma$ are hidden to maintain clarity and readability. The continuous line in the left sub-figure represents the Root Mean Square Error (RMSE) of wind speed. The unnudged simulation (NoOBS) shows an almost constant wind direction bias at all altitudes. Observation Nudging (OBS) generally outperforms NoOBS and is in better agreement with the measurements particularly at altitudes of interest to high altitude wind energy systems. It furthermore reduces the spread of the bias, illustrated by the smaller whiskers and boxes. The ΔU RMSE of both simulations show similar results below 100 m and above 700 m. The largest improvement or smallest error can be found between 250 and 600 m. This could be explained by a better performance of the mesoscale model at these altitudes due to a reduced impact of the air surface interaction that is strongly parameterized or due to a reduced nudging due to low LiDAR data availability.

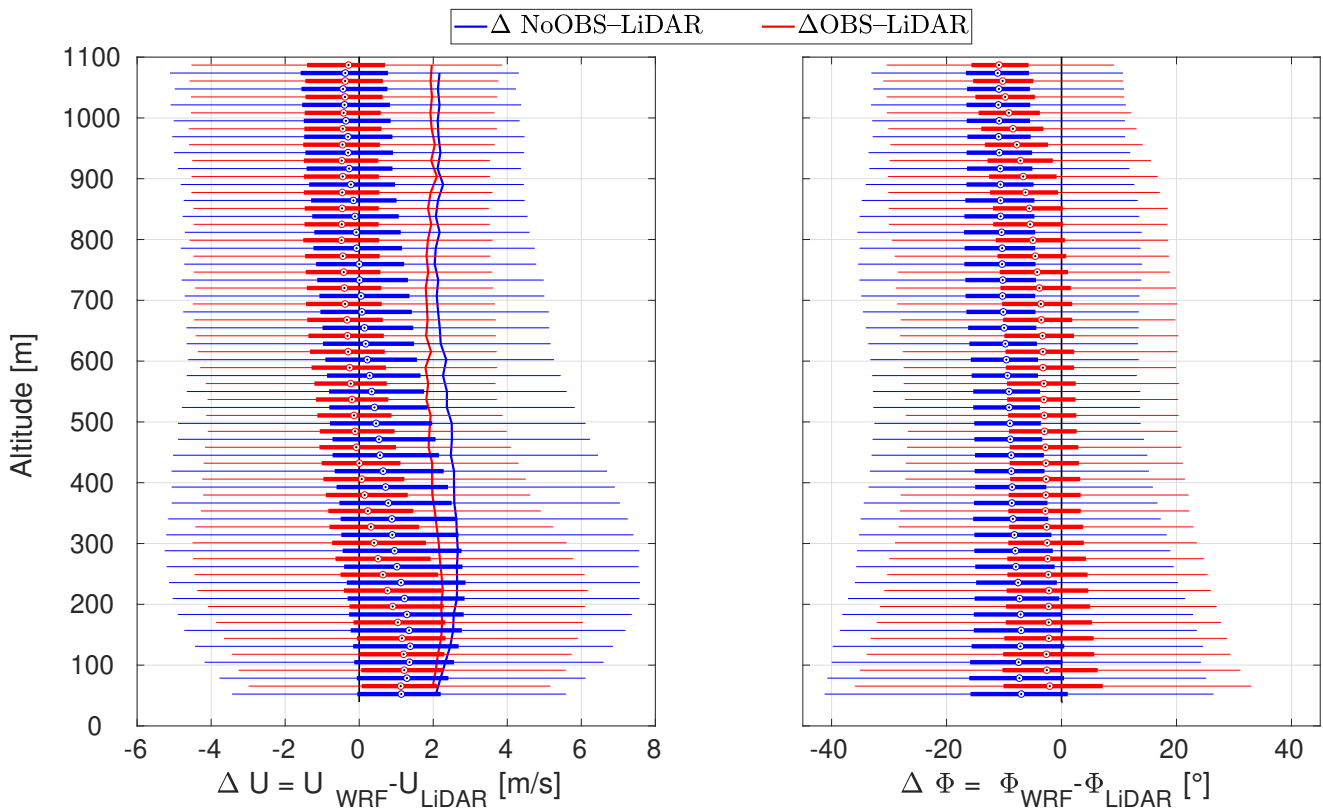


Figure 3. Statistical analysis of the bias between simulated and measured wind speed (ΔU) and direction bias ($\Delta \Phi$). The circle corresponds to the median, the colored box indicates the 25 % and 75 % percentile and the whiskers mark $\pm 2.7\sigma$. The solid lines in the left figure show the RMSE between the modeled and measured wind speed.

Observation nudging substantially reduces the directional bias $\Delta \Phi$ up to high altitudes. Similar to the wind speed bias, wind direction bias at 1100 m is almost the same for both simulations. The negative wind direction bias represents an anti-clockwise deviation. Other studies (Carvalho et al., 2014; Giannakopoulou and Nhili, 2014) have found similar wind direction biases. A



possible reason for this systematic bias is that WRF does not adequately resolve surface roughness resulting in lower surface friction leading to overly geostrophic winds (Mass and Ovens, 2010). The almost constant median wind direction bias indicates that WRF is able to capture the clockwise rotation of the ‘Ekman Spiral’ in the Northern hemisphere.

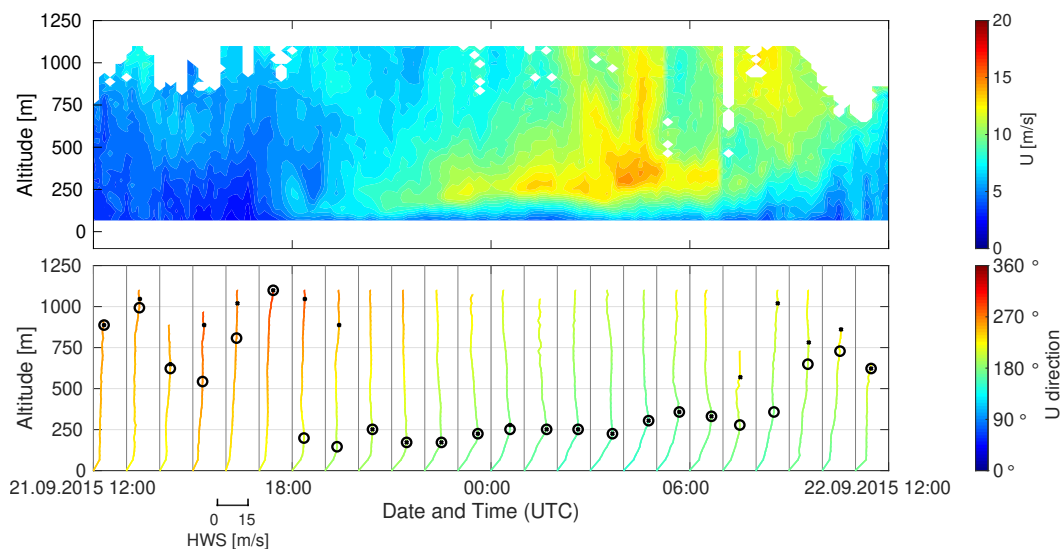
4.2 Representative nudging results

- 5 To visualize the impact of observation nudging on the mesoscale model output, we compare 10-minute mean horizontal wind speed for 24 hours on the 21st of September 2015 in figure 4 (an additional day can be found in the appendix figure A1). White space in the LiDAR measurements (see figure 4a) are data points that have been filtered out due to insufficient data quality. The dashed line is the WRF modeled SHF used to estimate atmospheric stability (see sub-section 4.5). The color of the profiles indicate the wind direction and LiDAR measured profiles are shown in grey for comparison. The black dot in each profile marks the altitude of highest wind speed while the black circle indicates the optimal altitude for the operation of an airborne wind energy system based on a simplified power approximation (see section 4.7).
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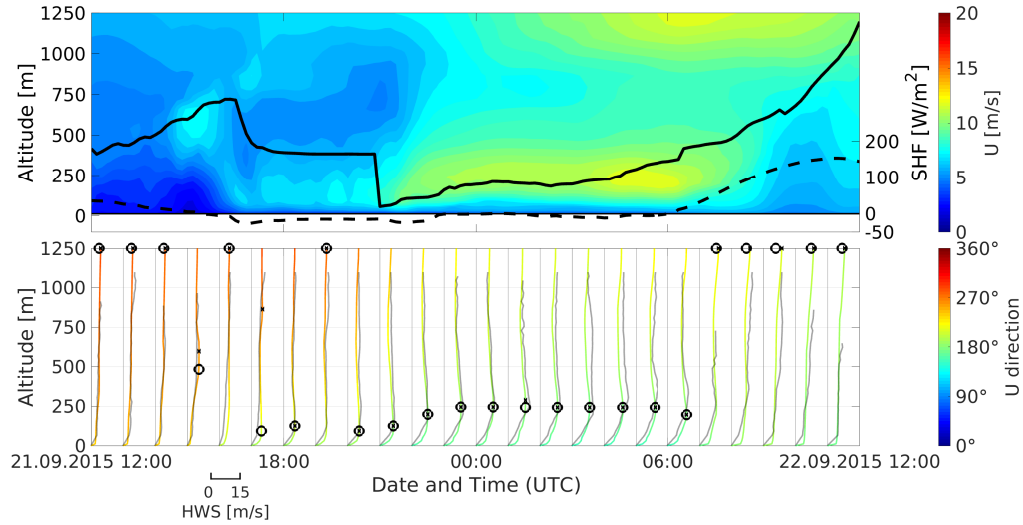
Even though observation nudging leads to statistical improvements in wind speed and wind direction prediction over the entire period (compare sub-section 4.1 and 4.4), individual days can still show a decline in model accuracy. The Low Level Jet (LLJ) as well as the high wind speeds at higher altitudes which the NoOBS model captures fairly well are significantly weaker in the OBS model. Implementing additional measurements at a higher frequency might yield results closer to measurements, but adding too many unphysical forcing terms might overly restrict the simulation.

15 in the OBS model. Implementing additional measurements at a higher frequency might yield results closer to measurements, but adding too many unphysical forcing terms might overly restrict the simulation.

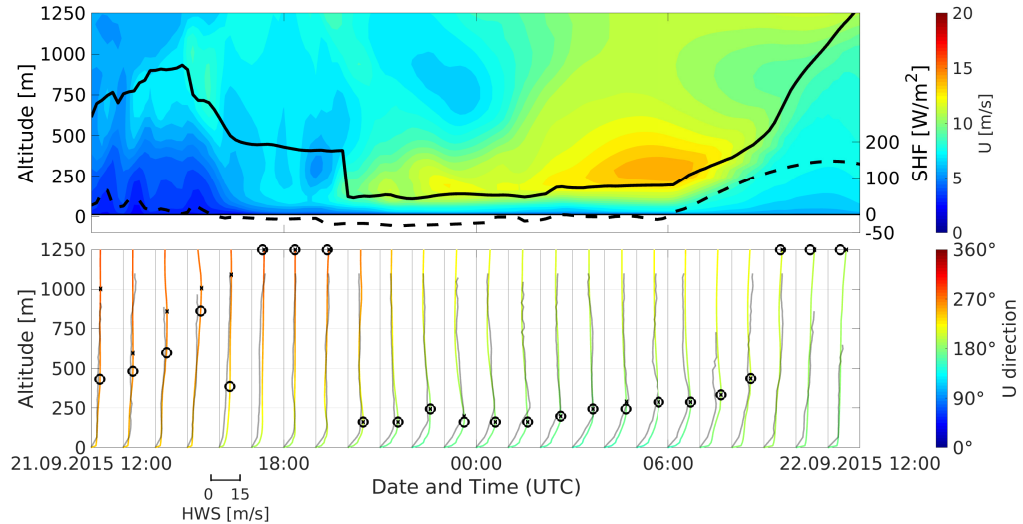
The Planetary Boundary Layer height (PBLH) (black line), which in the MYNN scheme is calculated from the profile of virtual potential temperature and from the profile of the TKE (Brunner et al., 2015; Nakanishi and Niino, 2004), is directly affected by wind speed observation nudging. During the investigated day, observation nudging leads to a lower daytime PBLH.



(a) LiDAR



(b) OBS



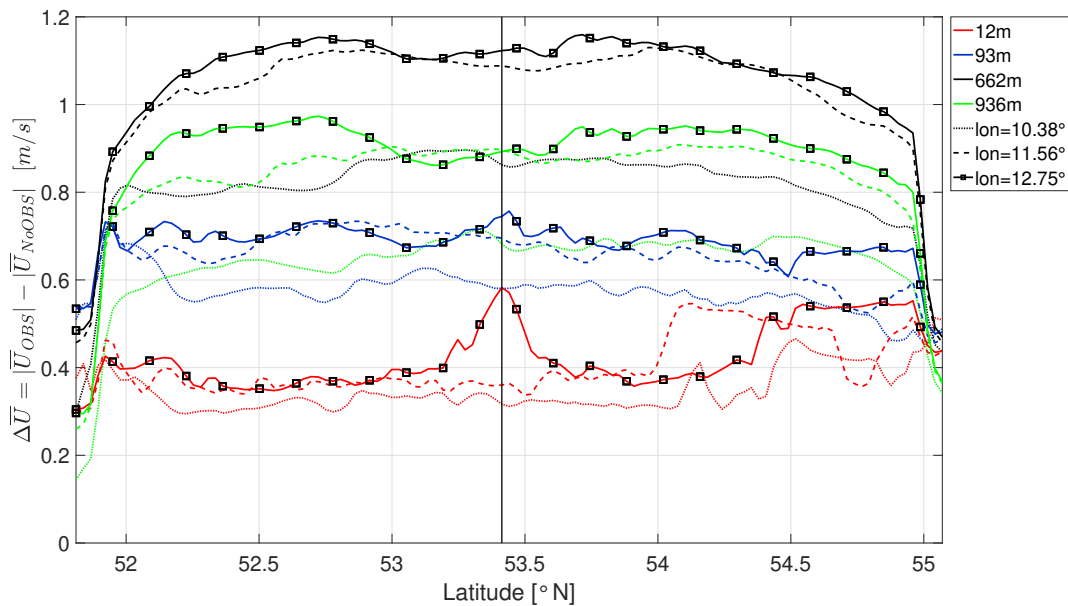
(c) NoOBS

Figure 4. Visualization of modeled and measured 10-minute mean wind speed, wind direction for 21st September 2015. The respective top figure shows the wind speed and WRF calculated SHF (dashed line). The bottom figure shows each hours 10 minute mean wind speed profile colored according to wind direction. X marks the altitude of highest wind speed and O the optimal operating altitude calculated as described in section 4.7

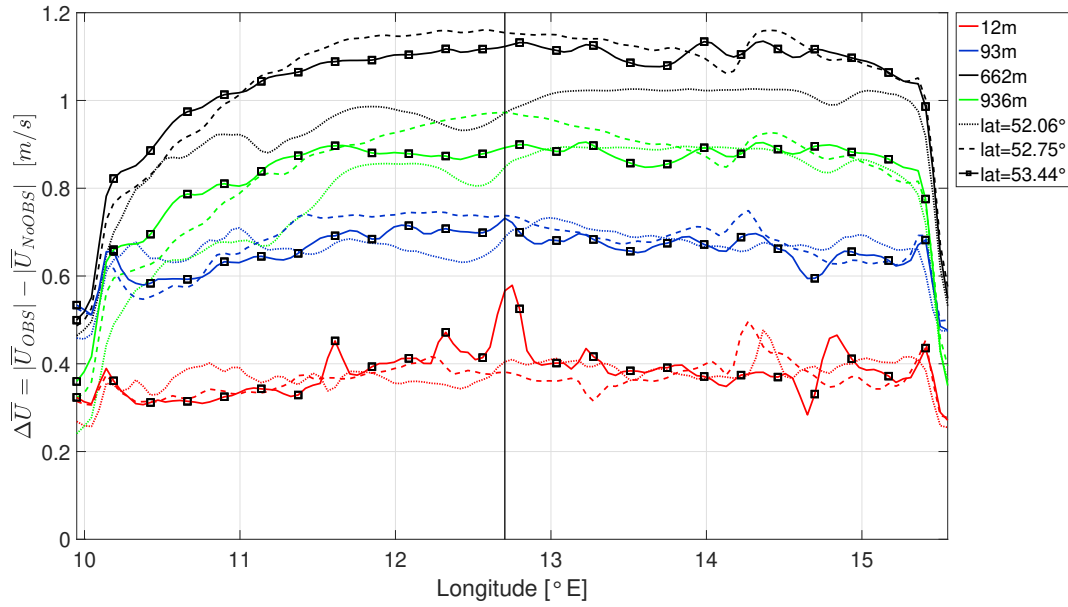


4.3 Spatial influence

Single location observation nudging influences the area within the radius of influence ($R_{xy} = 180$ km, see table A1 in the appendix) which here includes the entire inner domain ($150 \text{ km} \times 150 \text{ km}$). Figure 5 shows the mean absolute difference of horizontal wind speed ($\Delta U = |U_{OBS}| - |U_{NoOBS}|$) between the OBS and NoOBS model along lines of constant longitude and latitude for the entire simulation period. The grid cell where observations were assimilated is indicated by the vertical line and highlighted by the square marker. The four colors indicate different altitudes. As the outer domains remain unnudged, the boundary conditions of the inner domain remain the same which leads to the rapid decline in absolute difference towards the outside of the domain. Near surface results close to the measurement location experience the largest change in wind speed especially close to the surface (red line, $z = 12\text{m}$). The asymmetry could be caused by the downstream transportation of nudging effects (dominant wind direction: West).



(a) Mean absolute wind speed difference along lines of constant longitude



(b) Mean absolute wind speed difference along lines of constant latitude

Figure 5. Mean absolute wind speed difference $\Delta \overline{U}_{WRF}$ along lines of constant longitude (top) and latitude (bottom) within the nudged domain. Approximate distance of $d_3 \approx 180km$ (dotted lines), $d_2 \approx 75km$ (dashed lines), $d_1 \approx 0km$ (solid line) from the center (Lat: $53^\circ 10' 47.00''N$, Lon: $12^\circ 11' 20.98''E$).

The effect of observation nudging on horizontal wind speed remains almost unchanged along lines of constant longitude or latitude. The difference peaks between $400m$ and $600m$ and drops towards higher altitudes (as seen in figure 6) which shows the average absolute difference in wind speed along a slice of constant longitude and latitude through the center cell of the inner domain for the entire simulation period. Wind speeds at low and high altitudes are less affected by nudging while OBS
 5 wind speeds at mid-altitudes throughout the entire domain tend to be lower than the reference NoOBS. This can be attributed to surface and geostrophic effects dominating over observation nudging. The reduction in available high-altitude LiDAR data (see section 2) also reduces the effect of high-altitude nudging.

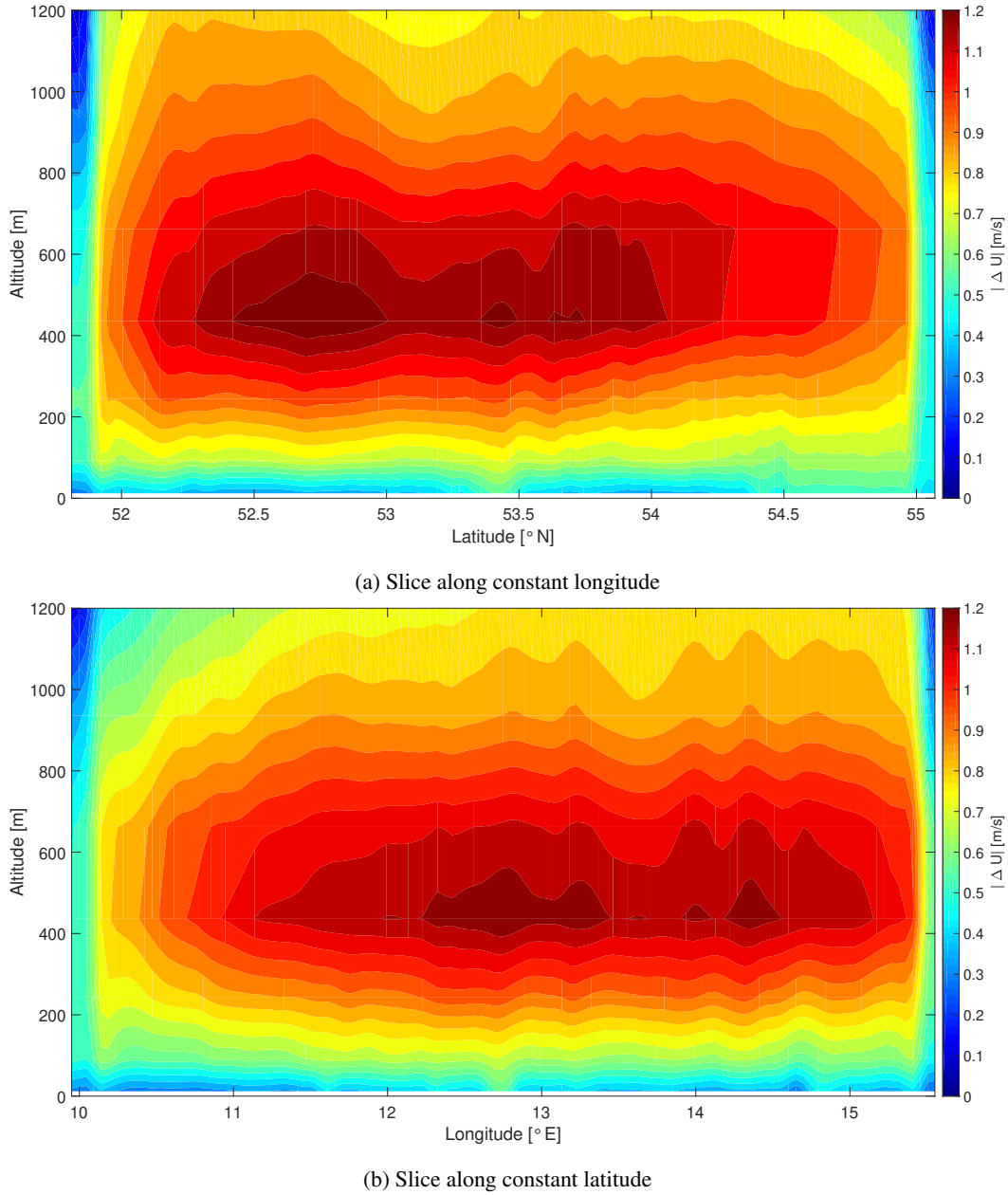


Figure 6. Absolute difference in horizontal wind speed $\Delta \overline{U}_{WRF}$ along lines of constant longitude (Lon: 12° 11' 20.98"E) and constant latitude (Lat: 53° 10' 47.00"N) through the center nudging point (i.e. the LiDAR measurement location).

4.4 Diurnal Variability

Average diurnal variation indicates typical wind speed variations for a given location and period. It further reinforces the benefit of dynamically adapting operating altitudes of AWES. The hourly average LiDAR wind speed depends on data availability



described in section 2. LiDAR availability below 100m on average decreases by about 10 percentage points during the noon hours, while it remains fairly constant at altitudes between 100m and 300m. Above this altitude, data availability increases in the afternoon by up to about 15 percentage points (Sommerfeld et al.).

Figure 7 shows the LiDAR measured and mesoscale modeled diurnal wind speed variation at the measurement location filtered by LiDAR availability, i.e. times where no LiDAR data were available were disregarded. A clear diurnal wind speed variation resulting from the cycle of stable and unstable stratification can be identified. On average OBS shows lower hourly wind speeds than NoOBS and is closer to measurements. The diurnal variation of the 6 months OBS, the 6 months NoOBS the 12 months NoOBS unfiltered data sets (Figure 8) deviate significantly from the measurements. Observation nudging leads to overall lower wind speeds and wind shear throughout the day in the unfiltered data set. Due to the large difference in average measured and unfiltered modeled diurnal wind speeds, it seems that LiDAR measurements alone can not appropriately represent average wind conditions aloft due to availability bias. Therefore, we believe that the nudged data set yields more representative results than the unnudged model or the measurements alone.

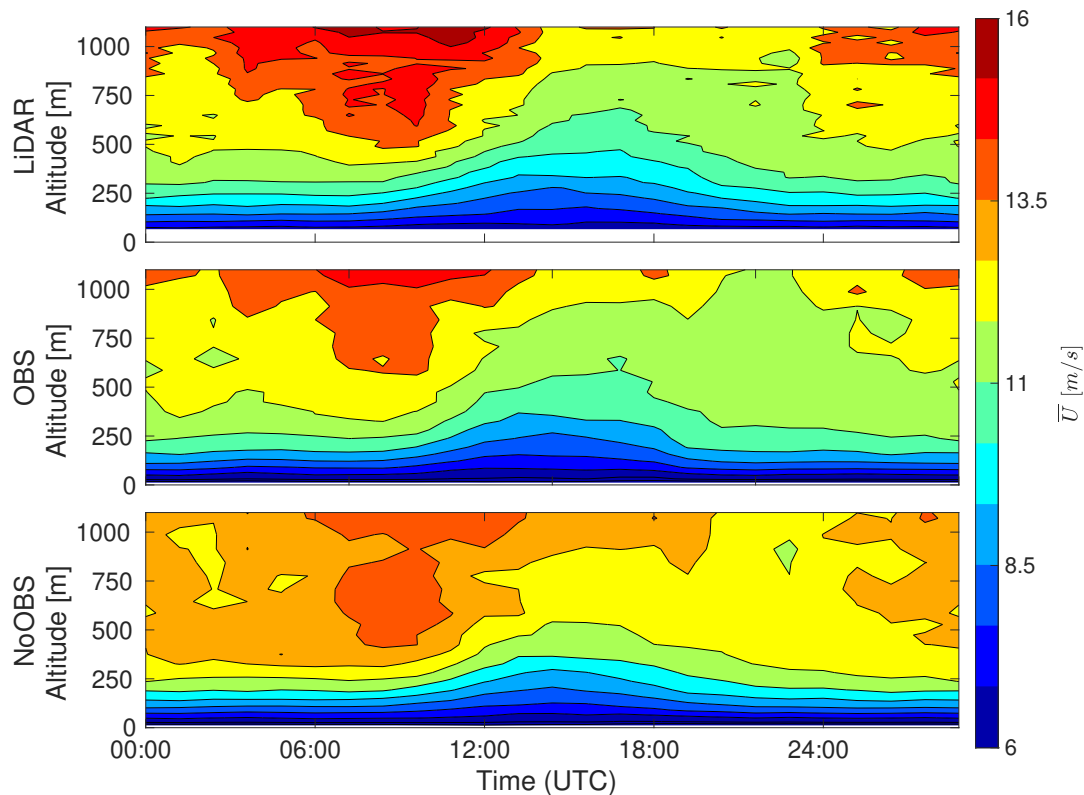


Figure 7. Hourly average diurnal variation of measured (top), OBS (center) and NoOBS (bottom) modeled horizontal wind speed \bar{U} filtered by LiDAR availability.

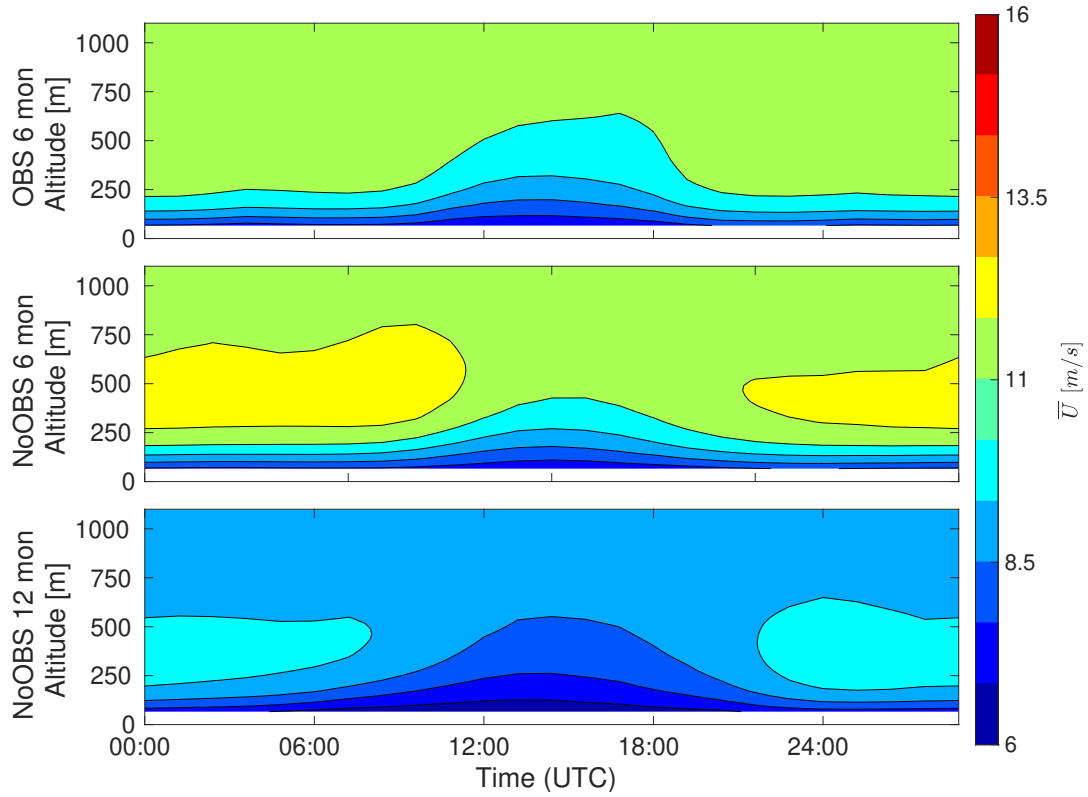


Figure 8. Hourly average diurnal variation of unfiltered OBS (top), 6 months NoOBS (center) and 12 months NoOBS (bottom) modeled horizontal wind speed \bar{U} filtered by LiDAR availability.

4.5 Wind speed probability distribution

The common way to approximate the probability distribution of the horizontal wind speed $f(U)$ is the *Weibull distribution fit* (equation 3) which describes the statistical distribution as a function of the scale parameter A and the shape parameter k (Troen and Lundtang Petersen, 1989).

$$f_{Weibull}(u) = \frac{k}{A} \left(\frac{u}{A}\right)^{k-1} e^{-\left(\frac{u}{A}\right)^k} \quad (3)$$

Previous investigation of the LiDAR measurements showed a multi-modality in the wind speed probability distribution caused by different atmospheric stability (Sommerfeld et al.). The left column in figure 9 visualizes the entire wind speed probability distribution. Its corresponding Weibull fit is shown in the center column and the difference between both can be found on the right hand side. Each row summarizes the various data sets first 6 months LiDAR, then 6 months

10 NoOBS followed by 12 months NoOBS.

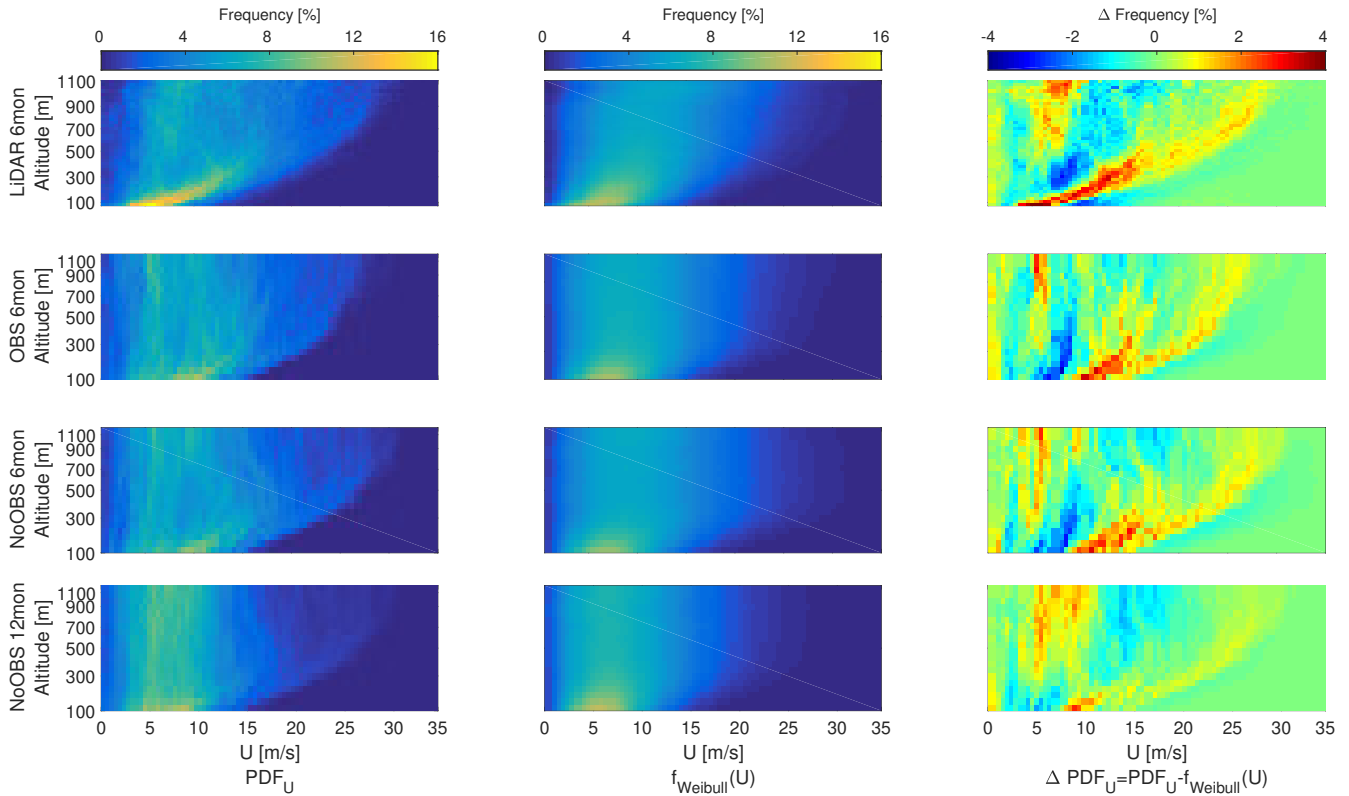


Figure 9. Probability distribution (left), Weibull fit (center) and difference between both (right) of 6 months LiDAR measurements (top row), 6 months OBS model (second row), 6 months NoOBS model (third row) and 12 months NoOBS (bottom row). The entire, (not filtered by LiDAR data availability) was used.

All 6 months data sets show a high occurrence of low and high wind speeds which indicates a multi-modal probability distribution. This effect is most pronounced in the LiDAR data set. The comparison of wind speed PDF with the Weibull fit (right column) further emphasizes the multi-modality as a simple Weibull fit is not able to capture the higher probability at low and high wind speeds. These distinct flow situations further drift apart with increasing surface distance. As a result the Weibull distribution overestimates occurrence of wind speeds in between the two peaks (blue area in right column). Both OBS and NoOBS slightly overestimate low altitude wind speed (see figure 3) compared to LiDAR measurements. Both models and the LiDAR measurements show a broadening of the probability distribution towards higher altitudes. High wind speeds become more likely while low wind speeds still occur. Therefore, AWES need to be able to operate in a wide range of wind speeds or be controlled in a way that they avoid extreme conditions. The 12 months NoOBS simulation shows lower wind speeds than the 6 months simulations as the included summer months generally have lower wind speeds due to higher probability of unstable stratification. The Weibull fit of this simulation tends to overestimate higher wind speeds and underestimate low wind speeds at all altitudes.



We use the sign of the WRF-calculated SHF as a simple proxy to differentiate stable and unstable wind conditions similar to (Sommerfeld et al.). The wind speed probability distribution follow the expected trends of low wind shear during unstable stratification and higher wind shear and wind speeds during stable stratification (?). Observation nudging reduces the occurrence of high wind speeds at high altitudes in comparison to NoOBS and leads to an increase in the probability of wind speeds around 5 m/s during times of positive SHF. The Weibull distribution fit of these sub-states is generally better at representing the modeled wind conditions.

Figure 10 shows the scale parameter A , shape parameter k and Hellinger distance H (Rüschendorf, 2014) between the wind speed PDF and the corresponding Weibull distribution fit for LiDAR (1st row), 6 months OBS (2nd row), 6 months NoOBS (3rd row) and 12 months NoOBS (4th row).

The different trends under positive and negative SHF of both Weibull parameters visualize the existence of entirely different flow regimes. The Hellinger distance between the Weibull fit and PDF (negative SHF: blue and positive SHF: red), the total data and a simple fit (black) as well as between the total data and the weighted sum of both Weibull fits (green) is shown in the right graph. All WRF models show an overall smaller H than a similar analysis of the LiDAR data set (see (Sommerfeld et al.)). The sharp bend in both A and k of the LiDAR data above 750 m is likely caused by insufficient data availability. NoOBS results show a sharp increase of A up to 250 m and a slight reduction above while OBS shows a trend close to the surface, A values remain almost constant above 500 m. No data set shows a convergence of A at higher altitudes indicating that these wind conditions are driven by different conditions in the free atmosphere. 12 months NoOBS simulations show lower scale parameter values as they include generally slower winds during summer. While A trends are quite different for LiDAR and WRF, k trends are more similar. They peak between 150 and 250 m and are especially high during stable stratification (Monahan et al., 2011). OBS trends of k are generally closer to measurement results than NoOBS.

Even though the Hellinger distance of individual Weibull fits for times of positive or negative SHF is generally higher than the Weibull fit of the entire data set, the weighted sum of both individual fits yields the best result at all altitudes.

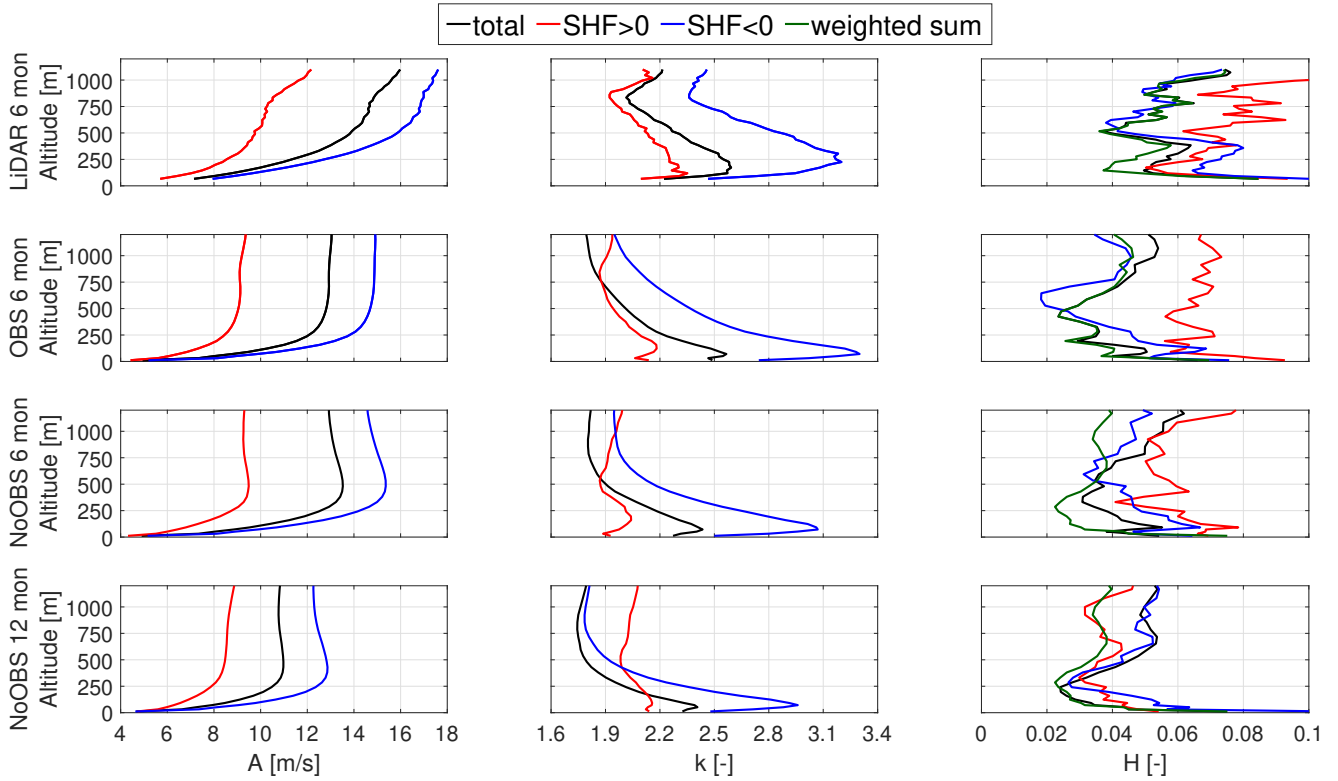


Figure 10. Weibull parameter trends over altitude and goodness of fit quantified by the Hellinger distance (right) over altitude for 6 months of LiDAR measurements (1st row), the 6 months OBS model (2nd row), 6 months NoOBS model (3rd row) and the 12 months NoOBS model (4th row)

4.6 Effect of stability on average wind shear

Atmospheric stability highly influences the shape of wind speed profiles which is important for determining optimal operating conditions for AWES (see section 4.7). We quantify the impact of observation nudging on various stability classes defined by the Obukhov length L_{WRF} (Obukhov, 1971) calculated from simulated friction velocity u_* , potential temperature θ , sensible surface heat flux SHF , the von Kármán constant k and gravitational acceleration g :

$$L_{WRF} = \frac{-u_*^3 \theta}{kg H_{sfc}} \quad (4)$$

Table 2 summarizes the Obukhov length bins and frequency of occurrence of each stability class.



Table 2. Stability classes according to Obukhov length calculated based on WRF results (Floors et al., 2011)

Stability classes	L [m]	# OBS 6 mon	# NoOBS 6 mon	# NoOBS 12 mon
Unstable (u)	$-200 \leq L_{WRF} \leq -100$	1509	1042	3827
Near unstable (nu)	$-500 \leq L_{WRF} \leq -200$	2121	1658	3736
Neutral (n)	$ L_{WRF} \geq 500$	7342	7648	10756
Near stable (ns)	$200 \leq L_{WRF} \leq 500$	4791	4987	6590
Stable (s)	$50 \leq L_{WRF} \leq 200$	4862	4861	9114
Very stable (vs)	$10 \leq L_{WRF} \leq 50$	1567	1765	5306
Other	$-100 \leq L_{WRF} \leq 10$	3729	3960	13231

In comparison with the unnudged simulation, OBS shows an increase in unstable and near unstable situations. Stable and near stable stratification seems almost unaffected by OBS nudging, while neutral and very stable stratification occur slightly less often. This might improve the overall predicting capabilities of WRF as the MYNN 2.5 boundary layer scheme overestimates the frequency of very stable conditions with an error of up to 9 % (Krogsæter and Reuder, 2015). Neutral conditions, still commonly used in many wind energy siting applications, only occur about 30 % of the time during the measurement period and only about 20 % of the time during the one year reference NoOBS simulation.

Figure 11 shows the mean wind speed profiles categorized and normalized by the corresponding friction velocity u_* . We assumed that the nudged simulation is sufficiently close to measurements and use the same categorization as in OBS, since no measurements were available to determine L_{LiDAR} . All profiles follow expected trends with unstable profiles showing the smallest wind shear and stable profiles showing the largest. Altitudes below 200 m are least affected by observation nudging as OBS remains almost unchanged from NoOBS (see section 4.1). Both models are in good accordance with measurements during unstable and near unstable conditions. The stable and very stable profiles of the unnudged simulation show a peak at around 300 m which is indicative of a characteristic low level jet. The more irregular trend of the very stable LiDAR data set could be caused by a small sample size since only 5 % of the overall data is considered very stable.

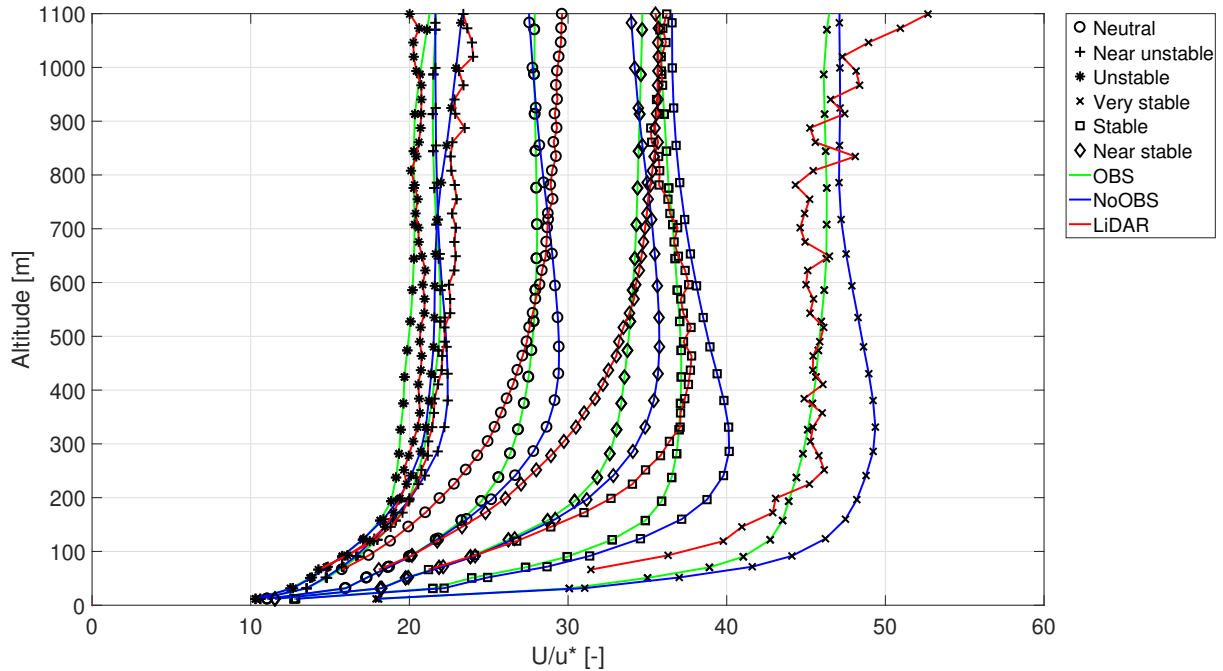


Figure 11. 6 months mean HWS profiles of LiDAR, OBS and NoOBS data classified by stability class defined by Obukhov length (table 2).

Expanding on the previous approach (subsection 4.5) of splitting the data into times of positive and negative SHF to differentiate states of unstable and stable stratification, we make use of k-means clustering (Lloyd, 1982) to identify 2 additional sub-states to better differentiate between the different flow situations associated with very stable and stable stratification. We chose to differentiate additional two sub-states which identify stable and very stable as well as unstable and shear driven conditions. LiDAR results for reference can be found in (Sommerfeld et al.). Figures 12 to ?? show the probability distribution of each sub-state for each model with the cluster centroids highlighted by white squares. All clusters show distinct trends that are consistent between data sets. The top left plot in each figure shows the probability distribution of a typical unstable stratification with low wind shear all the way up to 1100 m. The top right plot shows statistics of shear-driven wind profiles that occur during times of positive SHF. Stable (bottom right) and very stable stratification (bottom left) are characterized by strong wind shear and higher average wind speeds. NoOBS predicts a higher chance of wind speed reduction during very stable stratification above 600 m while wind speeds in OBS steadily increase up to 1100 m. Both models indicate the existence of LLJ during stable stratification between 200 and 400 m. The difference in high altitude wind speeds indicate the influence of different geostrophic winds.

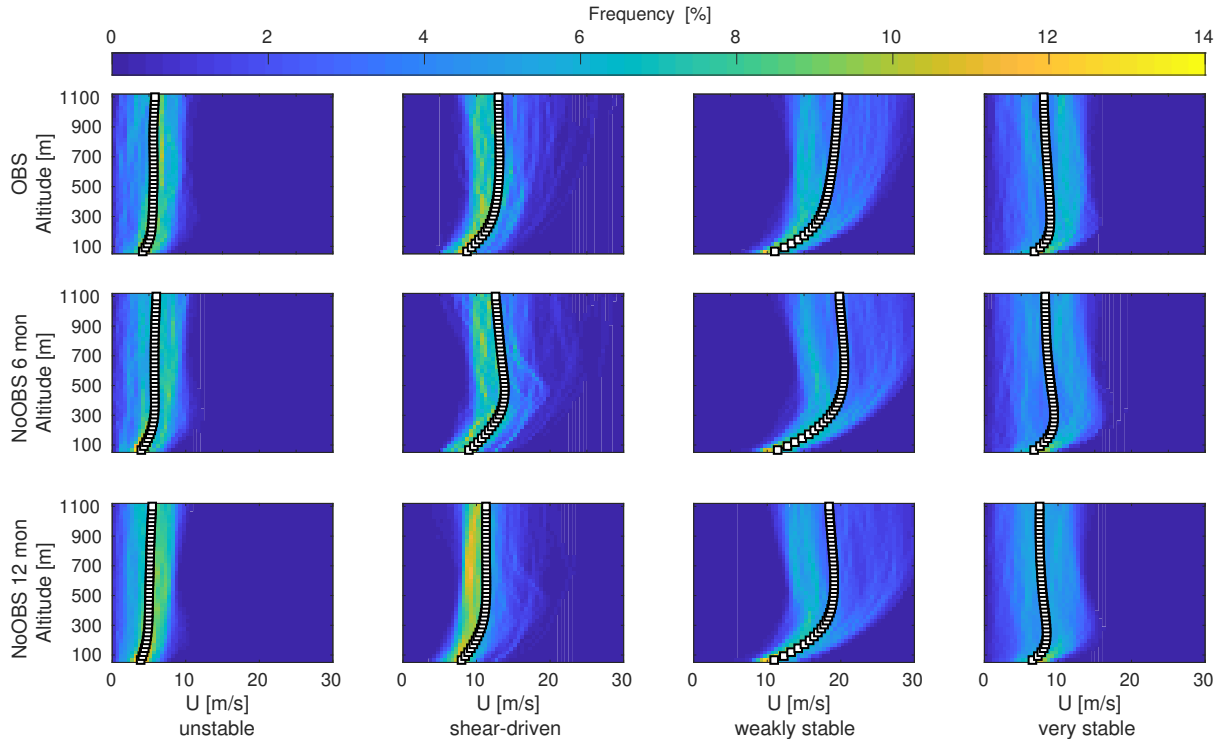


Figure 12. Probability density function and mean (white square) of k-means clustered, SHF allocated OBS, 6 months NoOBS and 12 months NoOBS data. The two leftmost columns show times of positive SHF and the two rightmost columns times of negative SHF.

4.7 Optimal operating altitude and power production

We estimate optimal operating altitude and traction power of a ground-generator AWES using a simple ground-generator (pumping-mode) AWES model adapted from Schmehl et al. (2013). We focus on OBS as we previously proved increased accuracy and use 12 months NoOBS to estimate annual values. The estimated optimal power per unit lifting area of the wing

5 p_{opt} is described by:

$$p_{opt} = \frac{\rho_{air}}{2} U^3 \sqrt{c_L^2 + c_D^2} \left[1 + \frac{c_L}{c_D} \right]^2 f_{opt} (\cos \theta \cos \phi - f_{opt})^2 \quad (5)$$

Air density ρ_{air} is calculated by a linear approximation of the standard atmosphere Champion et al. ($\rho_{air}(z) = 1.225 \text{ kg m}^{-3} - 0.00011z \text{ kg m}^{-4}$). Losses associated with misalignment of the wind direction and the aircraft position (azimuth angle ϕ , elevation angle θ) are included in the model. Additional losses caused by gravity and tether drag are neglected. As a result, lift

10 F_L and drag F_D force and therefore lift ($c_L=1.7$) and drag coefficient and drag coefficient ($c_D=0.06$) are assumed constant are geometrically related to the radial ($v_{a,r} = (\cos \theta \cos \phi - f)U$) and tangential ($v_{a,t} = (\cos \theta \cos \phi - f)U \frac{F_L}{F_D}$) apparent velocity components. The tether speed v_t is non-dimensionalized in the form of the reeling factor ($f = \frac{v_t}{U}$). Assuming an optimal non-



dimensional reeling factor ($f_{opt} = \frac{1}{3} \cos \theta \cos \phi$) and a quasi-steady state with the wing moving directly cross-wind with a zero azimuth angle ($\phi = 0$) relative to the wind direction we can estimate the optimal traction power.

Figure 13 summarizes the probability distribution of optimal operating altitude and optimal power with the white solid line showing the cumulative frequency of optimal operating altitude. Both simulations for this particular location and time period show similar trends with the most probable optimal altitude between approximately 200 and 400 m. Times of very high traction power are fairly rare and likely associated with low level jets. Lower power at higher altitudes is caused by the misalignment losses. Here we assume a constant tether length of 1500 m.

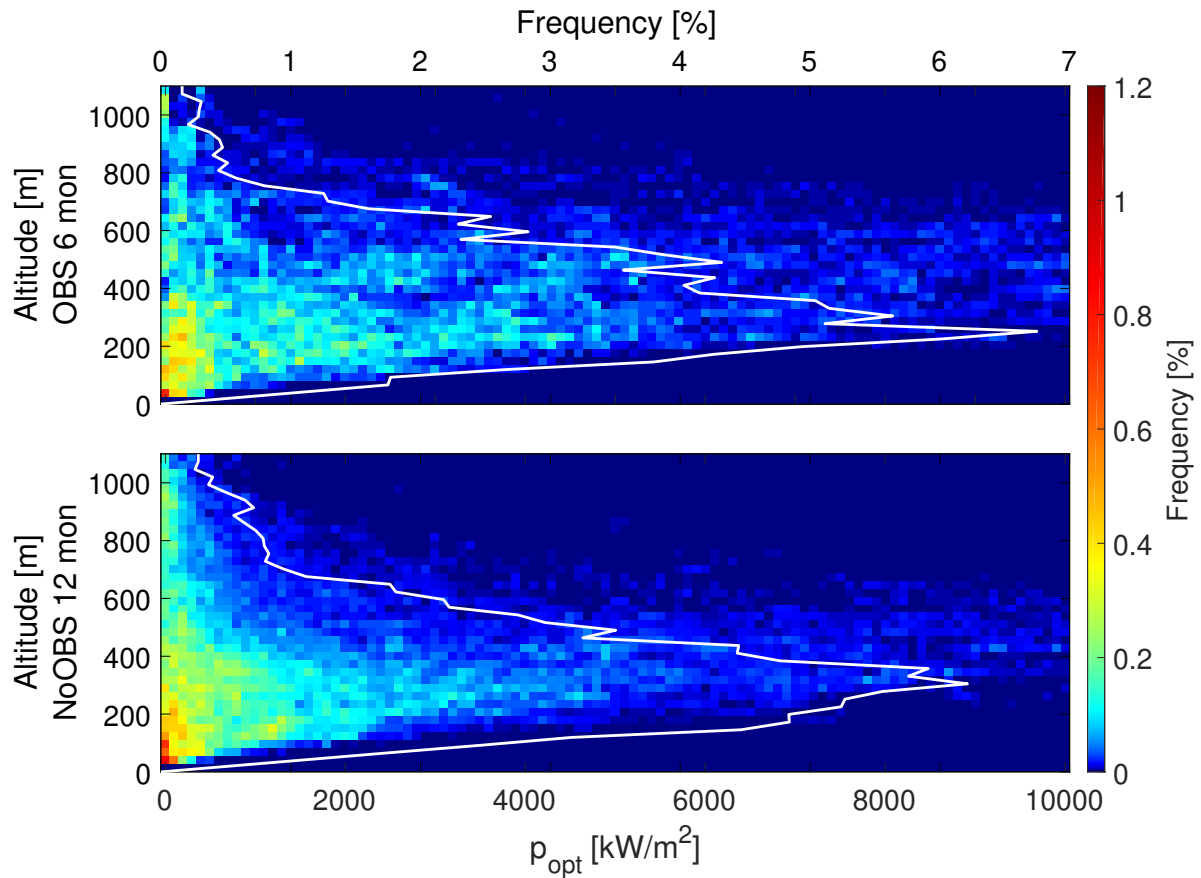


Figure 13. Probability of optimal traction power over optimal operating altitude based on a) 6 months LiDAR, b) 6 months OBS, c) 6 months NoOBS and d) 12 months NoOBS. The continuous white line shows the frequency of optimal operating altitude for the whole power range (top abscissa axis).

Figures 14 estimates the optimal traction power and operating altitude as a function of tether length based on the wind speed clustered average profiles shown in figure 12. The axis limits of different atmospheric conditions had to be adjusted as the



calculated power varied in order of magnitudes. All estimates show diminishing benefits of a longer tether. These incremental gains would probably be negated by additional drag and weight associated losses. Winds during times of very stable and unstable stratification lead to a clear optimal altitude independent of tether length between 200 and 400 m while weakly stable and shear-driven wind speed profiles lead to higher optimal operating altitudes and a broader range of optimal altitudes as a function of tether length.

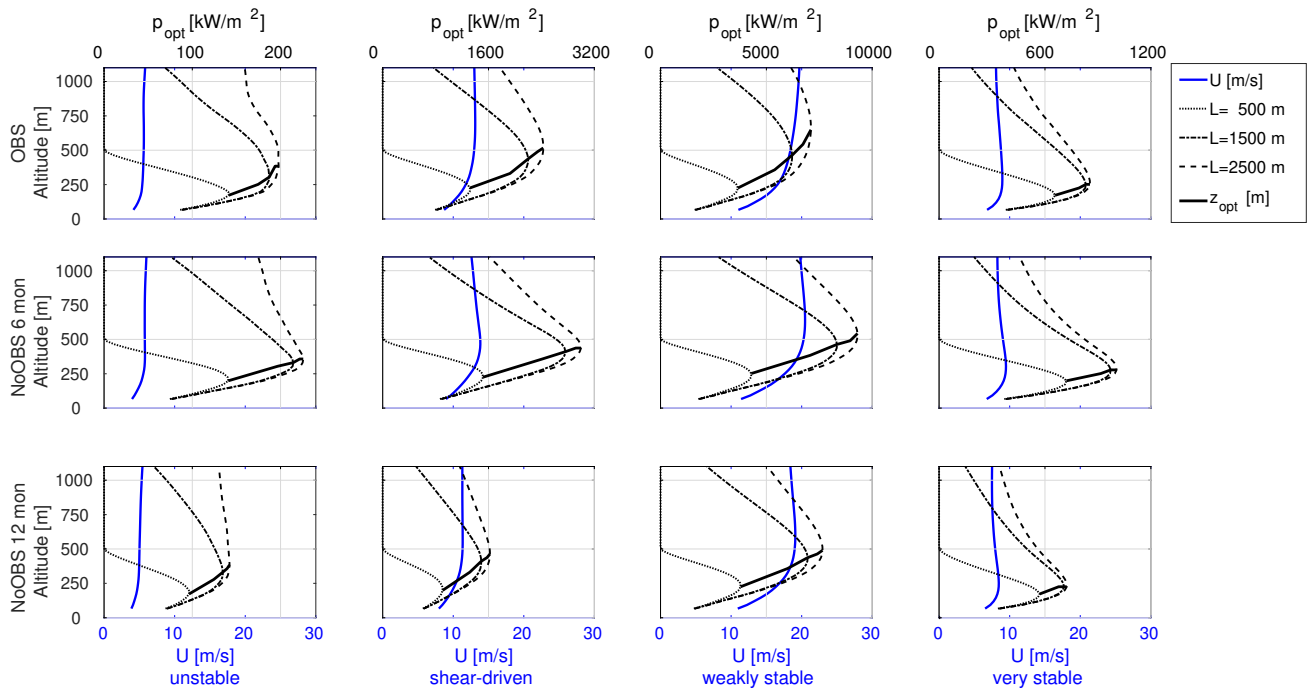


Figure 14. Optimal traction power per wing area p_{opt} (dashed lines) and optimal operational altitude (solid line) estimated based on mean k-means-clustered SHF-sampled wind speed profiles of 6 months OBS, 6 months NoOBS and 12 months NoOBS simulation for varying tether length ($L = 500 - 2500$ m)

5 Conclusions

Six months LiDAR measurements up to 1100 m were assimilated in WRF using observation nudging. An unnudged reference model (NoOBS), the nudged model (OBS) outputs and LiDAR measurements were compared in terms of wind speed and direction statistics, wind profile shape as well as spatial differences were quantified. Observation nudging only has marginal impact on simulated surface layer wind speeds as ground effects dominate the WRF model. Wind speeds between 300 and 500 m were most affected by observation nudging. Modeled wind speeds at these altitudes are statistically closest to measurements, making this an excellent approach for resource assessment of mid-altitude wind energy systems as measurement availability decreases. The impact of nudging weakens above these altitudes. Whether this is caused by lower measurement data availability



or a generally higher performance of the mesoscale model above the surface layer could not be determined. Observation nudging reduced the seemingly systematic wind direction bias between simulation and measurements at all altitudes. Due to the lack of high resolution measurements, unnudged mesoscale model data present the best we have got in terms of preliminary resource assessment.

- 5 Filtering the mesoscale model data according to LiDAR data availability yields similar diurnal variation with OBS being closer to measurements. Comparing the diurnal variation of the unfiltered model wind speeds to measurements shows a significant deviation which is likely caused by insufficient LiDAR data availability at higher altitudes. LiDAR measurements seem to be biased towards high wind speeds as measured winds are generally higher than the unfiltered mesoscale model data. The impact of observation nudging on the wind profiles in case of an unstably stratified boundary layer is relatively low while wind speed profiles under stable stratification are significantly affected and overall closer to measurements especially between 200 and 600 m. Variations of stratification, primarily those associated with the diurnal cycle, lead to a multi-modal wind speed probability distribution which is better represented by the weighted sum of two Weibull fits than by a single Weibull fit.

- 10 Using a simplified AWES model, assuming a constant tether length of 1500 m and neglecting drag and weight all data sets suggested an optimal operating altitude between 150 and 400 m. However, since stratification leads to a vast range of wind speed profiles AWES greatly benefit from dynamically adapting their operating altitude to maximize power production and minimize losses.

- 15 Future studies include using the enhanced mesoscale model output to drive large-eddy simulations, to provide a better insight into mid-altitude turbulence. The resulting data set will lead to the development of a mid-altitude engineering (spectral) wind model which can be used for design, load estimation, control and optimization of Airborne Wind Energy Systems. Mesoscale model data could be implemented into an AWES optimization framework to quantify the impact of various wind speed profiles on power production, optimal trajectory and system size. Furthermore, the possibility of merging the mesoscale output with LiDAR measurements to fill gaps in the measurement data set is being investigated.



Appendix A

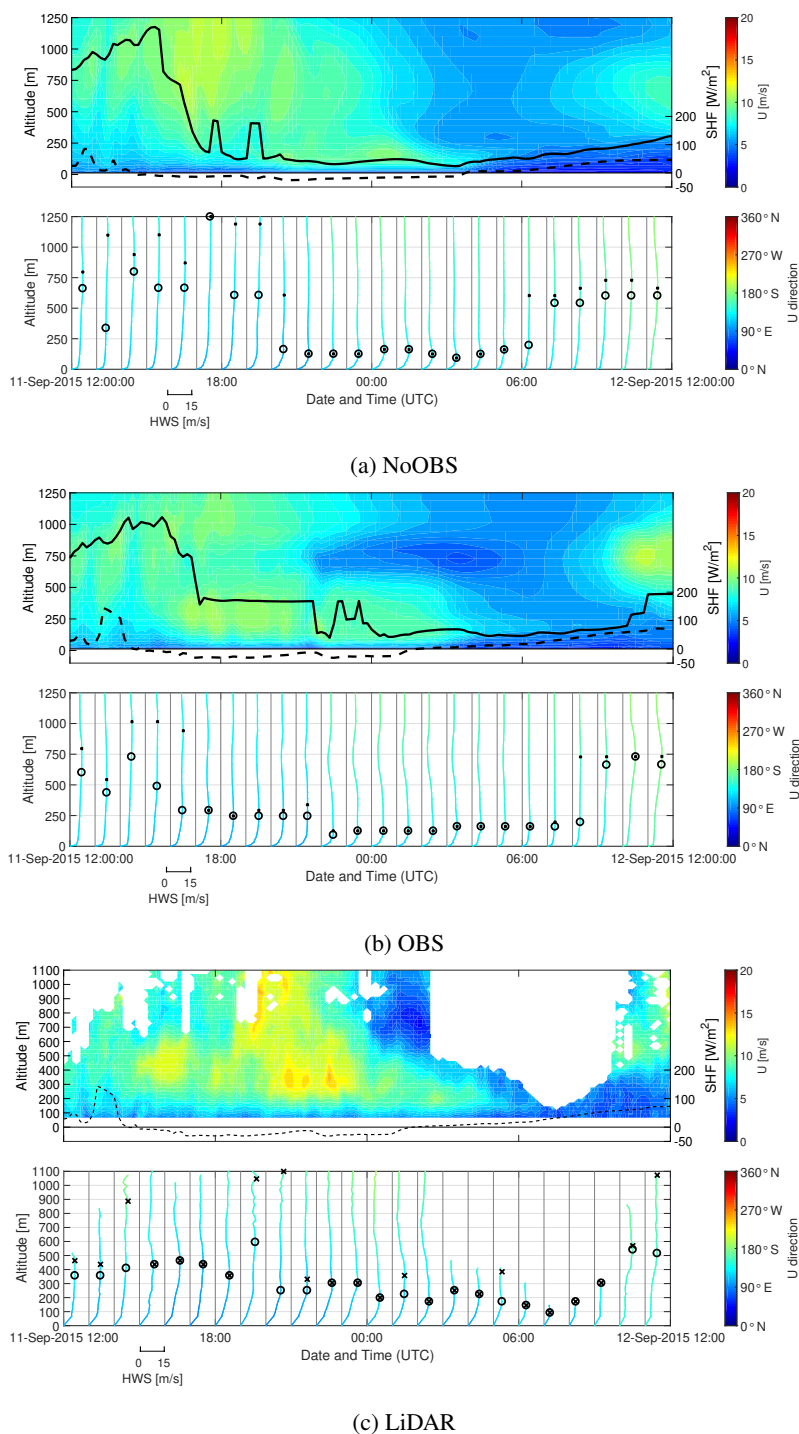


Figure A1. Contour plot and U profile; instead plot contour plots beneath each other and all profiles in 1 plot?



Table A1. WRF Observation nudging settings

WRF input parameter	value
grid_fdda	1,1,1,
gfdda_inname	"wrffdda_d<domain>",
gfdda_end_h	99999, 99999, 99999,
gfdda_interval_m	360, 360, 360,
fgdt	0, 0, 0,
if_no_pbl_nudging_uv	0, 0, 1,
if_no_pbl_nudging_t	0, 0, 1,
if_no_pbl_nudging_q	0, 0, 1,
if_zfac_uv	0, 0, 0,
k_zfac_uv	0, 0, 30,
if_zfac_t	0, 0, 0,
k_zfac_t	0, 0, 30,
if_zfac_q	0, 0, 0,
k_zfac_q	0, 0, 30,
guv	0.0003, 0.0003, 0.0003,
gt	0.0003, 0.0003, 0.0003,
gq	0.0003, 0.0003, 0.0003,
if_ramping	1,
dtramp_min	60.0,
io_form_gfdda	2,



WRF input parameter	value
obs_nudge_opt	0,0,1
Cressman Scheme	1
time_step	60
obs_rinxy	240,240,180
obs_rinsig	0.1
obs_twindo	3, 3,3
auxinput11_interval_s	360, 360, 360
obs_dtramp	40
obs_nudge_wind	1,1,1
obs_coef_wind	6.E-4,6.E-4,6.E-4
iobs_onf	2,2,2
auxinput11_interval_s	360, 360, 360
auxinput11_end_h	6, 6, 6
if_no_pbl_nudging_uv	0, 0, 1
if_zfac_uv (max_dom)	0,0,30
sf_sfclay_physics	5, 5, 5
sf_surface_physics	4, 4, 4
bl_pbl_physics (max_dom)	5, 5, 5
bl_mynn_tkeadvect	.true.,.true.,.true.
ra_lw_physics	1 ,1,1
ra_sw_physics	1 ,1,1
mp_physics	5, 5, 5

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