Cyclic overlay model of p-y curves for laterally loaded monopiles in cohesionless soil

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Abstract

The bearing behaviour of large-diameter monopile foundations for offshore wind turbines under lateral cyclic loads in cohesionless soil is an issue of ongoing research. In practice, mostly the p-y approach is applied in the design of monopiles. Recently, modifications of the original p-y approach for monotonic loading stated in the API regulations (API 2014) have been

10   proposed to account for the special bearing behaviour of large-diameter piles with small length-to-diameter ratios (e.g. Thieken et al. 2015, Byrne et al. 2015). However, cyclic loading for horizontally loaded piles predominates the serviceability of the offshore wind converters, and the actual number of load cycles cannot be considered by the cyclic p-y approach of the API regulations. This research is therefore focusing on the effects of cyclic loading on the p-y curves along the pile shaft and aiming to develop a cyclic overlay model to determine the cyclic p-y curves valid for a lateral load with a given number of load cycles.

15   The "Stiffness Degradation Method (SDM)" (Achmus et al. 2009) is applied in a three-dimensional finite element model to determine the effect of the cyclic loading by degrading the secant soil stiffness according to the magnitude of cyclic loading and number of load cycles based on the results of cyclic triaxial tests. Thereby, the numerical simulation results are used to develop a "cyclic overlay model", i.e. an analytical approach to adapt the monotonic (or static) p-y curve to the number of load cycles. The new model is applied to a reference system and compared to the API approach for cyclic loads.

20   ## 1 Introduction

The conversion of energy supply to the extensive utilization of renewable energies can only be realized by further expansion of offshore wind energy. In this regard, it is crucial to minimize the costs for offshore wind energy exploitation. Significant cost savings are possible by optimizing the foundation elements of offshore wind energy converters.

In the last years, the monopile foundation, consisting of a circular steel pipe of very large diameter (Fig. 1), was proven to be

25   an economic and robust foundation solution for water depths of up to around 40 m. At the time being, projects are realized with monopiles of up to 10 m outer diameter. However, there are still basic uncertainties in the design of such monopiles. In practice, usually the p-y method is applied in the calculation of the monopile behaviour. This is a special subgrade reaction method, which utilizes nonlinear and depth-dependent spring characteristics, the p-y curves. Here p is the resultant soil resistance (horizontal bedding stress times pile diameter) at a certain depth and y is the corresponding horizontal pile

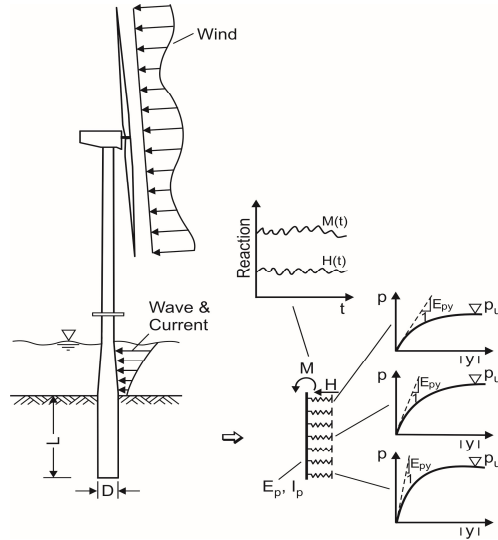
30   displacement. In offshore guidelines like e.g. API (2014) approaches to derive p-y curves dependent on the parameters of the present soil are given. For piles in sand, the only parameters required are the buoyant unit weight γ' and the angle of internal friction φ'. However, several investigations in recent years showed that these approaches, which have been calibrated by field test results of slender, flexible piles, cannot be used without modification for the large-diameter and almost rigid monopiles. This applies both to the p-y approaches for static (monotonic) and cyclic loads.

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Fig. 1: Monopile foundation of an offshore wind energy converter and p-y method used in design (schematic)

2 State of the art

In the classic approach for piles in sand according to API (2014), a tangent hyperbolic function is used to describe the dependence of bedding resistance p on horizontal displacement y at a certain depth below sea bottom z:

40
$$p = A \cdot p_u \cdot \tanh\left(\frac{k \cdot z}{A \cdot p_u} \cdot y\right) \tag{1}$$

Here p_u is the theoretical maximum value of bedding resistance, which basically is the passive earth pressure times pile diameter D. This value is calculated from Eq. 2 as a minimum of two values for shallow and deep failure modes p_{us} and p_{ud}, which depend on buoyant unit weight γ' and three coefficients C_1, C_2 and C_3 correlated with the angle of internal friction φ' (Fig. 2 left).

45
$$p_u = min \begin{cases} p_{us} = (C_1 \cdot z + C_2 \cdot D) \cdot \gamma' \cdot z \\ p_{ud} = C_3 \cdot \gamma' \cdot z \end{cases} \tag{2}$$

The k-value in Eq. 1 is a stiffness parameter and is in API (2014) also given dependent on the angle of internal friction (Fig. 2 right).

For the factor A in Eq. 1, the API approach distinguishes static and cyclic loading conditions. For static loading, $A_{stat} = 3.0 - 0.8 \cdot (z/D) \geq 0.9$ applies, whereas for cycling loading the constant factor (independent of depth) $A_{cyc} = 0.9$ shall be used.

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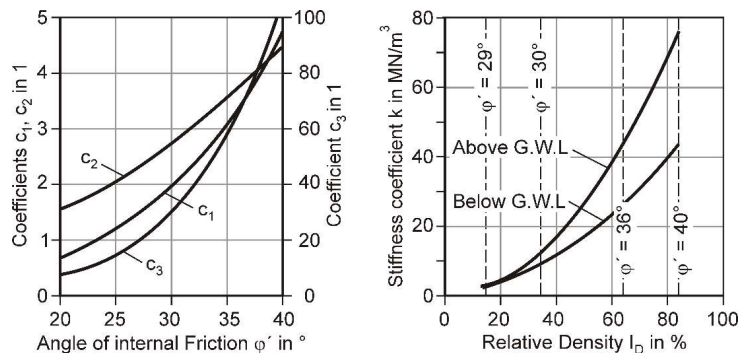


Fig. 2: Coefficients C_1, C_2, C_3 (left) und parameter k (right) according to API (2014)

Several investigations have shown that for large-diameter piles the pile-soil stiffness obtained with the static p-y method is overestimated under extreme loads and underestimated under smaller operational loads (cf. e.g. Thieken et al. 2015a).

55 Therefore, new static p-y approaches for monopiles in sand have been proposed in recent years. Sørensen (2012) replaced the k-value of the API guidelines by a k-value depending on depth z, the soil's oedometric stiffness E_s and the pile diameter D, which for large-diameter piles leads to greater displacements under service loads than the API approach. Kallehave et al. (2012) also suggested a modified initial stiffness formulation, but their target was to avoid an underestimation of stiffness under small operational loads, which is usually applied for the determination of the natural frequency of the whole structure. Here, the

60 parameter k is formulated dependent on depth z and pile diameter D. This modified p-y formulation results in a considerably "stiffer" behaviour than the API formulation. Thieken et al. (2015b) proposed a more sophisticated p-y curve approach, in which also the soil's greater stiffness for small strains is considered and which accounts for the effect of the pile deformation on the p-y curves by an iterative procedure. He showed that this approach gives reasonable results both for small operational and large service loads. Recently, Byrne et al. (2017) also proposed a new p-y approach especially developed for monopiles

65 in sand soil (see also Byrne et al. 2015, Burd et al. 2020). Herein, besides p–y springs also rotational springs and a pile tip spring are introduced to the beam-spring model. However, the spring characteristics are to be determined by calibration with a numerical model, which makes the approach not straightaway applicable to a certain system.

Cyclic loading of a pile can lead to both an increase of pile deformation with the number of load cycles and a reduction of the

70 pile capacity, whereby in sand soils the effect on deformation usually dominates the design. Cyclic loading effects are considered in design by applying cyclic p-y curves in the calculation. As shown above, in the approach of API (2014) cyclic loading is considered by a reduction of the parameter A and hence the bedding resistance p down to a depth of $z = 2.625\ D$. However, since the parameter A also affects the argument of the tanh-function, also displacements are affected, which means that the API consideration for cyclic loads is a mixture of p- and y-multiplier methods. The approach bases on field tests, in

75 which for the determination of cyclic loading effects only limited load cycle numbers (at maximum around 200) were realized (Cox et al. 1974). It is generally assumed that the approach represents the pile behavior due to around 100 load cycles.

Apart from the fact that the cyclic API approach is not validated for large-diameter monopiles, the consideration of just one cyclic p-y curve valid for 100 load cycles is not sufficient for the design of piles for offshore wind foundations. These foundations are subject to intense cyclic loading induced by wind and wave loading. The design checks for cyclically

80 accumulated deformations and in particular rotations of the foundation structure is quite important for wind energy structures. In most wind farm projects, a maximum permanent rotation of the tower of 0.5° is required. Thus, an accurate prediction of the accumulated pile rotation of the monopile to be expected over the whole lifetime of the structure is necessary. This means that the deformations must be calculated under consideration of the actual number of load cycles.

Dührkop (2009) conducted model tests with almost rigid monopiles in sand under cyclic loading. Based on the results, he

85 proposed a modification of Eq. 1 for the case of cyclic loading as follows:

$$p = \tilde{A}_{cyc} \cdot p_u \cdot \tanh\left(\frac{k \cdot z}{0.9 \cdot p_u} \cdot y\right) \tag{3}$$

with $\tilde{A}_{cyc} = r_A \cdot (3 - 1.143\ z/D) + 0.343\ z/D$.

The factor r_A is dependent on the number of load cycles. With $r_A = 1$, the API approach for monotonic loading and with $r_A = 0.3$ for cyclic loading is obtained. Thus, $r_A = 0.3$ can be used for a load cycle number of $N = 100$. For greater load cycle numbers,

90 r_A decreases. For $N > 10^5$, r_A shall be set to zero (Dührkop 2009). With this approach, the monopile deflection can be calculated dependent on the actual number of load cycles. However, the given A_{cyc}-function is valid only for the model test boundary conditions realized by Dührkop. For a certain system with different boundary conditions model tests or numerical investigations are necessary.

Besides from local approaches modifying the p-y curves, also global approaches predicting the increase of pile head deflection

95 or rotation can be applied. In general, the increase of head deflection due to one-way loading with full unloading can be

described by the following equation:

$$y_N = y_1 \cdot f_N(N) \tag{4}$$

Here y_N and y_1 are the horizontal pile head deflections after N load cycles and after 1 load cycle (monotonic loading), respectively. $f_N(N)$ is a function which describes the increase of deflections with the number of load cycles. As long as the

100   cyclic load amplitude is well below the ultimate pile capacity, sedation behaviour can be expected, which means that the deflection rate decreases with increasing number of load cycles. The most common functions of displacement of structures under cyclic loading that are found in literature are of the exponential type such as Eq. (5) (e.g. Little and Briaud 1988) and of logarithmic type such as Eq. (6) (e.g. Hettler 1981):

$$f_N = N^m \tag{5}$$

105   $$f_N = 1 + t \cdot \ln N \tag{6}$$

Here m and t are empirical accumulation parameters. Assuming that these parameters are constants, Eq. (5) and (6) imply that the function of load cycle number is independent of the load amplitude.

A few investigations regarding the above accumulation parameters exist. In addition to the above mentioned works, Lin and Liao (1999) and Long & Vanneste (1994) should be mentioned. However, it is not clear how pile geometry (in particular, pile

110   rigidity) and soil conditions affect the accumulation parameters. Based on model tests, LeBlanc et al. (2010) showed that the rate of deformation accumulation also depends on the load level, i.e. the ratio of maximum cyclic load to the ultimate pile capacity. In contrast, model test results of Peralta & Achmus (2010) did not show a significant effect of the load level.

For practical design, a simple-to-use approach for the derivation of cyclic p-y curves would be highly desirable, which just modifies a chosen static p-y curve by p- or y-multipliers depending on the number of load cycles and other relevant parameters.

115   Such an overlay model describes just the change of static p-y curves with increasing load cycle numbers and could be applied to arbitrary static p-y curve approaches.

A calculation approach termed "Stiffness Degradation Method" (SDM) combining numerical simulations and cyclic triaxial tests has been developed at the authors institute (Achmus et al. 2009). This method allows the calculation of pile deflection lines dependent on the actual number of cycles of a given load and with that also the derivation of p-y curves for a given

120   number of load cycles. This method is applied in the paper at hand for the development of a cyclic p-y overlay model. Therefore, the SDM is briefly described in the following section.

3 "Stiffness Degradation Method" (SDM)

The SDM is described in detail in Kuo (2008) and in other publications, e.g. Achmus et al. (2009) and Kuo et al. (2012), and thus here the method shall be outlined just briefly. A 3-dimensional finite element model is used to calculate the pile

125   deformation behaviour. The soil behaviour under static load is modelled by an elastoplastic material law with Mohr-Coulomb failure criterion and stress-dependent stiffness. The stiffness modulus, i.e. the oedometric stiffness determined under constrained lateral strain, is defined as follows:

$$E_s = \kappa \, \sigma_{at} \left(\frac{\sigma_m}{\sigma_{at}}\right)^{\lambda} \tag{7}$$

Herein $\sigma_{at} = 100$ kN/m² is a reference (atmospheric) stress, σ_m is the current mean principal stress in the considered soil element

130   and κ and λ are soil stiffness parameters.

For describing the increase of the plastic strain of soil with the number of load cycles in element tests (cyclic triaxial tests) an approach by Huurman (1996) is used. The decrease of the (secant) stiffness modulus of the soil with the number of cycles can be approximated by the following equation:

$$\frac{E_{s,N}}{E_{s,1}} = N^{-b_1 X^{b_2}} \tag{8}$$

135   Herein N is the number of cycles, b_1 and b_2 are regression parameters and $X = \sigma_{1,cyc}/\sigma_{1,f}$ is the cyclic stress ratio, whereby $\sigma_{1,cyc}$ is the maximum of the principal stress in a cycle and $\sigma_{1,f}$ is the main principal stress at failure (in a static test). For each element

of the finite element model, from the consideration of the initial stress state and the stress state after applying the horizontal load a cyclic stress ratio quantifying the intensity of cyclic loading is derived. With the reduced stiffness values obtained from Eq. (8), the system's behaviour under the lateral load is calculated again. The result represents the increased pile deformation after the considered number of cycles. An illustration of the procedure is given in Figure 3.

For cyclic one-way loading and drained conditions the SDM allows the evaluation of the pile deformation behaviour under consideration of the site specific soil conditions as well as the loading conditions and the number of cycles. The application requires the definition of six material parameters accounting the soil behaviour under static loading, for which comprehensive experiences exist, and two parameters b_1 and b_2 describing the stiffness degradation under cyclic loading.

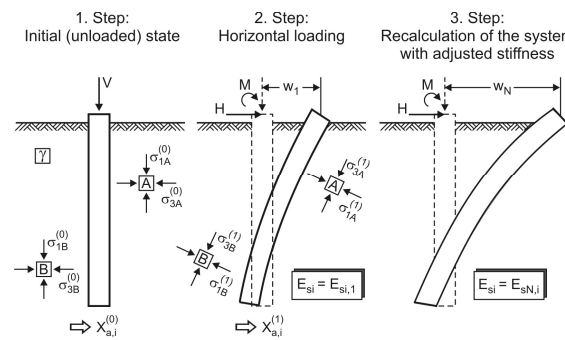



Fig. 3: Calculation steps of the Stiffness Degradation Method

The method has been validated by back-calculation of various series of model tests in medium dense as well as in dense sand (see Albiker 2016, Albiker & Achmus 2018). From these back-calculations, it could be concluded that for comparable relative densities of the soil also consistent sets of values for b_1 and b_2 have to be chosen. Value sets for medium dense and dense sand were determined by comparison of calculations and experimental measurements, and the ranges of values were also verified by regression values derived from cyclic triaxial tests (Albiker 2016).

4 Numerical simulations

4.1 General

The constitutive law for sand used in the SDM is a simple elastoplastic material law with Mohr-Coulomb failure criterion and stress-dependent formulated stiffness. Consequently, this constitutive law is also used in the simulations presented here. It was proven that this model yields reasonable results regarding the behaviour of monopiles under horizontal and moment loading (e.g. Achmus et al. 2009). Actually, a high accuracy of the simulation model for static loading is not crucial, since only the differences between static and cyclic pile behaviour are of relevance here. Basically, the overlay model to be developed shall be applicable to any static p-y approach.

The numerical calculation is done for half of the system (Fig. 4) and is divided in several phases:

- In the first calculation phase, the initial stress state in the soil is generated, considering the coefficient of earth pressure at rest $K_0 = 1 - \sin \varphi'$ in the determination of horizontal stresses. Based on this initial stress state, the oedometric stiffness modulus of each soil element is calculated from Eq. (7). Afterwards, the soil elements located at the location of the monopile are replaced by steel elements.
- In the second phase, the horizontal loading on the system is applied incrementally. After each load step, the horizontal stresses acting on the pile are integrated over certain depth sections of the pile in order to determine the p-values belonging to the current load for the considered depths. Plotting the p-values for different loading steps over the corresponding pile deformations y at the same depth give the p-y curves for static loading.

170 • For the derivation of cyclic p-y curves, the stress conditions in the soil are evaluated after each load step in order to determine the degraded soil stiffness dependent on the considered load cycle number N according to Eq. (8). The numerical simulation is then repeated under consideration of the reduced stiffness until the static load level is again reached. This procedure yields for each point of the static p-y curve a corresponding point of the cyclic p-y curve belonging to the load cycle number N. The calculations presented here were carried out for load cycle numbers of N

175 = 1 (static), 10, 100, 1000 and 10000.

The parameters of the sand used in the numerical simulations are given in Table 1 for three different relative densities. These are typical parameters for sands. The regression parameters b_1 and b_2 of the SDM model were chosen according to the evaluation of cyclic triaxial tests given in Albiker (2016).

180 **Table 1: Material parameters used for sand with three different relative densities**

Relative Density D_r	very dense	dense	medium dense
Buoyant unit weight γ' (kN/m^3)	10.31	10.00	9.76
Friction angle φ' (°)	40.0	37.5	35.0
Cohesion c' (kN/m^2)	1.0	1.0	1.0
Poisson's ratio ν	0.2	0.225	0.25
Oedometric stiffness parameter κ	900	600	400
Oedometric stiffness parameter λ	0.50	0.55	0.60
Regression parameters b_1 and b_2	0.12;0.32	0.134;0.65	0.15;0.5

Generally, p-y curves are dependent on the load conditions (e.g. lever arm, which is the ratio of bending moment and horizontal load) and on the deformation mode (deflection line) of the pile. Therefore, a procedure also applied by Thieken et al. (2015b) was followed, in which at first p-y curves (and here the corresponding overlay model) for purely translatoric displacement of

185 a rigid pile are derived. Afterwards, variable load conditions and hence variable deformation modes are considered in order to derive correction functions accounting for the actual pile deflection line.

4.2 p-y curves for constant deflection – basic overlay model

The basic p-y curves and the basic overlay model apply to a constant horizontal deflection of the pile, which was achieved by assigning identical prescribed displacements to all the pile nodes. By that, the effect of a pile rotation and pile bending is

190 switched off.

The pile diameter was varied between $D = 3$ m und $D = 8$ m in 1 m-steps. The pile length was set to $L = 25$ m in all calculations. Due to the enforced rigid body motion, wall thickness and pile bending stiffness plays no role.

The simulations were conducted with the finite element code Abaqus (Abaqus 2016) using 8-noded volume elements. The sufficient size of the model domain and sufficient fineness of the finite element mesh was proven by preceding sensitivity

195 analyses.

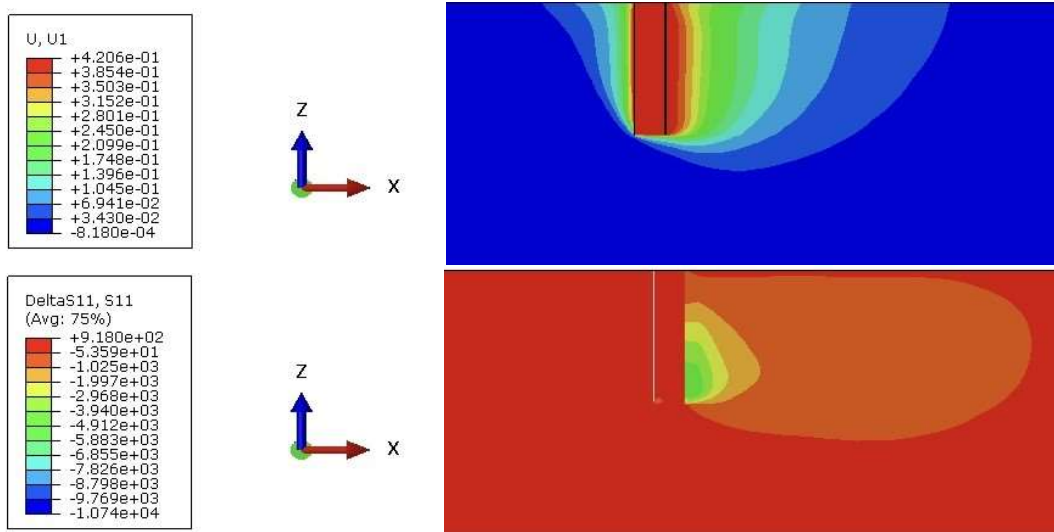
Fig. 4 shows exemplary the distribution of horizontal displacements and horizontal stresses for a monopile with 5 m diameter in very dense sand under static loading ($N = 1$). The evaluation of these calculation results yields for each considered depth along the monopile axis one point of the p-y curve.

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Fig. 4: Horizontal displacements (top) and stresses (bottom) for a monopile $D = 5$ m under static load in very dense sand ($N = 1$, prescribed pile displacement $y = 0.42$ m)

Fig. 5 shows the derived p-y curves at 4 different depths for the pile with $D = 5$ m in very dense sand). The maximum realized displacement was 0.42 m, which is more than 8% of the pile diameter. As to be expected, the bedding resistances and thus the

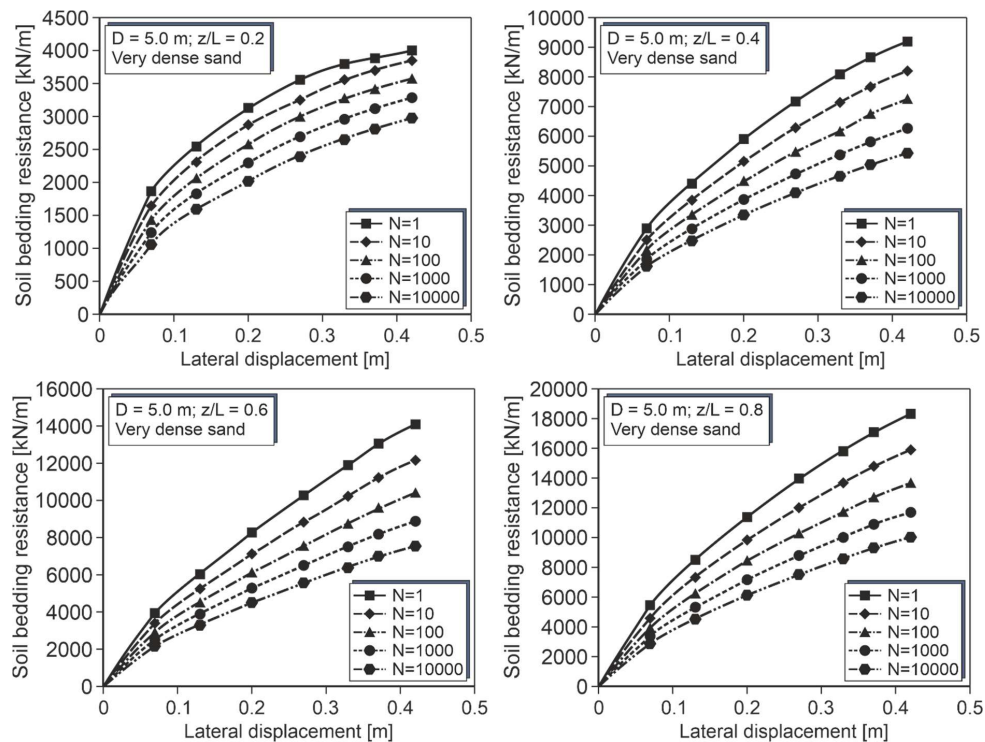
205 spring stiffness increase with increasing depth. Also as expected, cyclic loading leads to greater displacements and thus reduced spring stiffness. It is noteworthy that the relative difference of the cyclic curves to the static curve seems to be quite similar in all depths.

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Fig. 5: p-y curves for different cycle numbers (monopile $D = 5$ m, $L = 25$ m, very dense sand)

Since the applied SDM method accounts for cyclic effects by a stiffness reduction of the soil, it is deemed logical trying to transfer the static to the cyclic curves by a y-multiplier. Fig. 6 shows the determined y_N/y_1-values for the results shown in Figs. 4 and 5. Also regression curves are presented. Evidently, the same function $y_N/y_1=N^{0.091}$ independent of absolute displacement
215 and depth can well approximate the calculation results.

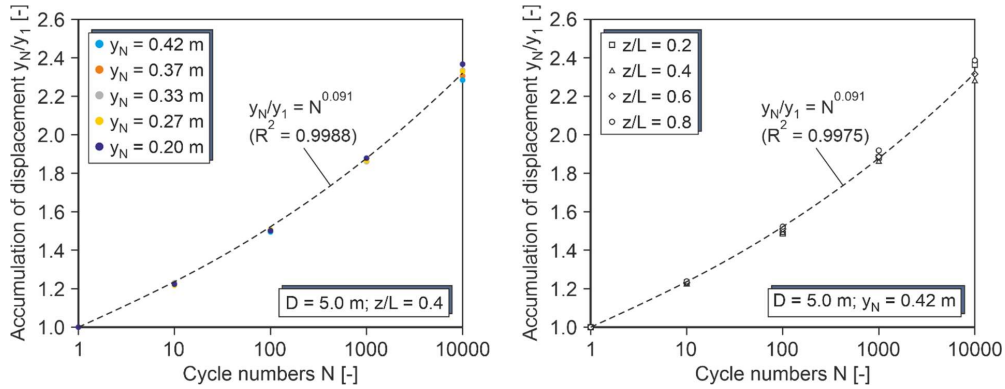



Fig. 6: y-multipliers for a monopile $D = 5$ m, $L = 25$ m in very dense sand

Fig. 7 depicts the effects of varying pile diameters and soil relative densities. Fig. 7 left shows for varied pile diameter and
220 relative depth the y-multiplier determined at a representative point of the respective p-y curve (y_N =0.42m). Obviously, the same function already presented in Fig. 6 gives a good approximation also for piles of other diameters than 5 m. Eventually, Fig. 7 right shows the calculated bandwidths of y-multipliers for varying relative densities of the sand, which were derived in the same manner as described above. A considerable dependence of the y-multipliers on relative density can be seen, which was expected because different regression parameters b_1 and b_2 in the SDM apply for different relative densities. A lower
225 relative density leads to stronger relative accumulation of pile displacements and hence to a stronger cyclic degradation of the p-y curves.

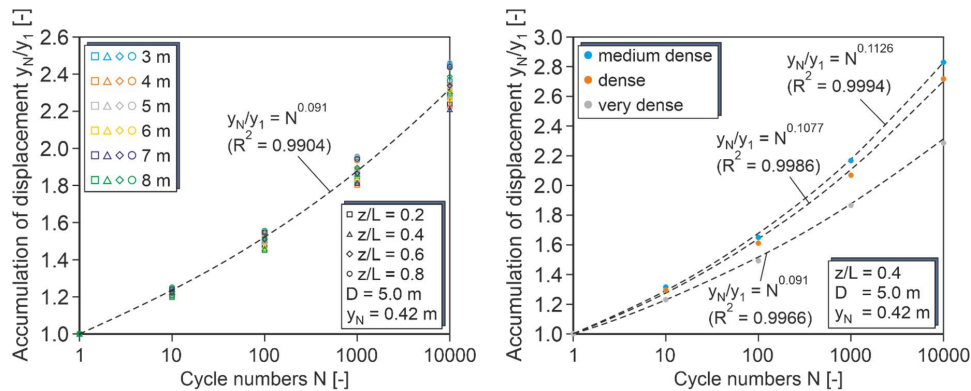



Fig. 7: y-multipliers for variable pile diameters (left) and for different relative densities of the sand (right)

230 The approach for the derivation of cyclic p-y curves from a given static p-y curve valid for constant lateral displacement of a pile (basic overlay model) can be summarized as follows:

$$y_N/y_1 = N^A, A = \begin{cases} 0.091 \ (very \ dense) \\ 0.1077 \ (dense) \\ 0.1126 \ (medium \ dense) \end{cases} \tag{9}$$

with: N: Cycle numbers $\in (1{\sim}10000)$.

Accounting for the internal friction angles φ' of the sands considered in the numerical simulations (cf. Table 1), the exponent

235   A can be expressed by

$$A = 0.1127 \cdot \sin(0.133\varphi' + 15.73) \tag{10}$$

with φ': Internal friction angle of sand in [°] $\in (35.0°\sim40.0°)$.

4.3 p-y curves for arbitrary loading conditions – advanced overlay model

In the next step, the effects of load eccentricity, pile bending stiffness and normalized pile length L/D shall be considered.

240   Hence, a parametric study was conducted, in which monopiles were loaded by a horizontal force and a bending moment applied
at the point of embedment (Fig. 8, the bending moment is the product of horizontal force and considered load eccentricity).
In the following, results for a reference system with a diameter of $D = 5$ m in very dense sand are presented. A wall thickness
of t = 7 cm was assumed, which is a typical value for monopiles of such diameter. Load eccentricities e/L = 0, 0.4, 0.6 and 1.0
and normalized pile lengths L/D = 5, 6, 7 and 8 were considered. Linear elastic behaviour was assigned to the steel elements

245   of the pile with Young's modulus $E_{pile} = 2.1 \cdot 10^8$ kN/m^2 and Poisson's ratio of $\nu_{pile} = 0.3$. For the very dense sand, the parameters
given in Table 1 were applied.

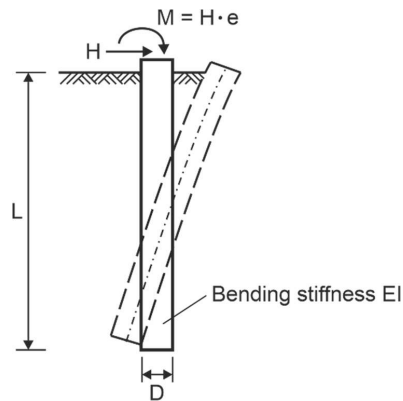



Fig. 8: System and applied loading for the advanced overlay model

Fig. 9 elucidates exemplarily how correction factors to be applied to the basic overlay model were derived. Depth-dependent

250   p-y curves for varied number of loading cycles were determined for given geometry and loading conditions. The curves were
then compared to the curves of the basic overlay model. It was again found that the transfer from the basic curves to the actual
curves could be well approximated by application of a y-multiplier independent of load level (cf. Fig. 9 right). Hence, a
correction factor Ω was defined as follows:

$$\Omega(N) = \frac{y_{actual}(N)}{y_{basic}(N)} \tag{11}$$

255   with y_{actual}, y_{bas} : pile displacements at a given depth z for the actual pile and load configuration and pile displacement for
the same p-value according to the basic overlay model.

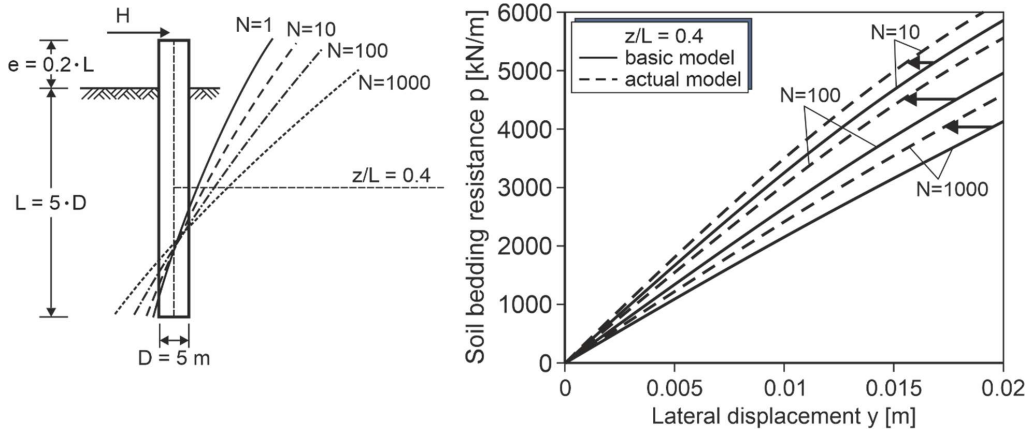
Fig. 9 shows that for the considered depth $z = 0.4\ L$ the actual p-y curves are stiffer than the curves determined with the basic
overlay model. This means that the correction factors are smaller than unity.

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Fig. 9: Exemplary comparison of p-y curves for constant horizontal displacement (bold lines) and p-y curves for the actual configuration (monopile in very dense sand)

The correction factors determined for the system given in Fig. 9 are presented in Fig. 10 (top right), together with the factors determined for other depths. It can be clearly seen that the correction factor is both dependent on the relative depth and on the

265 number of load cycles. The deviation of the actual and the basic p-y curves increases with increasing number of load cycles. Correction factors greater than unity, which mean a softening of the p-y curves, apply only to shallow depth ($z < 0.2\,L$). Below, only correction factors less than unity are found, which decrease almost linearly with increasing depth. The point of rotation of the monopile lies for the considered configuration in the region around $z = 0.8\,L$. Due to the very small deformation in this region, reliable p-y curves and corresponding correction factors cannot be determined. In the region below the rotation point

270 down to the pile tip, the correction factors are smaller than right above the rotation point and can as a first approximation be considered as constant over depth.

Fig. 10 also shows correction factors determined for monopiles with different eccentricities of the applied horizontal load. Evidently, the dependence of the correction factors on depth and number of load cycles is similar in all cases, but the values of the correction factors differ. Hence, the correction factors depend not only on depth and number of load cycles, but also on

275 load eccentricity and normalized pile length.
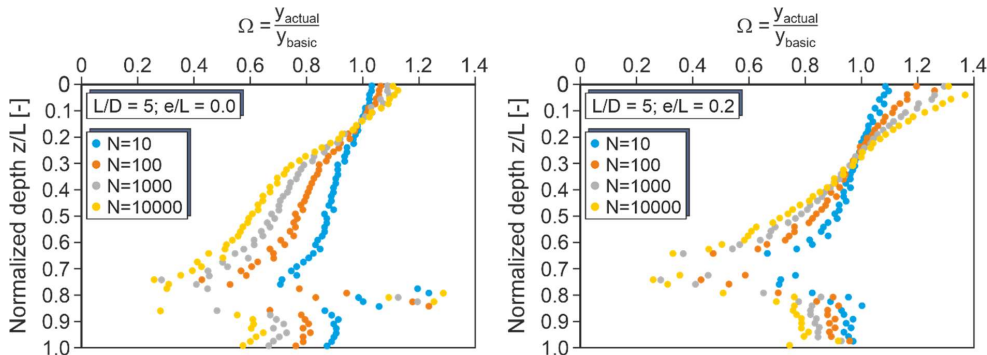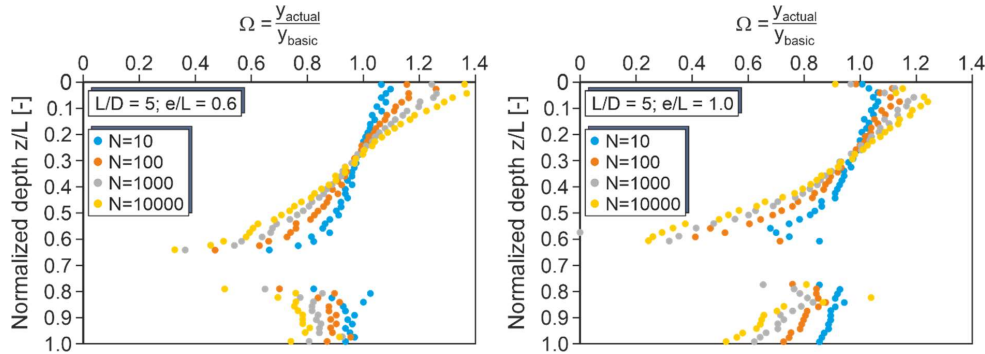
Fig. 10: Correction factors Ω for monopiles with L/D = 5 and different load eccentricities (very dense sand)

The Figs. 11 to 13 show the depth-dependent correction factors determined for relative monopile embedment lengths of L/D

280 = 6, 7 and 8. Evidently, also the embedment length of the monopile at least slightly affects the correction factors. In all cases, correction factors greater than unity apply only at shallow depths down to approximately z/L = 0.2. However, the inclination of the correction factor curve above the rotation point increases with increasing L/D and the almost constant values below the rotation point decrease slightly with increasing L/D.

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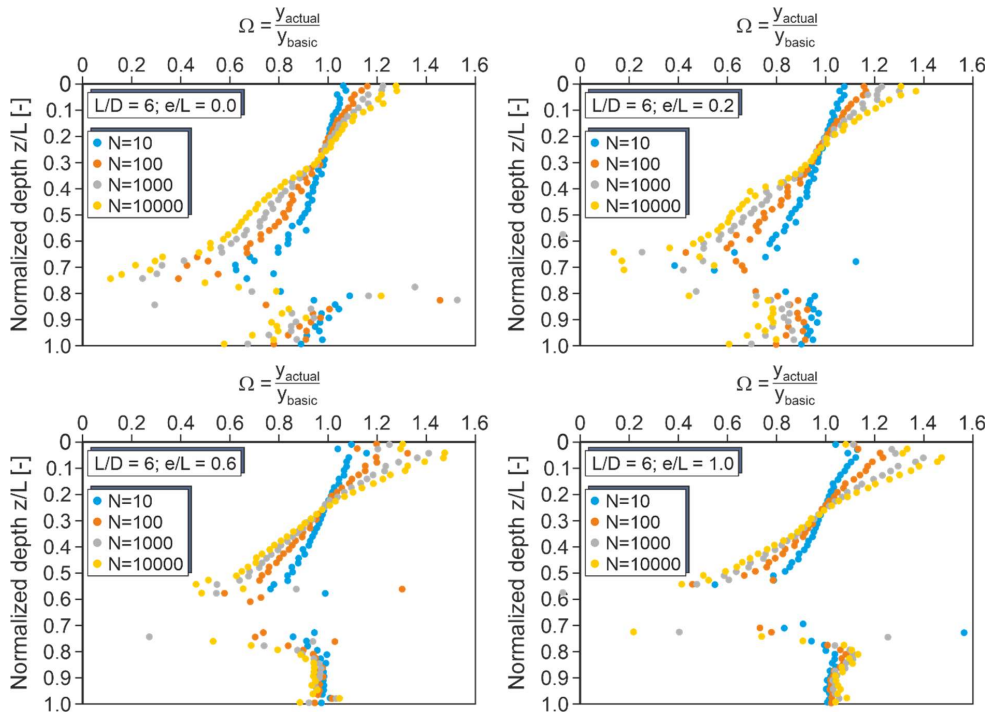


Fig. 11: Correction factors Ω for monopiles with L/D = 6 and different load eccentricities (very dense sand)

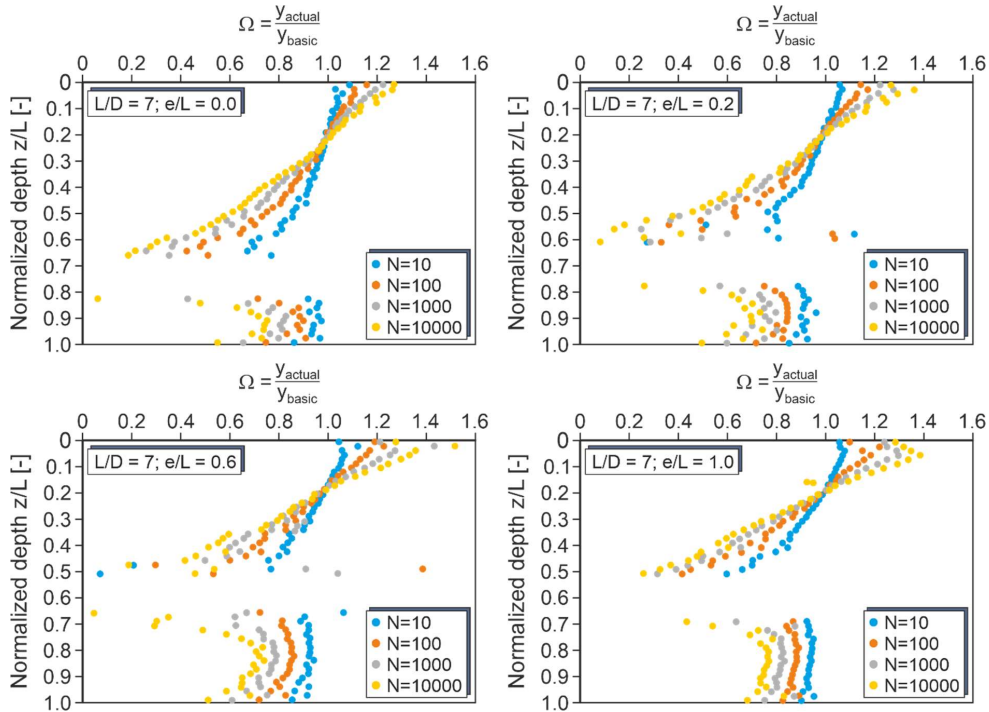



Fig. 12: Correction factors Ω for monopiles with L/D = 7 and different load eccentricities (very dense sand)

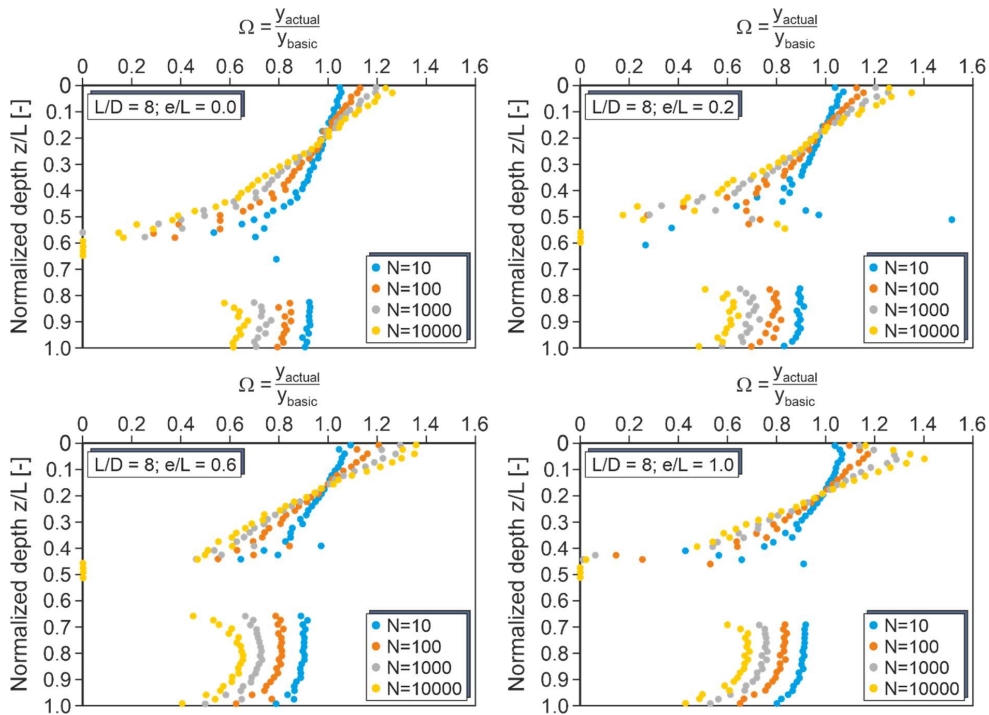



Fig. 13: Correction factors Ω for monopiles with L/D = 8 and different load eccentricities (very dense sand)

The following approach for calculation of the correction factor was found by systematic evaluation of the results of the parametric study conducted here:

Above the rotation point:

If $z/L < 0.2$: $\Omega(z, N, e, L) = 1 - (0.3\log(10N) + 0.38\,e/L + 0.06L/D) * (z/L - 0.2)$

If $z/L > 0.2$: $\Omega(z, N, e, L) = 1 - (0.3\log(0.1N) + 0.38\,e/L + 0.06L/D) * (z/L - 0.2)$ (12)

Below the rotation point: $\Omega(N, L, D) = N^{-0.007L/D}$

with:

z: Depth below sea bottom

L: Embedment length of the pile ($L/D \in (5 - 8)$)

N: Cycle numbers $\in (1 \sim 10000)$

e: Load eccentricity ($e/L \in (0.0 - 1.0)$)

With the purpose of determining a suitable cyclic p-y curve under true loading conditions, this correction factor Ω has to be applied to the y-multiplier of the basic overlay model. Hence, the following equation for the determination of cyclic y-multipliers eventually results:

$y_N/y_1 = N^A \cdot \Omega$ (13)

Users can apply these values on the displacements of a static p-y curve which was chosen by themselves to determine the cycle p-y curves at a desired cycle number.

It must be stated that Eq. (12) for the Ω-value was yet calibrated only for a pile diameter of $D = 5$ m and very dense sand. Supposedly, the relative density of sand has not a great effect on the Ω-values, but this has to be checked. A confirmation or extension of the Ω-approach for piles of other diameters than 5 m will be done in a next step of the work.

5 Model application and discussion

The derived cyclic overlay model is an easy-to-use approach to predict the translocation of p-y curves due to lateral cyclic load for any static p-y approach. In the following, the overlay model is applied to the static p-y approach stated by API (2014) (cf. section 2, Equations 1 and 2). The resulting deflections, bending moments and p-y curves can be compared to the results of the cyclic API approach, which is usually assumed to represent approximately 100 load cycles.

A monopile with a diameter of D = 5 m and an embedded length of L = 25 m (L/D = 5) in very dense sand (φ' = 40°, γ' = 10.31 kN/m³, cf. Table 1) is considered. A constant wall thickness of t = 7 cm and a load eccentricity e/L = 0.6 is assumed.

Fig. 14 shows deflection lines and bending moments for a horizontal load of H = 10 MN, calculated with the static API approach, the cyclic API approach and the cyclic overlay model for load cycle number of N=100, 1000 and 10000. The cyclic API approach predicts an increase of the pile head deflection (Fig. 14 left) with respect to the static approach of 30.5%, which is in rather good agreement with the result of the cyclic overlay model for N = 100 (22.1%). However, the overlay model also predicts pile head deflections for other load cycle numbers. For N = 1000 and 10000, the head displacement increases by 35.6% and 51.1%, respectively.

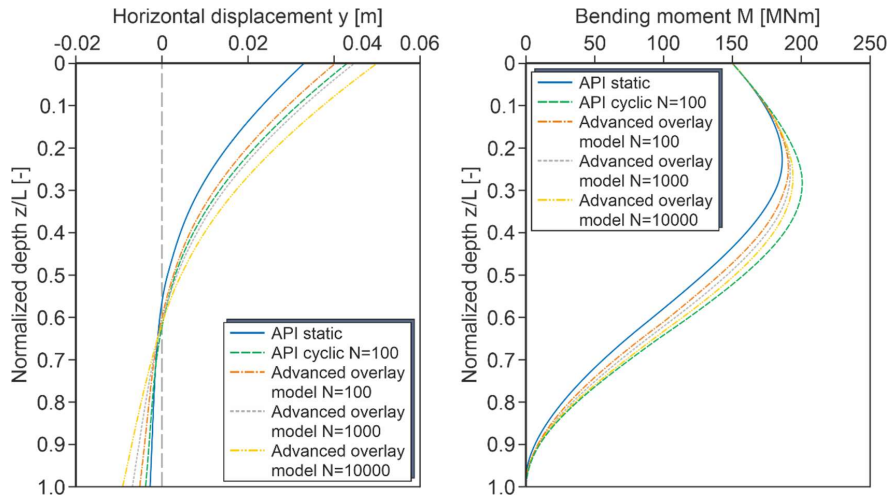



Fig. 14: Comparison of pile deflection lines (left) and bending moments (right)

Fig. 14 right shows that the cyclic API approach overestimates the maximum bending moment of the monopile. Compared to
335   the cyclic overlay model with N = 100, a 5.6% greater maximum bending moment is gained. Also the bending moments of the
cyclic overlay model with N = 1000 and 10000 are considerably smaller than for the cyclic API approach.

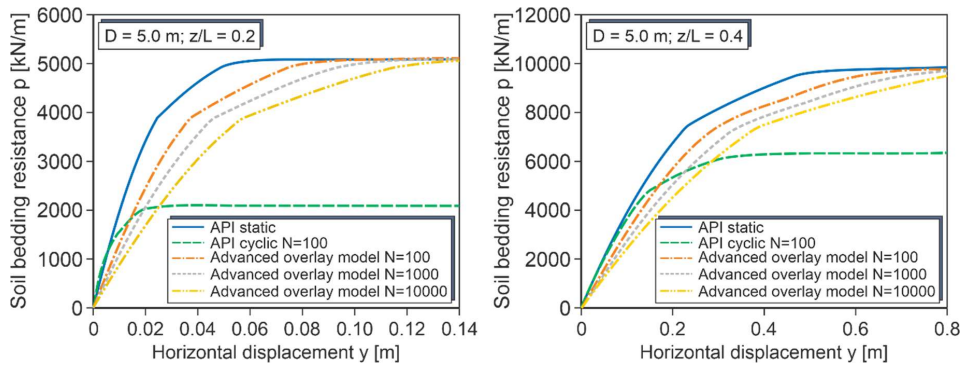
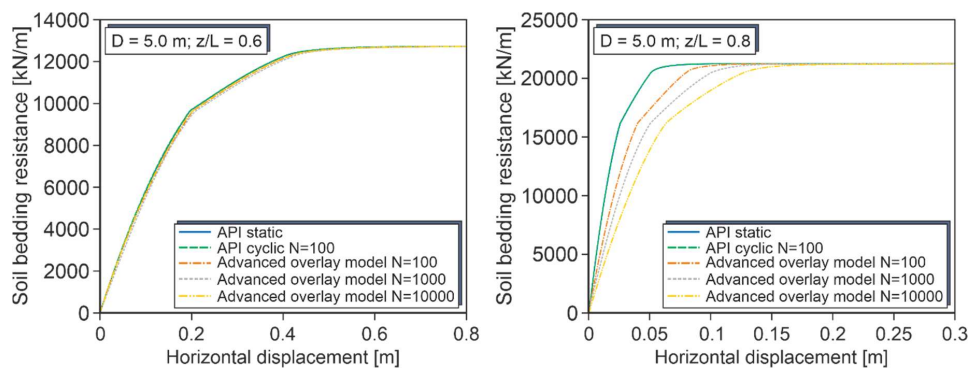
Fig. 15 shows the reason for that. Here, the p-y curves at four distinct depths along the monopile are depicted. The cyclic API
approach results in a severe degradation of bedding resistance and stiffness in shallow depth. In contrast, in greater depth (in
this example below z/L = 0.525) no modification of the p-y curves is to be considered. For a stiff or almost rigid pile, this is
340   of course unrealistic. It should be noted that the cyclic API approach was calibrated on lateral load tests on small and flexible
piles. According to the cyclic overlay model, the p-y curves are subject to softening along the whole pile length. Therefore, at
shallow depths much stiffer p-y curves apply, which results in considerably smaller maximum bending moments.

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Fig. 15: Comparison of cyclic p-y curves

6 Conclusions

By comparison of numerical simulations of monopile behaviour once under monotonic and once under cyclic loading with a defined number of load cycles (utilizing the SDM), a cyclic p-y overlay model for monopiles in sand soils could be developed.

350   Applying the derived equations for y-multipliers, arbitrary p-y curves for monopile behaviour under monotonic loading can be adapted to a given number of load cycles. The y-multipliers are formulated as a product of a term valid for constant horizontal deflection and a correction term accounting for the actual deflection line and loading conditions.

It was found that the first term could be formulated dependent only on the load cycle number and the angle of internal friction of the sand. In contrast, the second term was found to depend on load cycle number, monopile geometry (length-to-diameter

355   ratio), load eccentricity and relative depth.

The new cyclic overlay model gives plausible results and can be applied to any monotonic p-y approach for monopiles in sand. However, an experimental validation of the model is yet missing. It is planned to do this by cyclic large scale pile load tests in an ongoing research project.

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