

The digital terrain model in the computational modelling of the flow over the Perdigão site: the appropriate grid size

authored by

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Reply to the Associate Editor (Jakob Mann)

Dear Jakob

Please find herewith, our response to your review. After a box, with your text, we address every comment, suggestion or request (either unnumbered or numbered) in two separate sections. I hope that our response is satisfactory and the manuscript can proceed for publication.

Regards
Jose

Associate Editor Decision: Publish subject to minor revisions (review by editor) (22 Jun 2020) by Jakob Mann

Comments to the Author:

The reviews of the paper are quite critical and you chose not to comply with many of the comments. However, I think you need to be more clear in the conclusion about the limitations as both the reviewer request. It should be very clear, also in the conclusion, that the "threshold resolution" is only valid for this particular terrain. It should also be stated that this is not a critical investigation of flow result but that the flow solver is only used to estimate the impact of terrain resolution on the flow. The unrealism of the roughness should also be mentioned there. Please include these matters in the conclusion. You may then call the section "Discussion and conclusion". It is strange that most of the correction in the track changes document are not really changes like "flow" -> "flow" many places in the abstract and so in the rest of the paper. Did something go wrong?

Apart from these changes I would like you to

- 1) change figure 1: Remove strange box to the left in a). Make the height legend clearer (and with less significant digits. For b) explain the red dots in the figure caption.
- 2) Figure 11: This is three almost identical figures?!
- 3) I 297 bad reference "Table ??" and I 62 bad ref to citation.
- 4) refer to report with more details on the data and where they can be downloaded.

I think the paper is an important and unique contribution, but a bit more care in including the essence of the reviewers criticism is needed and also a bit more care in the preparation of the manuscript.

1 Unnumbered comments or requests

- The reviews of the paper are quite critical and you chose not to comply with many of the comments.

REPLY:

In our opinion, the criticism of both reviewers is entirely understandable and expectable. Our work is not conventional in the context of neither wind energy nor flow modelling, although being relevant in both areas of application. For instance, many of the references in section 1.1 (Literature survey) are related to geomorphology, aerial surveying or digital terrain modelling, in line with the title. When answering the reviewers, we intended to make this point and, of course, to comply with all their comments.

- However, I think you need to be more clear in the conclusion about the limitations as both the reviewer request. It should be very clear, also in the conclusion, that the "threshold resolution" is only valid for this particular terrain.

REPLY:

Because it is not the "threshold resolution" only, the conclusions end with the following sentence:

The conclusions hold under the conditions of the present work, namely terrain data and flow model equations and conditions. Under different conditions, further validation may be required.

- It should also be stated that this is not a critical investigation of flow result but that the flow solver is only used to estimate the impact of terrain resolution on the flow.

REPLY:

That note is already at the introduction of Section 5 on Flow modelling:

Because computational results do not consider, for instance, surface cover heterogeneity, discrepancies are expected when compared with experimental data, which are included here for guidance only.

- The unrealism of the roughness should also be mentioned there. Please include these matters in the conclusion.

REPLY:

A new text was added at the end of section 5.1.1

However, this [other option than uniform roughness] would increase the number of variables influencing the flow results, masking the effects of the digital terrain model alone. See for instance, the effects of forest resolution and wind orientation relative to the forest stands in the computational modelling of flow over forests in Lopes da Costa et al. (2006).

The final sentence at the end of the conclusions also covers the case of uniform roughness.

- You may then call the section “Discussion and conclusion”.

REPLY:

The final section was renamed “Discussion and conclusions”, as suggested.

- It is strange that most of the correction in the track changes document are not really changes like “flow” → “flow” many places in the abstract and so in the rest of the paper. Did something go wrong?

REPLY:

The initial version of the manuscript was written with ligatures (`fi`, `fl`, `ff`), as opposed to the latest one, without ligatures (`f\i`, `f\l`, `f\f`). The LaTeX package (*latexdiff*) used to identify the differences between pdf documents operates on the `.tex` files and identifies these differences hardly noticed in naked eye. In the latest version, the difference is not on the actual word “flow”, but on the increased spacing between the `f` and the `l`. The same applies to any word with the letter combinations `fi`, `fl` or `ff`.

2 Numbered requests

- 1) change figure 1: Remove strange box to the left in a). Make the height legend clearer (and with less significant digits. For b) explain the red dots in the figure caption.

REPLY:

Figure 1a) was of low quality and unnecessary; because it showed the terrain elevation, repeating information available in other (higher quality) figures, later in the manuscript. Figure 1a) should have been the point density, illustrating the information in the first paragraph. About Figure 1b), explanation on the red dots was included, as requested.

- 2) Figure 11: This is three almost identical figures?!

REPLY:

Yes, they are three almost identical figures. The differences appear at the right end of the horizontal scale; where they should, at the limits of the resolution of either DTM source (SRTM, Mil or ALS). This type of representation is not so uncommon in geomorphology (Nikora and Goring, 2004). Alternative representations, such as histogram would be worse in their ability to show the resolution of the finest terrain details.

The figures are complex and the interpretation is not easy. Thick lines are the spectra of DTM sources and thin lines the spectra of numerical meshes of different resolution obtained on those sources. The colour code identifies the DTM source. Moving from figures a) to c) (DTM of increasing order of resolution) the numerical meshes (80, 40, 20 and 10 m) are closer to the thick green line; i.e., tend to follow the highest resolution map (ALS). Because, in some cases, the thin and thick lines overlap, the end of every thin line is signalled with

an arrow. In the discussion of these figures, we tried to call the reader's attention to those small and important differences between the three sub-figures.

Figure 11 was redrawn to improve its readability.

3) l 297 bad reference "Table ??" and l 62 bad ref to citation.

REPLY:

You are referring to the file named `Diff` (the outcome of the LaTeX package *latexdiff*), with the differences between the initial and the revised versions of our manuscript. The file `wes-2019-96-manuscript-version3.pdf` (revised version), uploaded on 15 Apr 2020, was the one to look at, and there you can see that the reference to Table (Table 6) in line 286 (equivalent to line 297, in file `Diff`) is right¹. The same applies to line 62; i.e., line 61 in file `wes-2019-96-manuscript-version3.pdf`, where the reference is also correct.

In both cases, we are not sure why that happened. The documentation on *latexdiff* mentions some bugs, which might have been the case. After searching ? on the `Diff` file, we found two more question marks: at lines 76 and 317.

4) refer to report with more details on the data and where they can be downloaded.

REPLY:

The report entitled *Land characterisation of the Perdigão site: data guide* (Palma et al., 2020) is cited at the end of subsection 2.1, beginning of section 4, end of subsection 5.2, and under *Data availability* at the end of the paper.

New figures: apart from 1a and 11, Figures 14, 15 and 16 were also redrawn.

References

- V. Nikora and D. Goring. Mars topography: bulk statistics and spectral scaling. *Chaos, Solitons & Fractals*, 19(2):427–439, January 2004. ISSN 0960-0779. doi: 10.1016/S0960-0779(03)00054-7. URL <http://www.sciencedirect.com/science/article/pii/S0960077903000547>.
- J.M.L.M. Palma, V.T.P. Batista, V.M.M.G.C. Gomes, J.A.C. Lopes, J. Mann, and E. Dellwik. Land characterisation of the Perdigão site: data guide. Technical report, University of Porto and Technical University of Denmark, 6 2020. URL <https://perdigao.fe.up.pt/api/documents/versions/353?download>. This document contains information on the structure and organisation of the files for land characterisation of the Perdigão site, namely aerial lidar survey and orthophotos, computational topography meshes, digital surface cover and digital terrain models.

¹File `wes-2019-96-manuscript-version3.pdf` (entitled `wes-2019-96.pdf`) is also available at <https://wes.copernicus.org/preprints/wes-2019-96/> after clicking the Download icon at the right-hand side of the web page. Line numbers are different.

The digital terrain model in the computational modelling of the flow over the Perdigão site: the appropriate grid size

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Abstract. The digital terrain model (DTM), the representation of Earth's surface at regularly spaced intervals, is the first input in the computational modelling of atmospheric flows. The ability of computational meshes based on high (2 m, airborne laser scanning), medium (10 m, military maps) and low (30 m, shuttle mission, SRTM) resolution DTMs to replicate the Perdigão experiment site was appraised in two ways: by their ability to replicate the two main terrain attributes, elevation and slope, and by their effect on the wind flow computational results. The effect on the flow modelling was evaluated by comparing the wind speed, wind direction and turbulent kinetic energy by VENTOS[®]/2 at three locations, representative of the wind flow in the region. It was found that the SRTM was not an accurate representation of the Perdigão site. A 40 m mesh based on the highest resolution data, yielded at five reference points an elevation error of less than 1.4 m and an RMSE of less than 2.5 m, compared to 5.0 m, in the case of military maps and 7.6 m in the case of SRTM. Mesh refinement beyond 40 m yielded no or insignificant changes on the flow field variables, wind speed, wind direction and turbulent kinetic energy. At least 40 m horizontal resolution—*threshold resolution*—, and based on topography available from aerial survey, is recommended in computational modelling of the flow over Perdigão.

1 Introduction

A Digital Terrain or Elevation Model (DTM or DEM) is a representation of the Earth's surface elevation at regularly spaced horizontal intervals. Although the terrain model is the first input in computational modelling of atmospheric flows, its impact on flow results has not been a matter of concern, because the spatial resolution of publicly available DTMs is higher than the size of the computational grid often used to resolve the terrain. However, before a fluid flow database (Mann et al., 2017) can be used as a reference in flow model appraisal and development, the impact of the terrain modelling must be assessed. For studies of the atmospheric flow over Perdigão the publicly available DTMs were considered not accurate enough (Mukherjee et al., 2013; Simpson et al., 2015) and an airborne laser scanning campaign of the region was carried out in 2015; first to assist the design of the Perdigão campaigns in 2015 and 2017 (cf., Vasiljević et al., 2017; Fernando et al., 2019) and second, to provide the high resolution terrain data for computational flow modelling, on par with the resolution provided by the large number of measuring equipment within a small region.

The Perdigão site is located in the municipality of Vila Velha de Ródão, in the centre of Portugal (608250E, 4396621N: ED50 UTM 29N or in WGS84, 39°42'38.5"N 7°44'18.5"W). It is comprised by two parallel ridges, about 500 m elevation, 4 km length, SE-NW orientation, and distanced around 1.4 km from each other. The land is covered by a mixture of farming areas and patches of eucalyptus (*Eucalyptus globulus*) and pine trees (*Pinus pinaster*). The dominant winds are perpendicular to the ridges, assuring a largely two-dimensional flow.

The accuracy of a DTM depends on the data collection techniques, data sampling density and data post-processing, such as grid resolution and interpolation algorithms. In computational modelling of atmospheric flows, DTMs are often used from photogrammetry or satellite interferometry, such as *SRTM*, *Shuttle Radar Topography Mission*, (Farr et al., 2007) or *ASTER*, *Advanced Spaceborne Thermal Emission and Reflection Radiometer* (Yamaguchi et al., 1998), freely available at <https://earthexplorer.usgs.gov/>. SRTM has the widest cover and is the most commonly used terrain data. Its latest version (V3.0 1", 2014) is 1 arc-second on most of the planet's surface, i.e. about 23.75 m resolution and an absolute height error equal to 6.2 m at Perdigão's latitude (Farr et al., 2007). With the advent of high resolution techniques such as lidar aerial survey, terrain data has become available with resolutions above 10 m and vertical accuracy typically below 0.2 m (Hawker et al., 2018), and the question is whether such high resolution is needed in the computational modelling of atmospheric flows over complex terrain.

1.1 Literature review

Grid independent calculations is a concept very dear to computational fluid dynamics practitioners (e.g., Roache, 1998), as a mean for reducing discretisation errors. However, its application in the context of atmospheric flows is not that simple, because every level of grid refinement brings another level of surface detail; see for instance the coastline paradox (Mandelbrot, 1967, 1982). In this case, because the flow is driven by topography, the flow model results are directly correlated to the terrain data and our problem is common to what can be encountered in geomorphology, with applications in hydrology (e.g., Zhang and Montgomery, 1994; Wise, 2000; Deng et al., 2007; Savage et al., 2016), where the DTM grid size affects the drainage area. In

45 spite of its importance, to our knowledge, there is no systematic study on the appropriate grid size for resolving the terrain in
microscale modelling of atmospheric flow over complex terrain.

Work has been done in quantifying the impact of using different DTMs and resolution on terrain attributes, such as elevation,
slope, plan and profile curvature, and topographic wetness index. For instance, Mahalingam and Olsen (2016) notes that DEMs
are often obtained and resampled without considering the influence of its source and data collection method. Finer meshes do
50 not necessarily mean higher accuracy in prediction (with examples for landslide mapping where terrain slope has a great
influence) with the DEM source being an important consideration.

DeWitt et al. (2015) compared several DEMs (USGS, SRTM, a statewide photogrammetric DEM and ASTER) to a high-
accuracy lidar DEM to assess their differences in rugged topography through elevation, basic descriptive statistics and his-
tograms. Root mean square error ranged from 3 (using photogrammetric DEM) to circa 15 (using SRTM) or 17 m (using
55 ASTER).

Deng et al. (2007) indicated that the mesh resolution can change not only terrain attributes in specific points but also
the topographic meaning of attributes at each point. They concluded that variation of terrain attributes were consistent with
resolution change and that the response patterns were dependent on the landform classes of the area. Deng et al. (2007)
introduced the concept of threshold resolution, i.e. the resolution beyond which the model quality deteriorated quickly, but
60 below which no significant improvement in modelling results was observed.

Florinsky and Kuryakova (2000) developed an experimental three-step statistical method to determine an adequate resolu-
tion in DEM to represent topographic variables and landscape properties at a micro-scale (exemplified by soil moisture) by
performing a set of correlation analysis between resolutions.

Diebold et al. (2013) showed the effect of grid size in LES of flow over Bolund. Lange et al. (2017) addressed the question
65 of how to represent the small topographic features of Bolund in wind tunnel modelling, comparing a round and a sharp edge
of a cliff in a wind tunnel, to conclude that the cliff with the sharp edge gives an annual energy production of a wind turbine
near the escarpment that is ~~20 to 51~~ 20% to 51% of the round-edge case.

1.2 Objectives and outline

The objective of the present study is to determine the terrain resolution required to accurately resolve the atmospheric flow
70 over Perdigão and mountainous terrain in general. One needs to assess the terrain horizontal resolution before assessing the
effect of other (also important) causes of differences between experimental and computational results. Many computational
studies based on Perdigão data are expected and it is important to assess the terrain resolution requirements first.

In what follows, we describe the techniques used for aerial and terrestrial surveying (section 2), plus the post-processing of
those data and the determination of the main geometrical parameters of the Perdigão site (section 3). The results on terrain
75 attributes and computational flow modelling are the subject of sections 4 and 5. The paper ends (section 6) with conclusions
and recommendations on the most appropriate DTM and grid size required in the computational modelling of the flow over
Perdigão.

2 Topographical surveying: equipment and techniques

2.1 Airborne laser scanning (2015)

80 The lidar aerial survey (Mallet and Bretar, 2009) was performed on 15 March 2015 by NIRAS (2015), with assistance from Blom TopEye. The survey covered an area equal to 22071075 m^2 (Figure 1a) and was completed in one session, at an altitude of 500 m with a TopEye system S/N 444 and a camera mounted on a helicopter. The number of points of the lidar point cloud was approximately 993198375, an average point density inside the project area equal to 45 points/m^2 and 12.6 points/m², if restricted to the ground class points (Figure 1a and section 3.1). The photography (a total of 744 photos, stored as 300 m × 300 m tiles) was performed with a Phase One iXA180 camera, a medium format, 10328 pixel × 7760 pixel sensor resolution, yielding a ground resolution equal to 4.7 cm (Figure 1b).

Lidar data was checked for point density control by Blom's software TPDS (TopEye Point Density and Statistics), with the area being fully covered by lidar data with exceptions for watersheds. GPS signal was processed using data from three Portuguese reference network stations (CBRA, MELR and PORT, cf. DGT (2017)), after assistance by the Portuguese National Mapping Agency (*Direção-Geral do Território, Divisão de Geodesia*). Discrepancies between flight lines (based on Blom's software TASQ, TopEye Area Statistics and Qualities, calculated on subareas of 1 m and after matching of 204104275 observationobservations) showed a maximum altitude deviation and RMSE equal to 0.490 m and 0.061 m. In 7575 % of the subareas the RMSE was lower than 60 mm.

The ~~photography (a total of 851 photos, stored as 300 m × 300 m GeoTIFF files) was performed with a Phase One iXA180 camera, a medium format, 10328 pixel × 7760 pixel sensor resolution, yielding a ground resolution equal to 4.7 cm. The delivery comprised orthophotos of 5 cm and 20 cm resolution (Figure 1b).~~

The production raw data of the NIRAS (2015) campaign comprised the lidar point cloud in LASer (LAS) (version 1.2) format and the ortophotos in 20 and 5 cm resolution; for more information and availability on these data see Palma et al. (2020). The production of the digital terrain model based on the lidar data point cloud is the subject of section 2.3.1.

100 2.2 Terrestrial surveying (2017 and 2018)

During the installation of scientific equipment (Nov 2016–May 2017), terrain elevation was measured in situ (Palma et al., 2018) for an accurate and final determination of the elevation data of part of the instrumentation. The measuring equipment was a Leica system, comprised of the following units: (1) Leica MultiStation MS50, (2) Leica Viva GS14 - GNSS Smart Antenna, (3) Leica CRT16 Bluetooth Cap and (4) Leica GRZ121 360 Reflector PRO Surveying Prism.

105 In 2017, a piece of land required changes for installation of tower 20/tse04. The topographic survey of that region was carried out (Alves, 2018) and incorporated in the lidar based terrain model ~~as of March 2015. This survey was performed by Spectra Physics (SP60 GNSS receiver and data collector T41 with Survey Pro software) equipment and software by Sierrasoft (PROST Premium/Topko Standart, Version 14.3) for production of the local DTM at a 1:500 scale.~~

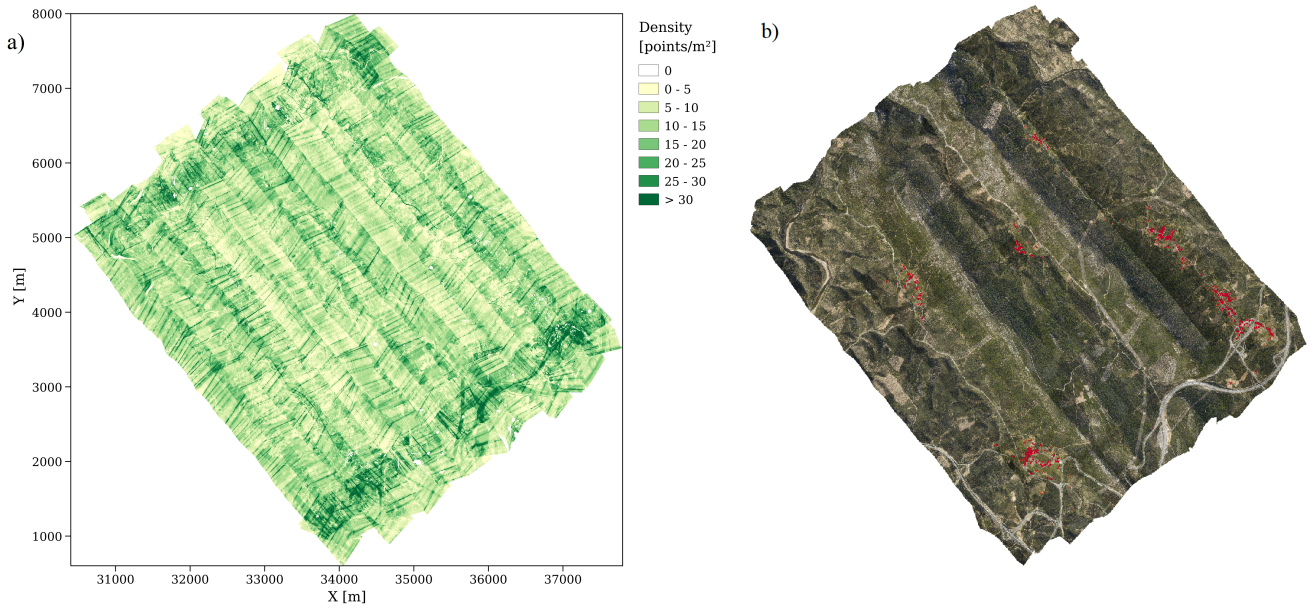


Figure 1. Lidar aerial survey and orthophoto: a) ground class points distribution; b) orthophoto (houses in red).

3 Terrain model

110 3.1 Airborne laser scanning (2015) Lidar point cloud processing

The lidar data was classified in laser pulse classes corresponding to four types of data (ground, vegetation, unassigned and noise) and stored in LASer (LAS) LAS File Format, and then post-processed by with tools pertaining to the LAStools® software suite (LAStools, 2019) in three stages, Figure ???.

115 Stage 1 was concerned with the extraction of the lidar raw data. The ground class data were mostly a mesh of regular spaced points, plus a few scattered points and small distinctive areas devoid of points, with abnormal values in their centre, attributed to lidar reading ground class point cloud had irregular spacing (Figure 1a), with lower point density in regions of vegetation clumping or non-overlapping scans. Some small, distinctive areas were found to be devoid of ground points, due to watersheds and lidar reading or classification errors.

120 Stage 2 involved the reclassification of abnormal data. A first procedure was used to reclassify a particular area of noise-classif noise-class points into the ground or vegetation ground or vegetation classes, which would otherwise be void of ground-ground points. Points with excessive (>700 m) or negative elevations a.s.l. (above sea level) were removed during this stage. Isolated points above or below the more spatially dense point cloud, classified as ground or vegetation ground or vegetation, were identified and removed using the lasnoise tool lasnoise tool (LAStools, 2019).

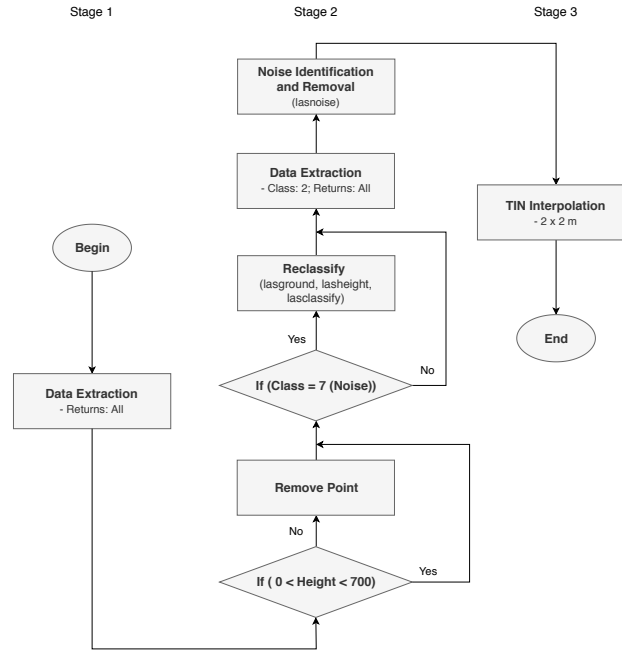


Figure 2. Workflow diagram for producing the terrain map using LAStools[®].

In Stage 3, a Triangulated Irregular Network (TIN), based on the Delaunay triangulation, was obtained for the **ground** **ground** classified points. The DTM was obtained by interpolating the heights into a regular mesh with a resolution of **2 × 2** **metre** **2 m × 2 m**, the highest horizontal resolution of the terrain elevation within the Perdigão site.

3.1.1 Buildings

It is not clear whether a DTM should comprise buildings and other **man-made** **human-made** artefacts that are usually part of digital surface models (DSM). In the context of the present study, buildings are **long-standing** **long-standing** structures, as a terrain feature, and we saw no reason for buildings not being part of the DTM. The houses, in Figure 1b, are family houses of about 15 m × 15 m and **3 m** **5 m** height that will show on the finest mesh only and as a point elevation. Unless there are a few neighbouring buildings, the ability to resolve isolated houses is limited.

The first task, to include the building data in the DTM, embraced the **extraction of unassigned (section ??) data points to a point database, containing points representative of obstacles, buildings or other types of structures detected by the lidar and different from vegetation or ground points. The second task involved the** digitalization of all buildings from the orthophotos. This process was needed to retain the building polygons as close as possible to their exact shape and **exclude possible outliers captured by the automatic points extraction, and also to perform a more eflocation. The second task involved the extraction of unassigned data points, which included buildings and adjacent vegetation, among other structures that fell within the polygons. These points were reclassified and precise interpolation of the data** using the **lasclassify** tool (LAStools, 2019), to

140 further remove adjacent and overhanging vegetation– and the resulting *building* class points were converted to the *ground* class.
 The third and ~~final stage was the interpolation of the buildings points included inside the digitized polygons for a continuous representation of the buildings. The interpolation scheme used in the ArcGIS platform (ESRI, 2016) was the natural neighbour method (Sibson, 1981), which preserves the shapes boundaries (Watson, 1994)~~final stage comprised the generation of a TIN from the new *ground* point cloud, followed by interpolation (blast2dem tool, LAStools (2019)) of the heights to a regular
 145 mesh with a resolution of $2\text{ m} \times 2\text{ m}$.

Calculations including the building data showed minor or no visible flow changes and were discarded. Nevertheless, for future use, two DTM versions, with and without buildings, are made available (Palma et al., 2020).

3.2 Two-dimensionality and main geometrical parameters

One of the reasons why Perdigão was selected was its geometry; namely, the parallelism between the two ridges and their large
 150 length relatively to the width, bringing the orography close to two-dimensionality.

3.2.1 Area of interest (AOI), reference lines and locations

For scaling and dimensional analysis, the main geometrical parameters of the Perdigão site were determined and the area of interest (AOI) was defined (Figure 3 and Table 1): a rectangular shape of ~~aproximately $3\text{ km} \times 4\text{ km}$~~ approximately $(3\text{ km} \times 4\text{ km})$, with lower left corner at 608589E; 4394131N and aligned with the centreline (ℓ_C , SE-NW direction, 135°). This area, cen-
 155 tred near station 131, included the SW and the NE ridge, the valley and the location of most of the instrumentation deployed in Perdigão. Note that the coordinate system was converted from ETRS89 PT-TM06 (original source) to ED50 UTM29 and will be used throughout the document as Eastings and Northings. Stations number (#) and code as in Perdigão web site (perdigao.fe.up.pt/).

3.2.2 Terrain profile and slope

160 The terrain profile (Figure 4) is not uniform along the valley, which becomes narrower and deeper along the SE-NW direction. For instance, the NW ridge height relative to a reference height (h_{ref} , the mean height of the surrounding terrain in a ~~$20 \times 20\text{ km}$~~ $20\text{ km} \times 20\text{ km}$ area) equal to 250 m a.s.l. varies between 201.1 and 251.4 m, and the distance between ridges is ~~1358.~~1358.0 and 1480.0 m on transects A and D (Table 2).

Apart from ℓ_C , six additional lines were defined: ℓ_{SW} and ℓ_{NE} along the SW and the NE ridges, and A, B, C and D, perpendicular to the ridges (SW-NE direction, 225°) and related to four main transects: A and D that delimit the northernmost
 165 (station 39) and southernmost (station 32) locations of the great majority of the instrumentation; and transects B and C that delimit a narrower region, determined by locations of stations 105/LRWS#5 and 20/tse04.

Other geometric variables (Figure 4) are the height of ridges (h_{SW} and h_{NE}) and valley (h_{val}) relative to the reference height (h_{ref}), the half-widths of the ridges (l_{SWw} , l_{SWe} , l_{NEw} and l_{NEe}) at half-height ($h_{SW}/2$ and $h_{NE}/2$), and the distance
 170 between ridges, ℓ .

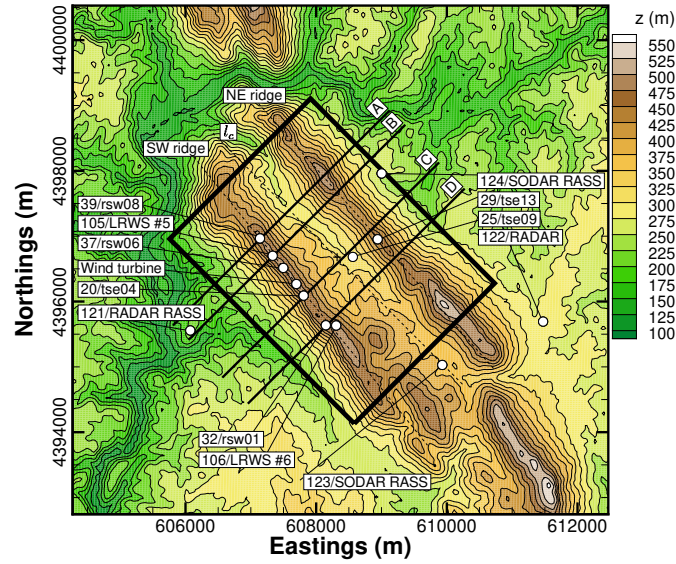


Figure 3. Area of interest and transects (ED50 UTM 29N).

Table 1. Reference points as in Figure 3 (ED50 UTM 29N).

#	Type/Code	Eastings (m)	Northings (m)	Elevation (m)
	Wind turbine	607697. <u>607697</u>	4396268. <u>4396268</u>	484.0
20	20/tse04	607808. <u>607808</u>	4396090. <u>4396090</u>	473.0
25	25/tse09	608561. <u>608561</u>	4396683. <u>4396683</u>	305.3
29	29/rsw01	608939. <u>608939</u>	4396953. <u>4396953</u>	452.9
32	32/rsw01	608149. <u>608149</u>	4395638. <u>4395638</u>	472.1
37	37/rsw06	607498. <u>607498</u>	4396514. <u>4396514</u>	482.5
39	39/rsw08	607140. <u>607140</u>	4396966. <u>4396966</u>	488.9
105	LRWS #5	607335. <u>607335</u>	4396701. <u>4396701</u>	485.9
106	LRWS #6	608307. <u>608307</u>	4395634. <u>4395634</u>	486.3
121	RADAR/RASS	606074. <u>606074</u>	4395558. <u>4395558</u>	223.7
122	RADAR	611474. <u>611474</u>	4395697. <u>4395697</u>	288.6
123	SODAR/RASS	609931. <u>609931</u>	4395029. <u>4395029</u>	361.9
124	SODAR/RASS	609003. <u>609003</u>	4397960. <u>4397960</u>	258.4

The ridges' orientation was determined by a linear regression of two z maxima, for each j (mesh oriented with SW-NE direction) on a 20 m grid, between transects A and D (≈ 1650 m) and between transects B and C (≈ 530 m). The deviations from parallelism are 4.3° if restricted to the region between A and D. Between transects B and C, where the core of the

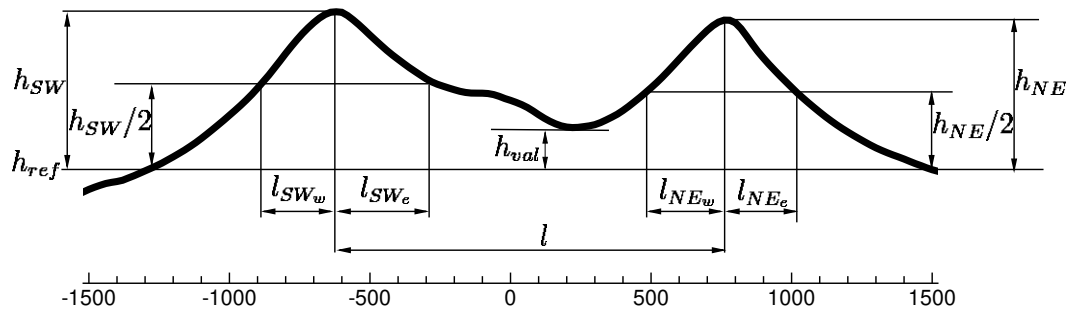


Figure 4. Terrain profileprofile: geometrical parameters.

Table 2. Main geometric variables of transects A, B, C and D (slope (S) in degrees ($^{\circ}$), and length and elevation (ℓ and h) in metre, $h_{ref} = 250$ m a.s.l.).

	A	B	C	D	Average
h_{SW}	237.2	237.3	228.3	222.0	231.2
h_{NE}	251.4	212.7	205.3	201.1	217.6
h_{val}	24.5	31.1	46.8	65.2	41.9
ℓ_{SWw}	277.8	214.0	232.0	212.3	234.0
ℓ_{SWe}	270.0	305.0	402.9	432.0	352.5
ℓ_{NEw}	286.9	320.2	249.5	268.7	281.3
ℓ_{NEe}	258.4	245.0	221.9	261.7	246.7
ℓ	1358.0	1384.0	1412.0	1480.0	1408.5
S_{SWw}	33.6	37.5	36.8	40.0	37.0
S_{SWe}	-45.1	-29.6	-22.7	-21.1	-29.6
S_{NEw}	30.7	25.7	27.8	25.7	27.5
S_{NEe}	-35.7	-30.1	-30.7	-24.1	-30.1

instrumentation was, the ridges were parallel within 2.8° ; i.e., 139.1° and 136.3° in the case of SW and NE ridges. The slope
175 ($S = |\tan(h_{SW,NE}/2)|/\ell_{SW,NE}$), also on a 20 m grid varies between 21.08° and 45.09° , always above the threshold for flow separation under neutral conditions (Wood, 1995).

4 Digital terrain model: results and discussion

The terrain elevation and slope are the two main terrain attributes for classification of terrain complexity and the ones to repli-
cate accurately by terrain models. In this section, three DTMs of the Perdigão site are analysed within the AOI, by comparing

180 terrain elevation and slope on meshes based on these terrain models with the terrain elevation and slope measured by the lidar
aerial survey data within the AOI.

The three DTMs (Figure 5 and section 4.4) were the following: (1) ALS, the area sampled by lidar with a 2 m resolution(~~file
#?? of Topography data on page ??~~); (2) Military, the Portuguese Army cartography around Perdigão, 10m horizontal resolu-
tion (~~file #2 of Topography data on page 25~~) available from Portuguese Army Geospatial Information Centre (*CIGeoE Centro*
185 *de Informação Geoespacial do Exército*), a total of eight sheets (numbers 290.4, 291.3, 302.2, 302.4, 303.1, 303.3, 313.2 and
314.1) at a scale equal to 1:25000; and (3) SRTM, the SRTM 30 m(~~file #1 of Topography data on page 25~~). Information on
availability of these data can be found in Palma et al. (2020) and under the heading Data availability, at the end of the present
study.

Because the ALS was the highest resolution map, and the most accurate representation of the terrain in Perdigão, it was the
190 one against which the accuracy of alternative terrain data sources was evaluated.

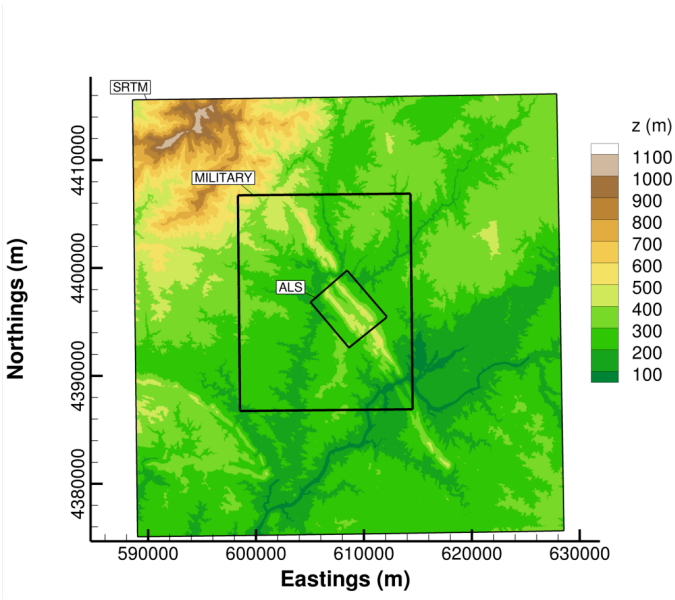


Figure 5. Total area comprised by SRTM, military and airborne data(~~+: domain-centre~~).

Concerning the terrestrial surveys in 2017 and 2018 (section 2.2), a sample of those measurements confirmed the high
quality of lidar airborne measurements. The survey carried in 2018, showed that the terrain change due to installation of tower
20, yielded alteration of the terrain that were not significant (lower than 1 m).

4.1 Mesh generation

195 For comparison of terrain attributes, elevation and slope, regularly spaced meshes of 80, 40, 20 and 10 m (size, $n_i \times n_j$,
respectively 39×51 , 77×101 , 153×201 and 305×401) were generated within the AOI. The resampling procedure was

similar to Deng et al. (2007); i.e., one out of two points was retained to assure that every point in the coarser resolutions existed on the finer ones. Coarser meshes are resampled versions of the 2 m resolution mesh, obtained by removing additional nodes.

4.2 Elevation at five reference points

Five points (Table 1) were selected for DTM comparison: towers 20/tse04, 25/tse09 and 29/tse13, the three 100 m meteorological towers, comprising a transect aligned with the dominant wind direction, and tower 37/rsw06 and the wind turbine location, along the SW ridge.

Figure 6 shows the absolute error ($z_{error} = z_{80,40,20,10} - z_2$), difference between the elevation at a given mesh and DTM source, with respect to the terrain elevation on the reference mesh (ALS₂). In the case of SRTM based meshes (Figure 6a), the error tends to a plateau at resolutions equal to 40 m. Similar behaviour is found in the case of the Mil database (Figure 6b), but at 20 m resolution; 20 and 10 m mesh increases the error at 20/tse04 and meshes at higher resolution to the uncertainty of this database must be avoided. Contrary to the SRTM and Mil, when using ALS (Figure 6c), with mesh refinement there is a noticeable error reduction at all 5 points.

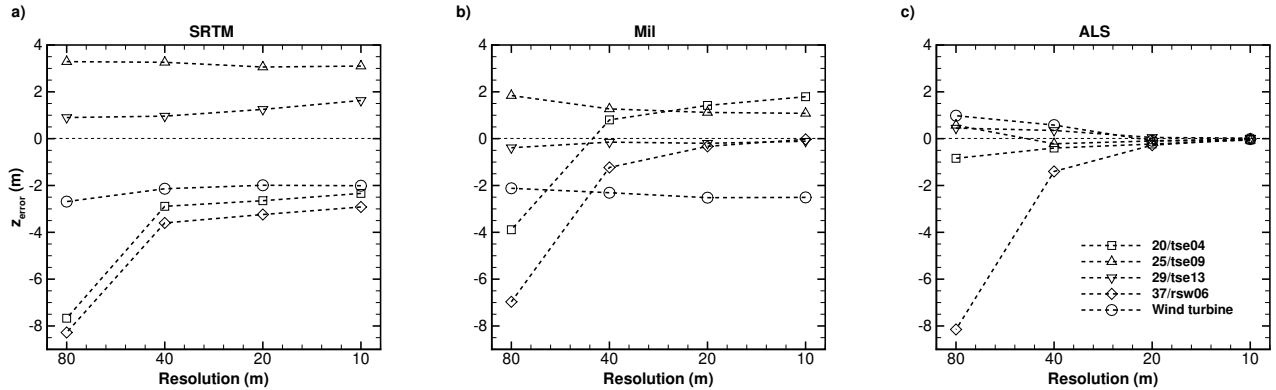


Figure 6. Impact of mesh resolution on reference points: a) SRTM; b) Mil; c) ALS.

4.3 Elevation and slope in the area of interest (AOI)

As the DTM quality increased from SRTM to Mil and ALS, the maximum terrain elevation (z_{Max}) also increased, from 530.2 to 540.5 and 540.8 m, and the minimum (z_{Min}) decreased from 165.0 to 158.8 and 156.8 m (Table 3). Maxima and minima terrain elevations are set by the DTM source; maxima and minima are similar for a given DTM regardless of the grid size, which was a consequence of the procedure for mesh refinement. The 10 m difference between SRTM and the ALS values is consistent with the RMSE of SRTM, equal to 6.2 m for Eurasia (Table 1, Farr et al., 2007) and also with the conclusions by DeWitt et al. (2015).

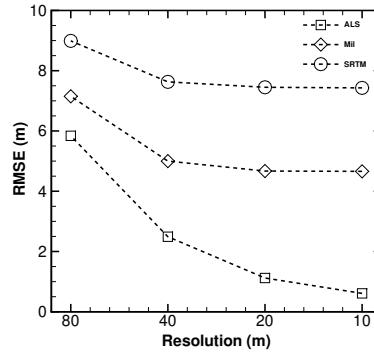


Figure 7. Impact of mesh resolution on RMSE.

Table 3. Maxima and minima terrain elevation, based on SRTM, Mil and ALS data.

Mesh	z_{Max} (m)			z_{Min} (m)		
	SRTM	Mil	ALS	SRTM	Mil	ALS
80	530.2	538.4	537.3	165.0	159.4	157.0
40	530.2	538.4	537.9	165.0	159.4	157.0
20	531.1	540.0	539.4	165.0	158.8	156.8
10	531.4	540.5	540.8	165.0	158.8	156.8
2	-	-	541.1	-	-	156.8

The error distribution (Figures 8 and 10a) shows an overprediction of the terrain elevation along the valley and an underprediction along the ridges, with both much reduced between the 80 and the 40 m resolution meshes, with the latter showing a mostly uniform error distribution of around 1 m (Figure 8b).

The RMSE error (Figure 7) over the whole AOI is consistent with the elevation error and the inherent uncertainty of every DTM source; with mesh refinement every DTM tends to its resolution level. The minimum RMSE of SRTM, Mil and ALS are 7.43, 4.66 and 0.61 m at resolutions of 10 m.

The maximum slope (55.85° and 64.76°) was about 59.50% higher on 20 and 10 m meshes compared with the coarser resolution (37.31° and 44.24° meshes, 80 and 40 m), Table 4. The negative slope increased from -37.33° to -67.81° , as the resolution increased from 80 to 10 m. The histogram of the slope in the x (SW-NE, 225°) direction (Silva, 2018) shifted to the right, as the content at low slopes, decreases and more and more higher slope locations were resolved. Because the ridges are quasi two-dimensional, the y (SE-NW, 135°) direction slope was residual (Silva, 2018) compared to the x direction slope (Figure 9) and is not shown here.

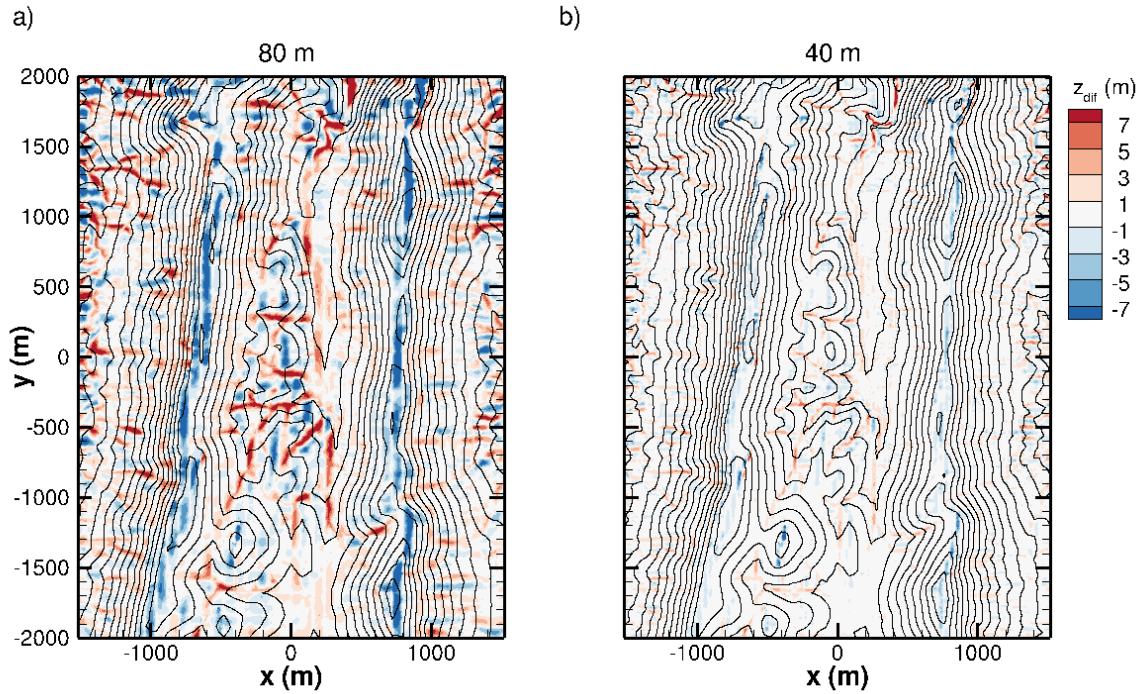


Figure 8. Elevation error of resampled meshes (ALS terrain data) over the AOI surface: a) 80 m mesh; b) 40 m mesh.

Table 4. Maxima and minima slope in the x (SW-NE, 225°) direction, based on SRTM, Mil and ALS terrain data.

Mesh	$S_{Max} (^\circ)$			$S_{Min} (^\circ)$		
	SRTM	Mil	ALS	SRTM	Mil	ALS
80	39.00	38.27	37.31	-36.11	-37.99	-37.33
40	41.61	43.10	44.24	-38.64	-47.61	-51.74
20	44.65	49.36	55.85	-47.18	-55.19	-59.31
10	47.86	51.74	64.76	-49.02	-61.31	-67.81
2	-	-	75.91	-	-	-81.13

The larger errors occurred at locations of higher slope (Figure 10) and these are the locations where the grid refinement was also the most effective in reducing the elevation error. For instance, errors equal to 11.5 m and -15.8 m (at $x = -720$ m and $x = 766$ m) on a 80 m mesh were reduced to 7.5 m and -2.5 m on a 40 m mesh.

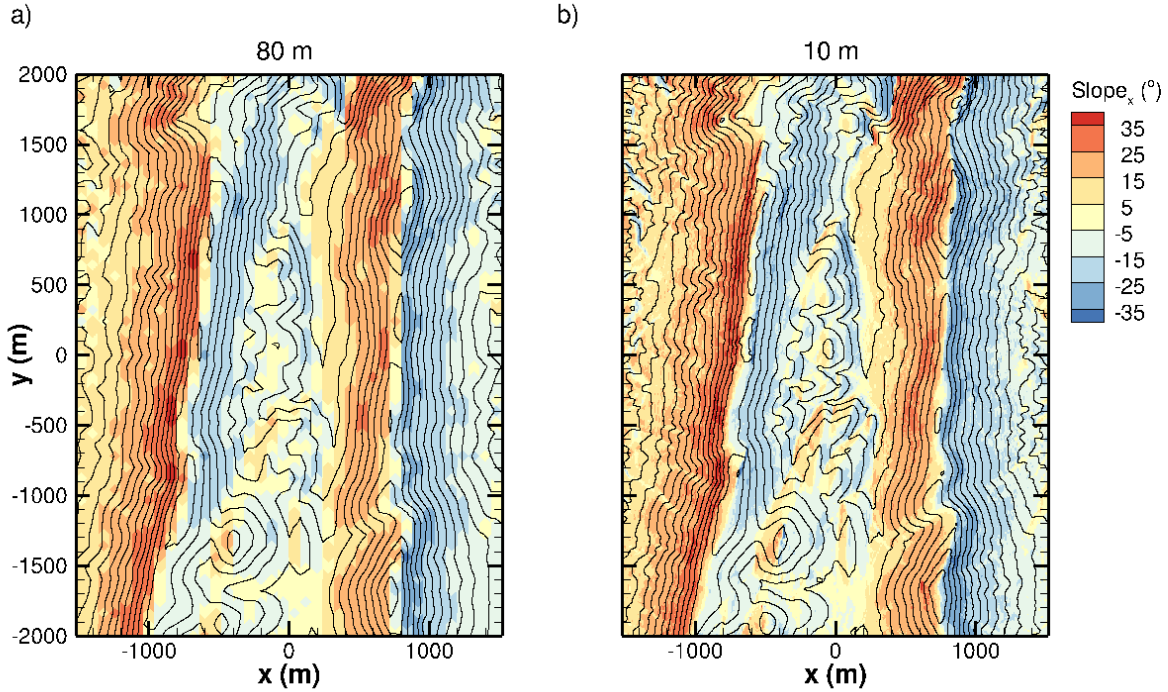


Figure 9. Slope in x (SW-NE, 225°) direction with different resolutions mapped on AOI's surface (ALS terrain data): a) 80 m mesh; b) 10 m mesh.

4.4 Spectra analysis

Spectra of terrain elevation show the ALS resolution one order of magnitude higher compared to SRTM data (Figure 11). The figure also displays two scaling ranges, typical of global topographies (e.g., Nikora and Goring, 2004), with exponents equal to $-7/4$ and $-11/3$.

235 As expected, there is an increase in resolved spectral range with mesh refinement and an overlap between meshes with ALS data. In the case of SRTM and Mil based meshes (Figures 11a and 11b), linear refinements (20 and 10 m meshes) cannot replicate the decay for higher frequencies and overcome the inherent resolution of the original data. Mesh quality was as good as the terrain data source. Only meshes based on the ALS (Figure 11c) have the ability to reproduce accurately the high-frequency range ($10^{-1} \text{ rad m}^{-1} < k < 1 \text{ rad m}^{-1}$). SRTM is restricted to around 30 m resolution and meshes ~~20×20 and~~
240 ~~10×10~~ 20 m × 20 m and 10 m × 10 m, with identical z_{Max} and z_{Min} (531 and 165 m), are unable to replicate the ALS measured values, z_{Max} and z_{Min} , Table 3. Grid refinement cannot go beyond the inherent resolution of the DTM.

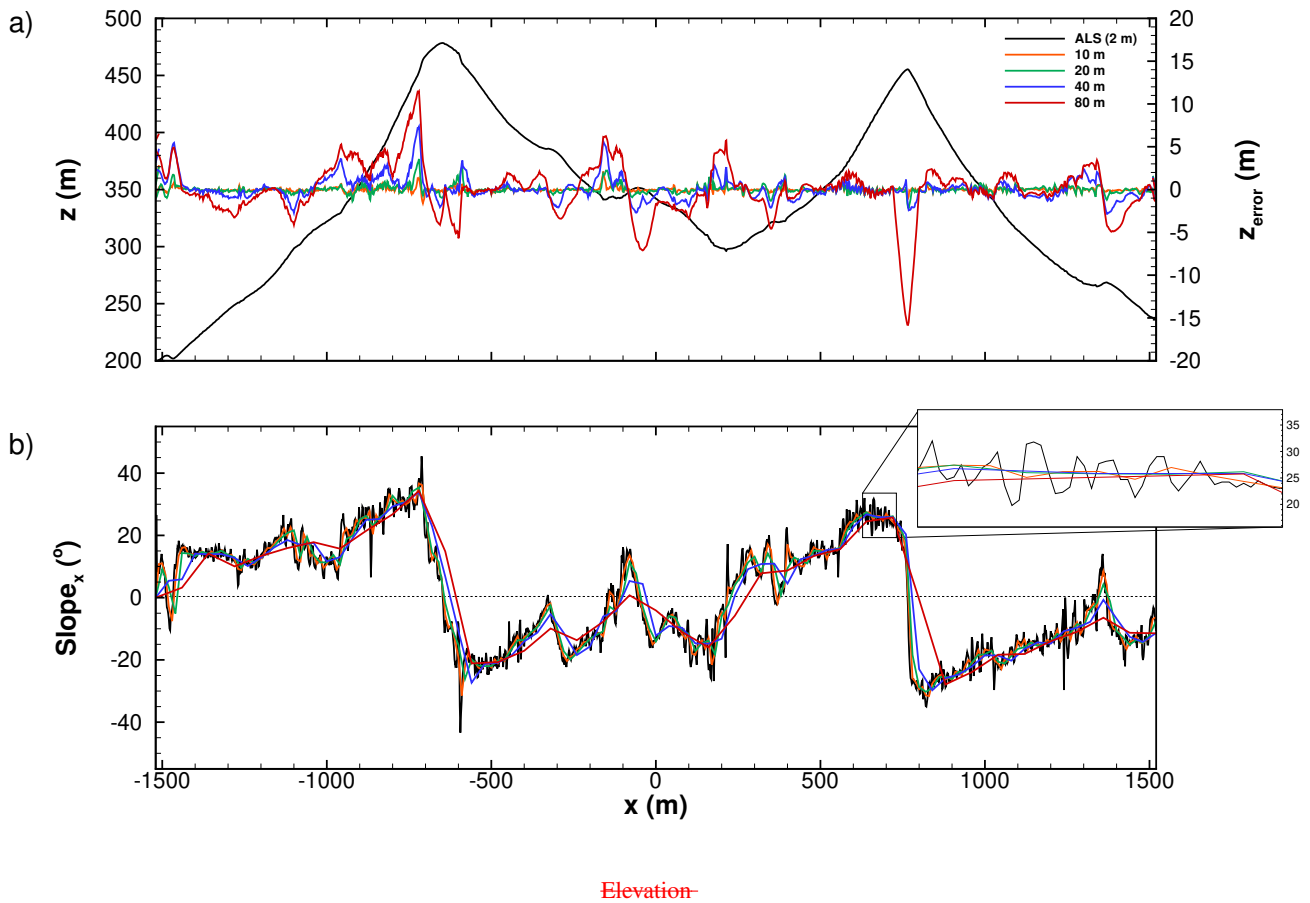


Figure 10. Terrain along transect C (see Figure 3). ALS based meshes: a) terrain profile and elevation error; b) slope in the x direction profiles on a plane that contains tower 20/tse04 (ALS terrain data).

4.5 RIX (ruggedness index)

The RIX (ruggedness index) is one of the major parameters in WAsP (Mortensen et al., 2004). It has the goal of quantifying the terrain complexity. The operational envelope of WAsP corresponds to a RIX value of 00%. The ALS data shows a maximum of 23.723.7% and an overall higher value of RIX (average 15.2215.22%), while SRTM reaches 19.7(average 11.0619.7% (average 11.6%). Lower resolution terrain data underestimate the terrain complexity.

5 Flow modelling

In this section, the results of computational runs on different meshes are discussed. A set of experimental data (UCAR/NCAR-EOL, 2019) (30 minutes averaged) on 4 May 2017, 22:09–22:39 UTM is also included. This was the day and the time when

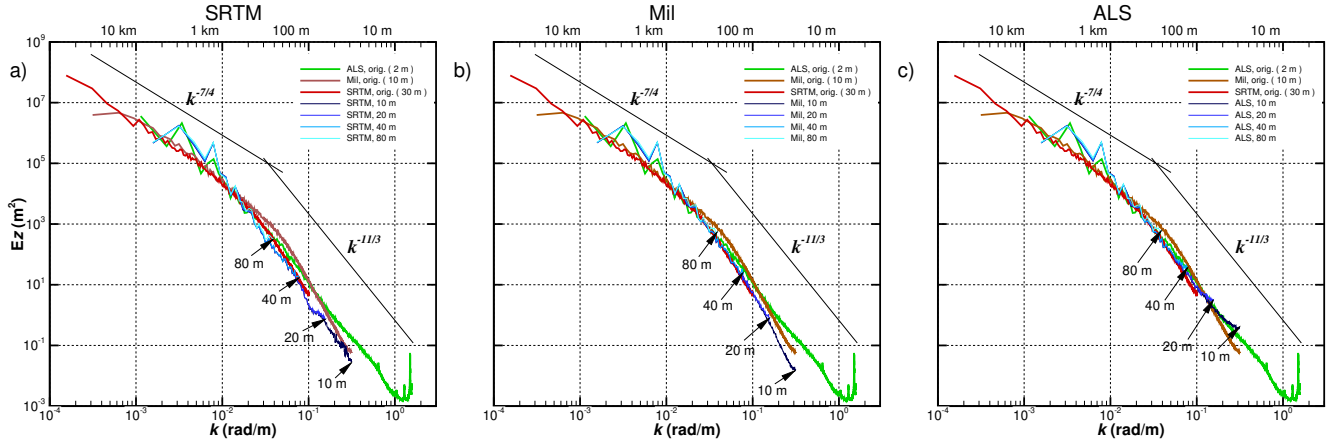


Figure 11. Spectra analysis for DTM and meshes: [a\) SRTM](#); [b\) Mil](#); [c\) ALS](#).

the assumption of conditions of stationarity based on measurements at tower 20/tse04 were valid, according with Carvalho (2019), and the flow was non-stratified based on a bulk Richardson number (R_B) equal to -0.03

$$R_B = \frac{g (\bar{\theta}_{100} - \bar{\theta}_2) \Delta z}{\bar{\theta}_{100} [(U_{100})^2 + (V_{100})^2]} \quad (1)$$

where $\bar{\theta}_{100}$ and $\bar{\theta}_2$ are the mean potential temperature at 100 m and 2 m a.g.l (above the ground level), $\Delta z = 100$ m, and U_{100} and V_{100} are the mean horizontal components of the velocity vector also at 100m a.g.l. . The temperature obtained from measurement data was converted into potential temperature using the following approximation (Stull, 1988):

$$\bar{\theta} \approx \bar{T} + \left(\frac{g}{c_p} \right) z \quad (2)$$

The data set choice was conditioned by the computational flow model being used. Because computational results do not consider, for instance, surface cover heterogeneity, discrepancies are expected when compared with experimental data, which are included here for guidance only.

5.1 Computational flow model

The computational code VENTOS®/2 (cf., Castro et al., 2003; Palma et al., 2008), developed for atmospheric flows over complex terrain, was used in steady state formulation. It solves the Reynolds-averaged Navier Stokes set of equations for a turbulent flow ($k - \varepsilon$ model), with a terrain-following structured mesh, allowing also the simulation of forested terrain (Costa et al., 2006) and wind turbine wakes (Gomes et al., 2014; Gomes and Palma, 2016).

265 5.1.1 Integration domain and boundary conditions

The model topography (domain size, $19\text{km} \times 18.8\text{km}$, around the central location 608250E, 4396621N) was obtained by bi-linear interpolation of terrain data. The positioning of the domain boundaries and its impact on flow variables were part of the work of Silva (2018).

At the inlet a log-law profile was set. To ensure an equilibrium shear stress, the k profile decreases with the square of height
270 above ground level. At the top of the domain a zero shear stress condition was used. The inlet profile's development is capped at the boundary layer's limit, all quantities being constant above that height. At the lateral boundaries a symmetry condition was applied.

The ground was modelled as a rough surface, a wall function, a log-law defining the velocity at the node closest to the ground, and the turbulence model quantities, k and ε . The values used in the computational model for z_0 (roughness length)
275 and u_* (friction velocity) were 0.1 (indicated by Wagner et al. (2019) as the roughness length near the double ridge area after conversion from the CORINE Land Cover classes) and 0.25. These values were uniform for the whole domain. The surface cover (forest patches and height) and its representation in the computational model (roughness length, leaf area index, use of a canopy model) is still a work in progress, as the presence of eucalyptus and pine tree patches in the area are expected to have a
280 ~~decisive-an~~ impact on the flow. However, this would increase the number of variables influencing the flow results, masking the effects of the digital terrain model alone. See for instance, the effects of forest resolution and wind orientation relative to the forest stands in the computational modelling of flow over forests in Costa et al. (2006).

5.2 Computational meshes

A total of 18 computational meshes (Table 5) was used. The central part of the domain ($4\text{km} \times 6\text{km}$, based on ALS and Mil terrain data), was resolved with uniform horizontal resolution (~~$20 \times 20, 40 \times 40$ and $80 \times 80 \text{ m}$~~ $20\text{m} \times 20\text{m}, 40\text{m} \times 40\text{m}$
285 and $80\text{m} \times 80\text{m}$), expanding towards the domain boundaries with factors f_x and f_y close to 1, to minimise the discretisation errors. The domain's height (3000 m) was discretised by 100 nodes (~~$n_k N_k$~~), with the first node 2 m above ground level and a grid expansion $f_z = 1.0435$, yielding a maximum cell size (Δ_z) equal to 124 m. For availability of meshes ALS.SW.## and ALS.NE.##, see Palma et al. (2020) and information under Data availability, at the end of this study.

A preliminary analysis showed that the flow variables had low sensitivity to the number of nodes in the vertical (n_k), opposed
290 to the height of the first node above ground level, which showed a significant impact and is worthy of further studies.

Three types of meshes were used: SRTM, with the whole domain based on the SRTM data; Mil, a combination of SRTM and Military maps; and ALS, based on all three DTM sources (Figure 5). A minimum of 8818 iterations and 3.87 hours of computing time were required, and a maximum of 20033 iterations and $50\times$ more computing time in the case of mesh Mil.NE.20. Number of iteration is a better indicator of the actual computing time, since the value given here was influenced by
295 the computer load at the time of the calculations.

Table 5. Computational meshes ($\Delta z_{Min} = 2\text{ m}$).

	Name	$\Delta_{x/y}$		$N_i \times N_j$	t_{CPU}	N_{iter}
		min	Max			
		(m)	(m)		(h)	
1	SRTM.SW.80	80	478.6	120×155	6.27	8818
2	SRTM.SW.40	40	400.0	200×270	52.96	11557
3	SRTM.SW.20*	20	414.0	320×470	-	-
4	Mil.SW.80	80	478.6	120×155	18.13	8906
5	Mil.SW.40	40	400.0	200×270	89.64	11040
6	Mil.SW.20	20	414.0	320×470	237.35	14095
7	ALS.SW.80	80	478.6	120×155	3.87	8898
8	ALS.SW.40	40	400.0	200×270	15.09	10996
9	ALS.SW.20	20	414.0	320×470	111.28	16606
10	SRTM.NE.80	80	478.6	120×155	19.92	9554
11	SRTM.NE.40	40	400.0	200×270	110.04	14227
12	SRTM.NE.20	20	414.0	320×470	242.57	15188
13	Mil.NE.80	80	478.6	120×155	28.43	9313
14	Mil.NE.40	40	400.0	200×270	101.90	13351
15	Mil.NE.20	20	414.0	320×470	191.38	20033
16	ALS.NE.80	80	478.6	120×155	3.74	9322
17	ALS.NE.40	40	400.0	200×270	93.49	11937
18	ALS.NE.20	20	414.0	320×470	80.21	18634
Expansion factors						
		$\min(\Delta_{x/y})$	f_x	f_y	f_z	
		80	1.0524	1.0331	1.0435	
		40	1.0471	1.0299	1.0435	
		20	1.0518	1.0271	1.0435	

* Did not meet residual criteria

5.3 Flow pattern

The flow modelling analysis was based on the flow patterns at two transects in the case of SW and NE winds (Figures 12 and 13) and wind speed, wind direction and turbulent kinetic energy results for SW (Figures 14–16).

As expected, the flow pattern (Figures 12 and 13) is characterised by separated flow regions in the leeside of either ridges. The figures are coloured by the spanwise velocity component (v), showing two different streams: up-valley on the leeside of SW ridge and down-valley on the upwind side of NE ridge (Figure 12) and down-valley in the case of NE winds (Figure 13).

The ridge height increases with the grid resolution (see insets) and the detachment point moves to higher elevations, yielding longer and deeper separated flow regions, see for instance Figure 13. Menke et al. (2019), in their analysis of the experimental

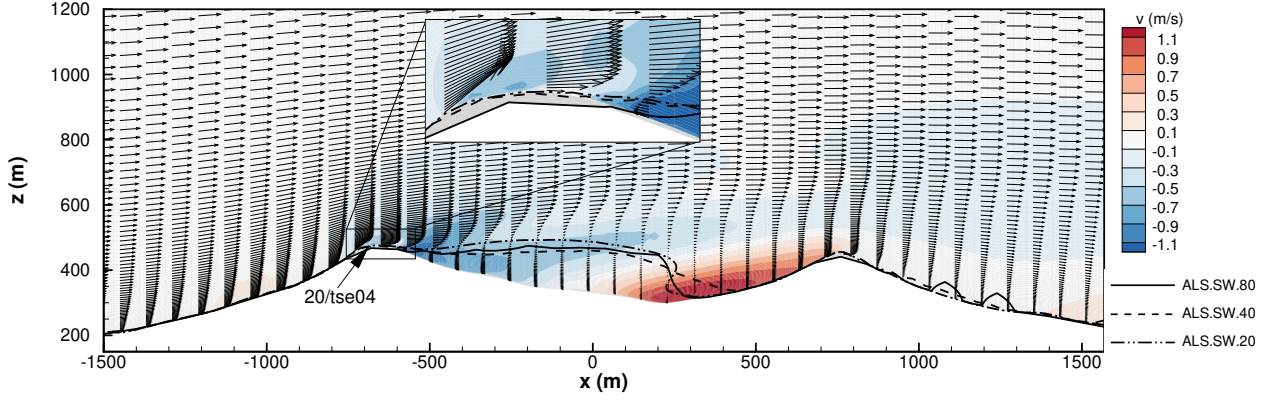


Figure 12. Impact of mesh resolution on separation zone in transect that crosses ~~Tower~~tower 20/tse04, in the case of SW winds.

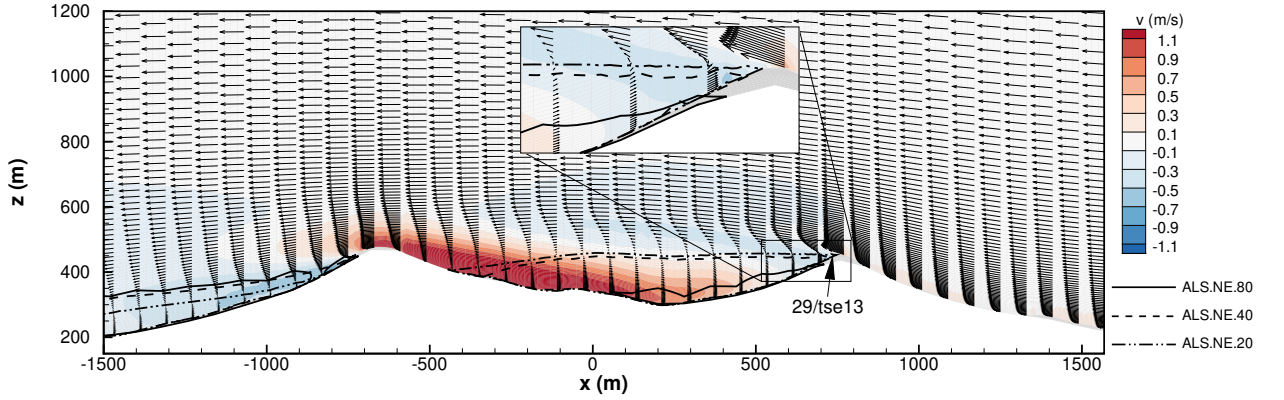


Figure 13. Impact of mesh resolution on separation zone in transect that crosses ~~Tower~~tower 29/tse13, in the case of NE winds.

data, reported average length and depth equal to 697 and 157 m for both SW and NE wind directions and stratification levels
305 based on the gradient Richardson number between -1 and 1; in the case of neutral flow, length and height equal to 807 and
192 m were reported for a 10-min period. The length and height of the separation zone, in Table 6, tend to increase with the
grid refinement (with the exception of the SW winds when refining from 40 to 20 m resolution), predicting a recirculation
region longer and narrower compared with the measurements.

Table 6. Length and maximum depth of separation zone.

	Length (m)	Height (m)
Southwesterly winds		
80	1040.1	142.9
40	1120.0	131.8
20	1000.1	155.0
Northeasterly winds		
80	762.5	135.1
40	1120.9	143.4
20	1159.3	151.8

5.4 Southwesterly winds

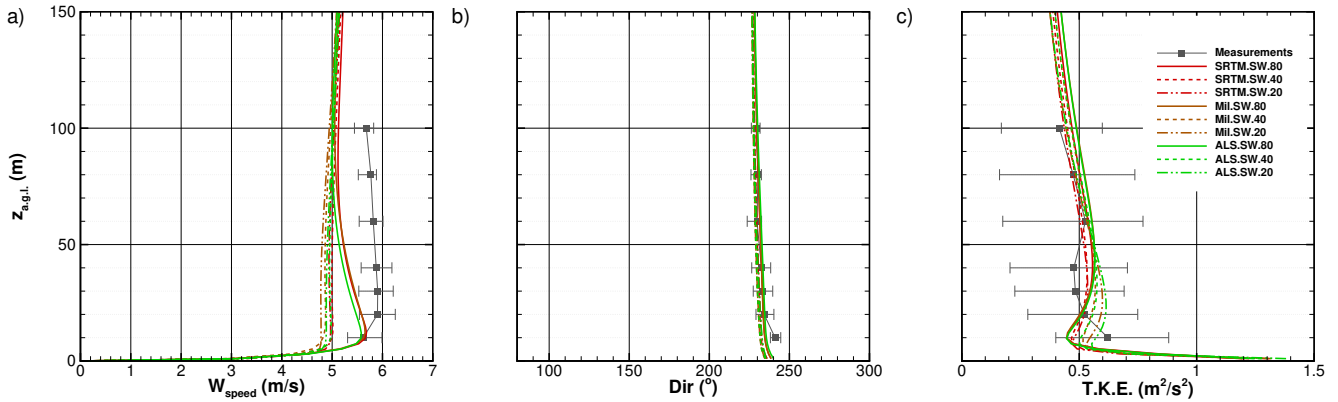
310 The wind speed, wind direction and turbulent kinetic energy profiles at towers 20/tse04, 25/tse09 and 29/tse13 (Figures 14, 15 and 16) show a good agreement of the wind direction with the measurements, a poor agreement of the wind speed (underprediction) at all towers, and underprediction of the turbulent kinetic energy in the valley and at the NE ridge (towers 25/tse09 and 29/tse13, Figures 15c and 16c). A good agreement between computational and experimental results is not expected, mainly because of the uniform roughness length; the important is the sensitivity of the computational results to the different numerical
315 meshes.

As an indicator of stationarity, the mean values of the experimental results over the 30-min period are plotted ~~such as~~, showing the minima and maxima within that period as error bars. Departure from stationarity condition reaches a higher magnitude in the valley (Figure 15), given the location of tower 25/tse09 inside the recirculation zone. Unsteadiness is a well-known characteristic of recirculation zones and their prediction is very sensitive to spatial resolution (Castro et al., 2003) and
320 terrain model as shown by Figure 15b. The separated flow region, tower 25/tse09 (Figure 15) is characterised by low wind speed and rotation of the wind with the distance above the ground. The wind speeds at $z_{asl} > 100$ decreases as the mesh is refined and the height of the recirculation zone increases (Table 6). The flow in the valley is aligned with the valley and therefore perpendicular to the ridges and the incoming wind. The predicted wind direction is in close agreement with the measurements, with the exception of 40 and 20 m meshes based on Mil DTM.

325 As a whole, the flow results appear to be more sensitive to the resolution than to the DTM; see, for instance, Figure 14a) with the results on 40 and 20 m meshes detached from results on the 80 m mesh. At least a resolution of 40 m is required.

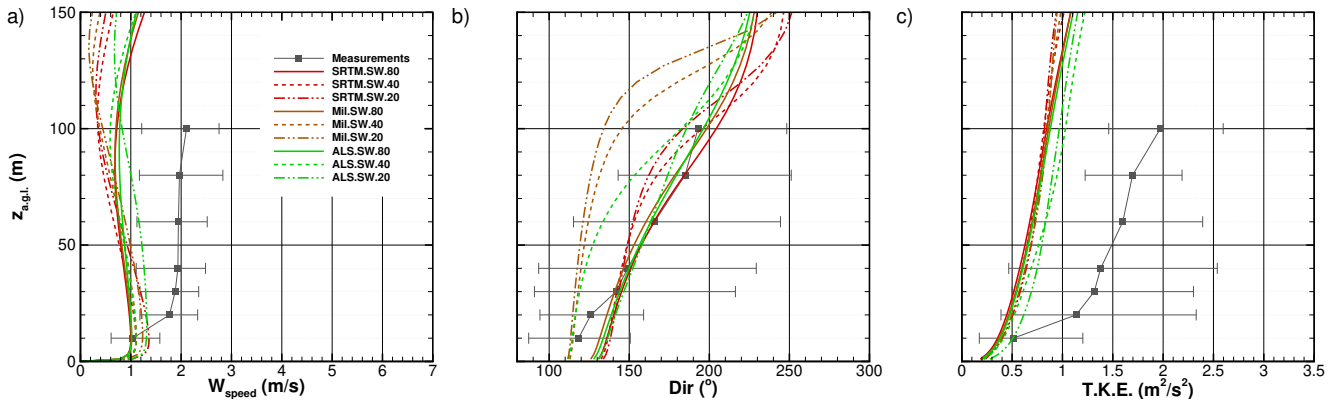
The profiles (not shown) in the case of NE winds (45°) are similar to SW winds, apart from the situation being reversed, since in this case the first and second ridge are the NE and SW ridges.

Differences between the profiles and the reference profile ALS₂₀ were measured in terms of RMSE (Tables 7, 8 and 9),
330 which, in general, show a pattern similar to the slope (Table 4), where the RMSE decreases either by refining the mesh or for a given mesh by moving from the SRTM, to Mil and ALS based meshes. RMSE values at towers 20/tse04 and 29/tse13 (Tables 7



Wind speed, direction and turbulent kinetic energy profile simulation

Figure 14. Simulation results and experimental data in tower 20/tse04 for SW winds: a) wind speed; b) wind direction; c) turbulent kinetic energy.



Wind speed, direction and turbulent kinetic energy profile simulation

Figure 15. Simulation results and experimental data in tower 25/tse09 for SW winds: a) wind speed; b) wind direction; c) turbulent kinetic energy.

and 9) on the hills depend on the dominant wind directions, showing the effects of the valley flow on the downstream hill. The effect of calculations on 20 m mesh compared to those on 40 m mesh are less than the effect of calculations on 40 m mesh compared to those on 80 m mesh.

335 6 Conclusions Discussion and conclusions

Meshes for computational modelling of flow over the Perdigão site were created, based on three digital terrain models: high-resolution (2 m resolution) airborne lidar survey (ALS), Military (10 m) and SRTM (30 m) data. The mesh appraisal was

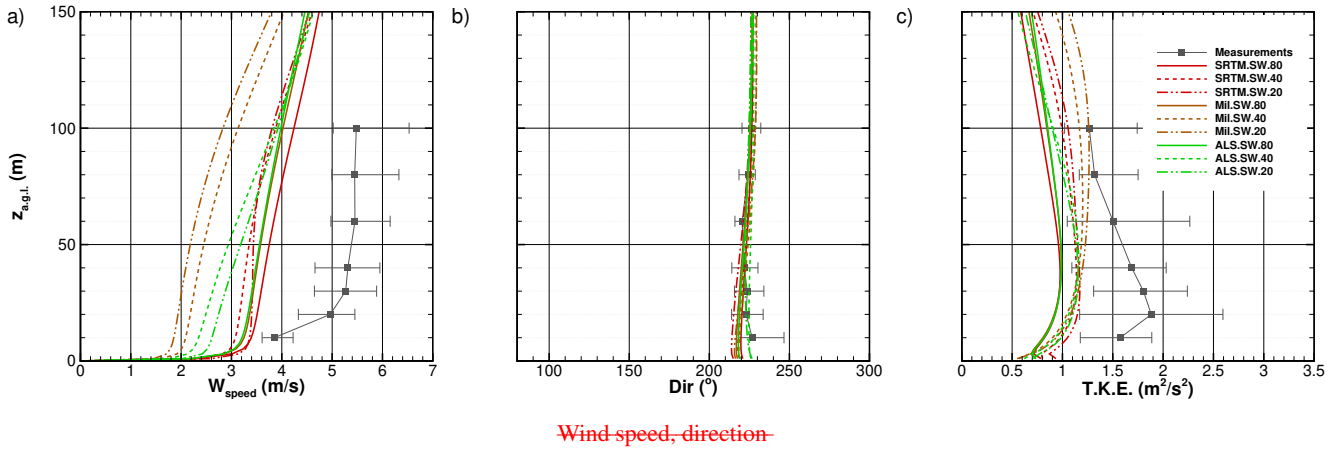


Figure 16. Simulation results and turbulent kinetic energy profile at experimental data in tower 29/tse13 for SW winds: a) wind speed; b) wind direction; c) turbulent kinetic energy.

Table 7. RMSE of wind speed, wind direction and turbulent kinetic energy for tower 20/tse04.

	W_{speed} (m/s)			Dir (°)			T.K.E (m ² /s ²)		
	SRTM	Mil	ALS	SRTM	Mil	ALS	SRTM	Mil	ALS
Southwesterly winds									
80	0.83	0.81	0.68	4.60	4.65	6.28	0.13	0.14	0.13
40	0.20	0.17	0.12	0.79	1.70	1.60	0.12	0.08	0.07
20	0.09	0.21	–	0.71	1.80	–	0.11	0.03	–
Northeasterly winds									
80	1.28	2.53	2.43	16.80	16.49	14.90	0.78	1.01	1.04
40	0.99	0.50	0.22	9.84	9.83	4.09	0.46	0.33	0.39
20	0.18	0.30	–	5.04	2.74	–	0.06	0.08	–

carried out in two ways: by their ability to replicate the two main terrain attributes, elevation and slope, and by their effect on the wind flow computational results (wind speed, wind direction and turbulence kinetic energy) at three locations.

340 About the digital terrain models, the main conclusions were the following:

1. The SRTM data is not an accurate representation of the Perdigão site.
2. Only meshes based on the ALS have the ability to reproduce the smaller scales between 10 and 100 m.
3. The ALS data yielded the lowest elevation errors; average RMSE around 5.8 m on 80 m, decreasing to 0.6 m on 10 m mesh.

Table 8. RMSE of wind speed, wind direction and turbulent kinetic energy for tower 25/tse09.

	W_{speed} (m/s)			Dir (°)			T.K.E (m ² /s ²)		
	SRTM	Mil	ALS	SRTM	Mil	ALS	SRTM	Mil	ALS
Southwesterly winds									
80	0.87	0.77	0.69	26.67	20.10	14.81	0.33	0.29	0.26
40	0.92	0.90	0.70	38.14	75.35	48.96	0.36	0.34	0.16
20	0.81	0.84	-	37.03	92.73	-	0.36	0.32	-
Northeasterly winds									
80	2.82	3.67	3.54	157.07	158.04	153.56	0.25	0.49	0.49
40	0.39	0.88	0.53	88.82	79.37	69.95	0.51	0.33	0.23
20	0.19	0.17	-	40.61	43.20	-	0.22	0.15	-

Table 9. RMSE of wind speed, wind direction and turbulent kinetic energy for tower 29/tse13.

	W_{speed} (m/s)			Dir (°)			T.K.E (m ² /s ²)		
	SRTM	Mil	ALS	SRTM	Mil	ALS	SRTM	Mil	ALS
Southwesterly winds									
80	1.19	0.82	0.77	4.87	7.16	5.92	0.33	0.28	0.27
40	0.51	1.68	0.44	6.30	8.45	6.05	0.16	0.52	0.10
20	0.83	2.33	-	10.40	10.03	-	0.28	0.70	-
Northeasterly winds									
80	0.44	0.49	0.44	16.15	17.73	16.79	0.13	0.15	0.13
40	0.26	0.16	0.24	6.94	10.26	5.35	0.06	0.07	0.06
20	0.18	0.09	-	2.98	4.66	-	0.04	0.03	-

- 345
4. The RMSE for SRTM does not go below 7.4 m. A 40 m horizontal resolution based on the ALS data is enough to achieve an error below 1.4 m in five key locations and below 0.28 m using a 20 m mesh.
5. The maximum terrain slope was about 1.8× higher (−67.81°) on a 20 m mesh resolution compared with an 80 m mesh resolution (−37.33°). An 80 m mesh does not accurately represent elevation and slope, mainly near the extreme elevation values (highs and lows).
- 350
- The effect of the terrain model on the wind speed, wind direction and turbulent kinetic energy at three locations (SW ridge, valley and NW ridge) and two incoming wind directions (SW and NE) were the following:
1. In the case of SW winds, the mesh resolution effects on the SW ridge were restricted to the first 100 m a.g.l., where mesh refinement decreased the wind speed and degraded the quantitative agreement with the experimental data, though replicating the profile shape.

- 355 2. Separated flow field in the valley is perpendicular to the main flow direction. This region increases in height and length with the mesh refinement.
3. The flow (mainly the wind direction) in the valley was the most affected by terrain resolution; low velocities (about 1 ms^{-1}) are associated with large variations of wind direction within the first 150 m a.g.l..

Concerning the digital terrain models and meshes, the conclusions were the following.

- 360 1. It was found that 40 and 20 m meshes are resolutions –threshold resolution– beyond which no or insignificant changes occur both in terrain attributes, elevation and slope, and in the flow field variables, wind speed, wind direction and turbulent kinetic energy.
2. It is recommended that at least 40 and 20 m meshes based on military and ALS be used to describe the Perdigão site, with SRTM restricted to far away regions.

365 The conclusions hold under the conditions of the present work, namely terrain data and flow model equations and conditions. Under different conditions, further validation may be required.

Data availability. Three datafile types are available. For more information see Palma et al. (2020)

Lidar-scanning files :-

Aerial survey files (as described in section 2.1) :

- 370 1. ~~5-Delivery information~~ Ortophotos in 5 cm and 20 cm resolution
~~6.1 Coordinate system in plane and height: PT-TM06/ETRS89 / Altimetric Datum from Cascais 6.2 File formats Laserdata: LAS 1.2~~ <https://perdigao.fe.up.pt/datasets/thredds/catalog/landCharacterization/Aerial%20Survey%20Lidar%20and%20Photography%20Data/Images/catalog>
2. ~~Ortho-mosaic:-~~
- 375 3. ~~This delivery includes a lidar point cloud, and 5 cm and 20 cm orthophotos.-~~
Lidar point cloud data
<https://perdigao.fe.up.pt/datasets/thredds/catalog/landCharacterization/Aerial%20Survey%20Lidar%20and%20Photography%20Data/Pointcloud/catalog>

~~Topography data-~~

380 Digital Terrain Models in local metric datum (as described in section 4) :

1. ~~DTM-SRTM raster map~~ of ~~Perdigão site, terrain elevation on a regularly spaced $2\text{ m} \times 2\text{ m}$ region, $\sim 100\text{ km}$ square area at resolution of 1 arc-second ($\approx 24\text{ m} \times 31\text{ m}$, Easting \times Northing) (non-uniform)~~
https://windsptds.fe.up.pt/thredds/fileServer/landCharacterization/Digital%20Terrain%20Models/dtm_srtm_1arcsec.zip
2. Military ~~map centred on Perdigão site, on a regularly spaced $10\text{ m} \times 10\text{ m}$ charts~~ raster map of Perdigão region, $16\text{ km} \times 20\text{ km}$ area at 10 m resolution
https://windsptds.fe.up.pt/thredds/fileServer/landCharacterization/Digital%20Terrain%20Models/dtm_mil_10m.zip
3. ~~SRTM map centred on Perdigão site, on a regularly spaced $30\text{ m} \times 30\text{ m}$ ALS~~ derived raster maps of Perdigão site, $\sim 5\text{ km} \times 6\text{ km}$ area (net) at 2 m resolution, without buildings
https://windsptds.fe.up.pt/thredds/fileServer/landCharacterization/Digital%20Terrain%20Models/dtm_als_no_buildings_2m.zip
4. ~~ALS derived raster maps of Perdigão site, $\sim 5\text{ km} \times 6\text{ km}$ area (net) at 2 m resolution with buildings~~
https://windsptds.fe.up.pt/thredds/fileServer/landCharacterization/Digital%20Terrain%20Models/dtm_als_buildings_2m.zip

395 **Computational meshes** ÷

Computational meshes (as described in section 5.2) :

1. ~~Mesh 1:~~ NE inflow, $20\text{ m} \times 20\text{ m}$ (ALS.NE.20, as in Table 5)
https://windsptds.fe.up.pt/thredds/fileServer/landCharacterization/Computational%20Topography%20Meshes/mesh_ne_20x20.dat
2. ~~Mesh 2:~~ NE inflow, $40\text{ m} \times 40\text{ m}$ (ALS.NE.40, as in Table 5)
https://windsptds.fe.up.pt/thredds/fileServer/landCharacterization/Computational%20Topography%20Meshes/mesh_ne_40x40.dat
3. ~~Mesh 3:~~ NE inflow, $80\text{ m} \times 80\text{ m}$ (ALS.NE.80, as in Table 5)
https://windsptds.fe.up.pt/thredds/fileServer/landCharacterization/Computational%20Topography%20Meshes/mesh_ne_80x80.dat
4. SW inflow, $20\text{ m} \times 20\text{ m}$ (ALS.SW.20, as in Table 5)
https://windsptds.fe.up.pt/thredds/fileServer/landCharacterization/Computational%20Topography%20Meshes/mesh_sw_20x20.dat
5. SW inflow, $40\text{ m} \times 40\text{ m}$ (ALS.SW.40, as in Table 5)
https://windsptds.fe.up.pt/thredds/fileServer/landCharacterization/Computational%20Topography%20Meshes/mesh_sw_40x40.dat

6. SW inflow, 80 m × 80 m (ALS.SW.80, as in Table 5)

https://windsptds.fe.up.pt/thredds/fileServer/landCharacterization/Computational%20Topography%20Meshes/mesh_sw_80x80.dat

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