Wind Energ. Sci. Discuss.,
https://doi.org/10.5194/wes-2020-14-AC1, 2020


WESD

Interactive comment

# *Interactive comment on* "Computational Analysis of High Lift Generating Airfoils for Diffuser Augmented Wind Turbines" *by* Aniruddha Deepak Paranjape et al.

**Aniruddha Deepak Paranjape et al.**

radha.parikh11@gmail.com

Received and published: 9 May 2020

The authors appreciate the efforts of the reviewer for his valuable comments especially with respect to the content improvement and the improvement of the structure of the paper. The paper has been modified following the reviewer suggestions. However the reviewer has some specific questions which have been answered below:

1. "This type of introductions is somewhat superfluous for a journal like WES. You may skip this and focus somewhat more on "hot spots"for DAWT's if you like. Otherwise skip it."



Printer-friendly version

Discussion paper

Taking the comments into consideration the introduction has been suitably edited adding clarity.

2. “This is, strickly spoken, not the case. The direction of the flow is changing across the blades. In the inertial frame of reference the major effect "seen" is a change of total pressure while the axial component of the incoming wind velocity is not changing, at least not when passing the rotor plane.”

   The authors understand the reviewer’s concerns regarding the the introduction of the AD section, it has since been edited keeping the reviewer’s comments in mind.

3. “figure 2 one would not conclude that the area ratio is indeed 1.84. Is there something that I do not understand? Please clarify!”

   The authors concede that there has been a mistake in the manner in which the image was titled. Appropriate corrections have been made.

4. “why do you call this a gene pool? This naming suggest you go for some genetic algorithm to generate new hybrid airfoils, but that is not done, at least not in this article.”

   The term genepool is a bit of a misnomer in this case. The authors simply wanted to highlight that the 12 airfoils are considered as a pool and not a genepool. The term has since been removed from the remainder of the paper.

5.
   (a) “And also add the set value for the thrust on the AD. Then clarify why you have chosed for that number and whether it is constant over the AD or the integrated value over the disk for varying axial velocity.

   (b) and what about the thrust value on the AD? Is that kept constant? Clarify this!

(c) what value?? (see above remark)!

(d) But I think it is key to provide the calculated thrust on the duct as a function of the thrust on the AD! So please add this information, which is implicitly generated and can hence be provided from your CFD implementation! This will significantly increase the value of this article! And the thrust coefficient is kept constant? And at which value?"

The above question is multi-part but all the questions hint at the fact the details regarding the coefficient of thrust were insufficiently highlighted in the paper. The thrust coefficient is $_T = 0.767$ obtained from experimental data conducted by Dighe et al. (On the effects of the shape of the duct for ducted wind turbines). A moderate value of thrust coefficient has been taken into consideration to evaluate the aerodynamic performance of the diffuser. The value and relevant clarifications have been added to the revised version of the manuscript.

6. "This needs some clarification. Do you mean that the ratio between the diffuser exit area and the area of the location of the AD is constant? And if so, you should provide its value (is it 1.84 as in Igra's experiments or different?). So this means that the angle of attack of the various airfoils considered in this first stage differs from airfoil to airfoil? Please clarify this."

   The area ratio is defined as the ratio of the diffuser exit to the area of the actuator disk plus the tip clearance. The authors understand that there has been some confusion regarding this definition in the paper. The area ratio is maintained constant by keeping the angle of attack of the airfoils as $0°$. This is the basis of the evaluation of the first stage. The revised manuscript has corrected this by keeping common terminologies across the paper for a clear understanding of the concept.

7. "You need to elaborate this. What exactly is your criterion to eliminate airfoils? Is it the achieved velocity augmentation? And since you do not modify the angle of

attack of a given airfoil it might well be eliminated because it is operating in an off-design operational setting point." The results section and other sections do not clearly highlight the above mentioned concern of the reviewer. The elimination is based on velocity augmentation. The velocity augmentation is compared to the test case and if the criteria of augmentation the airfoil is eliminated and the remaining airfoils are carried forward. The methodology employed is inspired from the one employed by Dighe et al. (On the effects of the shape of the duct for ducted wind turbines).

8. "Can you clarify the importance of this figure? I don't get it. Especially not the importance of the thickness ratio. Is this because of structural considerations? And why not present the camber of the considered airfoils because I can imagine that that is an important parameter creating superior diffuser performance."

   The authors understand that the previous manuscript had not been clear in highlighting the results of the simulations relevantly. The new manuscript has a revamped result section that takes into account the various points the reviewers had made, including appropriate and relevant graphs.

9. "But that would mean that the optimised aoa for e.g. all the Eppler airfoils considered is equal to 15 degrees? I can hardly imagine this! Elaborat on this!!."

   Based on our simulation data the maximum velocity augmentation was found to be almost consistent with a single angle of attack across the airfoil family that was under consideration. Simulations were performed in accordance to the simulation methodology as mentioned in the paper.

10. "A number of observations need to be made with this result:

    (a) the location of the AD does not seem to be in the "throat" of the diffuser. Why not?

(b) is the area ratio in this case defined as the ratio of the exit area (the diffuser area at the location of the trailing edge) and area of the AD (+tip gap?)

(c) can be clearly seen from the resulting velocity contour that the cp distribution differs from a normal cp distribution (a cp distribution of the same single airfoil). It is quite interesting, and important, that you present some of these pressure distributions in this article. E.g. two cp distributions at either the same a.o.a. or two distributions generating the same Cl. That will certainly help in better understanding the AD-diffuser interaction and hence strongly enhance the value of this article!"

(a) The position of the AD is fixed in the nozzle of the duct, which is the region of the narrowest cross section of the duct. This assumption corresponds to previous work done in the field of DAWT.

(b) The area ratio is indeed the ratio of the exit area and the area of the AD with the tip gap accounted for.

(c) The The authors have considered the suggestion of the reviewer some changes have been made to the new manuscript.

11. "You need to be more precise about the flange. What is the size and how is it mounted on the airfoil. EG: by adding a flange with a length xxx mounted at an angle of yyy degrees with respect to the pressure side of the airfoil...."

The authors note the suggestion and changes will be incorporated in the new manuscript. However, the flange has been added in accordance with the work performed by El-Zahaby et al. (CFD analysis of flow fields for shrouded wind turbine's diffuser model with different flange angles). The flange length is 30% of the chord length of the airfoil, at an angle of 15 deg with respect to the vertical on the pressure sides of the airfoils.





Printer-friendly version

Discussion paper

12. "It would help if figures 5 and 6 have the same legend."

    Relevant changes will be incorporated in the new manuscript.

Wind Energ. Sci. Discuss.,
https://doi.org/10.5194/wes-2020-14-AC2, 2020




# *Interactive comment on* "Computational Analysis of High Lift Generating Airfoils for Diffuser Augmented Wind Turbines" *by* Aniruddha Deepak Paranjape et al.

**Aniruddha Deepak Paranjape et al.**

radha.parikh11@gmail.com

Received and published: 9 May 2020

As authors, we appreciate the time and effort you have taken to review the paper. We have considered all the concerns that have been pointed out and have made efforts to incorporate the changes in our revised manuscript.

1. "It may be premature to consider optimization of airfoil choice using rather high end computational methods on a configuration that is relatively remote from a realistic design configuration which would have an axisymmetric structure, optimized loading and wake rotation".

The authors understand the reviewer's concerns. Although there is a significant amount of literature employing the use of high-fidelity numerical modeling techniques applied to DAWTs, there is no preliminary analysis that may help practitioners and potential manufacturers design diffusers with commonly available airfoil geometries. The paper is a step in that particular direction.

2. "In the penultimate sentence of Section 3.4, it is mentioned that “a constant duct thrust coefficient is maintained . . ..” Please state the value chosen for Ct."

   The information relevant to the coefficient of thrust has perhaps been insufficiently highlighted. A thrust coefficient of Ct = 0.767 was fixed in the case of our study. This value was obtained from the experiments carried out by Dighe et al. (On the effects of the shape of the duct for ducted wind turbines). This information has now been sufficiently highlighted throughout the paper.

3. Size of the duct is a cost factor and therefore it may be best to compare always at fixed area ratio although I would concede that it is worth knowing the variation with angle and area ratio

   The comparisons of the airfoils have been made within a particular family keeping the area ratios fixed at a particular angle of attack. For example: All the NACA airfoils have been compared to each other at $14^\circ$ However, the authors understand what the reviewer is hinting at, and the relevant information can be incorporated into the new manuscript.

4. I recommend presenting the velocity values in Table 1 with the same number of significant figures (3 would surely be enough?) and making Table 3 consistent.

   The new manuscript incorporates the suggestions made by the reviewer.

**Relevant Changes:**

1. Necessary changes made to the introduction
2. AD Section updated with relevant formulae
3. Diagram highlighting DAWT schematic updated
4. Added figure for final diffuser geometry highlighting various parameters
5. Diagram for simulation methodology changed for clarity
6. Methodology flowchart added
7. Significant figures for the paper has been made constant
8. Added relevant equations and values to make the paper comprehensive
9. Governing equations section removed
10. Result section completely overhauled keeping referee comments in mind
11. Result section has been split into three sections for detailed analysis
12. Camber ratio, thickness ratio vs normalized velocity graphs added
13. All contour legends have been made constant
14. Ct vs Normalized velocity graph added
15. Conclusion, appendix section added and references updated

# Computational Analysis of High Lift Generating Airfoils for Diffuser Augmented Wind Turbines

Aniruddha Deepak Paranjape[1], Anhad Singh Bajaj[1], Shaheen Thimmaiah Palanganda[1], Radha Parikh[1], Raahil Nayak[1], and Jayakrishnan Radhakrishnan[1]

1. Department of Aeronautical and Automobile Engineering, Manipal Institute of Technology, Manipal 576104, Karnataka, India.

**Correspondence:** Aniruddha Deepak Paranjape (aniruddha.deepak@learner.manipal.edu)

**Abstract.** The impetus towards sustainable energy production and energy access has led to considerable research and development in decentralized generators, in particular, diffuser augmented wind turbines. This paper aims to characterize the performance of a diffuser augmented wind turbines using high lift airfoils using a three-step computational analysis. The study is based on computational fluid dynamics, and the analysis is carried out by solving the unsteady Reynolds-averaged Navier-Stokes (RANS) equations in two dimensions. The rotor blades are modeled as an actuator disk, across which a pressure drop is imposed analogous to a three-dimensional rotor. We study the change in performance of the enclosed turbine with varying diffuser cross-sectional geometry. In particular, this paper characterizes the effect of a flange on the flow augmentation provided by the diffuser. We conclude that at the end of the three-step analysis, Eppler 423 showed the maximum velocity augmentation.

## 1 Introduction

Global energy demand is expected to more than double by 2050 owing to the growth in population and development of economies (Gielen et al., 2019). Wind energy is emerging as an alternative renewable source for energy production. Presently, wind turbines are typically installed away from the populated areas because of visual and noise regulations. This necessitates the transfer of electricity via grids over larger distances, which increases the levelized cost of electricity. While large wind turbines are placed where the wind topology is optimum, smaller wind turbines are locally built to supply power to meet the demands.

A conventional horizontal axis wind turbine (HAWT), which is often simplified and modeled as an actuator disk (AD), has the ability to extract 59.3% of power available in the wind - in accordance to the Betz limit. Diffuser augmented wind turbines (DAWTs) have the ability to increase the power extracted by the wind turbine by virtue of: increased mass flow rate through the rotor plane, improved wake mixing with the external flow, and lastly, improved performance even in cases where the flow may not be purely axial in nature.

The idea of a DAWT, also commonly referred to as a ducted wind turbine or shrouded turbine, was first explored by Lilley and Rainbird (Lilly and Rainbird, 1956). Since the early studies, numerous studies based on empirical, computational and experimental approaches have been conducted to investigate and optimize the efficiency of diffuser augmented wind turbines

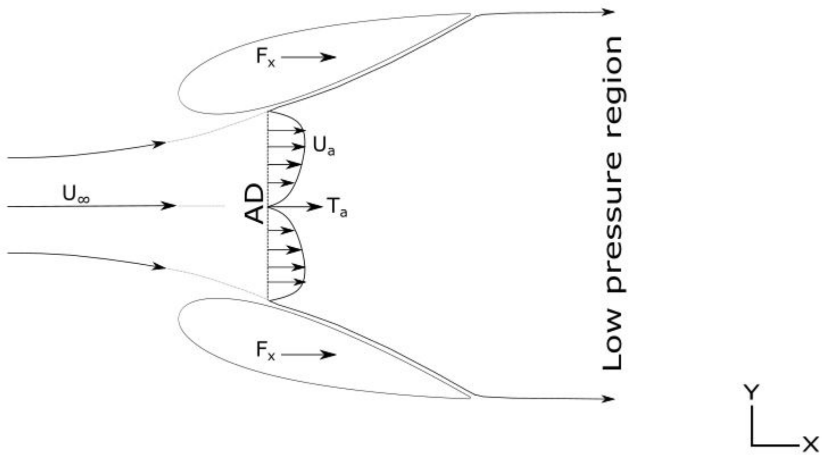


**Figure 1.** Schematic of a diffuser augmented wind turbine

through various means. By enclosing a diffuser around the turbine, the wake of the turbine blades is allowed to rapidly expand, resulting in a subsequent drop in pressure aft of the diffuser. This in turn leads to an increase in the mass flow rate of the incoming free stream air, thereby increasing the efficiency of the system beyond the Betz limit. Through wind tunnel testing, Igra (Igra, 1981) found that power coefficient could be improved by 80% of that of a conventional wind turbine just by placing a diffuser over it. Abe and Ohya (Ohya et al., 2008), varied the diffuser open angle by adding a flange around the diffuser exit. The study showed that flanged diffusers, that is, an additional geometric modification to the shroud can cause a larger wake expansion due to unsteady low pressure regions generated by the flange periphery. The mass flow rate is thus further increased by this geometric feature. Although there is a significant amount of literature employing the use of high-fidelity numerical modeling techniques applied to DAWTs, there is no preliminary analysis that may help practitioners and potential manufacturers design diffusers with commonly available airfoil geometries. Although studies such as the ones performed by Alquraishi (Alquraishi et al., 2019) document robust approaches towards tailoring the geometrical characteristics of airfoils using genetic algorithms, the authors highlight a simplified simulation pipeline that may assist designers in assessing the suitability of a pool of airfoils while designing DAWTs or other decentralized wind energy generators.

The use of high-lift airfoils in wind energy applications has been documented extensively in literature. High lift airfoils improve the aerodynamic efficiency ($C_L/C_D$) at low Reynolds number by virtue of a high lift coefficient with minimum drag penalties. Through this study, we investigate the effect of camber, thickness and a flange on high lift airfoil families, and characterize their performance. The turbine is modeled as an two-dimensional AD and a pressure drop is induced across this disk in accordance to Bernoulli's Theorem. This pressure drop characterizes a change in the velocity field as the flow passes the rotor and energy is subsequently extracted. In the study, we consider a two-dimensional flow field for the analysis, in accordance to studies conducted by Dighe (Dighe et al., 2018). The separation effects and flow losses from the tips are assumed to be negligible. The numerical analysis has been carried out using the commercially available computational fluid dynamics (CFD) solver ANSYS® Fluent.

The remainder of this paper is organized as follows: Section 2 describes the actuator disk modeling and presents the mathematical model used in the study. Section 3 discusses the simulation methodology, and the validation of the computational study.

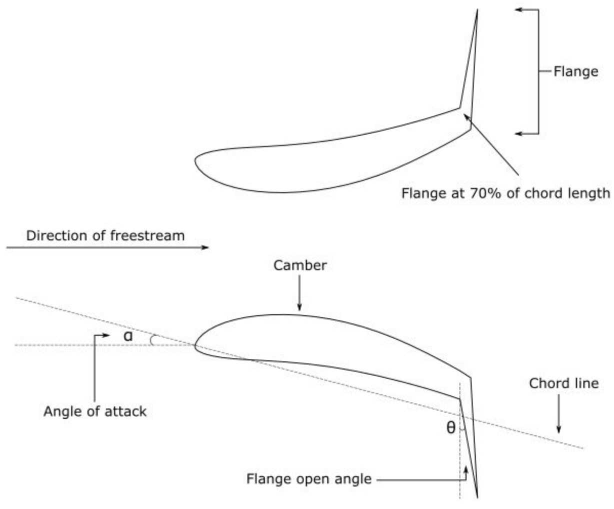


**Figure 2.** A schematic of the final geometry of the diffuser shape with all the parameters highlighted

## 2 Actuator Disk Modeling

The AD uses the mass and momentum conservation principles to balance the applied forces as compared to the axial and tangential momentum equations that balance the applied forces on the real rotor blades. Although a two-dimensional simplification may not account for three-dimensional effects such as wake rotation and lateral flow, several studies have validated this approach .

The AD is considered to have an infinitesimal width which exerts a constant thrust $\mathrm{T_{AD}}$, per unit surface. The turbine or AD coefficient is given by:

$$C_{\mathrm{T_{AD}}} = \frac{T_{\mathrm{AD}}}{\frac{1}{2}\rho {U_\infty}^2 S_{\mathrm{AD}}}$$

where, $\rho$ is the fluid density, $U_\infty$ is the free-stream velocity and $S_{AD}$ is the surface area of the AD.

The thrust force $T_{\mathrm{AD}}$ force can be written as:

$$T_{\text{AD}} = S_{\text{AD}}(\Delta p)$$

where $\Delta p$ is the pressure drop across the AD. $\delta p$, and ultimately $C_{\text{T}_{\text{AD}}}$ is input for the simulations as a constant, derived from experimental investigations conducted by (Tang et al., 2018). The current experimental configuration involves the consideration of an additional force created by the diffuser, $\text{T}_{\text{Duct}}$. Thus we can define $\text{C}_{\text{T}_{\text{Duct}}}$ as:

$$C_{\text{T}_{\text{Duct}}} = \frac{T_{\text{Duct}}}{\frac{1}{2}\rho {U_\infty}^2 S_{\text{AD}}}$$

The duct force $\text{F}_{\text{Duct}}$ creates a mass flow across the AD plane.:

$$\dot{m} = \rho S_{\text{AD}} U_{\text{AD}},$$

Although a constant coefficient of thrust is assumed, the velocity across the AD is not uniform. The average AD velocity can be found by integrating the free-stream velocity over the defined surface area of the AD:

$$U_{\text{AVG}} = \frac{1}{S_{\text{AD}}} \int \frac{\partial U}{\partial x} dS$$

Using the above results we can define a power coefficient for the diffuser geometry with an AD of surface area $\text{S}_{\text{a}}$:

$$C_{\text{P}} = \frac{P}{\frac{1}{2}\rho {U_\infty}^2 S_{\text{AD}}} = \frac{U_{\text{AVG}}}{U_\infty} C_{\text{T}}$$

Therefore the total thrust force can be represented as a vectorial sum of the AD force $\text{T}_{\text{AD}}$ and duct force $\text{T}_{\text{Duct}}$, given by:

$$T = T_{\text{AD}} + T_{\text{Duct}}$$

Thus the total thrust coefficient is given by:

$$C_{\text{T}} = C_{\text{T}_{\text{AD}}} + C_{\text{T}_{\text{Duct}}}$$

## 3 Computational Fluid Dynamics Methodology

### 3.1 Simulation Domain

To conduct the present study, ANSYS® and its constituent modules were used to generate, simulate, visualize and process the results. ICEM CFD®, ANSYS Inc. was used to generate the mesh required, as it offers great control and flexibility over the grid generation process. Figure 2 highlights the computational domain which was chosen as a C-Type topography, as it is easy to generate and minimizes the skewness of the mesh in the near-wall condition. It also has the ability to accurately simulate the flow at various angles of attack. The geometry consists of two-dimensional planar airfoils symmetrically placed about the central axis along with a rotor modeled as an AD. Following the work of Dighe et al, (Dighe et al., 2019) the tip clearance has been fixed at 2.5% . The free-stream velocity is set as 6 m/s for the present study and the flow is considered to be steady, uniform, incompressible and turbulent for the airfoil chord length. While the simulated conditions are two dimensional, the conditions are sufficient to gain enough insights due to the axisymmetric nature of the flow. For the given Reynolds number, the Y+ was kept well under 1 in order to calculate the wall spacing assisting the meshing process.

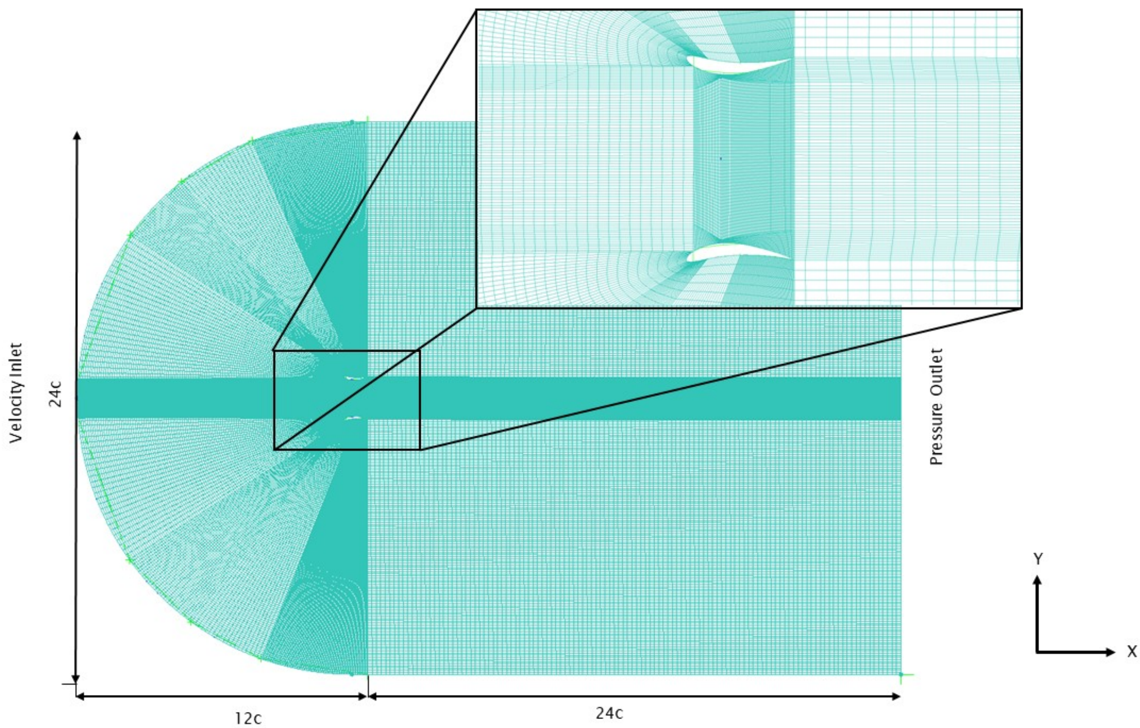


**Figure 3.** The C-Type topography computational grid

To properly model the viscous flows over the various diffuser configurations at turbulent Reynolds numbers, the Navier–Stokes equations are selected in Cartesian coordinate system. The turbulence model used is k-$\omega$ Shear Stress Transport (SST) which is expressed as a set of partial differential equations. The k-$\omega$ SST, which was developed by Menter (Menter et al., 1994), is a two equation robust model for turbulence growth and is one of the most widely used turbulence models. This is because the SST combines the use of $k-\omega$ in near wall flow and $k-\epsilon$ in free shear flow.

ANSYS Fluent® was used as the flow solver, while CFD Post® and GNU Octave® were used to process the results.

### 3.2 Simulation Methodology

The present study is to assess the basic aerodynamic performance of high lift airfoils when applied to a DAWT geometry. Figure 3 highlights 12 airfoils that have been chosen from 3 different airfoil families which are Eppler, NACA and Selig. The airfoils were selected based on their lift-drag ratio for the chosen Reynolds number. (Dighe et al., 2018)


**Figure 4.** Selection of high lift airfoils across different families

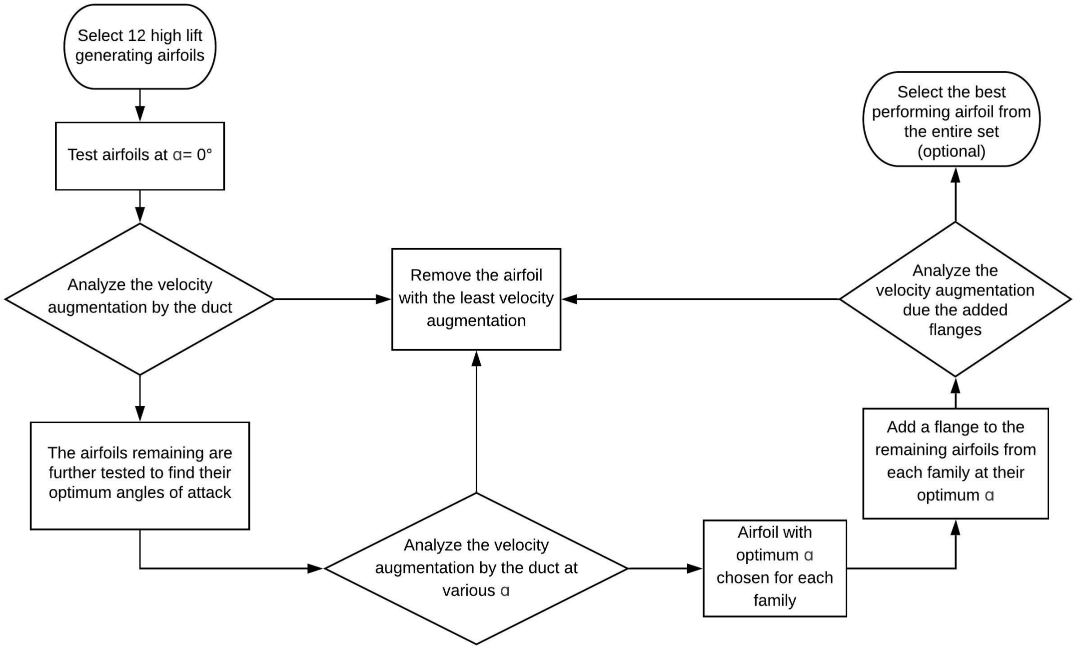


**Figure 5.** A flowchart that visualizes the simulation methodology and processes

The study was conducted in three stages. In the first stage, all airfoils were fixed at a constant angle of attack of $\alpha = 0°$ with respect to the horizontal. The angle of attack here corresponds to the area ratio. The area ratio is defined as the ratio of the area of the exit of the diffuser to the area of the AD ($S_{\mathrm{E}}/S_{\mathrm{AD}}$). The results obtained for each case were compared to the NACA 0012 test case. RANS equations were used in this analysis for maximum simplicity. Based on the results of the first stage of simulations, one airfoil was eliminated from each of the families on the basis of its velocity augmentation (Igra, 1981).

In the second stage, the angle of attack of the airfoils corresponding to their area ratios were varied and the end result was an optimized angle of attack for each of the families. After concluding simulations of the second phase, one airfoil from each family was eliminated based on its velocity augmentation again, leaving 2 best performing airfoils from each family. In the third stage, the six final airfoils were then analyzed at their optimum angles of attack and added with a 15° flange at the trailing edge at 70% of the chord to generate an unsteady low pressure region at the trailing edge which in turn increases the mass flow rate at the AD.

A constant diffuser thrust co-efficient of $C_{\mathrm{T}} = 0.767$ (Dighe et al., 2018) is maintained by keeping a constant pressure difference across the AD. Tip clearance has been fixed at 2.5% throughout the study. The effects of varying the tip clearances on the duct performance are beyond the scope of this study.

### 3.3 Grid Validation and Independence Studies

A grid validation was conducted to verify the accuracy of the mesh, while a grid convergence study was conducted to determine the optimum mesh configuration without sacrificing the accuracy of the result.

Igra's (Igra, 1981) experimental wind tunnel set-up was replicated in the numerical domain, to validate the mesh that was generated. Igra et al carried out numerous experiments during his research on diffuser augmented wind turbines. Of these, their work on experimental set-up of the 'Circular Wing Shrouds' was considered reference to validate our study. Analogous to the experimental set-up, the numerical domain uses the NACA 4412 airfoil which was simulated in a planar diffuser configuration. The angle of attack of the airfoils was fixed at 2° and the area ratio maintained at 1.84 for this configuration. Wall blockages and interferences were ignored for the experimental set-up to avoid elaborate wind tunnel corrections. The inflow velocity was maintained at 6 m/s. The results were analyzed against experimental pressure distributions and forces.(Dighe et al., 2019) The final mesh generated using ICEM CFD tool was akin to Igra's experimental results thus proving the validity of the mesh.

Three meshes were used with different number of nodes and elements, in order to optimize the mesh in terms of simulation time. All the meshes had NACA 4412 as the airfoil and were simulated under similar conditions with an inlet velocity of 6m/s.

**Table 1:** Grid Convergence Study Results

| Grid | Number of Elements | Velocity Output $(m/s)$ |
|---|---|---|
| Coarse | 4776 | 7.82 |
| Medium | 1752919 | 8.67 |
| Fine | 457512 | 8.76 |

The first mesh was coarse, with roughly 4627 nodes and 4776 elements in total and took 2 minutes to converge. As expected, the mesh gave a very poor result with a velocity of 7.82 m/s at the AD. The second mesh was a fine mesh with a total of roughly 174246 nodes and 175291 elements. This mesh took about 10 minutes for the solution to converge and gave a better and a more accurate result with a velocity of 8.67 m/s at the AD. The third mesh was even finer and had a total of 456031 nodes and 457512 mesh elements. This mesh took about 22 minutes for the solution to converge and gave a velocity of 8.76 m/s at the AD. The finest mesh differed by a 0.98% from the medium quality mesh. Thus the medium quality mesh with 174246 nodes and 175291 elements was chosen, as it was accurate with an added advantage of reduced computational time and power.

## 4 Results and Discussion

The following sections highlights the results of all the stages of the analysis. The airfoils were tested for different geometrical modifications and their aerodynamic performance. The under performing airfoils were removed from the rest of the analysis. The airfoils were evaluated at a constant diffuser thrust coefficient value $C_{\mathrm{T}} = 0.767$.

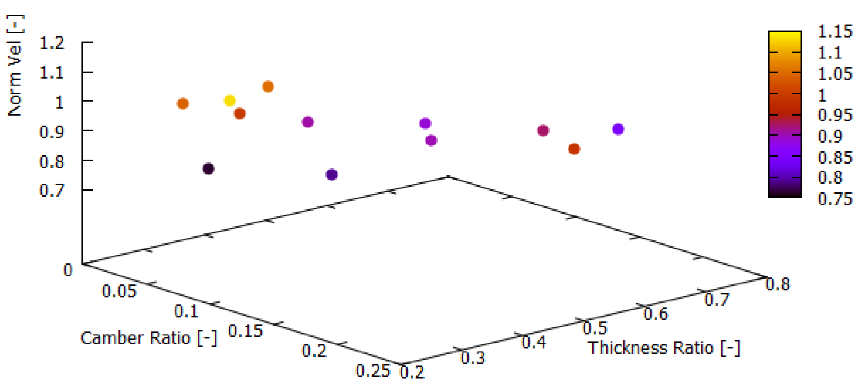


**Figure 6.** Effect of camber and thickness of the diffuser on the normalized velocity at the actuator disk

### 4.1 Stage 1: Constant $\alpha$

All the simulations for the first stage were performed with an angle of attack $\alpha = 0°$ to asses the basic aerodynamic performance of the airfoils. Figure 5. expresses the variations of the camber, thickness and diffuser velocities of the various airfoils, which are maintained at $\alpha = 0°$. The camber (mc) and thickness (t) are represented as ratios while the velocity at the AD has been normalized with respect to the free-stream velocity of 6 m/s. The camber ratio is defined as the maximum camber percentage to location of maximum camber on the chord expressed as a percentage. The thickness ratio is defined as the maximum thickness percentage of the airfoil to the position on the chord at which the thickness is maximum. To assess the graph, the velocity has been presented with a colour chart. The colours represent the performance of the airfoils compared to the base case. From the results of the graph, three under performing airfoils, one from each family was eliminated. The airfoils that were eliminated were Selig S1221 with a $mc = 0.0997$, $t = 0.555$ and with a normalized velocity of 0.8863, Eppler E222 with a $mc = 0.0379$, $t = 0.3279$ and with a normalized velocity of 0.7616 and lastly NACA 63(2)-615 with a $mc = 0.1$, $t = 0.4$ and with a normalized velocity of 0.7885. Looking at Figure 5 it is clear that camber plays a crucial role in velocity augmentation, even among high lift airfoils, while the effect of thickness is not so pronounced. This can be attributed to the effect of the curvature of the airfoil on the boundary layer. The boundary layer is subject to both curvature and a pressure gradient. For the convex surface of the curvature the angular momentum of the flow increases with an increase in curvature. As per the Rayleigh criterion the increase in angular momentum causes a stabilizing effect on the flow resulting in lower skin friction coefficient. Thus the direct effect of camber can be seen in higher velocity augmentation at the AD resulting in a higher $C_{\mathrm{P}}$ as per the classical definition of the power coefficient. This also highlights the strong correlation between the camber and the velocity augmentation at the AD, similar to previous studies done in DAWT.

### 4.2 Stage 2: Varying $\alpha$ to find the optimum angle for maximum velocity augmentation

For the second stage analysis, the best performing airfoils were taken from the results of stage one which were based on the velocity augmentation at the AD. As per the next step in the simulation methodology, their angles of attack and in doing so the area ratios were varied, keeping the $C_{\mathrm{T}} = 0.767$. The angles of attack were varied from $\alpha = 0°$ to $\alpha = 12°$ in steps of 4°, and subsequently by 1° till $\alpha = 20°$. For the initial variations of up to 12°, the flow remained attached to the surface of the airfoil. As the angle of attack was increased, an upward trend was noted in the velocity at the AD. This is a consequence of an increase in the mass flux of the wind as a result of the changing area ratios. Beyond a certain angle of attack and area ratio there was flow separation that was observed on the pressure side of the airfoil, which was found to be detrimental to the velocity augmentation of the airfoil. Thus, there was an optimum angle of attack and area ratio where there was maximum velocity augmentation. Based on the results of the simulation the optimum angle for Eppler, NACA and Selig was found to be $\alpha = 15°$, $\alpha = 14°$ and $\alpha = 18°$ respectively. Based on the criteria of velocity augmentation at the AD, the study was taken forward by eliminating the NACA 64A410, S1221 and E1210 airfoils which registered the least velocity augmentation in stage two.

### 4.3 Stage 3: Effects of a Flange

A third and final stage was conducted by adding a flange at 70% of the airfoil chord at an open angle of 15°, as per the study conducted by El-Zahaby et al (El-Zahaby et al., 2016). Figure 2 highlights the final geometry of the diffuser shape along with the various paramters that are at play. It was observed that there was a significant increase in the velocity at the AD after the addition of the flanges. This velocity increase can be attributed to a reduction in pressure due to vortices that are generated due to the effects of the flange and the diffuser shape. These vortices produce a region of unsteady low pressure which increases the mass flux of wind at the AD. Figure 6 consists of the velocity contours of the final set of airfoils a) NACA 2411, b) NACA

4412, c) Eppler 59, d) Eppler 423, e) Selig 1210, f) Selig 1223. The vortices are easily visualized in Figure 6 along with the flow separation due to flange.

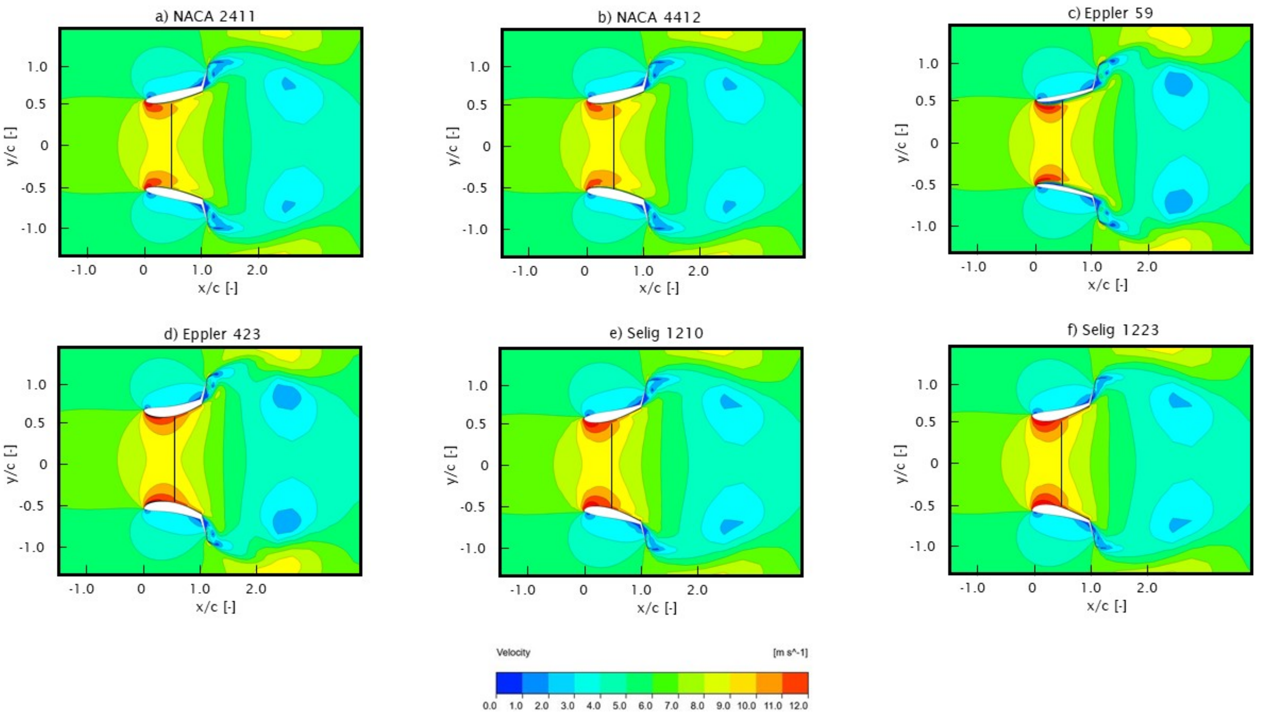


**Figure 7.** Velocity contours of the streamwise normalized velocity. The results depict performance of the stage three airfoils at $C_T = 0.767$

As per the classical definition of the power coefficient, the $C_P$ is affected by the velocity of the flow at the AD. The power co-efficient is an important parameter that is used to determine the diffuser performance. Figure 7 is used to visualized the effect of the thickness ratio and camber ratio on the $C_P$ in a 3D space. To assess the graph, the $C_P$ has been presented with a colour chart. NACA4412, S1223 and E423 are the best performing airfoils from each of the respective families in terms of velocity augmentation and $C_P$, with a velocity output of 9.216928 m/s, 9.410147 m/s and 9.432198 m/s respectively. Overall it was found that Eppler 423 showed the maximum velocity augmentation and $C_P$ among all the 12 airfoil geometries that were considered.

For the best performing airfoil, the thrust coefficient $C_T$ was varied and the resulting velocity at the AD was normalized with the free-stream velocity. Figure 8 shows an almost linear relation between the parameters. Increasing the $C_T$ results in a reduction of the velocity augmentation, this phenomenon can be compared to increasing the blockage to the flow by virtue of an increase in resistance. This is in agreement with other work performed in DAWT and DAWT theories. The current simulations are performed with a moderate value of $C_T$. The exact effects of the $C_T$ and tip clearance are out of the present scope of the study, but can be the subject matter of another study.

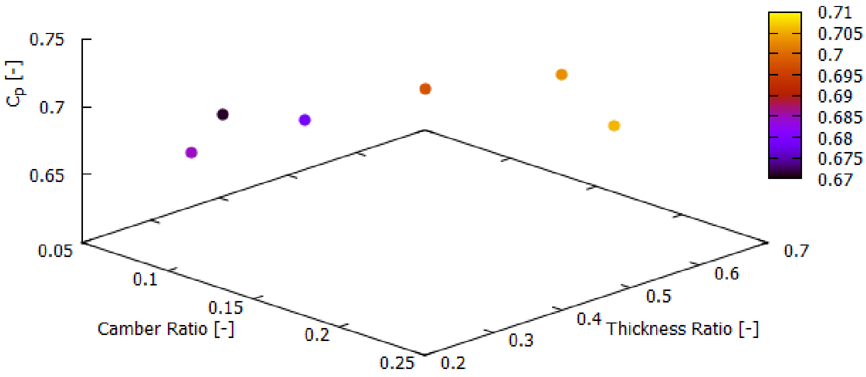


**Figure 8.** Effect of camber and thickness of the diffuser on the $C_P$ for the airfoils in the third stage

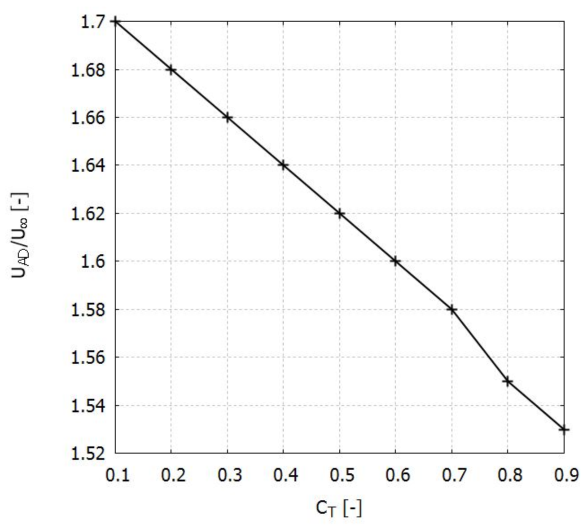


**Figure 9.** The result depicts the effect of varying the $C_T$ on the normalized velocity at the actuator disk

## 5 Conclusions

In the present study, the aerodynamic performance of DAWT using high lift airfoils was studied using an AD model. The study was performed using RANS simulations, the results of which are presented. Based on the previous studies, different diffuser geometries of 12 high lift airfoils was considered. A validation study was conducted to compare the numerical results to existing data and its results are reported. The diffusers, made up of the 12 airfoils were subject to evaluation based on three different stages. In the first stage the area ratio was kept constant by maintaining the $\alpha = 0°$. Based on the velocity augmentation, the best performing airfoils were tested by varying their area ratios and their corresponding angle of angles of attack in stage two. An optimum angle of attack was found at the end of stage two. A final third stage was performed by adding a flange of 15° to the airfoils. Based on the results of velocity augmentation and $C_{\mathrm{P}}$, it was concluded that E423 was the best performing airfoil. The detailed effects of tip clearance and $C_{\mathrm{T}}$ on the effects of diffuser performance can be a subject of future studies.

## 6 Appendix A

### Nomenclature

| | |
|---|---|
| $\alpha$ | Angle of attack of the airfoil [ ° ] |
| $\rho$ | Density of air $[kg/m^3]$ |
| $AD$ | Actuator Disk |
| $c$ | Diffuser chord length [m] |
| $C_{\mathrm{P}}$ | Power coefficient of the AD [-] |
| $C_{\mathrm{T_{AD}}}$ | Thrust coefficient of the AD [-] |
| $C_{\mathrm{T_{Duct}}}$ | Thrust coefficient of the Duct [-] |
| $C_{\mathrm{T}}$ | Total thrust coefficient of the AD model [-] |
| $DAWT$ | Diffuser Augemented Wind Turbine |
| $HAWT$ | Horizontal Axis Wind Turbine |
| $mc$ | Camber ratio [-] |
| $S_{\mathrm{AD}}$ | Reference area of the AD $[m^2]$ |
| $S_{\mathrm{E}}$ | Area of the exit of the diffuser $[m^2]$ |
| $T$ | Total thrust force of the diffuser $[N]$ |
| $t$ | Thickness raito [-] |
| $T_{\mathrm{AD}}$ | Thrust force on the AD $[N]$ |
| $T_{\mathrm{Duct}}$ | Thrust force on the diffuser $[N]$ |
| $U_{\mathrm{AD}}$ | Velocity at the AD plane $[m/s]$ |
| $U_{\mathrm{AVG}}$ | Average velocity at the AD plane $[m/s]$ |
| $U_{\infty}$ | Free-stream velocity $[m/s]$ |
| $x$ | Variable value vector parallel to the free-stream direction [-] |

$y$ Variable value vector normal to the free-stream direction [-]

*Author contributions.* ADP wrote the bulk of the paper, performed the CFD simulations and post-processed the results. ASB performed CFD simulations and contributed to writing and reviewing the paper. STP modeled the geometries and contributed significantly in writing the paper. RP modeled the geometries. RN performed CFD simulations and helped set up the CFD simulations. JR helped formulate ideas through group discussions.

*Competing interests.* The authors declare that they have no conflicting or competing interests.

## 7 References


Alquraishi, B. A., Asmuin, N. Z., Mohd, S., Abd Al-Wahid, W. A., Mohammed, A. N. (2019). Review on Diffuser Augmented Wind Turbine (DAWT). International Journal of Integrated Engineering, 11(1) Aly, M., El-Zahaby, Kabeel, A.,E., Elsayed., S.,S., Obiaa, M.,F.,: : CFD analysis of flow fields for shrouded wind turbine's diffuser model with different flange angles, Alexandria Engineering Journal (2016), https://doi.org/10.1016/j.aej.2016.08.036, 2017.

A. Aranake and K. Duraisamy: Aerodynamic optimization of shrouded wind turbines, Wind Energ. (2016) DOI: 10.1002/we.2068

Dighe,V. V., Oliveira,G.de.: On the effects of the shape of the duct for ducted wind turbines, AIAA SciTech Forum. 2018.

Dighe,V. V., Oliveira,G.de., Avallone,F., van Bussel G.J.W.: Towards improving the aerodynamic performance of a ducted wind turbine: A numerical study. Journal of Physics: Conf. Series, :10.1088/1742-6596/1037/2/022016, 2018. 16

Dighe, V., Suri, D., Avallone, F., and van Bussel, G.: Ducted wind turbines in yawed flow: A numerical study, Wind Energ. Sci. Discuss., https://doi.org/10.5194/wes-2019-62, in review, 2019.

Ghenai,C., Salameh, T., Janajreh, I.: Modeling and Simulation of Shrouded Horizontal Axis Wind Turbine Using RANS Method. JJMIE. 11. ISSN 1995-6665. 2017.

Gielen, D., Boshell, F., Saygin, D., Bazilian, M. D., Wagner, N., and Gorini, R.: The role of renewable energy in the global energy transformation, Energy Strategy Reviews, 24, 38–50, 2019.

Igra, O.: Research and development for shrouded wind turbines, Energy Cont. Momt Vol. 21. pp. 13 to 48, https://doi.org/10.1016/0196-8904(81)90005-4, 1981

Lilley, G.,M., Rainbird, W., J,: A preliminary report on the design and performance of ducted windmills Report No. 102, April, 1956.

Menter, F., R.,: Two-Equation Eddy-Viscosity Turbulence Models for Engineering Applications, AIAA JOURNAL Vol. 32,No. 8, August 1994

Mikkelsen, R. F.: Actuator Disk Methods Applied to Wind Turbines, Kgs. Lyngby, Denmark: Technical University of Denmark (DTU). MEK-FM-PHD, No. 2003-02, 2004

Ohya, Y., Karasudani, T., Sakurai, A., Abe, K-I., Inoue, M.:Development of a shrouded wind turbine with a flanged diffuser. Journal of Wind Engineering and Industrial Aerodynamics, 96(5), 524-539. https://doi.org/10.1016/j.jweia.2008.01.006, 2008.

Radhakrishnan, J., and Suri, D.: Design and Optimisation of a Low Reynolds Number Airfoil for Small Horizontal Axis Wind Turbines, IOP Conference Series: Materials Science and Engineering. Vol. 377. No. 1. IOP Publishing, doi:10.1088/1757-899X/377/1/012053, 2018

Suri, D.: Design of an Optimized Inlet Shroud for a Flanged Diffuser, 10.31224/osf.io/2qb6r, 2019.

Tang J, Avallone F, Bontempo R, van Bussel GJW, Manna M. Experimental investigation on the effect of the duct geometrical parameters on the performance of a ducted wind turbine. J Phys Conf Ser. 2018;1037(2):022-034.