

*In this document, the reviewer's comments are in black, the authors' responses are in red.*

We thank the reviewer for their thoughtful comments, which gave us an opportunity to revisit our analysis.

The manuscript describes a statistical (machine learning) approach to derive the uncertainty of wind data from mesoscale model simulations for longer time periods. The topic is relevant for wind energy. Thus, the manuscript should be published after revisions.

The manuscript is clearly written. Nevertheless, reading the manuscript rises a number of issues and questions which should be addressed in more detail in the manuscript.

(1) Lines 37-39: Using marine tower data (e.g., available offshore off the coasts of the Netherlands, Germany or Denmark) should at least be mentioned in the introduction in parallel to the possibility of using floating lidar data. There is more offshore wind data than those from buoys. Please add some references.

We have rephrased this part as: “Direct observations of the wind resource offshore are oftentimes limited to buoys, which offer measurements at very limited heights. Hub-height measurement of the wind resource offshore can be achieved with either offshore meteorological towers (e.g., Neumann et al. (2004); Fabre et al. (2014); Peña et al. (2014); Kirincich (2020)) or floating lidars (Carbon Trust Offshore Wind Accelerator, 2018; OceanTech Services/DNV GL, 2020). However, the often prohibitive costs connected to both these measurement solutions limit their availability to a handful of locations, despite recent efforts in leveraging their punctual hub-height measurements for wind speed vertical extrapolation over a larger region (Bodini and Optis, 2020; Optis et al., 2021a).”

(2) Given that there is some tower data (some of them for more than ten years), could testing of the results from this study against long-term time series from the FINO1 or FINO3 platform in the German Bight be an option?

Absolutely, using long-term tower data could be used in future work to model the actual error between WRF-modeled and observed wind speeds at hub-height. We had already mentioned this opportunity in the conclusions, but only with reference to floating lidar observations. We have now added an additional sentence to include tower data, too. That part now reads: “While floating lidars with publicly available data have only been deployed in the California OCS very recently (Gorton, 2020), a few lidars have been deployed off the U.S. Eastern Seaboard for more than 1 year. Observations from long-term offshore meteorological towers are also available in the North Sea in Europe. Our analysis could be expanded by first comparing the model-related boundary condition and parametric uncertainty with the full modeled wind speed uncertainty calculated by comparing modeled data and observations. Then, our proposed approaches could be expanded to temporally extrapolate the full modeled wind speed uncertainty; for example, quantified in terms of the variability of the residuals between modeled and observed wind.”

(3) The addressed wind conditions in this manuscript are those in coastal areas. Therefore, the reviewer is wondering why coastal effects in the wind fields are not addressed. This should at least be mentioned in the Introduction.

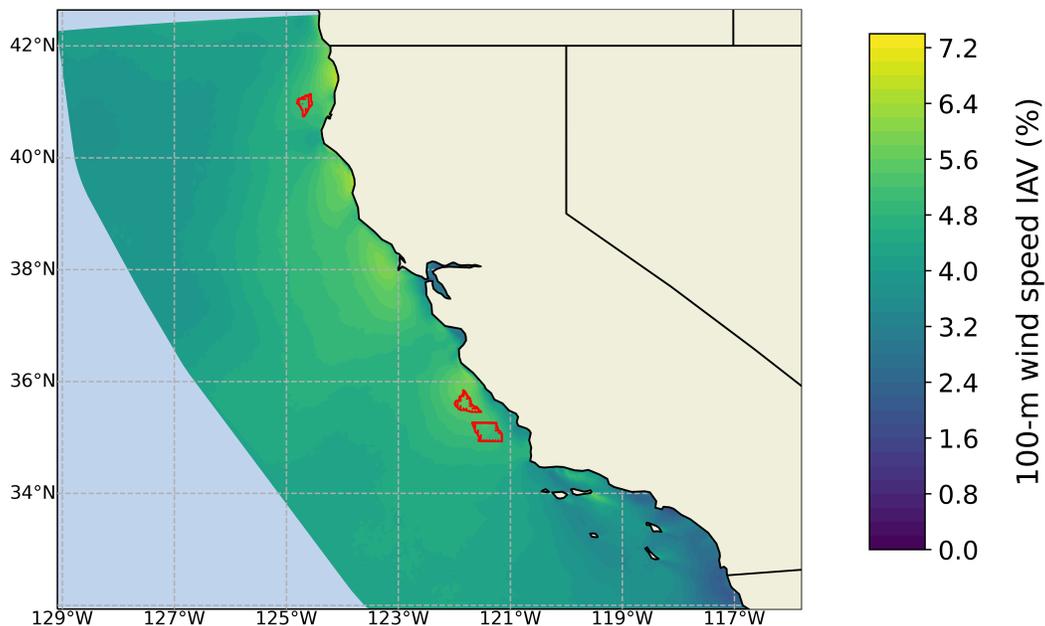
We have added the following part to the Introduction: “Given these constraints, numerical weather prediction (NWP) models at the mesoscale are often used to obtain an in space and time continuous mapping of the available offshore wind resource at the heights relevant for commercial wind power plant deployment (e.g., Mattar and Borvarán (2016); Salvação and Soares (2018)), with some studies (Papanastasiou et al., 2010; Steele et al., 2013; Arrillaga et al., 2016) also focusing on the validation of modeled coastal wind effects, such as sea breezes, which have a significant impact on offshore wind energy production (Archer et al., 2014).”

(4) Some configurations of the mesoscale model WRF have problems representing the atmospheric boundary layer in the transition region between land to open sea (see, e.g., Siedersleben et al., 2018, DOI 10.1127/metz/2018/0900). Has the WRF configuration chosen for this study been checked for the ability to properly simulate the transition from land to sea?

We did not specifically check this, but wind flow in the region is almost entirely from the northwest, with large open fetch and minimal land-sea interaction. Therefore, we expect any impacts from improperly modeling the transition layer would be minimal in this context.

(5) This study addresses uncertainties in wind speed. How does the magnitude of these possible uncertainties in wind speed modelling relate to, e.g., interannual wind speed changes due to long-term oscillations in the global circulation (NAO etc.) or due to climate change?

Assessing the impact of climate change and/or long-term oscillations is strictly outside the scope of our manuscript. However, to guide the interested reader in this analysis, we have calculated the interannual variability in modeled 100-m wind speed from the 20-year record used in the analysis, and included the following map in the Supplementary Materials:



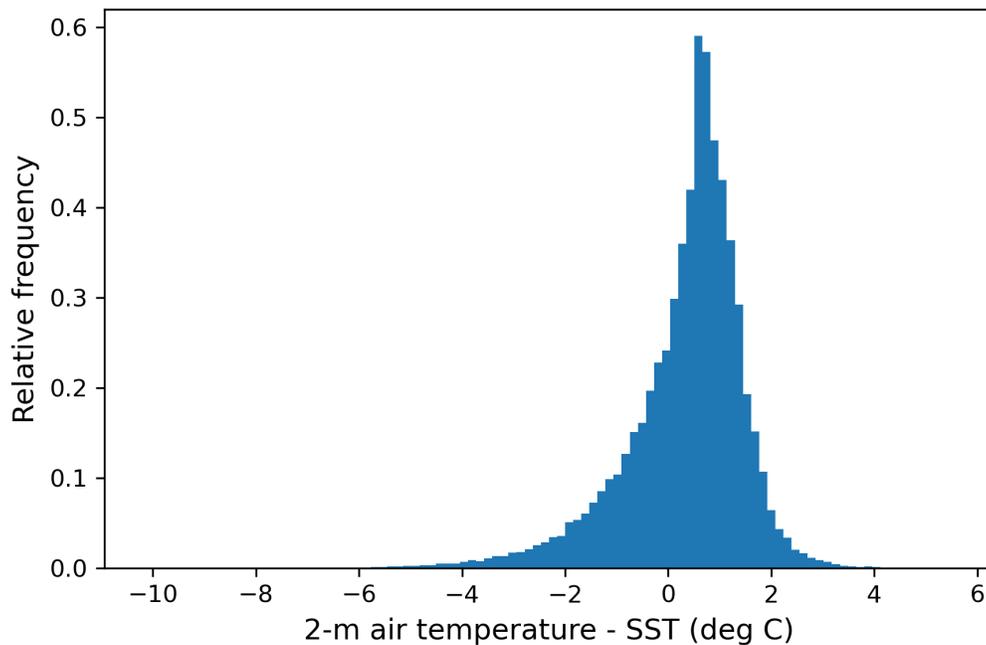
Also, we have added the following sentence at the end of the Conclusions:

“Finally, future work could focus on how interannual wind speed variability caused by climate change or long-term climatic and atmospheric oscillations (e.g., the North Atlantic oscillation) compares with the quantified uncertainty in modelled wind speed and how that should be taken

into account for wind energy development purposes. To facilitate this extension, we have included in the Supplementary Materials a map of the interannual variability in 100-m wind speed quantified from the 20-year WRF run.”

(6) Figure 7: Why do unstable thermal stratification conditions have such a small share of all cases? Shouldn't the lagged annual SST variation (due to the much larger thermal inertia of the water) compared to the air temperature variation lead to roughly equally frequent stable and unstable situations (stable in late winter and spring, unstable in late summer and autumn)? Please give an explanation for the found bulk Richardson number distribution.

To justify the distribution of bulk Richardson number, we have calculated the difference between air temperature and sea surface temperature at the considered site, using the 20-year WRF data:



As the histogram shows, the air temperature is generally higher than the sea surface temperature, likely because of ocean upwelling in the region, which leads to a generally cold sea water. This induces a stable stratification, which justifies the distribution of bulk Richardson number found and reported in the paper. We have added a comment on this in the paper, too (“This is consistent with the sea surface temperature being generally colder than the near-surface air (because of ocean upwelling), which causes a predominantly stable stratification.”).

(7) Why is the 2 m inverse Obukhov length chosen as a parameter at all in Section 2.2? This parameter can only be relevant for the whole rotor area of the future wind turbines in cases with perfect vertical mixing. In stable conditions the depth of the Prandtl layer is much shallower than turbine hub height so that the near-surface Obukhov length is most probably irrelevant for the 100 m wind speed. This is likely to be also true for cases in which internal boundary layers are present (which frequently happens in coastal areas).

See our answer to comment #9.

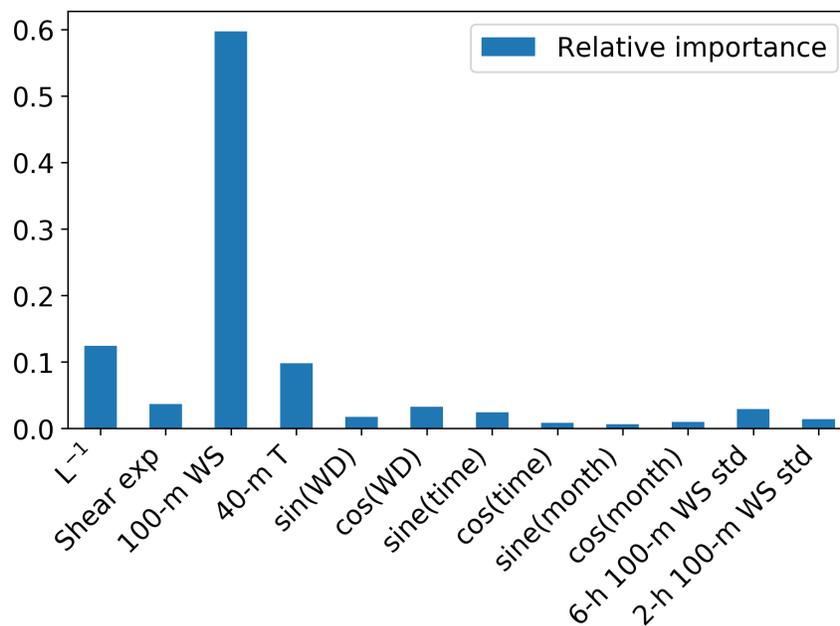
(8) Figure 3 demonstrates that the 2 m inverse Obukhov length is not a meaningful parameter, because it is always close to zero. Logically, the weight 0 has been attributed to this parameter in Table 4. So, once again, why has this parameter been included into this study?

[See our answer to comment #9.](#)

(9) Assumed that the inverse Obukhov length has nevertheless some relevance, a not-discussed contradiction is that there seems to be a slight bias of the inverse Obukhov length towards instability in Figure 3 while there is a strong bias of the bulk Richardson number towards stable conditions in Figure 7? This should be explained. It seems to confirm the irrelevance of the inverse Obukhov length stated above.

The observed range of inverse(L) is actually a quite typical one, if we consider that a value of  $L = \pm 200\text{m}$  (a somewhat typical threshold between neutral and stable/unstable conditions) would translate in a  $1/L$  threshold of  $\pm 0.005\text{ m}^{-1}$ . We have changed the x-axis limits in figure 3 to make the plot (where no real bias emerges) easier to understand.

That being said, we have performed the feature importance calculation for the input parameters to the ML algorithm at one test site (one of the three wind energy lease areas), and actually found how inverse(L) was the second most important input feature for the algorithm:



In any case, we agree with the reviewer that different choices for the stability parameter are possible, and using a different one could potentially improve the performance of the proposed algorithms (as hinted by the fact that inverse(L) was not deemed useful by the AnEn algorithm). We have added the following comment to Section 2.2: “We also acknowledge how different choices for the atmospheric stability parameter could be explored, potentially leading to a more accurate representation of stability at the heights of interest for wind energy development compared to the near-surface Obukhov length.”

(10) A major finding of this study is the increase in wind speed uncertainty close to the coast and for non-neutral stratifications. Does this point to weaknesses in the used method or to weaknesses

in the used mesoscale model? Or is this a natural feature which comes out of this study? Please discuss this point in the Conclusions.

The larger uncertainty in modeled hub-height wind speed near the coast was also found in Optis et al. 2020 when looking at the WRF ensemble members only. In their report, they comment that “Most of this sensitivity can be attributed to the choice of PBL scheme (MYNN or YSU) and the diverging wind profiles associated with each under strong stable atmospheric conditions near the coastline.” We have added the following sentences in the Conclusions of our paper: “In general, we find that the offshore wind speed boundary condition and parametric uncertainty increases near the coast. While the accuracy of the AnEn approach significantly degrades near the coast, the larger values in hub-height wind speed boundary condition and parametric uncertainty near the coast were also seen from the variability among the WRF ensembles (Optis et al. 2020), and attributed to diverging wind profiles associated with the choice of PBL scheme under strong stable atmospheric conditions near the coastline.”.

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We thank the reviewer for their thoughtful comments, which gave us an opportunity to revisit our analysis.

The manuscript by Bodini et al. on "Assessing Boundary Condition and Parametric Uncertainty in Numerical-Weather-Prediction-Modelled, Long-Term Offshore Wind speed Through Machine Learning and Analog Ensemble" focusses on comparing two different methods on how to extrapolate the ensemble uncertainty of a short (one year time) series to a long time series for the wind conditions along the coast of California.

The study is generally well written, figures are selected meaningfully and readable. However, I have a number of minor comments to be taking into account before I can recommend publication in Wind Energy Science.

Minor Comments:

- Line 28: Northern Europe is typically referred to as Scandinavia. I guess you rather mean central Europe here?

We have rephrased this as "In some areas of the world, such as the North Sea in Europe,"

- Line 43: "a continuous, in space and time" → I suggest: an in space and time continuous  
Changed.

- Line 76: "prohibitive, and innovative and more computationally" → remove the "and" before innovative

We have rephrased this.

- Line 103: "The 15 WRF ensemble members" → I strongly recommend creating a table here with one row per one of the 16 members and then the settings in the columns. It is hard to read and understand here.

We had a typo in the sentence. Year 2017 (and not the 15 ensemble members, as previously stated in the draft) was selected because of strong data coverage from the network of buoy and coastal radar observations used for model validation. We think that now the section is clear: all 16 WRF ensembles share the common WRF attributes in Table 1; the list at page 5 shows the various combination of additional WRF parameters that led to the creation of the 16 ensemble members.

- Line 131: "mean hourly wind speed" → How did you compile the mean hourly wind speed? How many timesteps have you written out from the WRF runs to compute the average?

We have added the following: "(calculated from 5-minute WRF raw output)".

Line 147: "the WRF across-ensemble standard deviation" → what is the across-ensemble standard deviation. Is this the standard deviation from the ensemble members?

The WRF across-ensemble standard deviation is explicitly defined in equation 1.

Line 156-157: Can you explain why you used both the standard deviation from preceding 2 and 6 hours and how these time intervals were selected?

We selected these time intervals to try to capture variability of atmospheric conditions over different time scales which based on our experience could have an impact on hub-height wind speed uncertainty. As stated in our answer to the next comment, we have acknowledged in the paper that the choice of input features in our analysis was not exhaustive, and that “Testing additional input features to the algorithms could also help further improving the accuracy of the proposed extrapolation.”

Line 161: "However, we found that including all the features" → can you explain how you found this? And did you try further features?

We compared the error metrics obtained (on a limited number of test sites) when using different sub-sets of input features, and found that the best results were obtained with all inputs together. We did not try additional features, but we agree that this might be interesting future work, and we have added the following sentence to the Conclusions: “Testing additional input features to the algorithms could also help further improving the accuracy of the proposed extrapolation.”

Table 2: It is quite difficult to read column two. Maybe it helps to add a small empty row after each row?

Done.

Table 4: I think you should at least try to explain why there is no weight on the inverse Obukhov length but a strong weight on shear.

As suggested by the other reviewer, in stable conditions the depth of the Prandtl layer is much shallower than turbine hub height so that the near-surface Obukhov length is likely irrelevant for determining uncertainty in the 100 m wind speed. We have now added some comments on this in the paper.

Line 230 and Line 303-304: "Applying the bias correction proposed in" → So, if this would likely reduced the AnEn bias, why didn't you do it? This should at least be explained.

The negative bias is likely caused by two reasons, the limited historical repository to search and the fact we take an *average* of the 16 ensemble members. When only having a limited historical repository, there is a balance between the prediction accuracy and the systematic bias. During our grid search analysis for the best number of ensemble members to generate, we observed that AnEn archives better bias (closer to zero) with fewer members but the prediction accuracy, e.g., RMSE, would drop. To the focus of this manuscript, prediction accuracy is the most important metric, and therefore, we set RMSE optimization to be the most important metric. Additional bias correction processes might be able to help AnEn prediction, but we would like to keep a fair comparison between ML and AnEn. In fact, the postprocessing technique can be computationally expensive when applied to a large domain. Therefore, extensive correction on AnEn has not been explored. We have added information on this in the following paragraph, where we have also added reference to another technique that can be explored in future work to reduce the AnEn bias:

“The bias from the AnEn approach is likely because of the reduced length of the search period (1 year), which might be too limited for identifying a significant number (16) of analogs. This setup constrains the AnEn ability to account for rare events (e.g., particularly high-wind-speed cases) when looking for similar atmospheric conditions in such a short repository. Also, when searching for the optimal number of analogs to use, there is always a trade-off between the prediction accuracy (e.g., the RMSE) and the prediction bias. For our analysis, the main goal was to maximize

the prediction accuracy, in alignment with the ML approach, and therefore we set the RMSE as the optimization metric. During our grid search analysis to determine the optimal number of analog members, we observed that AnEn archives better bias with fewer members, which would however worsen the prediction accuracy (RMSE). Applying the bias correction proposed in Alessandrini et al. (2019), using a machine-learning similarity for analog definition (Hu et al., 2021b), or adopting a quantile mapping that uses quantiles of the analog ensemble instead of its mean (Sidel et al., 2020) would help reducing the AnEn bias, at the potential expense of computational costs.”

Figures 6 and 8: There should be a space between caption text and unit.

Thank you for catching this, we have fixed this.

Line 279-280: "For each atmospheric stability class, the values shown are the" → Maybe an active sentence is better here, e.g., for each atmospheric stability class, we show....

Changed.

Line 293 and the whole Conclusions section: I suggest replacing Weather Research and Forecasting or the abbreviation WRF by "mesoscale" everywhere in the conclusion, because the results and conclusions should in principle be valid to any mesoscale ensemble dataset, shouldn't they?

We agree with the reviewer and have changed this as suggested.

Line 319: "deployed in the California OCS very recently" → I guess you mean this buoy? <https://a2e.energy.gov/data/buoy/lidar.z06.00> Maybe it's worth referencing the dataset (including the doi) here.

We have added a reference as suggested.

References: The references are vastly incomplete. Every journal paper should have a doi and every technical report a link or other accessibility information.

We have updated the references whenever possible.

# Assessing Boundary Condition and Parametric Uncertainty in Numerical-Weather-Prediction-Modeled, Long-Term Offshore Wind Speed Through Machine Learning and Analog Ensemble

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**Abstract.** To accurately plan and manage wind power plants, not only does the time-varying wind resource at the site of interest need to be assessed, but also the uncertainty connected to this estimate. Numerical weather prediction (NWP) models at the mesoscale represent a valuable way to characterize the wind resource offshore, given the challenges connected with measuring hub height wind speed. The boundary condition and parametric uncertainty associated with modeled wind speed is often estimated by running a model ensemble. However, creating an NWP ensemble of long-term wind resource data over a large region represents a computational challenge. Here, we propose two approaches to temporally extrapolate wind speed boundary condition and parametric uncertainty using a more convenient setup where a mesoscale ensemble is run over a short-term period (1 year), and only a single model covers the desired long-term period (20 year). We quantify hub-height wind speed boundary condition and parametric uncertainty from the short-term model ensemble as its normalized across-ensemble standard deviation. Then, we develop and apply a gradient-boosting model and an analog ensemble approach to temporally extrapolate such uncertainty to the full 20-year period, where only a single model run is available. As a test case, we consider offshore wind resource characterization in the California Outer Continental Shelf. Both the proposed approaches provide accurate estimates of the long-term wind speed boundary condition and parametric uncertainty across the region ( $R^2 > 0.75$ ), with the gradient-boosting model slightly outperforming the analog ensemble in terms of bias and centered root-mean-square error. At the three offshore wind energy lease areas in the region, we find a long-term median hourly uncertainty between 10% and 14% of the mean hub-height wind speed values. Finally, we assess the physical variability of the uncertainty estimates. In general, we find that the wind speed uncertainty increases closer to land. Also, neutral conditions have smaller uncertainty than the stable and unstable cases, and the modeled wind speed in winter has less boundary condition and parametric sensitivity than summer.

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## 1 Introduction

Offshore wind energy keeps increasing its market penetration as an inexpensive and clean source of energy. In some areas of the world, such as Northern the North Sea in Europe, offshore wind represents a well-established source of electricity, with a total installed capacity of about 15 GW, and a planned increase of up to 74 GW by 2030 (van Hoof, 2017). As the cost of offshore wind energy has been decreasing faster than expected (Stiesdal, 2016; Brandily, Tifenn, 2020), many other regions are currently planning to adopt offshore wind energy solutions to meet their energy needs. The United States fall within this group, with its offshore technical resource potential being estimated to be about twice the present national energy demand (Musial et al., 2016). While one single 30-MW offshore wind power plant has been operating since 2016 (Deepwater Wind, 2016), many other offshore wind plants are being planned, mostly concentrated along the Eastern Seaboard and the Outer Continental Shelf (OCS) off the coast of California, for a total of about 86 GW installed capacity expected by 2050 (Bureau of Ocean Energy Management, 2018).

Such extensive growth requires an accurate long-term characterization of the offshore wind resource (Brower, 2012). Direct observations of the wind resource offshore are ~~sparse, and~~ oftentimes limited to buoys, which offer measurements at very limited heights. ~~While the emergence of floating lidars is expected to provide better characterization of~~ Hub-height measurement of the wind resource ~~at wind turbine hub height (Carbon Trust Offshore Wind Accelerator, 2018; OceanTech Services/DNV-GL, 2020)~~ , especially considering recent proposed innovations offshore can be achieved with either offshore meteorological towers (e.g., Neumann et al. (2004); Fabre et al. (2014); Peña et al. (2014); Kirincich (2020)) or floating lidars (Carbon Trust Offshore Wind Accelerator . However, the often prohibitive costs connected to both these measurement solutions limit their availability to a handful of locations, despite recent efforts in leveraging their punctual hub-height measurements for wind speed vertical extrapolation ~~(Bodini and Optis, 2020; Optis et al., 2021a), their prohibitive costs still represent a major challenge~~ over a larger region (Bodini and Optis, 2020; Optis et al., 2021a). Given these constraints, numerical weather prediction (NWP) models at the mesoscale are often used to obtain ~~a continuous, an~~ in space and time ~~, continuous~~ mapping of the available offshore wind resource at the heights relevant for commercial wind power plant deployment ~~(e.g., Mattar and Borvarán (2016); Salvação and Soares (2018))~~ , with some studies (Papanastasiou et al., 2010; Steele et al., 2013; Arrillaga et al., 2016) also focusing on the validation of modeled coastal wind effects, such as sea breezes, which have a significant impact on offshore wind energy production (Archer et al., 2014).

Tens of billions of dollars will be invested in the U.S. offshore wind energy industry in the coming years. In order to minimize the financial risk associated with such major investments, not only is a characterization of the time-varying offshore wind resource needed, but an assessment of the uncertainty connected to this numerical prediction is of primary importance. A 1% uncertainty change in the mean wind resource translates to a 1.6%–1.8% uncertainty for the long-term wind plant

annual energy production (Johnson et al., 2008; White, 2008; Holstag, 2013; Truepower, 2014), with a significant increase in the interest rates for new project financing. However, assessing the uncertainty in modeled wind speed is a problematic task. NWP model ensembles tend to lead to an underdispersive behavior (Buizza et al., 2008; Alessandrini et al., 2013), so that only a limited component of the actual wind speed error with respect to observations can be quantified. The full uncertainty in NWP-model-predicted wind speed can be quantified only when direct observations of the wind resource are available. In this scenario, the residuals between modeled and observed wind speed can be calculated, and the model error is quantified in terms of its bias (i.e., the mean of the residuals) and uncertainty (i.e., the standard deviation of the residuals). The obtained model uncertainty would then be added to the inherent uncertainty of the wind speed measurements by using a sum of squares approach (JCGM 100:2008, 2008). However, as we have already mentioned, direct observations of the wind resource are not always readily available, especially offshore, so that other ways to quantify at least specific components of the full wind speed uncertainty are needed.

When considering NWP models, the choices of the model setup and inputs have a direct impact on the model wind speed prediction, and therefore on its uncertainty. Hahmann et al. (2020) recently provided a detailed analysis of the sensitivity in wind speed predicted by NWP models, as part of the development of the New European Wind Atlas. Among the various sources of uncertainty, the choices of the planetary boundary layer (PBL) scheme (Ruiz et al., 2010; Carvalho et al., 2014a; Hahmann et al., 2015; Olsen et al., 2017) and of the large-scale atmospheric forcing (Carvalho et al., 2014b; Siuta et al., 2017) have been shown to have a major impact. Model resolution (Hahmann et al., 2015; Olsen et al., 2017), spin-up time (Hahmann et al., 2015) and data assimilation techniques (Ulazia et al., 2016) have also been shown to contribute to the wind speed sensitivity. The variability of modeled wind speed that derives from all the different model choices leads to what we will call boundary condition and parametric uncertainty of the modeled wind speed. Optis et al. (2021b) recently explored best practices for quantifying and communicating NWP-modeled wind speed boundary condition and parametric uncertainty offshore. In their approach, an ensemble of Weather Research and Forecasting (WRF) model (Skamarock et al., 2008) simulations is created by considering different WRF versions, namelists, and external forcings, and the wind speed boundary condition and parametric uncertainty is then quantified in terms of its across-ensemble variability. The use of numerical ensembles for uncertainty quantification is not exclusive to the wind energy community, as it has been extensively applied in ample spectrum fields (e.g., Zhu (2005); Parker (2013); Murphy et al. (2004)). However, running a NWP ensemble across a large region and for the long-term period needed for an accurate characterization of the naturally varying wind resource is computationally prohibitive, and so that innovative and more computationally efficient ways are needed to quantify some components of the long-term wind speed uncertainty.

Here, we consider wind speed characterization in the California OCS, and we propose and compare two innovative techniques for modeled wind speed long-term boundary condition and parametric uncertainty quantification. To do so, we consider a setup that is computationally more affordable, wherein WRF ensembles are only run over a short period (1 year), and are accompanied by a single, long-term (20 years) WRF simulation. First, we use a machine-learning algorithm to temporally extrapolate the WRF-based boundary condition and parametric uncertainty from the ensemble year to the full 20-year period. While machine learning has been successfully applied to various atmospheric (e.g., Xingjian et al. (2015); Gentine et al. (2018);

Bodini et al. (2020)) and wind-energy-related (e.g., Clifton et al. (2013); Arcos Jiménez et al. (2018); Optis and Perr-Sauer (2019)) problems, this represents, to the authors' knowledge, its first application for NWP uncertainty extrapolation. We compare the machine-learning-based approach with the predictions from the analog ensemble (AnEn) technique (Delle Monache et al., 2013) to quantify uncertainty in the wind resource from the variability in modeled cases with similar atmospheric conditions. Typical applications of AnEn include renewable energy probabilistic forecast, for both solar (Alessandrini et al., 2015a, b; Cervone et al., 2017) and wind (Junk et al., 2015; Vanvyve et al., 2015) energy. The use of AnEn for long-term offshore wind speed uncertainty quantification represents a novel application of the technique.

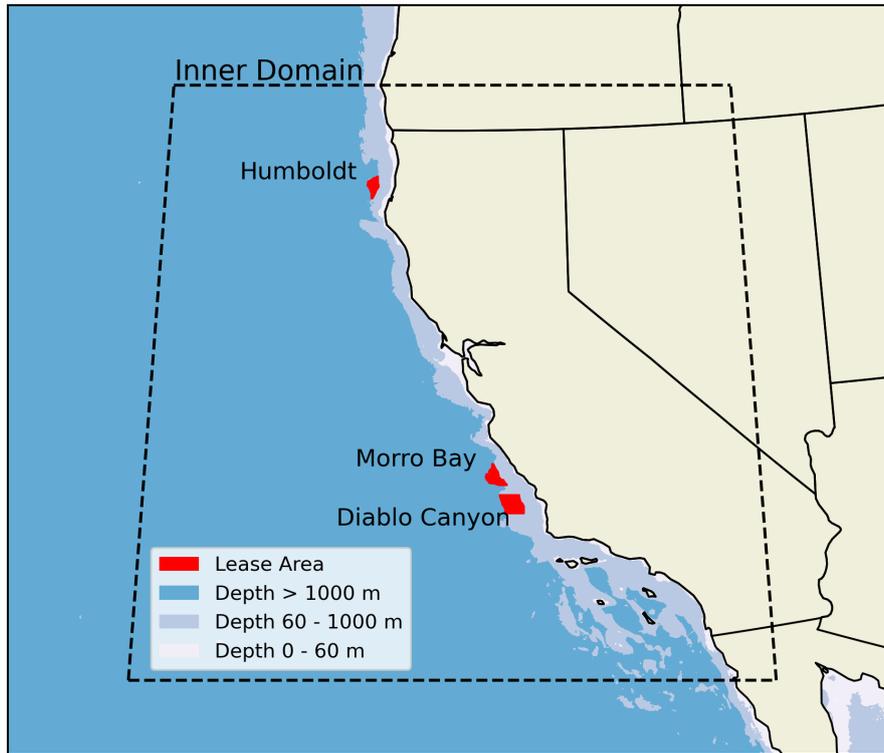
In the remainder of this paper, we describe the experimental setup and our proposed methods to quantify and temporally extrapolate modeled wind speed boundary condition and parametric uncertainty in Section 2. Section 3 validates the techniques used, and compares the mean long-term predictions from the two approaches. Also, we discuss physical insights into the main drivers for offshore wind speed boundary condition and parametric uncertainty. Finally, we conclude and suggest future work in Section 4.

## 2 Data and Methods

### 2.1 Numerical simulation setup

We consider a 20-year numerical data set recently developed by the National Renewable Energy Laboratory to provide accurate cost estimates for floating wind in the California OCS (Figure 1). As described in detail in Optis et al. (2020), this product includes a single WRF setup that is run for a 20-year period (2000-2019), and an additional 15 WRF ensemble members run over a single year (2017), which ~~were~~ was selected because of strong data coverage from the network of buoy and coastal radar observations used for model validation. All of the simulations are run with the common attributes in Table 1. A total of over 200,000 grid cells are included in the WRF inner domain, which we consider in our uncertainty analysis. The 16 WRF ensemble members are constructed based on variations of boundary conditions and key WRF model parameters that previous research determined to have a primary impact on modeled wind speed:

- Reanalysis forcing product: selected between ERA5, developed by the European Centre for Medium-Range Weather Forecasts (Hersbach et al. (2020)), and the Modern-Era Retrospective analysis for Research and Applications, Version 2 (Gelaro et al. (2017)), developed by the National Aeronautics and Space Administration.
- PBL parameterization: chosen between the Mellor-Yamada-Nakanishi-Niino (MYNN, Nakanishi and Niino (2004)) and the Yonsei University (Hong et al. (2006)) schemes.
- Sea surface temperature product: selected between the Operational Sea Surface Temperature and Sea Ice Analysis (OS-TIA) data set produced by the UK Met Office (Donlon et al., 2012) and the National Center for Environmental Prediction Real-Time Global product.



**Figure 1.** Map of the inner domain of the WRF numerical simulations for the California OCS. The current three wind energy lease areas are shown in red.

- Land surface model: chosen between the Noah model and the updated Noah multiparameterization model (Niu et al., 2011).

The setup we chose to use for the single long-term WRF run is the result of a validation process. We compared and validated the 16 model setups with observations from buoys from the National Data Buoy Center and coastal radar measurements from the National Oceanic and Atmospheric Administration profiler network. While these are the only observations in the area available for model validation, these data sets cannot be used for quantifying the model uncertainty in wind speed. In fact, both data sources have significant limitations that do not allow for a direct comparison with offshore WRF data at heights relevant for wind energy development. On one hand, buoys only measure wind speed close to the water level, which can have a very different regime than the hub-height winds. On the other hand, the coastal radars measure at more relevant heights for wind energy, but only at the interface between the ocean and land. Results from the validation (whose details can be found in Optis et al. (2020)) revealed that the WRF setup providing the most accurate results is the one using ERA5 as reanalysis product, MYNN as a PBL scheme, OSTIA as an SST product, and Noah as a land surface model. Therefore, we selected and adopted this WRF setup for the single 20-year WRF run.

**Table 1.** Common specification for all of the WRF runs considered in the analysis.

Feature	Specification
WRF version	4.1.2
Nesting	6 km, 2 km
Vertical levels	61
Atmospheric nudging	Spectral nudging on a 6-km domain, applied every 6 hours
Microphysics	Ferrier
Longwave radiation	Rapid radiative transfer model
Shortwave radiation	Rapid radiative transfer model
Topographic database	Global multiresolution terrain elevation data from the United States Geological Service and National Geospatial-Intelligence Agency
Land-use data	Moderate resolution imaging spectroradiometer 30s
Cumulus parameterization	Kain-Fritsch

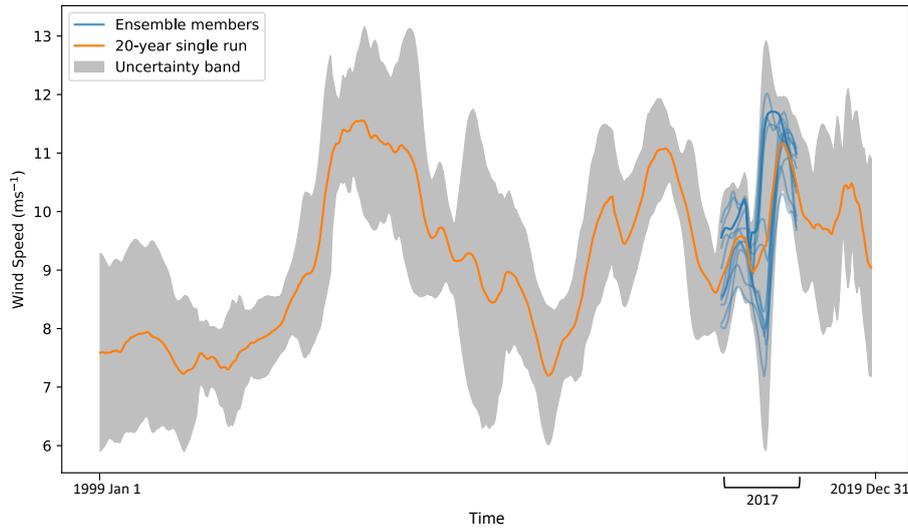
In our analysis, we use hourly average data ([calculated from 5-minute WRF raw output](#)), and we quantify the WRF wind speed boundary condition and parametric sensitivity in terms of the across-ensemble standard deviation of the WRF-predicted 100-m wind speed at any hour,  $t$ , normalized by the hourly average 100-m wind speed itself:

$$\sigma_{\text{WS}}(t) = \frac{\frac{1}{N} \sum_{i=1}^N (\text{WS}_i(t) - \overline{\text{WS}}(t))^2}{\text{WS}_1(t)} \quad (1)$$

where  $\text{WS}_i$  is the mean hourly 100-m wind speed from each ensemble member,  $\overline{\text{WS}}$  is the mean hourly wind speed averaged across the 16 ensemble members,  $\text{WS}_1$  is the mean hourly 100-m wind speed from the WRF control run (i.e., the one used for the long-term period), and  $N = 16$  is the total number of WRF ensemble members. Within a numerical ensemble framework, the use of (normalized) standard deviation as a primary uncertainty metric has been recommended by Optis et al. (2021b), as it provides more consistent estimates than the ensemble interquartile range. While we acknowledge that our quantification of the WRF wind speed boundary condition and parametric sensitivity is going to be limited by the finite number of choices made to construct the ensemble members, we note how the considered set of settings represents either state-of-the-art products or the most popular and widely accepted choices for WRF applied to wind resource characterization. In the next sections, we present the two approaches we propose to temporally extrapolate this boundary condition and parametric uncertainty from 2017 (i.e., the only year where the uncertainty can be directly calculated from the WRF ensemble members) to the remaining 19 years.

## 2.2 Machine-learning approach

The first approach we use to temporally extrapolate the boundary condition and parametric uncertainty in 100-m modeled wind speed is a machine-learning gradient-boosting model (GBM) (Friedman, 2002). We select a GBM because ensemble-



**Figure 2.** Qualitative illustration of the concept used to temporally extrapolate the 100-m modeled wind speed boundary condition and parametric uncertainty through the proposed machine-learning and analog ensemble approaches. Wind speed uncertainty is directly quantified as its WRF cross-ensemble normalized standard deviation (Eq. 1) on the single year in which ensembles were run, and then extrapolated to the remaining 19 years, which were run with only a single WRF setup, using the proposed GBM and AnEn approaches.

based algorithms are known to provide robust and accurate predictions in nonlinear problems. Moreover, we have tested a set of other machine-learning algorithms (random forest, generalized additive model), and the GBM provided the lowest prediction error. With this approach, at each of the more than 200,000 grid cells, we train the model on calendar year 2017 to predict the WRF cross-ensemble standard deviation of hourly average 100-m wind speed, normalized by the hourly average 100-m wind speed itself (Eq. 1). We then apply the trained model to quantify the modeled wind speed boundary condition and parametric uncertainty in the remaining 19 years where only the single WRF run is available (Figure 2). The input features we use to feed the GBM are all taken (as hourly averages) from the single WRF setup that is run for the full 20-year period, and are:

- Wind speed at 100 m ~~aboveground~~above ground level (AGL)
- Sine and cosine<sup>1</sup> of wind direction at 100 m AGL
- 160 – Air temperature at 40 m AGL
- Wind shear coefficient calculated between 10 and 200 m AGL
- Inverse of Obukhov length at 2 m AGL
- 100-m wind speed standard deviation calculated from the preceding 2 hours

<sup>1</sup>Sine and cosine are used to preserve the cyclical nature of this feature. Both are needed because each value of sine only (or cosine only) is linked to two different values of the cyclical feature.

**Table 2.** Hyperparameters considered for the gradient-boosting model.

Hyperparameter	Meaning	Sampled Values
Number of estimators	Number of trees in the forest	100–300
Learning rate	Rate by which the contribution of each tree is shrunk	0.05–1
Maximum depth	Maximum depth of the tree	4–10
Maximum number of features	Number of features to consider when looking for the best split	1–7
Minimum number of samples to split	Minimum number of samples required to split an internal node	2–20
Minimum number of samples for a leaf	Minimum number of samples required to be at a leaf node	1–20

- 100-m wind speed standard deviation calculated from the preceding 6 hours
- 165 – Sine and cosine<sup>1</sup> of the hour of the day
- Sine and cosine<sup>1</sup> of the month.

The distribution of these variables is presented and discussed in Section 3.1. We acknowledge that correlation exists between some of the input features used. However, we found that including all the features produced the best model accuracy. Also, principal component analysis could be applied to reduce the number of features used, but it is beyond the scope of our analysis.

170 [We also acknowledge how different choices for the atmospheric stability parameter could be explored, potentially leading to a more accurate representation of stability at the heights of interest for wind energy development compared to the near-surface Obukhov length.](#)

The learning algorithm is trained using the root-mean-square error (RMSE) as a performance metric to tune the algorithm weights. To avoid overfitting, we implement regularization during the training of the learning algorithm, using the hyperpa-  
175 rameters and value ranges listed in Table 2. At each site, we sampled 20 combinations of hyperparameters using a randomized cross validation. More details about the validation of the results from the proposed approach are given in Section 3.1.

### 2.3 Analog ensemble approach

The second approach we use to quantify and extrapolate modeled wind speed boundary condition and parametric uncertainty is based on the AnEn approach. At each site and for each hour (hereafter referred to as the "target hour") , the AnEn considers  
180 a set of atmospheric variables, which are consistent between the AnEn and the machine-learning approach, in a 3-hour window centered on the considered time stamp. Then, the AnEn looks for analog atmospheric conditions at the considered site using

**Table 3.** Variability of the RMSE of two weight optimization schemes: site-specific optimization and general domain optimization.

Location	Variability RMSE (m/s)	
	Site-specific optimization	General domain optimization
Morro Bay	0.5709	0.5723
Diablo Canyon	0.5523	0.5548
Humboldt	0.7240	0.7261

data from the single long-term WRF setup for year 2017. More in detail, the multivariate atmospheric state within the considered time window is compared with the atmospheric conditions modeled by the long-term WRF setup in all of the 3-hour time windows in 2017. For each hour in 2017, the AnEn calculates a similarity metric, formally defined as a multivariate Euclidean distance measure (Delle Monache et al., 2013):

$$\|F_t, A_{t'}\| = \sum_{i=1}^N \frac{\omega_i}{\sigma_i} \sqrt{\sum_{j=-1,0,1\text{h}} (F_{i,t+j} - A_{i,t'+j})^2}, \quad (2)$$

where  $F$  is the WRF-modeled atmospheric state at the search window centered at time,  $t$  (where  $t$  varies over the full 20-year period);  $A$  is the WRF-modeled atmospheric state over a window centered at time,  $t'$  (where  $t'$  varies in 2017);  $N$  is the number of atmospheric variables being considered to identify the analogs;  $\omega_i$  is the predictor weight associated with the atmospheric variable,  $i$ ; and  $\sigma_i$  is the standard deviation of the atmospheric variable,  $i$ , calculated over the search period.

Once the similarity metric is calculated for all of the hours ( $t'$ ) in 2017, the  $m$  analog hours with the highest similarity are selected to form the analog ensemble. Finally, the WRF-modeled across-ensemble 100-m wind speed standard deviation for each analog hour is considered. The average of these  $m$  values, normalized by the 100-m wind speed at that target hour from the single long-term WRF run, is then used as the AnEn extrapolated uncertainty to associate with the initial target hour. As previously mentioned, the AnEn approach is then repeated at each grid cell in the domain and target hour to generate a  $m$ -member ensemble forecast for the full long-term period.

The results from the AnEn approach are sensitive to the predictor weights,  $\omega_i$ , and the number of analog members,  $m$  (Junk et al., 2015; Alessandrini et al., 2019). Therefore, the AnEn approach first needs to be trained to determine the optimal values of these parameters, which maximize the accuracy of the AnEn predictions. In doing so, we use RMSE between 2017 AnEn-predicted and WRF-predicted wind speed uncertainty as the score metric for the optimization process. Training AnEn at each grid cell over our large domain is a computationally challenging task (Hu et al., 2021a). Therefore, we explore whether the same number of analogs and a single combination of optimized weights can be used over the whole domain. First, we perform a site-specific weight optimization at three sites, one for each wind energy lease area in the California OCS (Figure 1). Then, we alternatively tune a single combination of weights for all three sites, and we refer to this second approach as the general domain optimization. We compare the RMSE values from the two approaches in Table 3. At each site, the RMSE from the general domain optimization is only slightly higher (< 0.5% increase) than that from the much more expensive site-specific optimization. Therefore, we select the optimal number of analogs ( $m = 16$ , notably the same as the number of WRF ensemble

**Table 4.** Optimal weights associated with each physical variable in assessing the closeness of the match metric to identify the analogs.

Physical Variable	AnEn Weight
Wind speed at 100 m AGL	0.2
Wind direction at 100 m AGL	0.1
Temperature at 40 m AGL	0.1
Inverse of Obukhov length at 2 m AGL	0
Standard deviation of 100-m wind speed over preceding 6 hours	0.2
Standard deviation of 100-m wind speed over preceding 2 hours	0.2
Shear exponent calculated between 200 m and 10 m AGL	0.2

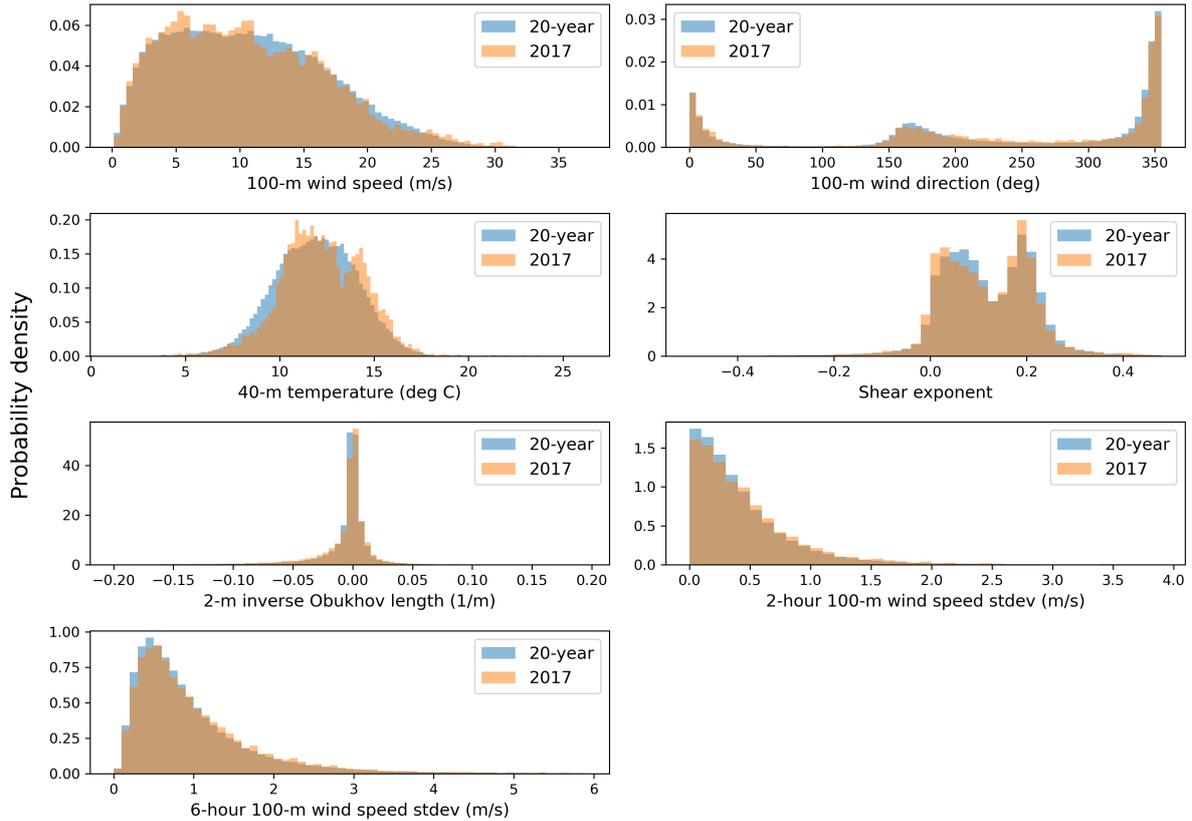
members) and weights resulting from the AnEn training at the three sites all together. The optimal weights are listed in Table 4.

## 210 3 Results

### 3.1 Validation of the proposed approaches

As a first step, we need to assess the accuracy and validity of our proposed approaches for the wind speed boundary condition and parametric uncertainty extrapolation. As an initial validation step, we compare the distributions of the atmospheric variables used as inputs to the machine-learning and AnEn algorithms for 2017 with what is found in the full 20-year period. In fact, in order for both approaches to be accurate, it is essential that the considered atmospheric variables in 2017 (i.e., where the models are trained) experience a range of variability representative of the full 20-year period (i.e., where the models are applied). By qualitatively comparing the distributions of the seven atmospheric variables at one of the three wind energy lease areas (Figure 3), the variability found in 2017 appears similar to what is found in the long-term 20-year period. To quantitatively confirm this, we apply a Levene’s test (Levene, 1961) to assess the equality of the variances of the two samples (2017 vs. 20-year period) for each atmospheric variable. We find that for all the seven variables, the null hypothesis of homogeneity of variance cannot be rejected (with  $p$ -values  $< 0.05$ ), thus confirming that it is highly unlikely that the variability found in 2017 is significantly different from the variability in the long term. Similar results are found at the two other wind energy lease areas (figures not shown).

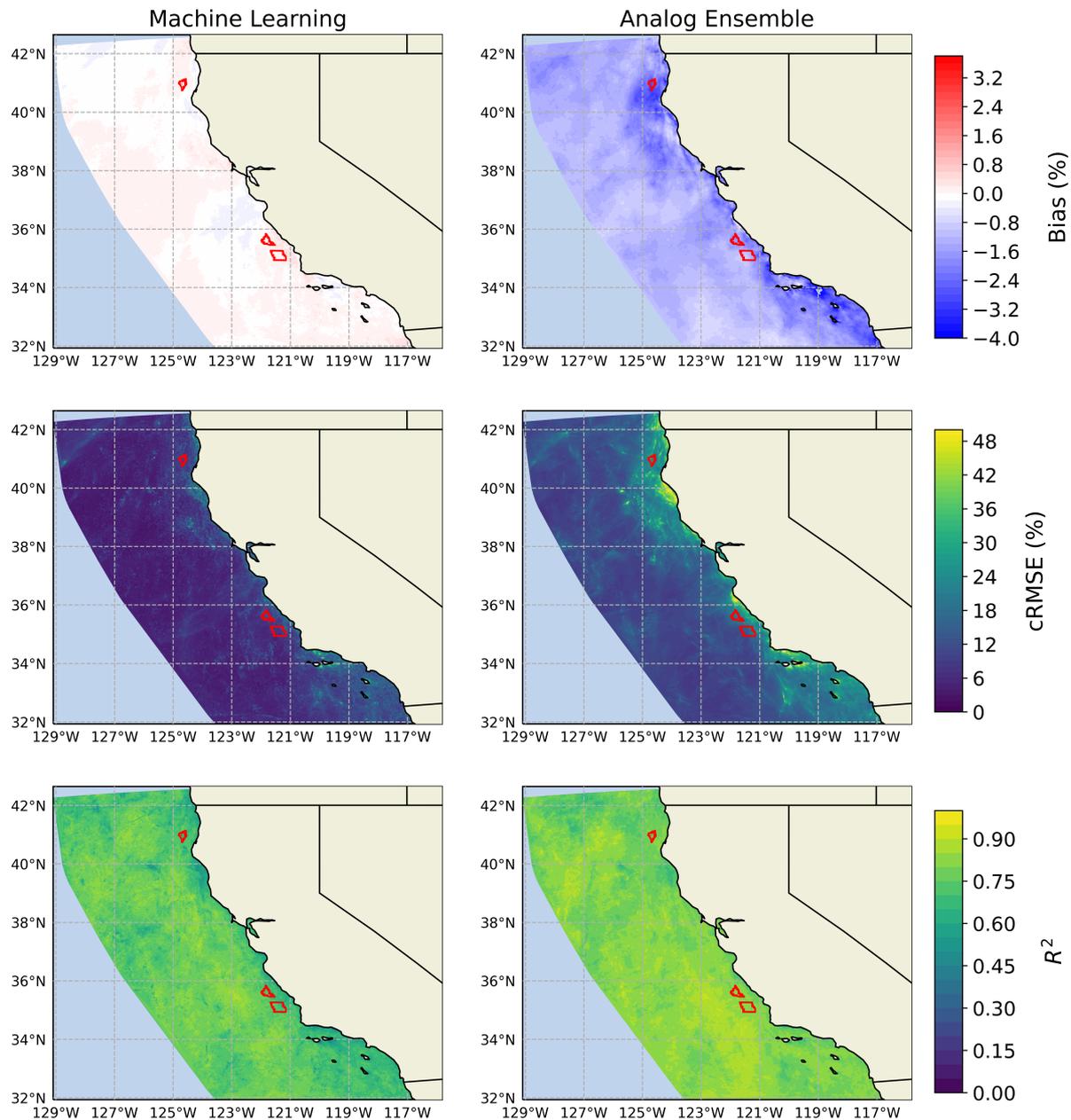
After proving that the basic assumptions of the proposed approaches are validated by the data, we need to test the accuracy of their predictions. To do so, at each grid cell we quantify the mean bias, centered or unbiased root-mean-square error (cRMSE), and coefficient of determination,  $R^2$ , between the machine-learning or AnEn predictions and the actual WRF ensemble variability. For the machine-learning approach, we calculate these error metrics over a testing set, obtained by training the learning algorithm on 80% of the 2017 data, and then testing it on the remaining 20%. To minimize the effects of the autocorrelation in the data, we select the testing set without shuffling the data. Also, to test the algorithm on the full seasonal variability of



**Figure 3.** Distributions of the atmospheric variables considered as inputs to the machine learning and AnEn algorithms from 2017 only and from the full 20-year period for a single site within the Humboldt wind energy lease area. Data are expressed in terms of their probability densities.

230 the atmospheric variables, we create the test set by selecting a contiguous 20% of data for each month in 2017. We compare these results with the three error metrics calculated when applying the AnEn approach, at each grid cell, for 2017. The maps of the various error metrics for the two approaches are shown in Figure 4. In general, the maps show how both approaches are capable of providing accurate predictions of the WRF boundary condition and parametric uncertainty across the whole off-shore domain. We find that the uncertainty predicted by the machine-learning model has a negligible bias (which is expressed as a percentage of the mean wind resource, the same as our normalized uncertainty metric) throughout the domain, whereas the uncertainty predictions from the AnEn approach are, on average, slightly lower than the WRF ensemble variability, with differences less than 3% at the three wind energy lease areas. The [bias-machine-learning approach also provides lower error after the bias is removed, especially closer to the coast, where the AnEn approach has local cRMSE values as high as 40%.](#) [On the other hand, we see that the AnEn approach provides a slightly stronger correspondence with the WRF data, with  \$R^2\$](#)

235



**Figure 4.** Map of testing bias, cRMSE, and  $R^2$  determination coefficient from the GBM model (left) and the AnEn approach (right). The wind energy lease areas are highlighted in red.

240 > 0.80 at the vast majority of the sites, whereas for the machine-learning model,  $R^2 > 0.75$ , with slightly lower values near the coast. The bias from the AnEn approach is likely because of the reduced length of the search period (1 year), which might be too limited for identifying a significant number (16) of analogs. This setup constrains the AnEn ability to account for rare

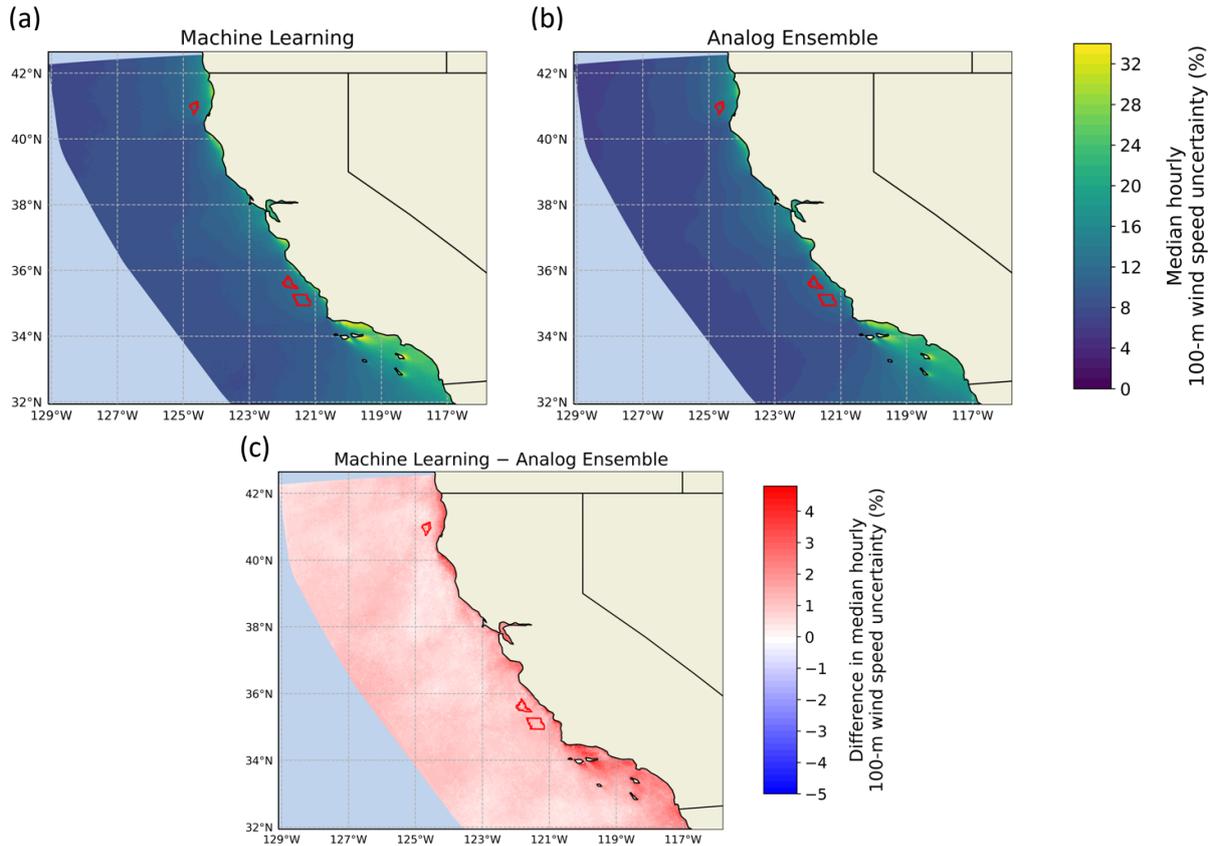
events (e.g., particularly high-wind-speed cases) when looking for similar atmospheric conditions in such a short repository. Applying the bias correction proposed in Alessandrini et al. (2019) or using a machine-learning similarity for analog definition (Hu et al., 2021b) would likely reduce the AnEn bias. The machine-learning approach also provides lower error after the bias is removed, especially closer to the coast, where the AnEn approach has local eRMSE values as high as 40%. On the other hand, we see that the AnEn approach provides a slightly stronger correspondence with the WRF data, with  $R^2 > 0.80$  similarity for analog definition (Hu et al., 2021b), or adopting a quantile mapping that uses quantiles of the analog ensemble instead of its mean (Sidel et al., 2020) would help reducing the AnEn bias, at the vast majority of the sites, whereas for the machine-learning model,  $R^2 > 0.75$ , with slightly lower values near the coast potential expense of computational costs.

### 3.2 Analysis of extrapolated wind speed boundary condition and parametric uncertainty

Now that the accuracy of both the proposed approaches has been assessed, we can analyze their long-term results. Figure 5 shows maps of the long-term median hourly boundary condition and parametric uncertainty for the 100-m wind speed predicted by the two proposed techniques, as well as the difference between the two. A strong agreement between the two approaches clearly emerges, with the AnEn approach predicting slightly lower values, as discussed from the analysis of the mean bias in Figure 4. In general, we find a larger uncertainty close to land, with values locally greater than 30% of the mean wind speed, whereas in open waters the median hourly uncertainty is smaller than 10% of the WRF-predicted wind speed. The difference between the median prediction from the two approaches also gets larger close to the land. For the current three wind energy lease areas in the region, the machine-learning approach quantifies a long-term median hourly uncertainty between 12% and 14% at all three sites. On the other hand, the AnEn approach provides slightly lower values, between 10% and 13%, again with little variability across the three sites.

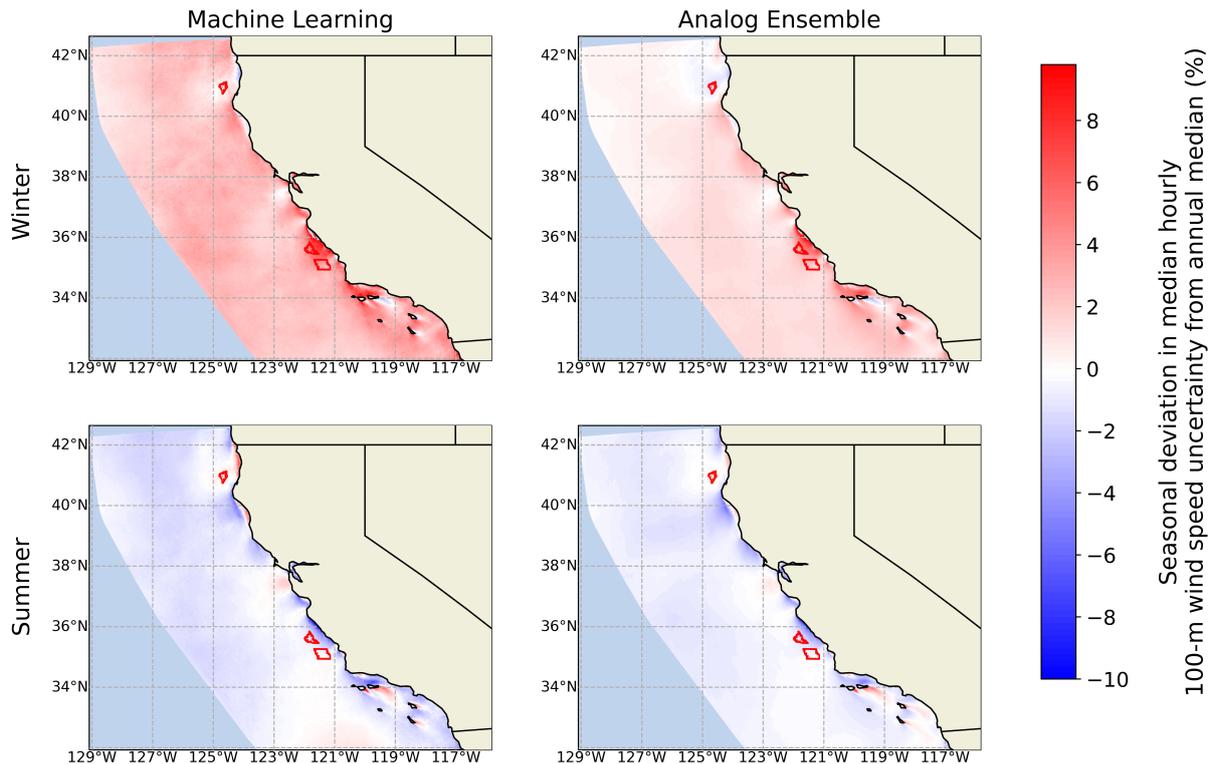
When focusing on offshore wind energy development, additional considerations are needed to understand how modeled wind speed uncertainty varies for the most relevant scenarios for energy production. When segregating data, having a long-term record allows for robust assessments of the variability among the considered classifications, which might otherwise have been much murkier when considering data from a short-term period only. Therefore, the twenty-fold increase of the size of the uncertainty data set provided by our proposed approaches brings an essential advantage to this direction.

Seasonality has a primary importance for the energy market, especially in a region such as California, with a strong peak in annual demand in summer, which recently led to detrimental rolling blackouts in the region. In this fragile scenario, assessing the uncertainty in the naturally varying long-term wind speed predictions could help assess the value that offshore wind energy can deliver to the California energy market, and achieve more accurate planning of the balance between supply and demand. Figure 6 compares maps of the seasonal deviation in median hourly normalized uncertainty for the 100-m wind speed in winter



**Figure 5.** Median hourly boundary condition and parametric uncertainty for the 100-m wind speed, as derived from the machine-learning approach (a), the analog ensemble (b), and the difference between the two (c).

(December, January, February) and summer (June, July and August). For each season, the values shown are the difference between the median hourly uncertainty for that specific season and the overall median value (i.e., what is shown in Figure 5). For most of the considered domain, we find a larger sensitivity in WRF-predicted wind speed in the winter months, with the  
 280 GBM showing a slightly larger seasonal deviation than the AnEn approach. At the Morro Bay and Diablo Canyon lease areas, the median winter uncertainty is between 2% and 8% larger than the annual median at the same locations. On the other hand, the Humboldt lease area shows a near-zero winter deviation, with the machine-learning approach predicting slightly increased winter uncertainty values, and AnEn predicting slightly negative ones. We find opposite results when considering the more energy-demanding summer months. Both Morro Bay and Diablo Canyon show a lower boundary condition and parametric  
 285 uncertainty in summer, with a difference from their annual median values smaller than 4%. On the other hand, negligible variability is observed at the Humboldt lease area. We note that spring and fall months displayed intermediate results when compared to summer and winter (figures not shown).

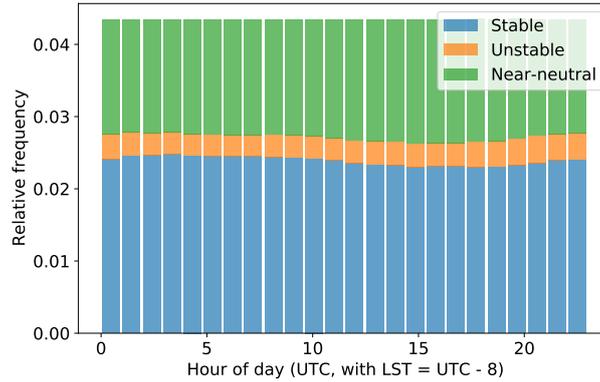


**Figure 6.** Seasonal deviation in median hourly normalized uncertainty in 100-m wind speed for winter (December, January, February) and summer (June, July and August), as derived from the machine learning approach (left) and the Analog Ensemble (right).

Finally, we quantify the impact of different stability regimes on the long-term wind speed uncertainty. Various approaches to classify atmospheric stability offshore have been proposed and applied offshore (e.g., Archer et al. (2016)), including the shape of the wind speed profile, the use of the Richardson number, and of turbulent kinetic energy. Here, we classify atmospheric stability based on the bulk Richardson number,  $Ri_B$ , calculated over the lowest 200 m, as done in Rybchuk et al. (2021) for the same data set:

$$Ri_B = \frac{g z_{200} (\theta_{200} - \theta_0)}{0.5 (\theta_{200} + \theta_0) WS_{200}^2} \quad (3)$$

where  $g = 9.81 \text{ m s}^{-2}$  is the acceleration caused by gravity,  $z_{200} = 200 \text{ m}$ ,  $\theta$  is potential temperature (K), and  $WS_{200}$  is the 200-m wind speed ( $\text{m s}^{-1}$ ). We consider stable conditions for  $Ri_B > 0.025$ , unstable conditions for  $Ri_B < -0.025$ , and near-neutral conditions otherwise. Figure 7 shows a histogram of the diurnal variability of the three stability regimes at the Humboldt wind energy lease area. We see a predominance of near-neutral and stable conditions, with a very weak diurnal variability. This is consistent with the sea surface temperature being generally colder than the near-surface air (because of ocean upwelling), which causes a predominantly stable stratification. Similar conditions are found at the other two wind energy lease areas. The maps in Figure 8 quantify how wind speed boundary condition and parametric uncertainty varies as a function of atmospheric

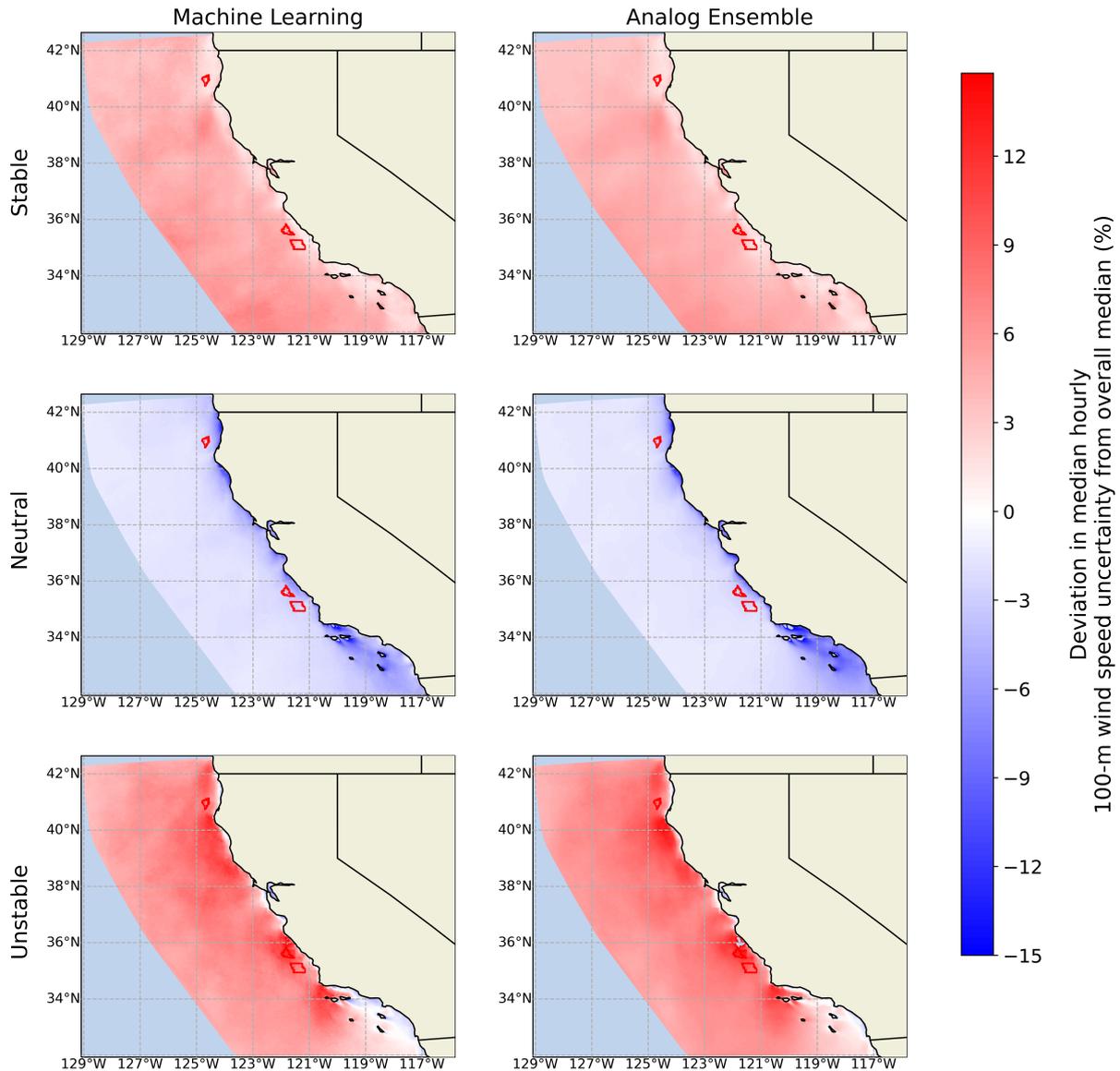


**Figure 7.** Daily distribution of atmospheric stability at the Humboldt wind energy lease area, as determined from the bulk Richardson number calculated over the lowest 200 m from the 20-year WRF simulation.

stability. For each atmospheric stability class, ~~the values shown are the~~ we show the difference between the median hourly uncertainty for that specific stability condition and the overall median value (i.e., what is shown in Figure 5). The proposed approaches show a remarkable agreement. Neutral conditions show the lowest boundary condition and parametric uncertainty. At the three wind energy lease areas, we find uncertainty values about 2%-4% lower than the overall median in near-neutral conditions. On the other hand, the rare unstable cases show the largest uncertainty, with deviations up to +10% from the median at the considered wind energy lease areas. Finally, stable conditions also show positive deviations in uncertainty throughout the considered domain, with differences on the order of +2-5% at the wind energy lease areas.

#### 4 Conclusions

As offshore wind energy becomes a widespread source of clean energy worldwide, the importance of having an accurate, long-term characterization of the offshore wind resource is crucial, not only in terms of its mean value, but also of the uncertainty associated with this estimate. In our analysis, we focused on the California Outer Continental Shelf (OCS), where a significant offshore wind energy development is expected in the near future, to propose innovative techniques to temporally extrapolate hub-height wind speed boundary condition and parametric uncertainty from a short-term ~~Weather Research and Forecasting (WRF) mesoscale numerical~~ ensemble to a long-term single ~~WRF model~~ run. First, we propose a gradient-boosting model algorithm, in which a regression model is trained over the short-term ~~WRF numerical~~ ensemble to predict its variability and then applied to the long-term single ~~WRF model~~ run. We compare this technique with an analog ensemble (AnEn) approach, wherein the extrapolated uncertainty for each time stamp in the long-term run is calculated by looking for similar atmospheric conditions within the short-term ~~WRF mesoscale numerical model~~ ensemble. Adopting our proposed approaches for uncertainty extrapolation helps save significant computational resources as the desired long-term boundary condition and parametric



**Figure 8.** Deviation in median hourly normalized uncertainty for the 100-m wind speed from the annual median, for different atmospheric stability regimes, as derived from the machine-learning approach (left) and the AnEn approach (right).

320 uncertainty information can be derived from a much simpler setup wherein the computationally expensive numerical ensembles are only run over a short-term period.

We find that both our proposed approaches agree well with the [WRF-mesoscale model](#) ensemble variability, thus providing a robust representation of the long-term wind speed boundary condition and parametric uncertainty. While AnEn has a slightly larger  $R^2$  coefficient with the [WRF-mesoscale model](#) across-ensemble data, we find that the gradient-boosting model has lower

325 bias and centered root-mean-square error. However, we expect the AnEn performance to improve if either the bias correction  
for rare events proposed in Alessandrini et al. (2019) or the quantile mapping approach presented in (Sidel et al., 2020) is  
incorporated in the analysis. In general, we find that the offshore wind speed boundary condition and parametric uncertainty  
increases near the coast, ~~especially for stable~~. While the accuracy of the AnEn approach significantly degrades near the coast,  
the larger values in hub-height wind speed boundary condition and parametric uncertainty near the coast were also seen from  
330 the variability among the WRF ensembles (Optis et al., 2020), and attributed to diverging wind profiles associated with the  
choice of PBL scheme under strong stable atmospheric conditions near the coastline. We also find that uncertainty is larger  
in stable and unstable conditions, lower in near-neutral cases. On average, the hourly uncertainty at the current three wind  
energy lease areas in the California OCS is between 10% and 14% of their mean hub-height wind speed. Summer months also  
experience lower uncertainty, which will benefit the energy planning in a season with a strong demand, which has, in the past,  
335 led to detrimental rolling blackouts.

Clearly, the magnitude of the boundary condition and parametric uncertainty component that we quantified in our analysis  
is strictly connected to the (limited) number of choices sampled within the considered model setups. Given this underdispersive  
behavior of the numerical weather prediction ensembles (Buizza et al., 2008; Alessandrini et al., 2013), we expect the  
uncertainty quantified from our ensemble to be lower than the model error with respect to measurements. Still, we note that  
340 the same caveat would apply if the uncertainty was directly quantified by running a long-term numerical ensemble, and thus  
the computational advantages of our proposed approaches still hold. Moreover, we emphasize how the choices made to build  
our numerical ensemble represent either state-of-the-art resources or the most widely accepted choices within the wind energy  
modeling community. Also, a quantification and temporal extrapolation of the full uncertainty in modeled wind speed would  
require concurrent observations (and the knowledge of the inherent uncertainty associated with them) to be computed. Given  
345 all these considerations, many opportunities exist to further expand our work. While floating lidars with publicly available data  
have only been deployed in the California OCS very recently (Gorton, 2020), a few lidars have been deployed off the U.S. East-  
ern Seaboard for more than 1 year. Observations from long-term offshore meteorological towers are also available in the North  
Sea in Europe. Our analysis could be expanded by first comparing the ~~WRF-related~~ model-related boundary condition and  
parametric uncertainty with the full modeled wind speed uncertainty calculated by comparing ~~WRF-modeled~~ data and obser-  
350 vations. Then, our proposed approaches could be expanded to temporally extrapolate the full modeled wind speed uncertainty;  
for example, quantified in terms of the variability of the residuals between modeled and observed wind. Testing additional  
input features to the algorithms could also help further improving the accuracy of the proposed extrapolation. Also, the site  
specificity of the proposed approaches would need to be investigated to understand if a learning model trained at a site e.g., one  
ocean basin) can still provide accurate predictions when applied at a different location. ~~Finally, analog-based techniques could~~  
355 Analog-based techniques could also be applied onshore, where the impact of more complex topography would likely need  
to be taken into account and incorporated in the algorithms. Finally, future work could focus on how interannual wind speed  
variability caused by climate change or long-term climatic and atmospheric oscillations (e.g., the North Atlantic oscillation)  
compares with the quantified uncertainty in modeled wind speed and how that should be taken into account for wind energy

360 development purposes. To facilitate this extension, we have included in the Supplementary Materials a map of the interannual variability in 100-m wind speed quantified from the 20-year WRF run.

*Code and data availability.* Data from the WRF simulations over the California OCS are available at <https://developer.nrel.gov/docs/wind/wind-toolkit/offshore-ca-download/>. The code for the considered machine-learning model is available at [https://github.com/nbodini/ML\\_UQ\\_offshore](https://github.com/nbodini/ML_UQ_offshore). The code for the AnEn approach is available at <https://weiming-hu.github.io/AnalogEnsemble>.

365 *Author contributions.* NB and MO envisioned the analysis. MO ran the numerical simulation. NB performed the machine-learning analysis, in close consultation with MO. WH performed the AnEn analysis, with the guidance of GC and SA. NB wrote the majority of the manuscript, with significant contributions and feedback from all coauthors.

*Competing interests.* The authors declare that they have no conflicts of interest.

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## References

- Alessandrini, S., Sperati, S., and Pinson, P.: A comparison between the ECMWF and COSMO Ensemble Prediction Systems applied to short-term wind power forecasting on real data, *Applied Energy*, 107, 271–280, <https://doi.org/https://doi.org/10.1016/j.apenergy.2013.02.041>, 2013.
- Alessandrini, S., Delle Monache, L., Sperati, S., and Cervone, G.: An analog ensemble for short-term probabilistic solar power forecast, *Applied Energy*, 157, 95–110, <https://doi.org/https://doi.org/10.1016/j.apenergy.2015.08.011>, 2015a.
- Alessandrini, S., Delle Monache, L., Sperati, S., and Nissen, J.: A novel application of an analog ensemble for short-term wind power forecasting, *Renewable Energy*, 76, 768–781, <https://doi.org/https://doi.org/10.1016/j.renene.2014.11.061>, 2015b.
- Alessandrini, S., Sperati, S., and Delle Monache, L.: Improving the analog ensemble wind speed forecasts for rare events, *Monthly Weather Review*, 147, 2677–2692, <https://doi.org/https://doi.org/10.1175/MWR-D-19-0006.1>, 2019.
- Archer, C. L., Colle, B. A., Delle Monache, L., Dvorak, M. J., Lundquist, J., Bailey, B. H., Beaucage, P., Churchfield, M. J., Fitch, A. C., Kosovic, B., et al.: Meteorology for coastal/offshore wind energy in the United States: Recommendations and research needs for the next 10 years, *Bulletin of the American Meteorological Society*, 95, 515–519, <https://doi.org/https://doi.org/10.1175/BAMS-D-13-00108.1>, 2014.
- Archer, C. L., Colle, B. A., Veron, D. L., Veron, F., and Sienkiewicz, M. J.: On the predominance of unstable atmospheric conditions in the marine boundary layer offshore of the US northeastern coast, *Journal of Geophysical Research: Atmospheres*, 121, 8869–8885, <https://doi.org/https://doi.org/10.1002/2016JD024896>, 2016.
- Arcos Jiménez, A., Gómez Muñoz, C., and García Márquez, F.: Machine learning for wind turbine blades maintenance management, *Energies*, 11, 13, <https://doi.org/https://doi.org/10.3390/en11010013>, 2018.
- Arrillaga, J. A., Yagüe, C., Sastre, M., and Román-Cascón, C.: A characterisation of sea-breeze events in the eastern Cantabrian coast (Spain) from observational data and WRF simulations, *Atmospheric Research*, 181, 265–280, <https://doi.org/https://doi.org/10.1016/j.atmosres.2016.06.021>, 2016.
- Bodini, N. and Optis, M.: The importance of round-robin validation when assessing machine-learning-based vertical extrapolation of wind speeds, *Wind Energy Science*, 5, 489–501, <https://doi.org/https://doi.org/10.5194/wes-5-489-2020>, 2020.
- Bodini, N., Lundquist, J. K., and Optis, M.: Can machine learning improve the model representation of turbulent kinetic energy dissipation rate in the boundary layer for complex terrain?, *Geoscientific Model Development*, 13, 4271–4285, <https://doi.org/https://doi.org/10.5194/gmd-13-4271-2020>, 2020.
- Brandily, Tifenn: Levelized Cost of Electricity 1H 2020: Renewable Chase Plunging Commodity Prices, Tech. rep., Bloomberg New Energy Finance Limited, <https://www.bnef.com/core/lcoe?tab=Forecast%20LCOE>, 2020.
- Brower, M.: *Wind Resource Assessment: A Practical Guide to Developing a Wind Project*, John Wiley & Sons, Hoboken, New Jersey, <https://doi.org/10.1002/9781118249864>, 2012.
- Buizza, R., Leutbecher, M., and Isaksen, L.: Potential use of an ensemble of analyses in the ECMWF Ensemble Prediction System, *Quarterly Journal of the Royal Meteorological Society: A journal of the atmospheric sciences, applied meteorology and physical oceanography*, 134, 2051–2066, <https://doi.org/https://doi.org/10.1002/qj.346>, 2008.
- Bureau of Ocean Energy Management: *Outer Continental Shelf Renewable Energy Leases Map Book*, Tech. rep., Bureau of Ocean Energy Management, [https://www.boem.gov/sites/default/files/renewable-energy-program/Mapping-and-Data/Renewable\\_Energy\\_Leases\\_Map\\_Book\\_March\\_2019.pdf](https://www.boem.gov/sites/default/files/renewable-energy-program/Mapping-and-Data/Renewable_Energy_Leases_Map_Book_March_2019.pdf), 2018.

- 410 Carbon Trust Offshore Wind Accelerator: Carbon Trust Offshore Wind Accelerator Roadmap for the Commercial Acceptance of Floating LiDAR Technology, Tech. rep., Carbon Trust, <https://prod-drupal-files.storage.googleapis.com/documents/resource/public/Roadmap%20for%20Commercial%20Acceptance%20of%20Floating%20LiDAR%20REPORT.pdf>, 2018.
- Carvalho, D., Rocha, A., Gómez-Gesteira, M., and Santos, C. S.: Sensitivity of the WRF model wind simulation and wind energy production estimates to planetary boundary layer parameterizations for onshore and offshore areas in the Iberian Peninsula, *Applied Energy*, 135, 234  
415 – 246, <https://doi.org/10.1016/j.apenergy.2014.08.082>, 2014a.
- Carvalho, D., Rocha, A., Gómez-Gesteira, M., and Silva Santos, C.: WRF wind simulation and wind energy production estimates forced by different reanalyses: Comparison with observed data for Portugal, *Applied Energy*, 117, 116 – 126, <https://doi.org/10.1016/j.apenergy.2013.12.001>, 2014b.
- Cervone, G., Clemente-Harding, L., Alessandrini, S., and Delle Monache, L.: Short-term photovoltaic power forecasting using Artificial Neural Networks and an Analog Ensemble, *Renewable Energy*, 108, 274–286, <https://doi.org/https://doi.org/10.1016/j.renene.2017.02.052>,  
420 2017.
- Clifton, A., Kilcher, L., Lundquist, J., and Fleming, P.: Using machine learning to predict wind turbine power output, *Environmental research letters*, 8, 024 009, <https://doi.org/https://doi.org/10.1088/1748-9326/8/2/024009>, 2013.
- Deepwater Wind: Block Island Wind Farm, URL <http://dwwind.com/project/block-island-wind-farm>, 2016.
- 425 Delle Monache, L., Eckel, F. A., Rife, D. L., Nagarajan, B., and Searight, K.: Probabilistic weather prediction with an analog ensemble, *Monthly Weather Review*, 141, 3498–3516, <https://doi.org/https://doi.org/10.1175/MWR-D-12-00281.1>, 2013.
- Donlon, C. J., Martin, M., Stark, J., Roberts-Jones, J., Fiedler, E., and Wimmer, W.: The operational sea surface temperature and sea ice analysis (OSTIA) system, *Remote Sensing of Environment*, 116, 140–158, <https://doi.org/https://doi.org/10.1016/j.rse.2010.10.017>, 2012.
- Fabre, S., Stickland, M., Scanlon, T., Oldroyd, A., Kindler, D., and Quail, F.: Measurement and simulation of the flow field  
430 around the FINO 3 triangular lattice meteorological mast, *Journal of Wind Engineering and Industrial Aerodynamics*, 130, 99–107, <https://doi.org/https://doi.org/10.1016/j.jweia.2014.04.002>, 2014.
- Friedman, J. H.: Stochastic gradient boosting, *Computational statistics & data analysis*, 38, 367–378, [https://doi.org/https://doi.org/10.1016/S0167-9473\(01\)00065-2](https://doi.org/https://doi.org/10.1016/S0167-9473(01)00065-2), 2002.
- Gelaro, R., McCarty, W., Suárez, M. J., Todling, R., Molod, A., Takacs, L., Randles, C. A., Darmenov, A., Bosilovich, M. G., Reichle, R.,  
435 et al.: The modern-era retrospective analysis for research and applications, version 2 (MERRA-2), *Journal of Climate*, 30, 5419–5454, <https://doi.org/https://doi.org/10.1175/JCLI-D-16-0758.1>, 2017.
- Gentine, P., Pritchard, M., Rasp, S., Reinaudi, G., and Yacalis, G.: Could machine learning break the convection parameterization deadlock?, *Geophysical Research Letters*, 45, 5742–5751, <https://doi.org/https://doi.org/10.1029/2018GL078202>, 2018.
- Gorton, A.: Atmosphere to Electrons (A2e). 2021. buoy/lidar.z06.00. Maintained by A2e Data Archive and Portal for U.S. Department of  
440 Energy, Office of Energy Efficiency and Renewable Energy, Tech. rep., Pacific Northwest National Lab.(PNNL), Richland, WA (United States), <https://doi.org/10.21947/1669352>, 2020.
- Hahmann, A. N., Vincent, C. L., Peña, A., Lange, J., and Hasager, C. B.: Wind climate estimation using WRF model output: method and model sensitivities over the sea, *International Journal of Climatology*, 35, 3422–3439, <https://doi.org/10.1002/joc.4217>, 2015.
- Hahmann, A. N., Sile, T., Witha, B., Davis, N. N., Dörenkämper, M., Ezber, Y., García-Bustamante, E., González Rouco, J. F., Navarro, J.,  
445 Olsen, B. T., and Söderberg, S.: The Making of the New European Wind Atlas, Part 1: Model Sensitivity, *Geoscientific Model Development Discussions*, 2020, 1–33, <https://doi.org/10.5194/gmd-2019-349>, 2020.

- Hersbach, H., Bell, B., Berrisford, P., Hirahara, S., Horányi, A., Muñoz-Sabater, J., Nicolas, J., Peubey, C., Radu, R., Schepers, D., et al.: The ERA5 global reanalysis, *Quarterly Journal of the Royal Meteorological Society*, 146, 1999–2049, <https://doi.org/https://doi.org/10.1002/qj.3803>, 2020.
- 450 Holstag, E.: Improved Bankability, The Ecofys position on Lidar Use, Ecofys report, 2013.
- Hong, S.-Y., Noh, Y., and Dudhia, J.: A new vertical diffusion package with an explicit treatment of entrainment processes, *Monthly Weather Review*, 134, 2318–2341, <https://doi.org/https://doi.org/10.1175/MWR3199.1>, 2006.
- Hu, W., Cervone, G., Clemente-Harding, L., and Calovi, M.: Parallel Analog Ensemble –The Power Of Weather Analogs, NCAR Technical Notes NCAR/TN-564+ PROC, p. 1, <https://doi.org/doi:10.5065/P2JJ-9878>, 2021a.
- 455 Hu, W., Cervone, G., Young, G., and Monache, L. D.: Weather Analogs with a Machine Learning Similarity Metric for Renewable Resource Forecasting, arXiv preprint arXiv:2103.04530, 2021b.
- JCGM 100:2008: Evaluation of measurement data — Guide to the expression of uncertainty in measurement, Joint Committee for Guides in Metrology, 2008.
- Johnson, C., White, E., and Jones, S.: Summary of Actual vs. Predicted Wind Farm Performance: Recap of WINDPOWER 2008, in: AWEA Wind Resource and Project Energy Assessment Workshop, [http://www.enecafe.com/interdomain/idlidar/paper/2008/AWEA%20workshop%202008%20Johnson\\_Clint.pdf](http://www.enecafe.com/interdomain/idlidar/paper/2008/AWEA%20workshop%202008%20Johnson_Clint.pdf), 2008.
- 460 Junk, C., Delle Monache, L., Alessandrini, S., Cervone, G., and Von Bremen, L.: Predictor-weighting strategies for probabilistic wind power forecasting with an analog ensemble, *Meteorologische Zeitschrift*, 24, 361–379, <https://doi.org/https://doi.org/10.1127/metz/2015/0659>, 2015.
- 465 Kirincich, A.: A Metocean Reference Station for offshore wind Energy research in the US, in: *Journal of Physics: Conference Series*, vol. 1452, p. 012028, IOP Publishing, <https://doi.org/https://doi.org/10.1088/1742-6596/1452/1/012028>, 2020.
- Levene, H.: Robust tests for equality of variances, *Contributions to probability and statistics. Essays in honor of Harold Hotelling*, pp. 279–292, <https://doi.org/https://doi.org/10.2307/2285659>, 1961.
- Mattar, C. and Borvarán, D.: Offshore wind power simulation by using WRF in the central coast of Chile, *Renewable energy*, 94, 22–31, <https://doi.org/https://doi.org/10.1016/j.renene.2016.03.005>, 2016.
- 470 Murphy, J. M., Sexton, D. M., Barnett, D. N., Jones, G. S., Webb, M. J., Collins, M., and Stainforth, D. A.: Quantification of modelling uncertainties in a large ensemble of climate change simulations, *Nature*, 430, 768–772, <https://doi.org/https://doi.org/10.1038/nature02771>, 2004.
- Musial, W., Heimiller, D., Beiter, P., Scott, G., and Draxl, C.: Offshore wind energy resource assessment for the United States, Tech. rep., National Renewable Energy Laboratory (NREL), Golden, CO (United States), <https://www.nrel.gov/docs/fy16osti/66599.pdf>, 2016.
- 475 Nakanishi, M. and Niino, H.: An improved Mellor–Yamada level-3 model with condensation physics: Its design and verification, *Boundary-Layer Meteorology*, 112, 1–31, <https://doi.org/https://doi.org/10.1023/B:BOUN.0000020164.04146.98>, 2004.
- Neumann, T., Nolopp, K., and Herklotz, K.: First operating experience with the FINO1 research platform in the North Sea; Erste Betriebserfahrungen mit der FINO1-Forschungsplattform in der Nordsee, *DEWI-Magazin*, 2004.
- 480 Niu, G.-Y., Yang, Z.-L., Mitchell, K. E., Chen, F., Ek, M. B., Barlage, M., Kumar, A., Manning, K., Niyogi, D., Rosero, E., et al.: The community Noah land surface model with multiparameterization options (Noah-MP): 1. Model description and evaluation with local-scale measurements, *Journal of Geophysical Research: Atmospheres*, 116, <https://doi.org/https://doi.org/10.1029/2010JD015139>, 2011.
- OceanTech Services/DNV GL: NYSERDA Floating Lidar Buoy Data, <https://oswbuoysny.resourcepanorama.dnvgil.com>, 2020.

- Olsen, B. T., Hahmann, A. N., Sempreviva, A. M., Badger, J., and Jørgensen, H. E.: An intercomparison of mesoscale models at simple sites  
485 for wind energy applications, *Wind Energy Science*, 2, 211–228, <https://doi.org/10.5194/wes-2-211-2017>, 2017.
- Optis, M. and Perr-Sauer, J.: The importance of atmospheric turbulence and stability in machine-learning models of wind farm power  
production, *Renewable and Sustainable Energy Reviews*, 112, 27–41, <https://doi.org/https://doi.org/10.1016/j.rser.2019.05.031>, 2019.
- Optis, M., Rybchuk, O., Bodini, N., Rossol, M., and Musial, W.: 2020 Offshore Wind Resource Assessment for the California Pacific Outer  
490 Continental Shelf, Tech. rep., National Renewable Energy Laboratory (NREL), Golden, CO (United States), <https://www.nrel.gov/docs/fy21osti/77642.pdf>, 2020.
- Optis, M., Bodini, N., Debnath, M., and Doubrawa, P.: New methods to improve the vertical extrapolation of near-surface offshore wind  
speeds, 6, 935–948, <https://doi.org/https://doi.org/10.5194/wes-6-935-2021>, 2021a.
- Optis, M., Kumler, A., Brodie, J., and Miles, T.: Quantifying sensitivity in numerical weather prediction-modeled offshore wind speeds  
through an ensemble modeling approach, *Wind Energy*, <https://doi.org/https://doi.org/10.1002/we.2611>, 2021b.
- 495 Papanastasiou, D., Melas, D., and Lissaridis, I.: Study of wind field under sea breeze conditions; an application of WRF model, *Atmospheric  
Research*, 98, 102–117, <https://doi.org/https://doi.org/10.1016/j.atmosres.2010.06.005>, 2010.
- Parker, W. S.: Ensemble modeling, uncertainty and robust predictions, *Wiley Interdisciplinary Reviews: Climate Change*, 4, 213–223,  
<https://doi.org/https://doi.org/10.1002/wcc.220>, 2013.
- Peña, A., Floors, R., and Gryning, S.-E.: The Høvsøre tall wind-profile experiment: a description of wind profile observations in the atmo-  
500 spheric boundary layer, *Boundary-layer meteorology*, 150, 69–89, <https://doi.org/https://doi.org/10.1007/s10546-013-9856-4>, 2014.
- Ruiz, J. J., Saulo, C., and Nogués-Paegle, J.: WRF Model Sensitivity to Choice of Parameterization over South America: Validation against  
Surface Variables, *Monthly Weather Review*, 138, 3342–3355, <https://doi.org/10.1175/2010MWR3358.1>, 2010.
- Rybchuk, A., Optis, M., Lundquist, J. K., Rossol, M., and Musial, W.: A Twenty-Year Analysis of Winds in Califor-  
nia for Offshore Wind Energy Production Using WRF v4. 1.2, *Geoscientific Model Development Discussions*, pp. 1–41,  
505 <https://doi.org/https://doi.org/10.5194/gmd-2021-50>, 2021.
- Salvação, N. and Soares, C. G.: Wind resource assessment offshore the Atlantic Iberian coast with the WRF model, *Energy*, 145, 276–287,  
<https://doi.org/https://doi.org/10.1016/j.energy.2017.12.101>, 2018.
- Sidel, A., Hu, W., Cervone, G., and Calovi, M.: Heat Wave Identification Using an Operational Weather Model and Analog Ensemble, in:  
100th American Meteorological Society Annual Meeting, <https://ams.confex.com/ams/2020Annual/meetingapp.cgi/Paper/371727>, 2020.
- 510 Siuta, D., West, G., and Stull, R.: WRF Hub-Height Wind Forecast Sensitivity to PBL Scheme, Grid Length, and Initial Condition Choice in  
Complex Terrain, *Weather and Forecasting*, 32, 493–509, <https://doi.org/10.1175/WAF-D-16-0120.1>, 2017.
- Skamarock, W. C., Klemp, J. B., Dudhia, J., Gill, D. O., Barker, D. M., Duda, M. G., Huang, X.-Y., Wang, W., and Powers, J. G.: A De-  
scription of the Advanced Research WRF Version 3, Tech. Rep. NCAR/TN-475+STR, Mesoscale and Microscale Meteorology Division,  
National Center for Atmospheric Research, Boulder, Colorado, USA, <https://doi.org/10.5065/D68S4MVH>, 2008.
- 515 Steele, C., Dorling, S., Glasow, R. v., and Bacon, J.: Idealized WRF model sensitivity simulations of sea breeze types and their effects on  
offshore windfields, *Atmospheric Chemistry and Physics*, 13, 443–461, <https://doi.org/https://doi.org/10.5194/acp-13-443-2013>, 2013.
- Stiesdal, H.: Midt i en disruptionstid, IngeniÅren, <https://ing.dk/blog/midt-disruptionstid-190449>, 2016.
- Truepower, A.: AWS Truepower Loss and Uncertainty Methods, Albany, NY, [https://www.awstruepower.com/assets/  
AWS-Truepower-Loss-and-Uncertainty-Memorandum-5-Jun-2014.pdf](https://www.awstruepower.com/assets/AWS-Truepower-Loss-and-Uncertainty-Memorandum-5-Jun-2014.pdf), 2014.

- 520 Ulazia, A., Saenz, J., and Ibarra-Berastegui, G.: Sensitivity to the use of 3DVAR data assimilation in a mesoscale model for estimating offshore wind energy potential. A case study of the Iberian northern coastline, *Applied Energy*, 180, 617 – 627, <https://doi.org/10.1016/j.apenergy.2016.08.033>, 2016.
- van Hoof, J.: Unlocking Europe’s offshore wind potential, Tech. rep., PricewaterhouseCoopers B.V., <https://www.pwc.nl/nl/assets/documents/pwc-unlocking-europes-offshore-wind-potential.pdf>, 2017.
- 525 Vanvyve, E., Delle Monache, L., Monaghan, A. J., and Pinto, J. O.: Wind resource estimates with an analog ensemble approach, *Renewable Energy*, 74, 761–773, <https://doi.org/https://doi.org/10.1016/j.renene.2014.08.060>, 2015.
- White, E.: Continuing Work on Improving Plant Performance Estimates, in: AWEA Wind Resource and Project Energy Assessment Workshop, 2008.
- Xingjian, S., Chen, Z., Wang, H., Yeung, D.-Y., Wong, W.-K., and Woo, W.-C.: Convolutional LSTM network: A machine learning approach  
530 for precipitation nowcasting, in: *Advances in Neural Information Processing Systems*, pp. 802–810, 2015.
- Zhu, Y.: Ensemble forecast: A new approach to uncertainty and predictability, *Advances in Atmospheric Sciences*, 22, 781–788, <https://doi.org/https://doi.org/10.1007/BF02918678>, 2005.