Reply to comments by Reviewer Nr. 3

Giorgia Guma on behalf of the authors IAG, University of Stuttgart

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The authors would like to thank the reviewer for his/her efforts and valuable comments. They are very much appreciated and incorporated into the revised paper.

In the present document the comments given by the 3rd reviewer are addressed consecutively. The following formatting is chosen:

- The reviewer comments are marked in blue and italic.
- The reply by the authors is in black color
- A marked-up manuscript is added. Changed section with regard to the comments by reviewer 3 are marked in green. Changed sections with regard to comments by more reviewers are marked in gray.

General comments

1. "The overall subject of presenting a high fidelity FSI model is of considerable relevance for the research community as the turbines are continuously upscaled leading to more flexible designs where the aeroelastic effects become more and more important and require such FSI models to be truly analysed. The authors also mention this motivation in the introduction. However, a limitation of the paper content is that the simulations are carried out on a turbine design that is more than 20 years old and with a structural design that is much stiffer than designs that are more recent. Also the size of 2MW and a diameter of 80m for the chosen turbine is quite different from both recent reference turbine designs (e.g. the INNWIND and AVATAR reference rotors defined several years ago) in the research community as well as industrial designs that now have exceeded 10MW and 200m in diameter. The actual choice of the DANAERO turbine might be because detailed aerodynamic measurements are available for this turbine but the experimental data are only used in one case in the paper. So due to fact that the simulations are carried out on a relative stiff turbine design, some of the results and discussions of e.g. impact of flexibility on elastic torsion which are in the range of tenths of a degree, become somewhat theoretical without any real impact."

Thank you for your comment. Yes, you are right, this is a pretty old design, but the availability of high quality aerodynamic measurements data gives the IEA Task 29 participants the possibility to validate and improve models and approaches of different levels of fidelity. These field measurements have been especially used within another subtask in order to validate the pure aerodynamic model that was then used within the simulations of the aeroelastic task, and therefore for this paper. The main focus is to analyze the influence of resolved turbulence on the aeroelastic response of the turbine and therefore only a reference case has been validated with experimental results.

Specific comments

1. "The present title indicates that the paper has a considerable focus and part on simulating turbulent inflow conditions. However, it is a limited part of the paper so it could be considered to change the title, e.g. to: A High Fidelity Simulation Tool for Aeroelastic Simulations of Wind Turbine"

We think that modifying the title in this way would lead the reader to wrongly think that this FSI tool has been developed within this project. Although turbulence seems to be just a small part of the job, everything was made in order to get step by step to our last stop, turbulence respectively.

- 2. "Introducing the turbine used for the simulations as ".. the DANAERO turbine ..." is not precise as many in the research community do not know that specific turbine. So it should be changed to a real description of the turbine, e.g. "a 2MW NM80 turbine with an 80m diameter rotor". Also the text: ".. specific case of the DANAERO experiment.." could be more informative, e.g. like: ".. of the inflow turbulence is analysed for a specific case in comparison with experimental data from the DANAERO experiment." Thank you for the suggestion, we have changed in R3:S1 (page 1, line 1) and R3:S1bis (page 1, line 6).
- 3. "Minor typos in line 22 and 29" They have been corrected in $\boxed{\textbf{R3:S2}}$ (page 1, line 25) and $\boxed{\textbf{R3:S3}}$ (page 2, line 31).
- 4. "Line 96-97 The description of the turbulence generation by body forces is very brief please expand, e.g. over what axial distance are the body forces applied and how much does the turbulence decay down to the turbine?" We expanded it at R3:S4 (page 4, line 98).
- 5. "Line 128 What is the actual FMT time simulation length and what did determine the length ?" The FMT rigid has been calculated for a total of 20 revolutions, where 10 of them have been calculated in uniform inflow only. Afterwards, 10 revolutions more have been calculated in flexible state and rigid state at the same time, in order to be comparable. The DANAERO rotor presents a high induction, therefore it takes a long time for the wake to fully develop and to the loads to stabilze. In order to save computational costs we inject turbulence and let the structures deform, only after a cheaper simulation reached a low residuum, stable loads and a wake development long enough to avoid effects on the loads too. This informations has been added in R3:S5 (page 8, line 161).
- 6. "Line 165 -167 The discussion of this case is very short please expand" Thank you, it has been expanded in **R3:S6** (page 11, line 208). Please, consider that the pictures have been changed.
- 7. "Line 165-167 Why is not this case simulated with turbulence as the experimental data are shown, probably from several revolutions in turbulent inflow" We have calculated a case with the same turbulence intensity but only in rigid, and for completeness it is now added to the same caption. Anyhow we did not calculate it taking into account flexibility because of the low turbulence intensity in the experiment, that would have not lead to a structural response much different from the one in uniform case. So, at the end, we did not do it in order to save computational cost, because we thought it was enough for the validation.
- 8. "Line 173 174 The percentage values are shown with two decimals. They are probably based on the time trace values so maybe better just to show one decimal or how accurate are these values?" We agree that 2 decimals can be too brave, and therefore we changed it just to one, as you can see in [R3:S9] (page 11, line 221).

- 9. "Line 187 that Mx in 6 please correct" It has been corrected in R1:S8 (page 12, line 235)
- 10. "Line 215 An increase in power for coupled case of 3.5% is quite much is it a time varying flow due to separation in the region of 40-50% radius or what can be the causes?" We analyzed the pressure distribution at 40% and 50% of the blade radius in order to verify it, and added the pictures in the text. We detected a maximum pressure difference between the two cases on the pressure side of 2.5%. This sums together with the increase of the rotor disk area (due to the stretching of the pre-bended blade) and can explain the evaluated increase in power. We added this in R3:S11 (page 15, line 284).
- 11. "Line 248" ... in FMT a peak appears close to the first flap bending eigenfrequency of the blade (f1 = 0.938Hz) that could lead to instabilities .. ". Please show the position of that frequence by a vertical line in the spectrum. As concerns instability how can this lead to instability?" Thank you for your comment. Yes, you are right if the FFT of FMT tip deformations shows a peak close to f1, and FMU not, this peak is too small to be able to draw any conclusion about it. The sentence has been deleted and therefore no line on the spectrum was added, because not necessary anymore.
- 12. "Line 282-285 Could numerical stabilities in the coupling generate the considerable number of small oscillations?" Thank you for your comment. If there would be a stability problem of the coupling, it would show also in the deformations. These show for example in BMU, RMU and FMU to be really smooth, see fig. 6 and 16. The load oscillation occurs already in the rigid cases and it is a natural result of unsteady simulations where local inherently unsteady flow separation in the hub region causes slight load fluctuations. Therefore we do not think that it can be anyhow related to the stability of the coupling.

Aero-elastic analysis of wind turbines under turbulent inflow conditions

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Abstract. The aero-elastic response of a R3:S1 2 MW NM80 turbine with a rotor diameter of 80m and the interaction phenomena are investigated by the use of a high-fidelity model. A time-accurate unsteady fluid-structure interaction (FSI) coupling is used between a computational fluid dynamics (CFD) code for the aerodynamic response and a multi-body simulation (MBS) code for the structural response. Different CFD models of the same turbine with increasing complexity and technical details are coupled to the same MBS model in order to identify the impact of the different modeling approaches. The influence of the blade and tower flexibility and of the inflow turbulence is analyzed R3:S1bis R2:S6 starting from a specific case of the DANAERO experiment, where a comparison with experimental data is given. A wider range of uniform inflow velocities are investigated by the use of BEM as aerodynamic model. Lastly a fatigue analysis is performed from load signals in order to identify the most damaging load cycles and the fatigue ratio between the different models, showing that a highly turbulent inflow has a larger impact than flexibility, when low inflow velocities are considered. The results without the injection of turbulence are also compared and discussed to the one provided by the BEM code AeroDyn.

1 Introduction

The current design trend of wind turbines is leading to rotor diameters getting larger and larger, but they have to be light order to decrease the cost of wind power generations in terms of leveling energy costs (\$/kWh) and make it a competitive resource in comparison to other electric generations systems. A lot of research is done to investigate materials and construction techniques in order to allow lighter designs with the consequence that the rotor blades are becoming more and more flexible, which leads to large deformations with associated non-stationary loads and oscillations, resulting in unexpected changes in performances or even flutter, if the damping is negative. Additionally, large rotor wind turbines are in reality subjected to diverse inflow conditions, such as shear, turbulence and complex terrain, leading to higher wind instabilities and fluctuations. Moreover, the aerolastic instabilities strongly affect the operational life of wind turbines (Hansen et al. (2006)). Most of the available simulation tools for wind turbines aeroelasticity are based on engineering models like BEM for the aerodynamics and 1D MBS for the structural response, like for example in Riziotis et al. (2008) and Jeong et al. (2011). These models are cheap but rely on different correction models to take unsteadiness and 3D effects into account (Madsen et al. (2012)). In recent years, high-fidelity FSI has been frequently used for wind turbine applications. Sayed et al. (2016) implemented a coupling of the CFD solver FLOWer to the CSD (Computational Structure Dynamics) solver Carat++, where R3:S2 polly the blades

have been coupled either to a 1D beam or a 2D shell structural model. Yu et al. (2014) used a loose CFD-CSD coupling with an incompressible CFD solver and non-linear Euler-Bernoulli beam elements for the structure in order to investigate the aeroelastic response of the generic NREL 5 MW rotor. The communication in this case was only once per revolution. The same turbine was also used by Bazilevs et al. (2011b) and Hsu et al. (2012) by means of FSI between a low-order Arbitrary Lagrangian-Eulerian Variational Multi Scale (ALE-VMS) flow solver and a Non-Uniform Rational Basis Spline (NURBS) based structural solver. For the same turbine, Heinz et al. (2016) compared R3:S3 the coupling of the flow solver Ellypsys3D with the aeroelastic solver HAWC2 to the BEM results of HAWC2 alone. While he considered uniform inflow, Li et al. (2017) additionally considered a turbulent inflow synthetically generated by the use of a Mann box (Mann (1994)). Dose et al. (2018) presented a method to couple the flow solver OpenFOAM to the FEM-based beam solver BeamFOAM. A CFD-MBS coupling between the URANS solver TURNS and the MBS solver MBDyn was used by Masarati et al. (2011) to investigate the NREL Phase VI rotor.

Wind turbines are especially susceptible to fatigue damage, due to the oscillating characteristic of the affecting loads. Fatigue analysis are normally performed by manufacturers for certification purposes, and therefore they are mostly BEM-based. In the EU-project AVATAR (Schepers (2016)) it was shown that BEM-based calculations against high fidelity calculations led to a 15% error in the computation of fatigue. This error motivated the TKI WoZ VortexLoads project (Boorsma et al. (2019)), where starting from turbulent inflow conditions BEM based and CFD based calculation have been compared with each other and to experimental results.

In section 2 of this paper, the high-fidelity framework (as presented in Klein et al. (2018)) is described for fluid-structure interaction coupled simulations on the NM80 2MW wind turbine rotor, also known as DANAERO rotor, (DANAERO). Additionally, the inflow conditions and setup for the different cases are listed. Different setups are used with increasing complexity in order to isolate and characterize the effects of different parameters. In section 3, the aeroelastic response of the reference turbine is shown and the variation between the models with different elaboration is exposed. Lastly, Damage Equivalent Loading (DEL) calculation is performed in post processing of the different simulations, using two different time varying input variables.

2 Methodology

50 2.1 DANAERO wind turbine

The DANAERO wind turbine rotor is used for this paper. This is the reference wind turbine in the IEA Task 29 IV, also known as MEXNEXT IV, (IEA Task 29). In this project different, institutions and universities around the world compare their own codes and approaches, using them for the calculations planned into different subtasks of the same project. The results are not only compared to each other, but also to experimental results provided by the DANAERO experiment (Madsen et al. (2010)). The experiment were conducted between 2007-2010 in cooperation between the Technical University of Denmark and the industrial partners Vestas, Siemens LM and DONG Energy, and then post processed and calibrated in the follow up project DANAEROII, (Troldborg et al. (2013)). In this way it is possible not only to understand limitations and problematics of the different approaches, but also to improve them. The turbine has a rotor diameter of around 80 m, a tilt angle of 5 degrees and

around 1.4 m prebend. Hub, nacelle and tower have been modelled within the present study as cylinders, based on the available diameter distribution provided in the structural model.

2.2 CFD model and inflow conditions

The simulations are performed with the CFD code FLOWer (Raddatz (2009)). Firstly developed at the German Aerospace Center (DLR), FLOWer is now since many years expanded at the Institute of Aerodynamic and Gas Dynamic (IAG) for helicopter and wind turbine applications. It is a URANS and DES finite volume solver for structured meshes. The present simulations are run using the Shear-Stress-Transport (SST) k-omega model according to Menter (Menter (1994)), using a fully turbulent boundary layer. Two different spatial discretization schemes are available, a second order central cell-centered Jameson-Schmidt-Turkel (JST) ((Jameson et al.(1981)) and a fifth order weighted essentially non-oscillatory (WENO) (Kowarsch et al. (2013)) scheme. The second one is applied in the present study on the background mesh in order to reduce the dissipation of the vortices. The time-stepping scheme is an artificial 5-stage Runge-Kutta scheme and multi-grid level 3 is applied to accelerate the convergence of the solution. The time integration scheme is an implicit procedure called dual-time stepping where at the beginning of each timestep t an estimation of the solution is guessed. The closer this is to the final value, the smaller the necessary number of inner iterations to reach convergence. Independent grids need to be created for each single component, combined and overlapped by the use of the Chimera technique.

The CFD model of the blade is created from the provided CAD file, where a "water tight" outer surface is extracted. For hub, nacelle and tower, surface databases are recreated (cylinder-based) from provided geometrical properties. Meshes are generated by the use of the commercial software Pointwise in combination with in-house scripts. All components have been meshed ensuring $y^+ \le 1$ in the boundary layer region. The blades are meshed in an O-mesh topology with 257 points over the the profile and 201 points in radial direction, for a total of around 9 Mio cells for each blade. The background mesh consists of hanging grid nodes in which the component meshes are embedded with the Chimera technique. Three different CFD models have been created for the turbine, with increasing fidelity:

- 1. One-third model (BMU) of the rotor (only one blade) suited for uniform inflow conditions;
- 2. Full model of the turbine (FMU) including nacelle and tower suited for uniform inflow conditions;
- 3. Full model of the turbine (FMT) including nacelle and tower suited for turbulent inflow conditions;

The differences between the three models consist in the background that were used. Model 1 has no ground, because it is just a 120° model of the turbine. Model 2 has no friction on the ground in order to avoid the generation of a wind profile. Finally, model 3 has friction on the ground in order to consequently propagate the sheared turbulent inflow and is much more expensive in comparison to case 2 (87 Mio cells against 58 Mio), because an additional refinement is added upwind where the turbulence is injected, and different boundary conditions need to be applied in order to ensure a correct propagation of the turbulence. The 120° model is much cheaper than the other two, because it uses the periodic characteristic of a 3-bladed wind turbine, but of

- course it considers neither tilt angle nor tower influence. The different boundary conditions and CFD models are depicted in fig. 1. In the following the meaning of the different boundary conditions is clarified:
 - NAVIER-STOKES and EULER wall represent the ground with and without friction, respectively;
 - FARFIELD represents the uniform inflow boundary condition;
 - PERIODIC/PERIODIC ROT represent the symmetrical boundary condition for the full and 120° model, respectively;
 - GUST is the Dirichlet boundary condition, by which arbitrary unsteady inflow can be applied;
 - PRESSURE OUTLET defines the outflow based on pressure;

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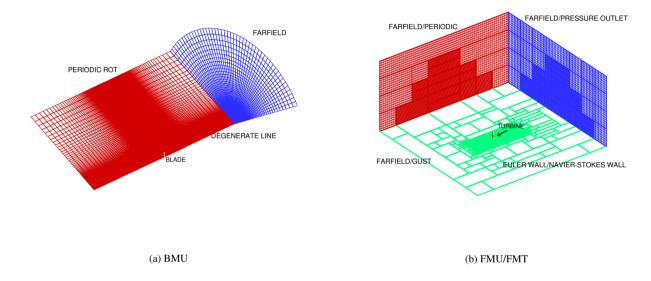


Figure 1. Details of the meshes and boundary conditions for BMU and FMU/FMT

All simulations are run based on the conditions defined in the subtask 3.1 of the IEA task 29, see (IEA Task 29). Those require a rated inflow velocity of 6.1 m/s in the uniform case. R3:S4 For FMT, synthetic turbulence is generated by the use of a Mann Box (Mann (1994)) and injected in the flowfield at a plane 4 diameters (4D) upstream from the tower bottom. This is added using a momentum source term as prescribed in Troldborg et al. (2014) and superimposed to the steady uniform inflow. The turbulence on this plane is updated every time step using Taylor's frozen turbulence hypothesis (Troldborg et al. (2014)). A Turbulence Intensity (TI) of 20%, a length scale of 0.59*hub height (according to the IEC standard normative 61400) and a stretching factor $\Gamma = 3.9$ to approximate the Kaimal spectral model (as prescribed in Kim et al. (2018)) are preset. A mesh refinement of the background is applied from the inflow plane in order to allow a better propagation of the turbulence. The effective TI at the rotor is usually lower than the one prescribed in the Mann box, because it decays for both physical and numerical reasons. From an empty box calculation with a TI of 6.8% a turbulence decay of around 14% was calculated, and

therefore it is assumed for this case that the effective TI amounts to 17.2%. Sheared inflow is superimposed by the use of a power law with $\alpha = 0.025$. Due to the low reference velocity considered during the DANAERO experiment, a really high TI was chosen in order to be able to identify distinctively the effects of a turbulent atmospheric boundary layer. DDES is used instead of URANS for the CFD solution, changing the boundary conditions accordingly.

2.3 MBS solver

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2.3.1 Structural model

The multi-body dynamics (MBD) simulation code SIMPACK is used to simulate the structural dynamics of the turbine (as in Jassmann et al. (2014) and Luhmann et al. (2017)). The structural properties of the entire turbine have been modeled starting from the provided HAWC2 aeroelastic data. A multi-body system consists of rigid or flexible bodies interconnected by force and joint elements that impose the kinematic and dynamic constraints. Each body, represented by one or more markers, may then have three translational and rotational displacements as result of deformations and motion. The body motion is described by a set of Differential-Algebraic Equations (DAEs), a combination of differential motion equations and algebraic constraints. The blades are modeled as nonlinear SIMBEAM body types **R1:S1** (three dimensional beam structures in SIMPACK, described by a node-based nonlinear finite differences approach). These have been discretized into 22 Timoschenko elements in radial direction, taking into consideration also gravitational and centrifugal forces. Structural damping is applied using the Rayleigh damping model with $\alpha = 0.025$ and $\beta = 0.014$. Due to its small expected deflections, the tower has been modeled as a linear SIMBEAM discretized into 25 Euler-Bernoulli elements, the hub has been modeled with 2 linear Euler-Bernoulli elements and the nacelle is modeled with one only rigid node, i.e. it can move but not deform, see fig. 2. Loads provided from the CFD are damped for the first 200 timesteps (equivalent to 200 Azimuth degrees) in order to avoid strong and fast deformations that can lead to numerical instabilities in the calculation. **R2:S1** In order to validate the structural model, the natural frequencies of the singles blade and turbine are compared to the measured ones from Hansen et al. (2006) in table 1.

Single Blade	Single Blade
Measured	Computed
1.01	0.938
1.91	1.884
2.96	2.687

Full Turbine	Full Turbine
Measured	Computed
0.437	0.4812
0.444	0.4862
0.839	0.869
0.895	0.9201
0.955	0.9626
1.838	1.8758
1.853	1.912
2.135	2.5477
2.401	2.7265

Table 1. Comparison natural frequencies between the measured ones and the computed by SIMPACK: single blade on the left and full turbine on the right.



Figure 2. Visualization of the structural MBD model

2.4 BEM model

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R1:G1 R2:G1 A simplified aerodynamic model based on Blade Element Momenutm (BEM) theory has been generated with the NREL code AeroDyn (Aerodyn (2005)). This has the advantage of beeing already incorporated in SIMPACK as additional module, and it can be therefore easily coupled to the structural model. In this case, the blade needs to be modeled aerodynam-

ically with as many nodes as structurally, i.e. 21 for each blade. Polars have been extracted from 3D CFD calculations in order to avoid the use of any tip or hub correction model and ensure as much consinstency as possible to the CFD calculations, as it was already shown in Guma et al. (2018). The 3D polars have been provided in a range of AOA between around -30° to $+30^{\circ}$ and have been extracted from the CFD solution using the RAV method (Rahimi et al. (2018)) and then extrapolated up to -180° to $+180^{\circ}$ using the Viterna method. Axial and tangential induction corrections have been taken into account. Tower shadow effect has been taken into account depending on the computed case (single blade or full turbine). The comparison of the sectional loads per unit length in normal (F_N) and tangential (F_T) direction between BEM and CFD is depicted in fig. 3. In this case only one blade, with no tower shadow and rigid conditions has been taken into consideration, averaging the results of the three last revolutions. The curves show a good agreement, and therefore the BEM model of the turbine is validated. It is out of the scope of this paper to discuss limitations and capabilities of BEM under turbulent inflow conditions. Therefore, only uniform inflow cases have been calculated using BEM as aerodynamic model of the turbine. The chosen setups are shown in table 2.

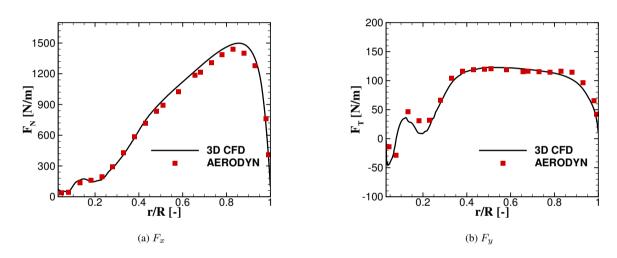


Figure 3. Normal (on the left) and tangential (on the right) sectional load in comparison for a single rigid blade 3D CFD vs AeroDyn

Inflow Velocity (m/s)	RPM	Pitch Angle (°)
6.1	12.3	0.15
9.0	17.83	1.20
13.0	19.08	3.49

Table 2. Computed cases with uniform inflow in BEM. The first case is the one computed also with CFD.

2.5 FSI setup and computed cases

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In order to allow the communication between FLOWer and SIMPACK, moving, undeformed and reference system markers need to be defined as prescribed in (Klein et al. (2018)). In the present study no controller is taken into account, that is why each simulation is conducted with a fixed rotational speed and pitch. R2:S7 These have been set according to the inflow velocity of 6.1 m/s, that is at the same time the chosen uniform inflow velocity and the average velocity at which the Mann box is generated. Even if a high TI is set, the resulting velocity is always far away from cut-off. Therefore, the controller would mainly change the RPM and not the pitch angle. The change in RPM has an influence on the full system natural frequencies (that is expected to be small), on the blade-tower passage frequency, and on the thrust. This would increase with the RPM and therefore the flapwise tip deformations. The used coupling algorithm is explicit, i.e. deformations and loads are exchanged only once per physical timestep. In particular, the loads at the end of the flow calculation timestep are used to calculate deformations that are applied to the subsequent step, see fig. 4. The chosen timestep in this case corresponds to 1 azimuthal degree. An already converged rigid simulation of the turbine that ran already for at least 10 revolutions is used as restart for the coupled simulation in order to speed up the calculation and save computational time. R3:S5 The DANAERO rotor has a high induction, therefore it takes many revolutions for the wake to fully develop and for the loads to stabilize. In order to save computational time, turbulence is injected and flexibility is activated, only after a cheaper simulation (FMU) reached a low residuum, a difference lower than 1\% in the averaged loads and deformations between two revolutions, and a wake development long enough to avoid effects on the loads too.

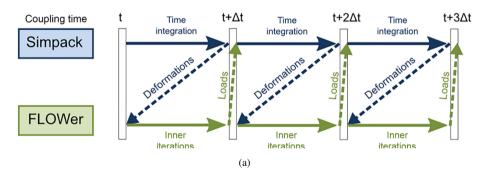


Figure 4. Explicit coupling strategy

For the BMU case it was sufficient to run the coupled simulation for only 6 further revolutions to achieve convergence and periodicity of the results. For the FMU, RMU and FMT at least 10 revolutions have been run, although periodicity cannot be reached in the FMT case, because the simulation time is much shorter than the length of the used Mann box. The elapsed time for the coupled simulations (starting from a rigid converged solution) varies from a minimum of 15 hours with 1632 processors for the BMU to a maximum of 48 hours with 4320 cores for the FMT case. All simulations are run on the SuperMUC-NG supercomputer at the Leibniz-Rechenzentrum in Munich.

All the CFD-MBD computed cases and differences can be seen in table 3. R1:S3 For each mentioned case a rigid and a coupled version is available, although RMU R (rigid) and FMU R (rigid) represent the same case.

Case Name	Inflow Conditions	CFD Structures	Flexible Structures
BMU	uniform	one blade and 1/3 hub	blade
RMU	uniform	rotor, nacelle, tower	rotor
FMU	uniform	rotor, nacelle, tower	rotor, nacelle, tower
FMT	sheared turbulent inflow	rotor, nacelle, tower	rotor, nacelle, tower

Table 3. Computed cases with inflow condition, CFD modeled structures and flexibility

2.6 Damage Equivalent Loading (DEL)

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The DEL is a constant load that leads, when applied for a prescribed number of cycles, to the same damage as that caused by a time varying load over the same period. With this method, two or more signals can be compared in order to get insight into the fatigue loadings that blades are facing during normal operation. The approach is based on the S-N curves (stress vs number of cycles) of the material on a log-log scale, so that the material behavior is defined by the slope of a line. Additionally, a rainflow algorithm is applied to recognize the relative fatigue cycles in a load signal by filtering peeks and valleys. This algorithm allows to estimate the amount of loads change depending on the amplitude of the cycle. In this way closed stress hysteresis cycles can be identified defining not only their amplitude, but also how often they appear. The consequent damage is, in fact, dependent on the combination of the last two factors. The used formulation in this paper is the one from Heindrinks et al. (Hendrinks et al. (1995)) in which the different load signals are compared on a quantitative basis and using not only the range but also the mean of the load cycles. According to this method, the final expression of the DEL resulting from a prescribed signal is:

$$DEL = S_{r,eq} = \left(\sum_{i=1}^{n} \frac{\left(S_{r,i} * \frac{S_u - S_{m,eq}}{S_u - S_{m,i}}\right)^m}{Neq}\right)^{\frac{1}{m}},\tag{1}$$

where n is the total number of cycles detected by the rainflow counting, $S_{r,i}$ is the amplitude of the i-th cycle, S_u is the ultimate load, $S_{m,i}$ is the mean value of the ith cycle, Neq is the number of cycles corresponding to DEL, $S_{m,eq}$ is the equivalent mean value of the cycle with amplitude DEL and, finally, m is the slope of the S-N curve, considering a symmetric Goodman diagram with straight life lines.

 $S_{r,i}$ and $S_{m,i}$ are direct output of the rainflow counting, meaning that they are an individual and inevitable characteristic of the spectrum itself. Differently, Neq, S_u , $S_{m,eq}$ and m need to be chosen in advance. S_u and m are material dependent, where a log-log S-N curve is considered in order to have a straight line, respectively a constant m, while S_u can be calculated in first

approximation as 5 times the maximum load in the provided spectrum. Neq and $S_{m,eq}$ are user dependent. It is then clear that the absolute value computed by the DEL strongly depends on the choice of the constants, but as long as the same constants are considered, the DEL values are consistent within each other and, therefore, comparable.

3 Results

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3.1 Aeroelastic effects

In this first section, the effects of aeroelasticity on the reference wind turbine are analyzed. The considered DANAERO experiment was performed at a low inflow velocity $(6.1 \ m/s)$, that is why it is expected to have small deformations, and therefore especially a low tower effect. The used structural model is always the same, imposing opportunely the flexibility of the components as prescribed in table 3. This means that the calculation of gravitational and centrifugal forces, that is made directly in SIMPACK, is always taking the tilt angle into account, even in the BMU case.

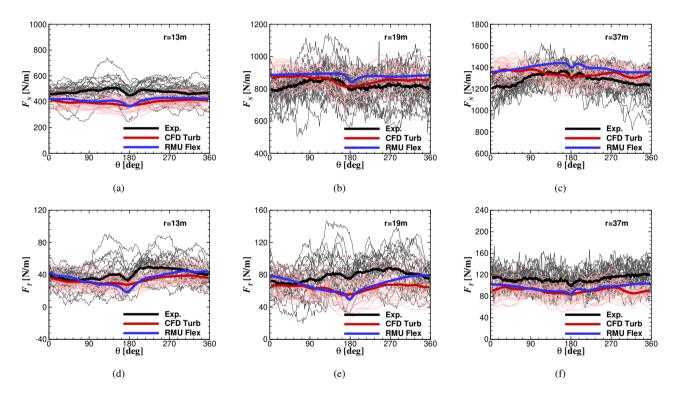


Figure 5. Comparison of experimental normal loads (F_N) in (a), (b), (c) and tangential loads (F_T) in (d), (e), (f) for three different radial sections (r = 13m, r = 19m, r = 37m) over the blade. The blue line represents the full turbine with flexible blades. The red line represents a rigid rotor without tower but a turbulent inflow with the same TI as in the experiments. Grey and pink thin lines represent the data per revolution for the experiments and "CFD Turb", respectively.

As validation of the results, the sectional normal [R2:S9] (F_N) and tangential (F_T) loads according to the chord length for 3 different radial positions in comparison to experiments are shown in fig. 5.

R3:S6 R2:S2 Results of different field tests have been considered and averaged (black line). As described in section 2.2, turbulence has been generated in a stochastic way, and therefore the experimental and simulation time series of each revolution are not directly comparable, but need to be averaged. For the validation, two different test cases have been compared: an entire CFD model of the turbine with flexible blades with uniform inflow conditions (RMU C, blue line) and an only rotor CFD model completely rigid but with an inflow turbulence comparable to the experiments (CFD Turb, red line). It can be seen that in the outside region, although a correct modeling of the inflow provides results closer to the experiment, the shape of the experimental curve is mostly good matched by the RMU C curve. In the hub region, the two modeling approaches do not show much difference from each other, although the flexible case gives slightly better results.

3.1.1 BMU vs **RMU**

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The first considerations are made comparing BMU and RMU; the two differ from each other by the presence of a rigid tower and a tilt angle in the CFD model. Deformations in flap-wise, edge-wise and torsion direction of the tip of the blade can be seen in fig. 6. It can be noticed that, due to the inertia of the blade, the tip deformation starts its downturn by 180° but shows **R1:S4** this local minimum with a delay of around 20° by 2.35% of the rotor radius.

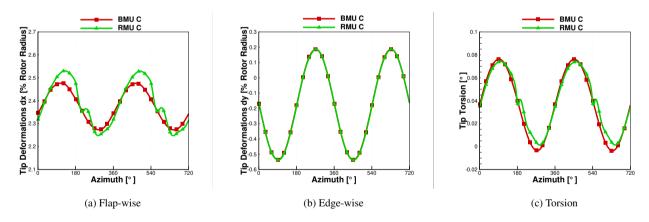


Figure 6. Tip deformations in comparison: BMU coupled (C) vs RMU coupled (C). Out-of-plane deformation in (a), in-plane deformation in (b) and torsion in (c).

A clear sinusoidal trend can be seen in both cases, that leads to an oscillation of the tip deflection from around R3:S9 2.3% to 2.5% of the blade radius for the BMU case, and from around 2.2% to 2.5% for the RMU case. R1:S5 The reason for this is the presence of the tilt angle (5°) that leads the gravitational and centrifugal forces to produce an oscillating deformation component in flap-wise direction. On the contrary, the aerodynamic contribution remains almost constant in time, with an oscillation smaller than 1%. As previously mentioned, the CFD model in BMU has no tilt, but the structural model does, that is why the resulting centrifugal and gravitational forces are accordingly affected. This leads to the oscillation in the response of

BMU. This oscillation turns out to be stronger than the blade-tower passage for RMU, therefore after the minimum due to the blade-tower interaction, there is a recovery that immediately collapses in order to follow the sinusoidal trend. The difference in the maximum deflection between BMU and RMU is 2.4% and is due to a higher oscillation of the affecting loads in the rigid version of RMU, as can be seen in fig. 7, where the global thrust (F_x) and torque (M_x) in the rigid and coupled case on the blade are plotted.

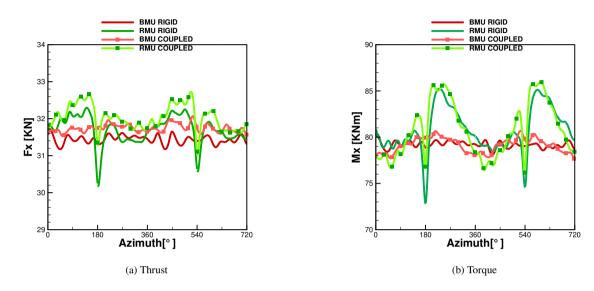


Figure 7. Thrust and torque in comparison BMU vs RMU, both rigid and coupled

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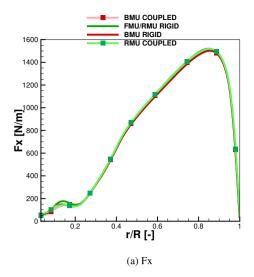
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The tip deformations in edge-wise direction are only dependent on the gravitational forces and show therefore almost no difference between BMU and RMU. The same happens for the torsion, whose minimum value is slightly lower in RMU with a really low maximum value of 0.075° .

Regarding the global thrust and torque in the BMU case for rigid and coupled conditions, it can be seen that M_x in R1:S8 fig. 7 has an oscillatory trend, directly related to the sinusoidal oscillation of the blade. The global thrust is slightly shifted to higher values in case of coupling, where the mean value increases of 1%. This is due to the deformation of a pre-bended blade, resulting in an increase of the effective rotor surface. Even if the torque oscillates more in the flexible case than in the rigid state, the average difference is lower than 0.1% and therefore negligible. The RMU case shows a larger oscillation due to the tower passage, and as in the BMU case, the structural coupling leads to a shift of both thrust and torque curves to higher values. In particular, directly before the tower passage, the flexible blade reaches higher values of thrust (in average 1 to 2% more) with a consequent higher thrust in front of the tower (in average 2 to 3% more). The same effect, although less evident, can be seen for the torque. Averaging over three revolutions, the maximum difference in the produced power is up 2.3% and can be seen between BMU R (rigid) and RMU C (coupled). Lastly, the difference in the sectional loads, averaged over the last revolution, is analyzed in fig. 8. These are the sectional forces normal and tangential to the rotor plane.



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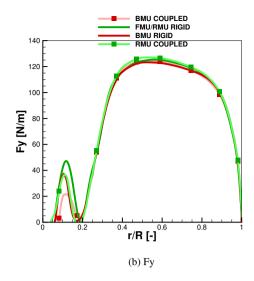


Figure 8. Normal and tangential time averaged sectional loads in comparison BMU vs RMU, both rigid and coupled

The normal forces in coupled and rigid conditions show almost no difference. In the tangential loads, the one responsible for the power at the shaft, a small increase (around 1%) can be observed between 40% and 60% of the blade radius, due to a local slightly higher angle of attack (around 0.8% more), connected with the positive value of torsion showed before, and due to the increase of the effective rotor area.

R1:G2 | R2:G2 | While the CFD calculation have been made based on the operating conditions of the DANAERO experiment, further simulations have been conducted using BEM in order to determinate the generalization level of the results. Tip deformations in flap-wise direction can be seen in fig. 9a, 9b and 9c. where an oscillation from 2.3% to 2.5% of the blade radius can be observed as in CFD. In these BEM calculations the tilt angle needs to be in either both aerodynamic and structural models or in none of them, therefore the only difference between BMU and RMU is the blade-tower passage effect. Differently from CFD, where the impact was almost negligible, large oscillation occur due to the blade-tower passage, that already for the case with an inflow velocity of $6.1 \, m/s$ decreases up to $10 \, \%$ (in comparison to no tower shadow). Increasing the inflow velocity and the RPM, these oscillations become strong enough to preclude the deformations to reobtain the same shape as in BMU. An overestimated blade-tower passage effect can be observed in the produced torque too, see fig. 9d, 9e and 9f. In particular, while with CFD a reduction of this effect was observed when the structures were flexible (by low inflow velocity), this is not appearing using BEM, that shows only an increase of it for high velocities of around $11 \, \%$ (see fig. 9f). At the same time, while flexibility shows almost no effect on the average torque at low velocities, up to 6% difference can be observed at $13 \, m/s$. Especially in this case it can be seen that the RMU C case converges back to the sinusoidal form of BMU C after a time equivalent to 150 degrees in which this oscillation is damped out.

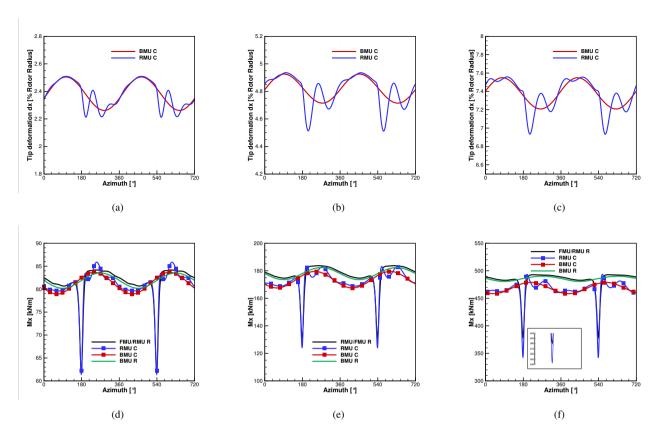


Figure 9. Aero-elastic calculations using BEM as aerodynamic model. Tip deformations in flap-wise direction BMU vs RMU: 6.1 m/s in (a), 9.0 m/s in (b) and 13 m/s in (c). Torque (M_x) generated by one blade BMU vs RMU: 6.1 m/s in (d), 9.0 m/s in (e) and 13 m/s in (f).

3.1.2 RMU vs **FMU**

As mentioned in section 2.5, the difference between RMU and FMU consists on the flexibility of tower and nacelle. The flapwise, edge-wise and torsion deformations in comparison between RMU and FMU can be seen in fig. 10. Due to the low inflow velocity, the tower deflection contributes only 0.1% of the blade radius to the total blade out-of-plane deflection.

Considering the edge-wise deflection, the average value increases from 0.43% of the blade length for RMU to 0.65% for FMU due to the additional contribution of the tower top deformation. For the same aforementioned reasons, the torsion deflection has in average the same value, but $\boxed{\textbf{R1:S10}}$ due to the tower's torsion contribution, it shows a higher amplitude of the oscillation that increases in the FMU case up to 17% more. The global thrust (F_x) and torque (M_x) can be seen for the RMU and FMU rigid and coupled conditions in fig. 11. Here, 1% deviation can be seen by addition of flexibility, although almost no difference is shown between RMU and FMU coupled, due to the small deflections of the tower top.

As for on the difference in FMU between rigid and coupled conditions, it can be seen that the decay due to the tower passage decreases by 6% **R1:S11** (difference in M_x between rigid and coupled at 180°). This has a direct effect on the maximum value

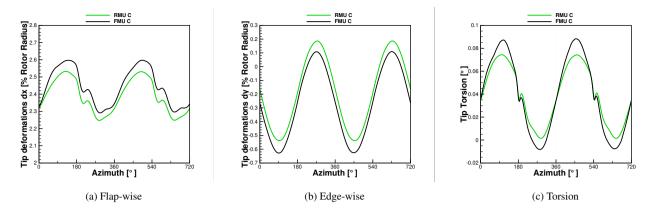


Figure 10. Tip deformations in comparison RMU vs FMU

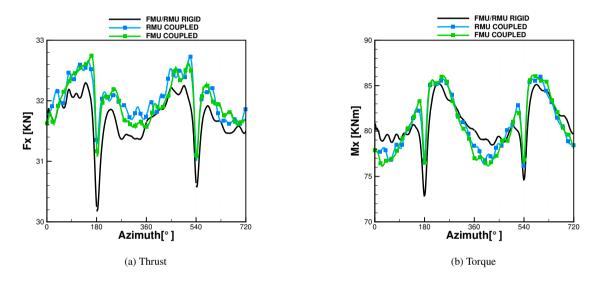
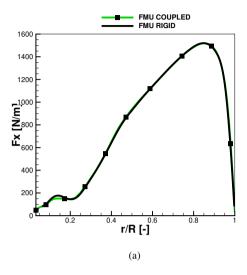


Figure 11. Thrust and torque in comparison RMU vs FMU, both rigid and coupled

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reached directly after the recovery, which is also always higher than in the rigid case. It can also be observed that within one revolution the amplitude of the oscillation is higher in the coupled simulation. By averaging the results over the revolutions, it is found that the coupled case produces 3.5% more power than the rigid case. In order to understand this behavior, the averaged sectional loads of the FMU rigid and coupled cases are compared, see fig. 12. The area of interest is from 20% of the blade radius, because near the hub the difference between the two curves is mostly due to the strong unsteadiness affecting the hub region, where separation is occurring. The loads in normal direction F_x are not affected at all by the coupling. In contrast, the tangential loads F_y , the ones generating the torque M_x and therefore the power, show some difference in the range between 40% and 70% of the blade radius (around 2 % more). This effect was also discussed by Sayed et al. (2016), who explained it with a slight increase of the angle of attack in this region R3:S11 that is confirmed in pressure distributions at 40% and 50% in

fig. 13. A maximum c_p difference of around 2.5% in the pressure side can be noticed. Considering that differently from Sayed et al. (2016), no decrease of the AOA is occurring in the outer region of the blade (for this inflow conditions), no compensation of this effect occurs and together to the increase of the rotor disk area, the increment in produced power is explained.



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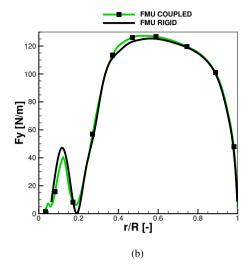
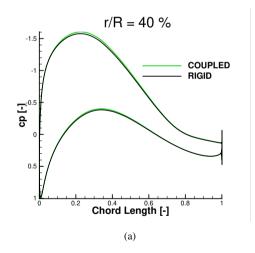


Figure 12. Sectional loads comparison in FMU both rigid and coupled



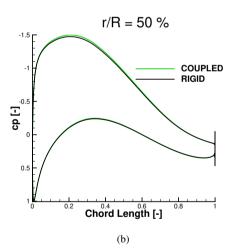


Figure 13. Pressure distributions for FMU rigid and coupled in comparison.

R1:G3 R2:G3 As in section 3.1.1, the simulations including the tower and its flexibility have been repeated using BEM and two more cases at higher inflow velocities have been added. As it can be seen in fig. 14a, 14b and 14c, almost no tower influence can be seen in the total blade deformation, because the predicted tower top deformation by AeroDyn is really low. Therefore, almost no difference can be noticed between FMU C and RMU C in the produced torque, but only the flexibility

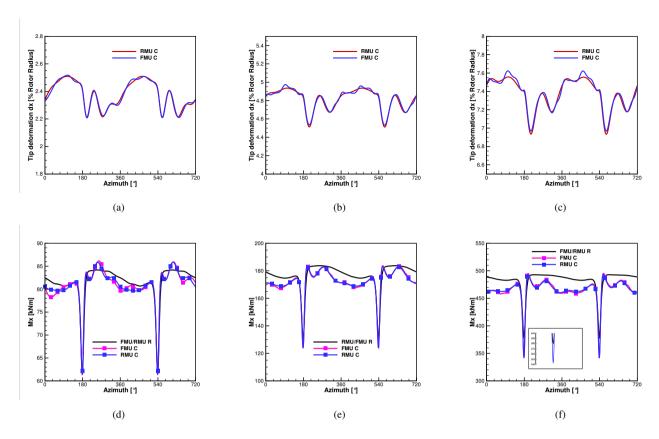


Figure 14. Aero-elastic calculations using BEM as aerodynamic model. Tip deformations in flap-wise direction RMU vs FMU: 6.1 m/s in (a), 9.0 m/s in (b) and 13 m/s in (c). Torque (M_x) generated by one blade BMU vs RMU: 6.1 m/s in (d), 9.0 m/s in (e) and 13 m/s in (f).

effect that increases with the inflow velocity leading up to 6 % less power produced in comparison to rigid. Again, no decrease of the blade-tower passage effect can be noticed by 6.1 m/s, but only its increase at high velocity. Differently from CFD, the predicted torque using BEM in the flexible case is always lower than the rigid case, and the curves show less oscillation than in CFD because of the lack of time-dependent 3D effects that BEM cannot capture.

3.1.3 FMU vs **FMT**

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Figure 15 shows iso-surfaces of the λ_2 -criterion for both inflow cases. The interaction can be seen between the near wake vortices and the Karman vortex street of the tower. The tower faces not only the turbulence of the flow, but also the wake generated by the blades, resulting in a strongly turbulent flow and oscillations in the computed loads.

The comparison of the tip deformations in flapwise and edgewise directions and the torsion can be seen in fig. 16. The FMU case reaches a periodic steady state already after 2 revolutions, oscillating flap-wise with an average of 2.45% of the blade length. The same convergence trend can be seen for the edge-wise deformation and for the torsion, both of them almost negligible. All three are oscillating according to the rotational frequency.

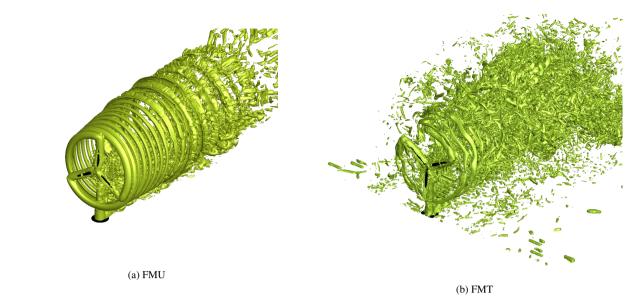


Figure 15. Visualization of the λ_2 criterion

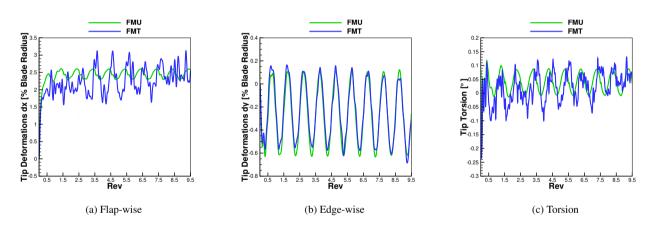


Figure 16. Tip deformations in comparison FMU vs FMT

The flap and torsion deformations are mostly affected by the presence of turbulence. Especially in the flap direction, 5 major peaks in 10 revolutions can be observed where the maximum deformation is around 3.1% of the blade length, that is 47% higher than the maximum in the uniform case. At the same time, the minimum flap-wise displacement, that is not due to the tower passage, is 30% lower than in the uniform case. For the torsion deformations, the turbulence is mostly affecting the minimum, that for FMU is -0.008°, while it is -0.09° for FMT. In the defined coordinate system, a negative torsion moves the trailing edge more downwind. The edge-wise displacement, although in both cases oscillating around a mean value of 0.22%, has higher values for the first 8 minima of FMT.

This can be explained by the tower top deformations in flap-wise direction in fig. 17. In FMT the tower displacement is always smaller than in the FMU, and the tower deflection has an additional tilting effect on the rotor and consequently on the gravitational forces. After the eighth revolution, the tower top shows larger peaks in FMT than in FMU, leading to the opposite effect of a smaller peak in the edge-wise deformation.

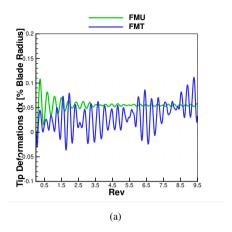


Figure 17. Tower top deformation in flap-wise direction

The spectra of the deformations is depicted in fig. 18, where the rotor frequency together with the higher harmonics are marked by a symbol. High amplitudes of the harmonics of the rotor frequency can be seen in flap-wise direction, where the first one is particularly strong. Additionally, it can be recognized that due to the inflow turbulence in FMT, the higher harmonics of the rotor frequency are obscured in the broadband of the spectrum. In edge-wise direction, that is mostly influenced by gravitation and not from aerodynamics, no strong increase can be seen for the rotor frequency, and the same happens for the torsion. On the other hand, the broadband has higher amplitudes in FMT than in FMU.

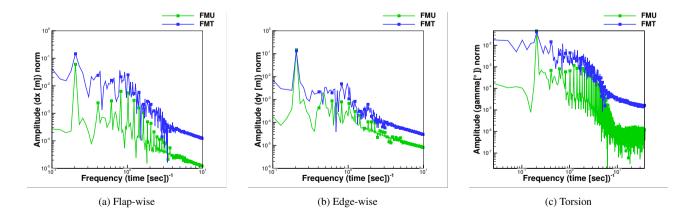
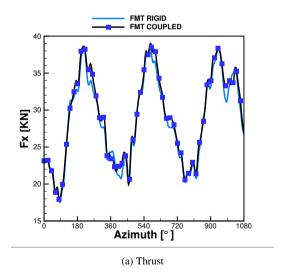


Figure 18. Spectra of the deformations in comparison FMU vs FMT

The effect of the tower can be again recognized in both FMU and FMT with a delay of around 20°, where a sudden drop in the tip deformations can be seen in fig. 16. Nevertheless this drop is almost negligible in comparison to the total affecting oscillation.

The loads resulting from the above described deformations of the FMT case are shown in fig 19 (the FMU has been already discussed in section 3.1.2). Independently of the rigidity of the structure, the turbulence leads to a much higher amplitude in the oscillation of the loads in comparison to FMU as seen in R1:S12 fig. 11. In fact, the torque M_x fluctuates between 140 kNm and 10 kNm, while in FMU it ranges between 86 kNm and 72 kNm. Due to this high oscillation, the blade-tower passage can be hardly recognized. Unlike in the FMU case, the addition of flexibility has not marked consequences neither in thrust nor in torque. Some peaks are increased in the flexible case, e.g. in both thrust and torque at 250° , 315° , 700° and 1000° . Averaging the result in time, the torque is increased by 2.5% (against 3.5% in the uniform case) due to flexibility. As for the blade-tower passage, the fluctuation inducted by the turbulence is the predominant source of oscillation; the flexibility represents only a secondary cause. This is valid only for the present case, where the inflow velocity and therefore the consequent deformations are small. In fig. 20, the sectional loads averaged over the same revolution for both rigid and coupled conditions are plotted. It can be seen that although the shape of F_y has changed between 30% and 70% of the blade length due to the strong oscillation brought by the turbulence, almost no difference is observed by the inclusion of flexibility R1:S13 in comparison to the uniform case as in fig. 12.



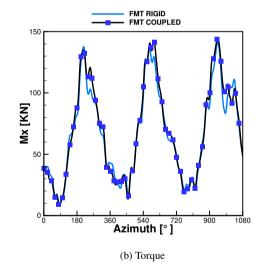


Figure 19. Global loads in FMT: comparison between rigid and coupled

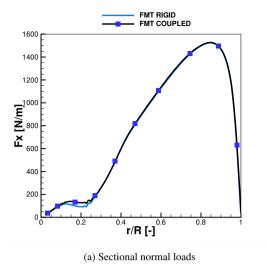
3.2 DEL analysis

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For the fatigue loading study of the different considered cases, the necessary constants described in section 2.6 have been set to $Neq = 10^5$, $S_{m,eq} = 0$ and m = 11, where the last one is material dependent. The first two, as described in Hendrinks et



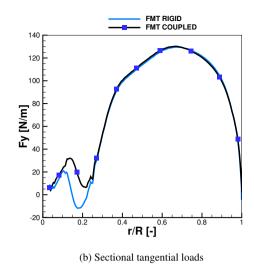
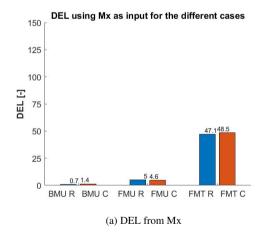


Figure 20. Sectional loads in FMT: comparison between rigid and coupled

al. (1995), do not influence the results, because when making fatigue comparison, it is not the absolute value, but the ratio between the output from two signals, that is of interest. R2:S4 In order to consistently compare the cycle counts, the last three revolutions of each simulation case have been considered. The chosen input signals for the following analysis are the flap-wise and edge-wise blade root moment, M_y and M_x respectively. The first signal represents an unwanted action of the wind on the blade, while the second one is responsible for the power production.



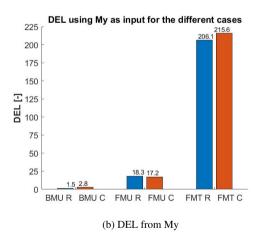
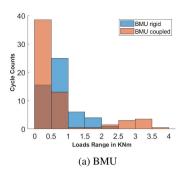


Figure 21. DEL calculation for the different cases using in (a) M_x and in (b) M_y ; R and C stays for "rigid" and "coupled"

The results are shown in fig. 21 and switching in BMU from rigid (R) to coupled (C), doubles the DEL, independently of the used input variable. It is observed in fig. 22a that the flexibility increases mainly the number of small cycles of the signal (fluctuations) and adds a few cycles with higher amplitude. In the case of FMU, already in rigid, DEL is increased by 7 times

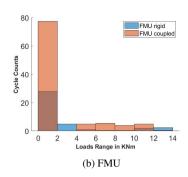


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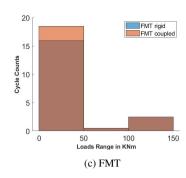


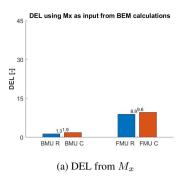
Figure 22. Comparison of number of cycle counts to load ranges using M_x as input

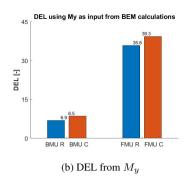
in comparison to BMU, due to the tower passage and this effect is more pronounced using M_y as input. It is interesting to observe that in this case, the coupling has almost no effect on the total damaging. This is because, as shown in section 3.1, the flexibility has two opposing influences on the loads: on the one side the increase of the oscillations and their mean value, and on the other side the decrease of the blade-tower passage effect. These two effects almost counter act each other leading in total to a comparable value of fatigue.

Switching the FMT case from rigid to flexible increases the DEL, because, as seen in fig. 22c, the flexibility adds a few more small cycles but no big cycles, that are completely dominated by the impact of turbulence. Independently from the chosen input, the addition of turbulence drastically increases the fatigue. Much fewer cycles are detected by the rainflow counting, but they all have an amplitude larger than the largest cycles in FMU and BMU.

R1:G4 R2:G4 Finally, the ability of BEM of predicting the fatigue loading for the BMU and FMU cases is discussed. As it can be seen in fig. 23a, BEM predicts slightly higher fatigue for BMU using M_x as input signal than in CFD and that is because, as prescribed in section 3.1.1, the BEM model presents a tilt angle also in the BMU case (differently from CFD), leading to a sinusoidal oscillation of the forces. That means that altough the CFD calculations present many more smaller cycles due to unsteady 3D effects, the DEL is mostly affected by the big ones. The same impact, but more pronounced can be seen in BMU using M_y as input signal. This shows that modelling the turbine as a single blade in CFD when a tilt is given, can lead to a high underevaluation of the fatigue.

Differently in the FMU case (no tilt modelling problem occurs), where for both rigid and coupled and for both chosen input signals, BEM predicts higher fatigue than CFD. The difference between the rigid and coupled case remains the same as predicted by CFD (so almost none), but the single values are almost two times the one from CFD. The reason for this can be explained looking at the cycle count in fig. 23c. Although BEM predicts a smaller number of short cycles than CFD, cycles with around 25 kNm appear, influencing mostly the fatigue calculation. Those cycles represent the blade-tower passage, which effect shows to be overestimated by AeroDyn in comparison to CFD and therefore leads to higher DEL values.





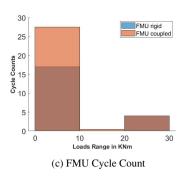


Figure 23. DEL calculation using BEM: results for M_x in (a) and for M_y in (b). Cycle count in comparison to load ranges for FMU using as input M_x in (c).

370 4 Conclusions

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In the present work, different CFD models of the DANERO turbine rotor were generated and coupled to a MBD structural model of the same turbine, by means of a loose (explicit) coupling. The aeroelastic response of the reference turbine was calculated by the use of models increasing their complexity and fidelity. The effects of a turbulent inflow conditions were analyzed in comparison to uniform inflow, showing that turbulence has a R1:S14 larger influence on the DEL than flexibility and blade-tower passage together. The consequent fatigue loading in the difference cases was compared and discussed, showing that for small inflow velocities, a high turbulence has the major impact on fatigue, where the flexibility has a negligible contribution. Comparison to BEM predictions have been shown, demonstrating that the blade-tower passage is overestimated by BEM leading to higher fatigue values.

Author contributions. G. Guma generated a part of the CFD model, the MBD model, ran the coupled simulations, and performed the post
processing and analysis. G. Bangga generated a part of the CFD model. T. Lutz and E. Krämer supported the research, defined and supervised the work and revised the manuscript.

Competing interests. The authors declare that they have no conflict of interest.

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