Large-eddy Simulation of a Wind-turbine Array subjected to Active Yaw Control

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Abstract. This study validates the large-eddy simulation (LES) ~~technique for the prediction of the~~ for predicting the flow through a wind turbine array subjected to active yaw control. The wind turbine array consists of three miniature wind turbines operated in both non-yawed and yawed configurations under full-wake and partial-wake conditions, for which wind tunnel flow measurements are available. The turbine-induced forces are parametrised by three different models: the standard actuator disk model (ADM-std), the blade element actuator disk model (ADM-BE), also referred to as the rotational actuator disk model (ADM-R), and the actuator line model (ALM). The time-averaged turbine power outputs and the profiles of the wake flow statistics (normalised streamwise mean velocity and streamwise turbulence intensity) obtained from the simulations using the ADM-std, the ADM-BE and the ALM are compared with experimental results. We find that simulations using the ADM-BE and ALM yield flow statistics that are in good agreement with the wind-tunnel measurements for all the studied configurations. In contrast, the results from LES with the ADM-std show discrepancies with the measurements under yawed and/or partial-wake conditions. These errors are due to the fact that the ADM-std assumes a uniform thrust force, thus failing to capture the inherently ~~non-uniform~~ inhomogeneous distribution of the turbine-induced forces under partial wake conditions. In terms of power prediction, we find that LES using the ADM-BE yields better power ~~prediction~~ predictions than the ADM-std and the ALM in ~~both non-yawed and yawed conditions~~ the cases considered in this study. As a result, we conclude that LES using the ADM-BE provides a good balance of accuracy and computational cost for the simulations of the flow through wind farms subjected to AYC.

1 Introduction

As an indispensable part of the global transition to carbon neutrality, wind power has experienced a rapid growth worldwide in the past decades (GWEC, 2021). The majority of the wind power projects are developed in the form of wind farms, i.e., a cluster of wind turbines installed within a designated area, outputting the generated electricity to centralised substations before transmitting it to the grid. ~~In comparison~~ Compared with distributed wind power, which consists of ~~the installation of~~ installing stand-alone turbines in different locations, developing wind energy in wind farms has many advantages, such as reducing the construction and maintenance overhead per turbine. On the other hand, wind turbines in wind farms often encounter ~~the phenomenon of~~ wake interference, i.e., wind turbines are exposed to the wakes of upwind turbines. This phenomenon can cause significant power losses and increase fatigue loads, and it has become the subject of many studies of wind farm flows (Barthelmie and Jensen, 2010; Archer et al., 2018; Porté-Agel et al., 2020). Active yaw control (AYC), or active wake steering, is a ~~novel~~ wake-interference mitigation strategy that is drawing increasing interest in the research community. In this strategy, the upwind wind turbines are intentionally yawed to deflect their wakes away from downwind turbines. With a proper yawed configuration, the reduced power outputs in the yawed upwind turbines can be compensated by the increased power output in the downwind turbines. Therefore, a net power gain in the entire wind farm can be achieved.

Various early studies (Grant et al., 1997; Grant and Parkin, 2000) have revealed that the characteristics of the wake of a yawed turbine are significantly different from its non-yawed counterpart. Most notably, the yawed wake is deflected to the downwind-inclined side of the rotor. ~~? first~~

Medici and Alfredsson (2006) indicated the potential of exploiting this phenomenon to optimise wind farm power using active yaw control, and he validated this concept with wind tunnel experiments. Since then, there has been a push in the wind energy community towards understanding the wake characteristics of yawed turbines. Jiménez et al. (2010) first derived an analytical wake model based on the top-hat velocity profile as an extension to the well-known Jensen wake model (Jensen, 1983) for non-yawed turbines. Bastankhah and Porté-Agel (2016) performed a wind tunnel study of a yawed miniature wind turbine in a turbulent boundary layer flow, and they found that the time-averaged profiles of the velocity deficit and the wake skew angle are Gaussian and self-similar in the far wake region. Exploiting this phenomenon, they developed a closed-form analytical model for the velocity deficit profiles of yawed turbines. Comparing with the top-hat Jimenez model, they found that the Gaussian model results are in better agreement with the measurements. Zong and Porté-Agel (2020a) developed a momentum-conserving method to superpose the wake velocity deficits behind multiple yawed turbines. Qian and Ishihara (2018) developed a bi-Gaussian parametric model for the turbulence intensity distribution in the wake of a yawed turbine. In a follow-up study, Qian and Ishihara (2021) also proposed a superposition model for predicting turbulence intensity in the wakes of multiple yawed turbines. The Qian and Ishihara model is based on the principle of the linear sum of squares of the added turbulence intensity, and it introduces a parametric correction for partial-wake scenarios.

Another distinctive feature of the wake of a yawed turbine is the formation of a counter-rotating vortex pair (CVP), which is induced by the lateral forces applied by the yawed turbine. Howland et al. (2016) carried out wind tunnel experiments on a yawed permeable disk in laminar inflows. They found that the permeable disk's wake is significantly asymmetrical, or "curled", in the spanwise direction. The ~~curled wake is deformed by the~~ presence of the CVP deforms the curled wake. Bastankhah and Porté-Agel (2016) also observed the CVP in the wind tunnel study of a yawed miniature wind turbine immersed in a turbulent boundary-layer flow. The curled wake pattern can sustain itself beyond the near-wake region and can still be observed at the location where a downwind turbine can be installed. Motivated by these experimental results, researchers made several efforts to incorporate the physics of the CVP in yawed wake modelling. Shapiro et al. (2018) treated the yawed turbine as a surface with an elliptic vorticity distribution and used lifting line theory to model the CVP formation. Based on the vorticity distribution proposed by Shapiro et al. (2018), Martínez-Tossas et al. (2019) developed a curled-wake model by solving the linearised Euler equations. King et al. (2021) derived an analytical approximation of the model of Martínez-Tossas et al. (2019) and formulated a reduced-order curled wake model that is computationally efficient. Zong and Porté-Agel (2020b) investigated the physics of the CVP in wind tunnel experiments and developed a point-vortex transportation model that reproduces the formation mechanism of the top-down asymmetric kidney-shaped wake behind a yawed turbine.

Besides experimental and theoretical approaches, numerical modelling is also a popular approach among researchers studying AYC. Large-eddy simulation (LES), due to its relatively high fidelity, is widely used to investigate wind turbine wakes. In LES, the turbine-induced forces can be represented by three main ~~types of~~ models. Jiménez et al. (2010) first used a standard actuator disk model (ADM-std), which assumes a uniform distribution of the thrust force on the rotor disk, to parametrise the yawed turbine-induced forces in LES. The ADM-std was also adopted by other researchers studying the wakes of multiple turbines (Munters and Meyers, 2018; Stevens et al., 2018; Boersma et al., 2019). As an ~~improvment~~ improvement to the ADM-std, the blade element actuator disk model (ADM-BE), also referred to as the rotational actuator disk model (ADM-R), is proposed by Wu and Porté-Agel (2011) and Porté-Agel et al. (2011), which uses the blade element theory to parametrise the non-uniform thrust and tangential forces on the turbine rotor in LES. The ADM-BE was later applied by Fleming et al. (2018) to study the large-scale trailing vortices in yawed wind turbine wakes. The actuator line model (ALM), proposed by Sørensen and Shen (2002), is also a widely used method in LES studies of yawed turbines (Fleming et al., 2016; Wang et al., 2017; Stevens et al., 2018; Archer and Vasel-Be-Hagh, 2019). The ALM parametrises the rotor-induced forces on line elements distributed along each blade. Unlike LES using the ADM, LES using the ALM can produce the tip vortices in the near wake region. However, LES using the ALM also requires higher temporal and spatial resolution than the ADM counterpart (Martínez-Tossas et al., 2017), thus consuming substantially more computational resources.

Lin and Porté-Agel (2019) have previously validated an LES framework using the ADM-BE to simulate the wake of a stand-alone wind turbine subjected to AYC. Since the ultimate goal of AYC is to be applied to wind farms, it is natural to extend the validation to multiple turbines. This study compares the results of LES using different turbine parametrisations (ADM-std, ADM-BE and ALM) with wind tunnel measurements of a three-turbine array (Zong and Porté-Agel, 2021) in different turbine layouts and yawed configurations.

The rest of the paper is structured as follows: ~~Section~~ Sec. 2 discusses the numerical configurations used in the simulations and the methodology for evaluating the power output. ~~Section~~ Sec. 3 presents the simulation results obtained from LES using different turbine parametrisations and compares them with wind tunnel measurements. ~~Section~~ Sec. 4 presents the conclusions drawn from these results and discusses the possible extension of this work.

2   Methodology

2.1   Governing equations

A GPU-accelerated version of the WiRE-LES code is used in this study. The code has been developed at the Wind Engineering and Renewable Energy Laboratory (WiRE) of the École Polytechnique Fédérale de Lausanne (EPFL), and it has been used and validated in previous studies of wind turbine wakes, e.g., in Wu and Porté-Agel (2011), Porté-Agel et al. (2011), Abkar and Porté-Agel (2015) and Lin and Porté-Agel (2019).

The WiRE-LES solves the spatially filtered incompressible Navier-Stokes (N-S) equations:

$$\frac{\partial \widetilde{u}_i}{\partial x_i} = 0,$$

$$\frac{\partial \widetilde{u}_i}{\partial t} + \widetilde{u}_j \left(\frac{\partial \widetilde{u}_i}{\partial x_j} - \frac{\partial \widetilde{u}_j}{\partial x_i} \right) = -\frac{\partial \widetilde{p}^*}{\partial x_i} - \frac{\partial \tau_{ij}}{\partial x_j} - \frac{f_i}{\rho} + \frac{F_p}{\rho} \delta_{i1}, \tag{1}$$

in which $\widetilde{u}_i$ is the spatially filtered velocity ($i = 1, 2, 3$ representing the streamwise, spanwise and vertical directions, respectively); $\widetilde{p}^*$ is the modified kinematic pressure; f_i is the body force exerted by the wind turbine on the flow; F_p is the pressure gradient imposed to drive the flow; $\tau_{ij} = \widetilde{u_i u_j} - \widetilde{u}_i \widetilde{u}_j$ is the kinematic sub-grid scale (SGS) stress, and it is parametrised using the modulated gradient model (MGM) proposed by Lu and Porté-Agel (2010):

$$\tau_{ij} = 2k_{sgs} \left(\frac{\tilde{G}_{ij}}{\tilde{G}_{kk}} \right), \tag{2}$$

in which $\tilde{G}_{ij}$ is defined as follow:

$$\tilde{G}_{ij} = \frac{\tilde{\Delta}_x^2}{12} \frac{\partial \tilde{u}_i}{\partial x} \frac{\partial \tilde{u}_j}{\partial x} + \frac{\tilde{\Delta}_y^2}{12} \frac{\partial \tilde{u}_i}{\partial y} \frac{\partial \tilde{u}_j}{\partial y} + \frac{\tilde{\Delta}_z^2}{12} \frac{\partial \tilde{u}_i}{\partial z} \frac{\partial \tilde{u}_j}{\partial z}, \tag{3}$$

k_{sgs} is the zero-clipped SGS kinetic energy:

$$k_{sgs} = \mathbf{1}_{\tilde{G}_{ij}\tilde{S}_{ij} < 0}(\tilde{G}_{ij}\tilde{S}_{ij}) \frac{4\tilde{\Delta}^2}{C_\epsilon^2} \left(-\frac{\tilde{G}_{ij}}{\tilde{G}_{kk}} \tilde{S}_{ij} \right)^2, \tag{4}$$

in which $\mathbf{1}_{\tilde{G}_{ij}\tilde{S}_{ij} < 0}(\tilde{G}_{ij}\tilde{S}_{ij})$ is an indicator function taking the value of 1 if $\tilde{G}_{ij}\tilde{S}_{ij} < 0$ and 0 if $\tilde{G}_{ij}\tilde{S}_{ij} \geq 0$; $\tilde{S}_{ij}$ is the filtered strain rate; $\tilde{\Delta}$ is defined as $\sqrt[3]{\tilde{\Delta}_x \tilde{\Delta}_y \tilde{\Delta}_z}$, in which $\tilde{\Delta}_x$, $\tilde{\Delta}_y$ and $\tilde{\Delta}_z$ are the filter widths in the streamwise, spanwise and vertical directions. $C_\epsilon = 1.6$ is the model coefficient obtained from the simulations of the ABL flow using dynamic procedures (Lu and Porté-Agel, 2014).

2.2   Wind turbine parametrisation

In the WiRE-LES, three different types of wind turbine parametrisation are implemented (Fig. 1): the ADM-std, the ADM-BE and the ALM. In the ADM-std, a wind turbine is modelled as a permeable disk with thrust forces uniformly distributed within the rotor diameter. The magnitude of the thrust force is computed as:

$$F_x = \frac{1}{2} \rho A C_T U_{in}^2, \tag{5}$$

in which ρ is the air density; A is the sweeping area of the rotor disk; C_T is the thrust coefficient of the wind turbine, and U_{in} is the incoming wind speed. Since the turbines in wind farms often operate in the wakes of upwind turbines, their incoming velocities are retrieved as ~~follow:~~ follows:

$$U_{in} = U_{loc}/(1 - a)U_{loc}, \tag{6}$$

in which U_{loc} is the local disk-averaged velocity at the rotor, and a is the induction factor estimated from the thrust coefficient:

$$a = \frac{1}{2}(1 - \sqrt{1 - C_T}). \tag{7}$$

Using the reconstructed inflow velocity, we update the thrust coefficient and the power coefficient of the turbine by interpolating the thrust and power curves of the WiRE-01 miniature wind turbine (Bastankhah and Porté-Agel, 2016).
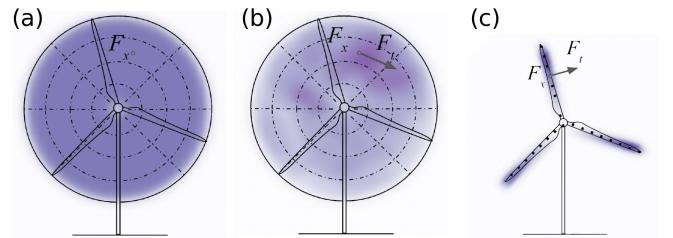
Figure 1. Schematic representation of the three wind turbine parametrisations used in WiRE-LES: (a) the ADM-std; (b) the ADM-BE; (c) the ALM. To illustrate the differences in the distribution of the forces computed using the three models, the normalised contours of the instantaneous force distribution (normalised by the respective maximum value) induced by each model are plotted.

In the ADM-BE, the turbine-induced forces are parametrised using the blade element theory. In contrast with the ADM-std, the forces in the ADM-BE are computed from the local velocity information and the aerodynamic properties of each blade element. As a result, the forces are non-uniform across the rotor. Furthermore, the ADM-BE ~~not only~~ takes the thrust forces into account ~~but also~~ and models the tangential forces on the rotor. As a result, the ADM-BE introduces wake rotation in the wake of a turbine. After subdividing the rotor into an axisymmetric

grid, the ADM-BE computes the local thrust force F_x and the local tangential force F_t as ~~follow~~follows:

$$F_x = \frac{1}{2}\rho U_{ref}^2 c\sigma\Phi(C_L\cos(\phi) + C_D\sin(\phi)),$$
$$F_t = \frac{1}{2}\rho U_{ref}^2 c\sigma\Phi(C_D\cos(\phi) - C_L\sin(\phi)),$$

(8)

in which U_{ref} is the resultant inflow velocity at a given blade section; c is the chord length, and σ is the solidity of the blade section; Φ is the Prantl tip-loss correction factor; ϕ is the angle between the relative axial and the tangential velocity components at the blade element; C_L and C_D are the lift and drag coefficients interpolated from a 2D tabular dataset (Revaz et al., 2020) using the angle of attack (AoA) at a given blade element. A more detailed description of the ADM-BE and its application in yawed turbines can be found in Wu and Porté-Agel (2011) and Lin and Porté-Agel (2019).

The ALM computes the turbine-induced forces on line elements distributed on the moving turbine blades. The normal and the tangential forces on each source point are also computed from the blade element theory:

$$F_x = \frac{1}{2}\rho U_{ref}^2 cw\Phi(C_L\cos(\phi) + C_D\sin(\phi)),$$
$$F_t = \frac{1}{2}\rho U_{ref}^2 cw\Phi(C_D\cos(\phi) - C_L\sin(\phi)).$$

(9)

Notice that the solidity σ in the ADM-BE equations ~~are~~ is replaced by the width of the blade sections w in the ALM equations.

2.3 Case configuration

In this study, four simulation cases are set up to reproduce the boundary-layer wind tunnel experiments of a wind turbine array subjected to active yaw control described by Zong and Porté-Agel (2021). The wind turbine array consists of three WiRE-01 miniature wind turbines. The diameter of the turbine $D = 0.15$ m, and the hub height $Z_{hub} = 0.125$ m. Each turbine is separated from the closest neighbouring turbines by a constant distance $S_x = 5D$ in the streamwise direction.

The configurations of the cases are ~~summarized~~ summarised in Table 1. In Cases 1 and 2, the turbine rotor locations are aligned in the streamwise direction (i.e., lateral offset $S_y = 0D$), while a lateral offset $S_y = D/3$ is applied in Cases 3 and 4. In Cases 1 and 3, no active yaw control is applied (i.e., zero yaw angle for all turbines), while yawing configurations of $(25°, 15°, 0°)$ and $(20°, 20°, 0°)$ are applied in Cases 2 and 4, respectively. These were found to be the optimal yawing strategies that maximised the overall power output from the experiments (Zong and Porté-Agel, 2021). The wind turbine rotational speeds ω are also chosen to match those of the experiments.

Schematics of the simulation domain are shown in Fig. 2. The size of the domain in the streamwise direction is

Table 1. Case configurations of the wind tunnel experiments, with the specifications of the lateral offset S_y, the yaw angles $\gamma = (\gamma_1, \gamma_2, \gamma_3)$ and the rotational speeds $\omega = (\omega_1, \omega_2, \omega_3)$.

No.	S_y	γ	ω (RPM)
Case 1	$0D$	$(0°, 0°, 0°)$	(2183, 1405, 1560)
Case 2	$0D$	$(25°, 15°, 0°)$	(2113, 1666, 1744)
Case 3	$D/3$	$(0°, 0°, 0°)$	(2156, 1639, 1755)
Case 4	$D/3$	$(20°, 20°, 0°)$	(2094, 1824, 2072)

$21.3D$. To minimise the blockage effect, the size of the simulation domain is $10.7D$ in the spanwise direction and $5.3D$ in the vertical direction. The pressure gradient is imposed up to the height $Z_{bl} = 0.3$ m to create a boundary layer with the same height as in the experiments. The friction velocity ~~$u_* = 0.26$~~ $u_* = 0.265$ m s^{-1} and the roughness length ~~$z_0 = 10^{-4}$~~ $z_0 = 9\times10^{-5}$ m in the LES cases are chosen so that the streamwise mean inflow velocity and the streamwise turbulence intensity at the hub-height match the wind tunnel measurements (Fig. 3).

2.4 Numerical configuration

In the WiRE-LES, the spatially filtered N-S equations are solved by the pseudospectral method in the horizontal directions and ~~by~~ the second-order finite-difference method in the vertical direction. Explicit time integration is carried out using the Adams–Bashforth method. Such a choice of numerical schemes has also been applied and validated in previous wind turbine wake flow studies (Wu and Porté-Agel, 2011; Lin and Porté-Agel, 2019).

The simulation domain is discretised into a uniform ~~mesh~~ grid with the cell numbers of $256 \times 128 \times 128$ in the streamwise, spanwise and vertical directions, respectively. Since the 3/2 rule is applied in the spectral filter in the horizontal directions for the de-aliasing, the ratio between the filter size $\tilde{\Delta}$ and the grid size (Δ) in the horizontal directions is $\tilde{\Delta}_x/\Delta_x = \tilde{\Delta}_y/\Delta_y = 1.5$. In the vertical direction, the ratio is $\tilde{\Delta}_z/\Delta_z = 1$. Therefore, the aspect ratio of the grid is $\Delta_x : \Delta_y : \Delta_z = 2 : 2 : 1$ and the aspect ratio of the filter is $\tilde{\Delta}_x : \tilde{\Delta}_y : \tilde{\Delta}_z = 3 : 3 : 1$. ~~The ratios between the rotor diameter and the filter widths are~~ In the spanwise direction, the ratio of the rotor diameter to the filter size is $D/\tilde{\Delta}_y = 8$ ~~and $D/\tilde{\Delta}_z = 24$ in the spanwise direction y and the vertical direction z, respectively~~, and the ratio to the grid size is $D/\Delta_y = 12$. In the vertical direction, the ratios of the rotor diameter to the filter size and the grid size are $D/\Delta_z = D/\tilde{\Delta}_z = 24$. The time step is chosen such that the Courant number is kept around 0.1. The total simulated physical time is 15 minutes, and the last 10 minutes of the simulation are used to obtain flow statistics and power outputs.
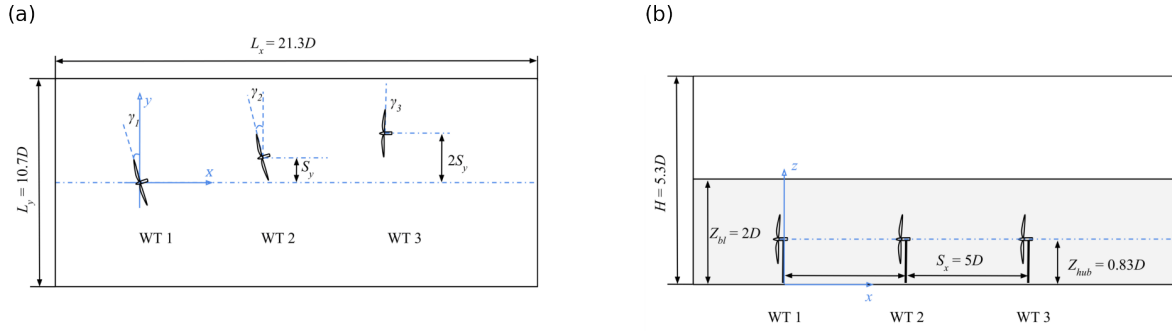
Figure 2. Schematic plots of the simulation domain (not to scale): ~~(a)~~ **(a)** top view~~(b)~~ ; **(b)** side view.
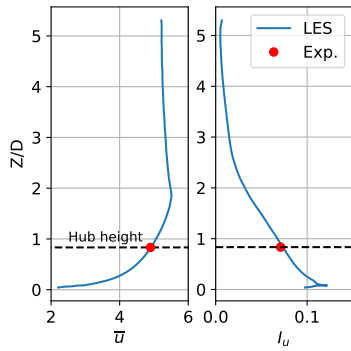
Figure 3. Vertical profiles of the streamwise mean velocity $\overline{u}$ and the streamwise turbulence intensity I_u. Blue solid lines represent the LES results and red dots represent the corresponding measurement data at the hub-height.

Periodic boundary conditions are used on the lateral boundaries in the horizontal directions (x and y). ~~On~~ In the vertical direction (z), a slip-wall condition is imposed on the top boundary, and a non-penetration wall is applied on the bottom boundary with specified stress based on the logarithmic law of the wall. A precursor method is used to generate the turbulent inflow for the simulation (Wu and Porté-Agel, 2011; Porté-Agel et al., 2013; Abkar and Porté-Agel, 2015), and a shifting boundary method is applied (Munters et al., 2016) at the inflow to mitigate the ~~the~~ formation of spurious locked-in streak-like structure (Fang and Porté-Agel, 2015).

3 Results

3.1 Mean velocity

For the cases with zero lateral offset (Cases 1 and 2), contours of the normalised streamwise mean velocity in the $x-y$ plane at hub height are shown in Fig. 4. In Case 1, the turbines are not yawed, and the turbine array is aligned with the inflow direction. The second and the third turbines are fully exposed to the wakes of their upwind turbines. In Case 2, with the yaw angles $\gamma = (25°, 15°, 0°)$, the wakes of the yawed turbines are redirected to the side where the turbine rotor plane is inclined into the downwind direction. As a result, the second and the third turbines in Case 2 are partially exposed to the wake of their respective upwind turbines.

Spanwise profiles of the normalised streamwise mean velocity at hub height are shown in Fig. 5. Behind the first turbine, we find that the maximum velocity deficits are slightly underestimated by LES using the ADM-std in the near wake for both non-yawed (Fig. 5a) and yawed configurations (Fig. 5b). As the wake develops further downstream, the results of the three models converge to the measurements. Behind the second turbine, the wakes of the turbine parametrised by the ADM-std have slightly larger velocity deficits and wake widths compared to the measurements in the non-yawed configuration (Fig. 5c). In the yawed configuration (Fig. 5d), the velocity deficits ~~in~~ obtained from LES using the ADM-std ~~results~~ are overestimated on the side where the turbine rotor is inclined downwind and are underestimated on the upwind-inclined side. As a result, the velocity profiles are further shifted to the negative spanwise (y) direction ~~compared to~~ than the measurements. Behind the third turbine, the three models yield reasonable predictions of the mean velocity in the non-yawed configuration (Fig. 5e), while the ADM-std ~~produces again~~ again produces an unrealistic shift in the velocity profiles in the yawed configuration (Fig. 5f).

Fig. 6 and Fig. 7 ~~show a comparison between~~ compare measured and simulated contours and spanwise profiles of the mean velocity, respectively, for the partial-wake cases under consideration. Due to the lateral offset of the turbines, the second and the third turbines are partially exposed to the incoming wakes in both non-yawed and yawed configurations. In Cases 3 and 4, where the partial-wake condition occurs, shifted velocity profiles with respect to the measurements are observed in the wakes of the second and the third turbines ~~in~~ parametrised by the ADM-std~~results~~. Furthermore, an under-
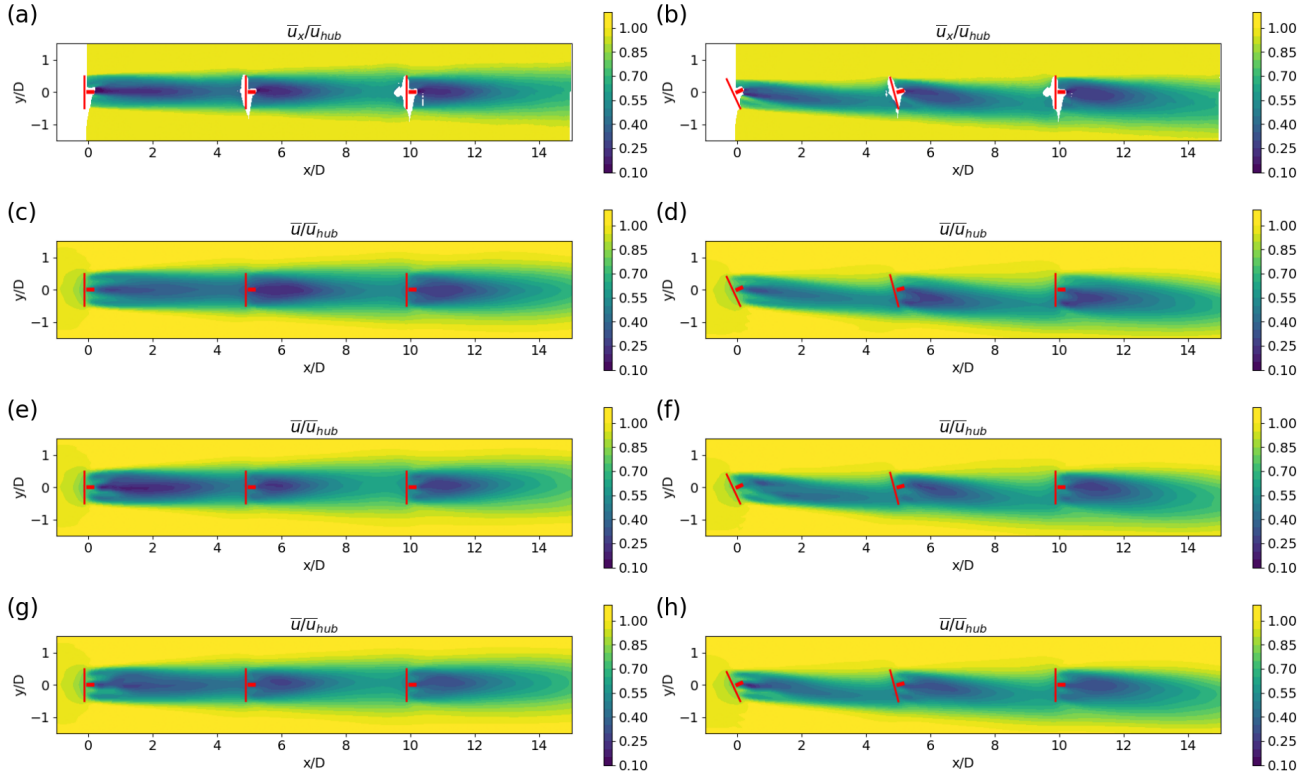
Figure 4. Contours of the normalised streamwise mean velocity $\overline{u}/\overline{u}_{hub}$ in the $x - y$ plane at hub height obtained from the wind-tunnel experiments and LES using the ADM-std, ADM-BE and ALM. The lateral offset of the turbines is zero (Cases 1 and 2). **(a)** Experiment, $\gamma = (0°, 0°, 0°)$; **(b)** Experiment, $\gamma = (25°, 15°, 0°)$; **(c)** the ADM-std, $\gamma = (0°, 0°, 0°)$; **(d)** the ADM-std, $\gamma = (25°, 15°, 0°)$; **(e)** the ADM-BE, $\gamma = (0°, 0°, 0°)$; **(f)** the ADM-BE, $\gamma = (25°, 15°, 0°)$; **(g)** the ALM, $\gamma = (0°, 0°, 0°)$; **(h)** the ALM, $\gamma = (25°, 15°, 0°)$.

estimation of the velocity deficits is also observed in the wake of the third turbine ~~in~~ parametrised by the ADM-std ~~results of~~ in Case 4.

Fig. 8 shows the trajectories of the location of the maximum velocity deficit in the wake ~~,~~ in different configurations. The trajectories ~~of the~~ obtained from LES using the ADM-BE and the ALM are in good agreement with the measurements. On the other hand, the trajectories obtained from LES using the ADM-std ~~results~~ are shifted from the measurements behind the turbines in ~~the partial wake condition~~ partial wake conditions. This is consistent with the shifted pattern ~~of the ADM-std results~~ observed in the velocity ~~profile plots~~ profiles (Fig. 5 and Fig. 7). This ~~issue~~ observation can be explained by a key model assumption of the ADM-std: the turbine-induced forces are modelled as thrust forces uniformly distributed on the rotor disk. ~~When a wind turbine is~~ To illustrate this point, we plot the time-averaged thrust forces per unit area on the rotor disk of WT 3 in Case 2, which is a turbine partially exposed to the ~~incoming wake , the~~ wake of its upstream turbine (Fig. 9). We can see that the normal thrust force parametrised by the ADM-std ~~overestimates the thrust force in the rotor sections~~ ~~with more wake exposure and underestimates the thrust forces in the less-exposed sections. As aresult, the velocity deficits are overestimated behind the rotorsections with more exposure to the incoming wake and underestimate behind the less-exposed section. This, in turn, leads to the observed spurious lateral shift in the location of the maximum velocity deficit. On the other hand, the~~ (Fig. 9a) is uniform on the rotor. By contrast, the forces parametrised by the ADM-BE (Fig. 9b) and the ALM ~~both resolve the non-homogeneous force distribution~~ (Fig. 9c) have non-uniform distributions on the rotor~~, producing results that are in better agreement with the~~ : specifically, larger thrust forces are found on the right side of the contours. The differences in the thrust force distribution lead to a shift from the measurements in the ~~partial-wake condition, characterized by the inhomogeneous inflows to the turbine.~~ maximum velocity deficit trajectories in the cases using the ADM-std.
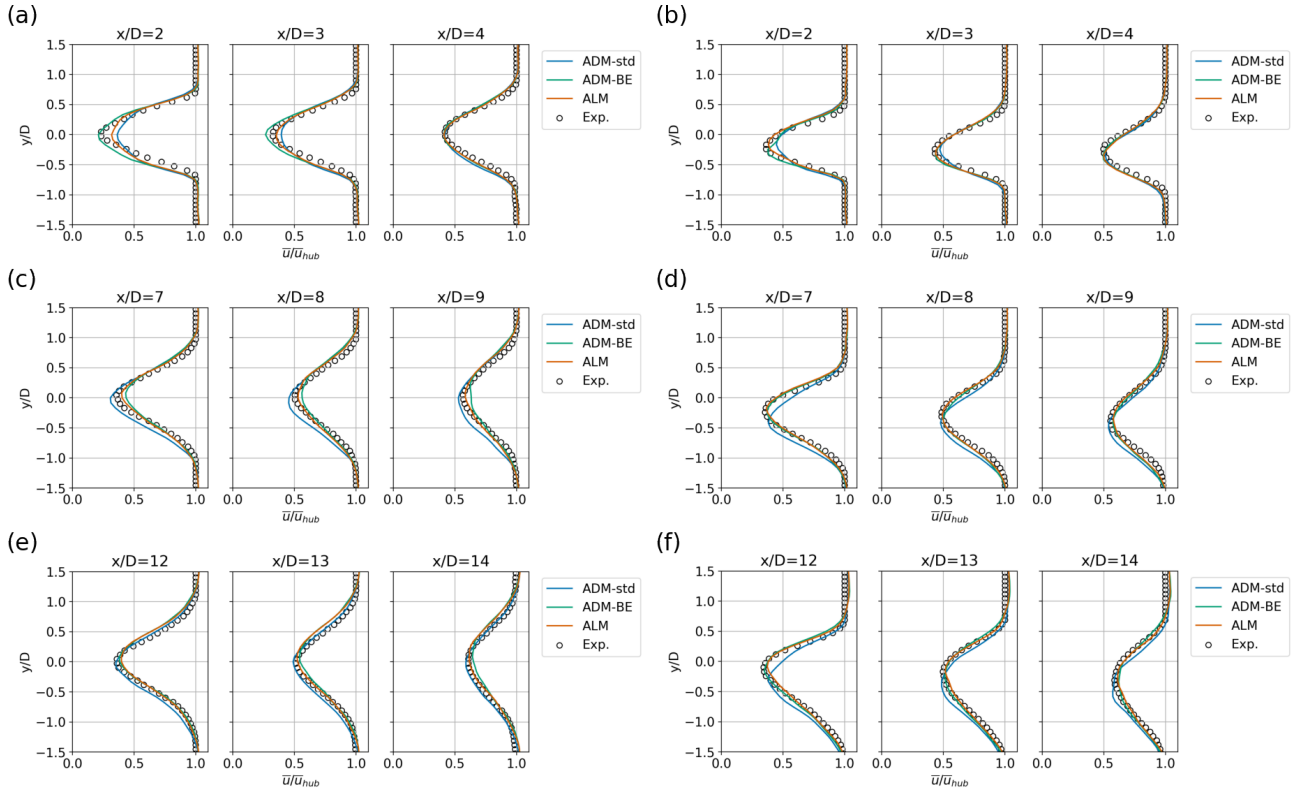
Figure 5. Spanwise profiles of the normalised streamwise mean velocity $\overline{u}/\overline{u}_{hub}$ in the $x-y$ plane at hub height obtained from the wind-tunnel experiments, LES using the ADM-std, ADM-BE and ALM. The lateral offset of the turbines is zero (Cases 1 and 2). **(a)** WT 1, $\gamma = (0°, 0°, 0°)$; **(b)** WT 1, $\gamma = (25°, 15°, 0°)$; **(c)** WT 2, $\gamma = (0°, 0°, 0°)$; **(d)** WT 2, $\gamma = (25°, 15°, 0°)$; **(e)** WT 3, $\gamma = (0°, 0°, 0°)$; **(f)** WT 3, $\gamma = (25°, 15°, 0°)$.

3.2 ~~Turbulence intensity~~

3.2 Turbulence statistics

Contours and profiles of the streamwise turbulence intensity in the $x-y$ plane at hub height are shown in Fig. 10 and Fig. 11, respectively. The experiment results of the non-yawed and yawed configurations are compared with the corresponding LES results using the ADM-std, ADM-BE and the ALM. Since the wind tunnel measurements of the turbulence intensity are not available for Case 3 and Case 4, we only analyse Case 1 and Case 2 with zero offset.

In the measurement contours shown in Figures 10a and 10b, large magnitude of turbulence intensity is observed at the edges of the wake due to the strong shear in these regions. In the non-yawed case (Figures 10a), the turbulence intensity in the wakes is largely symmetric with respect to the wake ~~center-line~~ centre-line. In the yawed case (Fig. 10b), the turbulence intensity on the positive y side of the wake is larger than the turbulence intensity on the negative y side.

By comparing the LES results with the measurements in the turbulence intensity contours (Fig. 10), we find that the results of LES using the ADM-std show discrepancies with the measurements in the yawed case with the partial-wake condition. In the wakes behind the second and the third turbine, LES using the ADM-std overestimates the turbulence intensity with respect to the measurements on the negative y side of the wake. This is consistent with the overestimation of the mean velocity gradient in LES using the ADM-std ~~results~~ on the positive y side of the skewed wake (Fig. 5). Furthermore, in comparison with LES using the ADM-BE and the ALM, we find that LES using the ADM-std underestimates the magnitude of the ~~turbulent~~ turbulence flux $\overline{u'v'}$ on the positive y side of the wake ~~.~~ (Fig. 12). Since the turbulence production term is defined by taking a product of the velocity gradient and the turbulence flux, such differences in ~~the results of~~ LES using the ADM-std lead to an incorrect turbulence intensity distribution in the partial-wake scenario. Comparisons of the turbulence intensity profiles in Fig. 11 also show that LES using the ADM-std, the ADM-BE and the ALM slightly overspread the turbulence in the wakes: the turbulence intensity profiles of the LES results are wider than the measurements in both non-yawed and yawed cases.
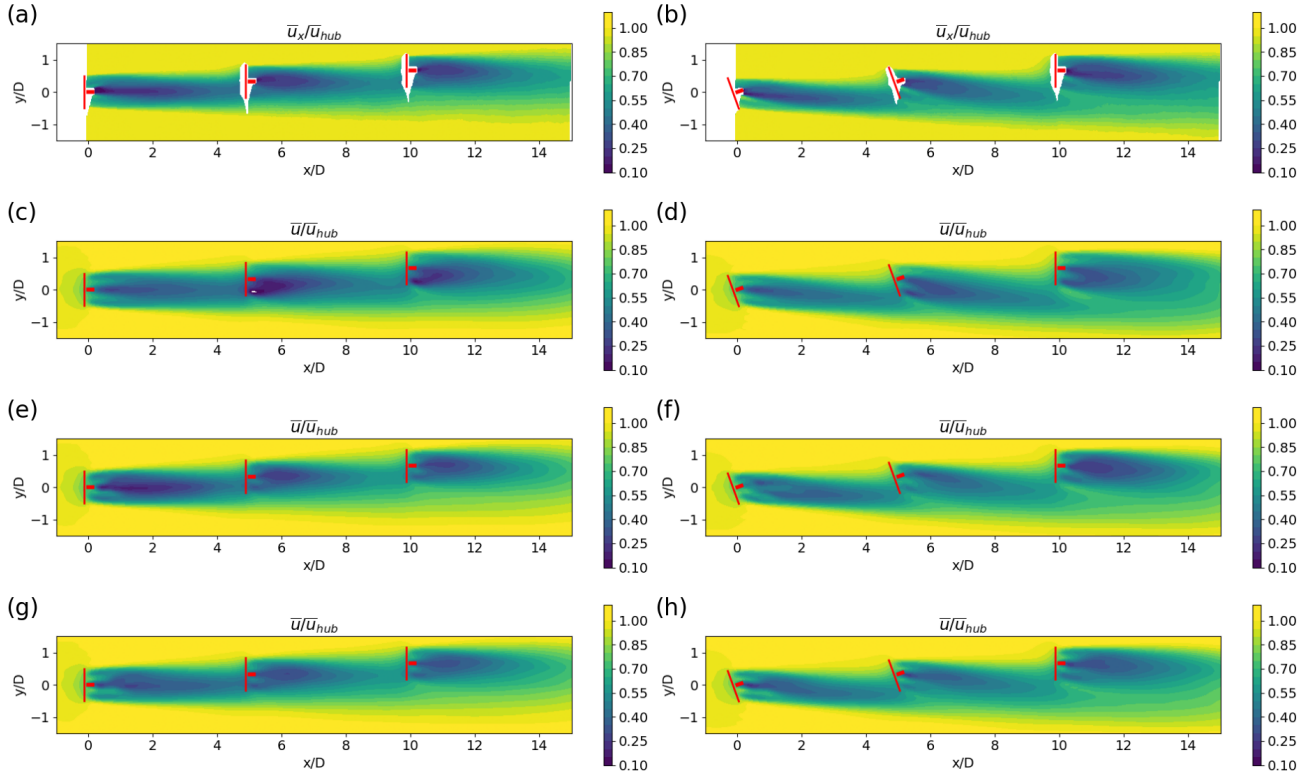
Figure 6. Top-view contours of the normalised streamwise mean velocity $\overline{u}/\overline{u}_{hub}$ in the $x - y$ plane at hub height obtained from the wind-tunnel experiments, LES using the ADM-std, ADM-BE and ALM. The wind turbines are offset in the spanwise direction with a distance of $D/3$ (Cases 3 and 4). **(a)** Experiment, $\gamma = (0°, 0°, 0°)$; **(b)** Experiment, $\gamma = (20°, 20°, 0°)$; **(c)** the ADM-std, $\gamma = (0°, 0°, 0°)$; **(d)** the ADM-std, $\gamma = (20°, 20°, 0°)$; **(e)** the ADM-BE, $\gamma = (0°, 0°, 0°)$; **(f)** the ADM-BE, $\gamma = (20°, 20°, 0°)$; **(g)** the ALM, $\gamma = (0°, 0°, 0°)$; **(h)** the ALM, $\gamma = (20°, 20°, 0°)$.

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This phenomenon is caused by the fact that the turbine forces in the LES are smeared by smoothing kernels in the turbine parametrisations. As a result, the shear layer produced at the ~~edges of the wakes is wider compared to the the~~ wake's edges is wider than the measurements, causing the wider turbulence intensity profiles in the LES results.

3.3 ~~Normalised power output~~ Power prediction

Finally, we compare the power ~~outputs obtained from~~ prediction obtained from LES using the ADM-std, the ADM-BE and the ALM with the power measured in the wind tunnel experiments ~~. The normalised power outputs (normalised by the power output of the non-yawed turbine facing an undisturbed inflow) of the zero and the $D/3$ offset cases are shown in Fig. ??.~~

~~Normalised power outputs $\tilde{P}_i = P_i/P_1$: the power output of ith turbine P_i is normalised by the power of the first turbine P_1. The error of the $\tilde{P}_i$ obtained from LES using the ADM-std, ADM-BE and ALM with respective to the experiments are shown in (b), (d), (f) and (h).~~

~~In Case 1, with zero lateral offset and zero yaw angle, the~~ performed by Zong and Porté-Agel (2021). Fig. 13 shows the simulated power coefficients of a zero-yawed stand-alone turbine and their relative errors to the measurements. The power coefficients are obtained from the simulations using a baseline grid (specified in Sec. 2.4) and a refined grid ($\times 2$ refinement in x, y and z directions from the baseline grid). We find that the ADM-BE yields the ~~smallest errors with respect to the measurements while the~~ best predictions in the baseline and refined grid cases. Moreover, the errors in the predictions of the ADM-BE are within the measurement uncertainty ($\pm 4.5\%$) in both cases. By contrast, in the baseline grid case, the power coefficients predicted by the ADM-std ~~yields the largest. In Case 2, with the yaw angles of $(25°, 15°, 0°)$, the ADM-std~~ and the ~~ADM-BE yield similar power output in the first and the third turbine, while the ADM-BE has the largest underestimation in the second turbine. The ALM , on the~~ ALM have errors that are larger than the uncertainty upper bound. When the grid is refined, the error in the power coefficients predicted by the ALM is halved to a level below the uncertainty bound. On the other
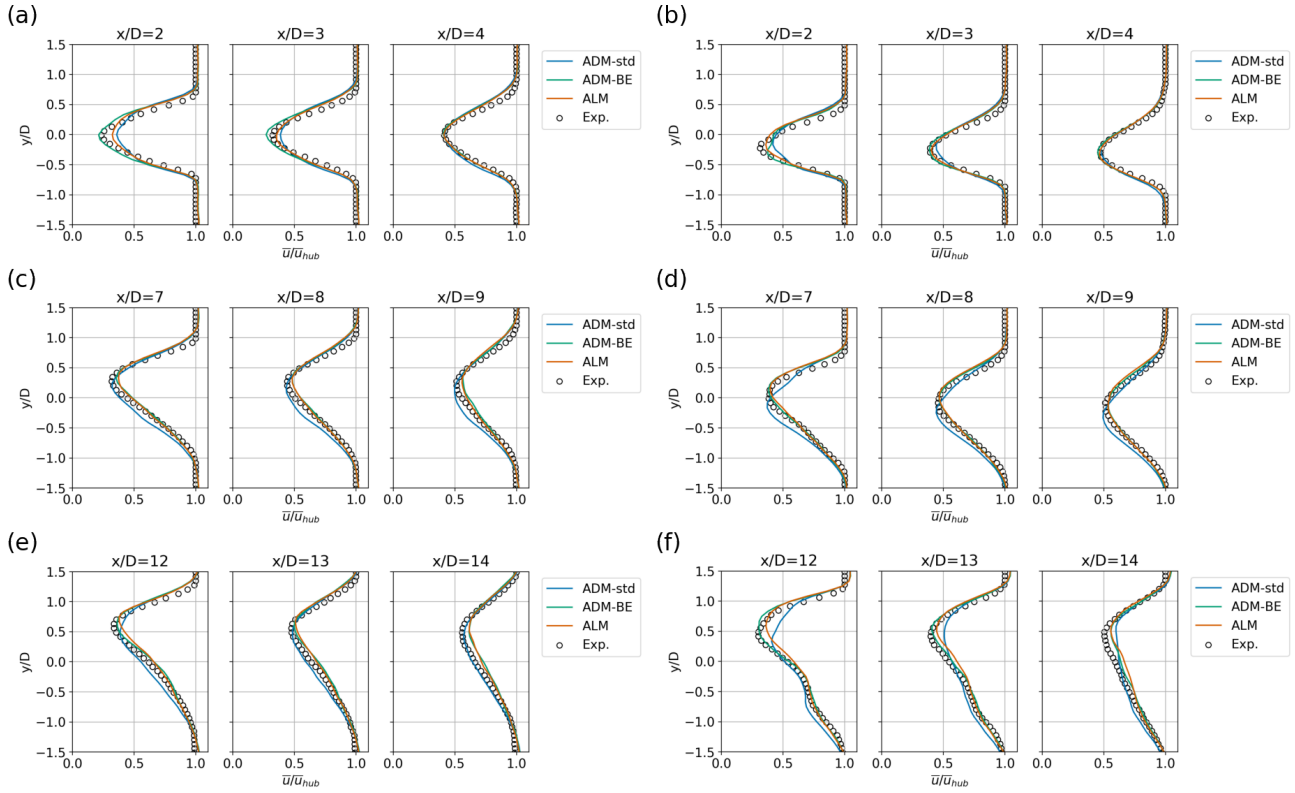
Figure 7. Profiles of the normalised streamwise mean velocity $\overline{u}/\overline{u}_{hub}$ in the $x-y$ plane at hub height obtained from the wind-tunnel experiments, LES using the ADM-std, ADM-BE and ALM. The wind turbines are offset in the spanwise direction with a distance of $D/3$ (Cases 3 and 4). **(a)** WT 1, $\gamma = (0°,0°,0°)$; **(b)** WT 1, $\gamma = (20°,20°,0°)$; **(c)** WT 2, $\gamma = (0°,0°,0°)$; **(d)** WT 2, $\gamma = (20°,20°,0°)$; **(e)** WT 3, $\gamma = (0°,0°,0°)$; **(f)** WT 3, $\gamma = (20°,20°,0°)$.
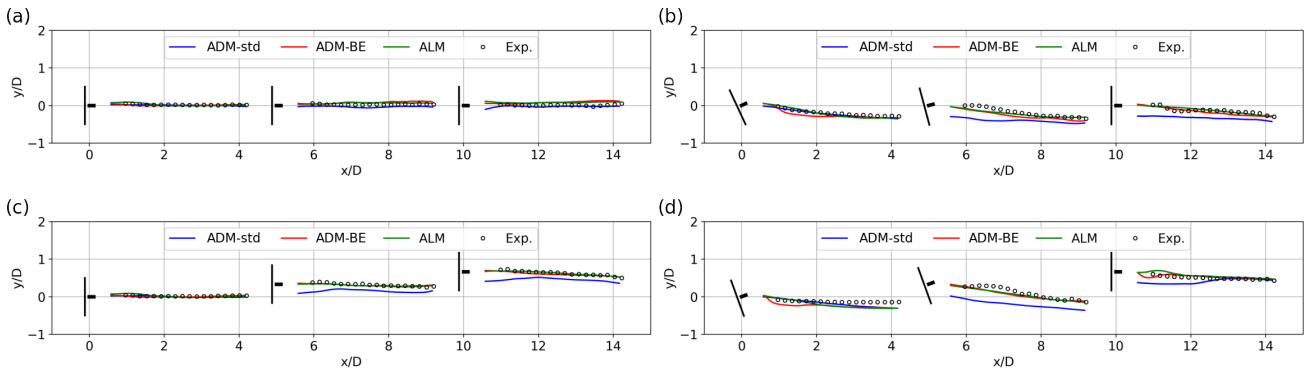
Figure 8. Trajectories of maximum velocity deficit location obtained from the wind-tunnel experiments, LES using the ADM-std, ADM-BE and ALM. **(a)** Case 1: $\gamma = (0°,0°,0°)$, zero offset; **(b)** Case 2: $\gamma = (25°,15°,0°)$, zero offset; **(c)** Case 3: $\gamma = (0°,0°,0°)$, $D/3$ offset; **(d)** Case 4: $\gamma = (20°,20°,0°)$, $D/3$ offset.

hand, ~~has the largest overestimation in the first turbine but the least in the third turbine. In Case 3 and Case 4, with a D/3 lateral offset, the ADM-BE outperform the~~ the prediction of the ADM-std ~~and the ALM and have the smallest errors in the~~

~~power outputs in both non-yawed and yawed configurations.~~ only changes marginally with the grid refinement and still overestimates the power coefficient to a level beyond the measurement uncertainty. 5
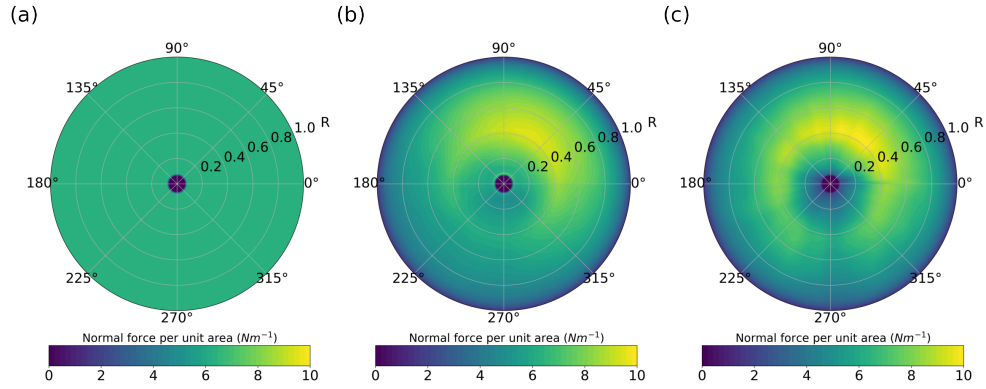
Figure 9. Back-view contours of the time-averaged normal force per unit area on the rotor disk of WT 3 in Case 2. The turbine forces are parametrised by **(a)** the ADM-std; **(b)** the ADM-BE; **(c)** the ALM.
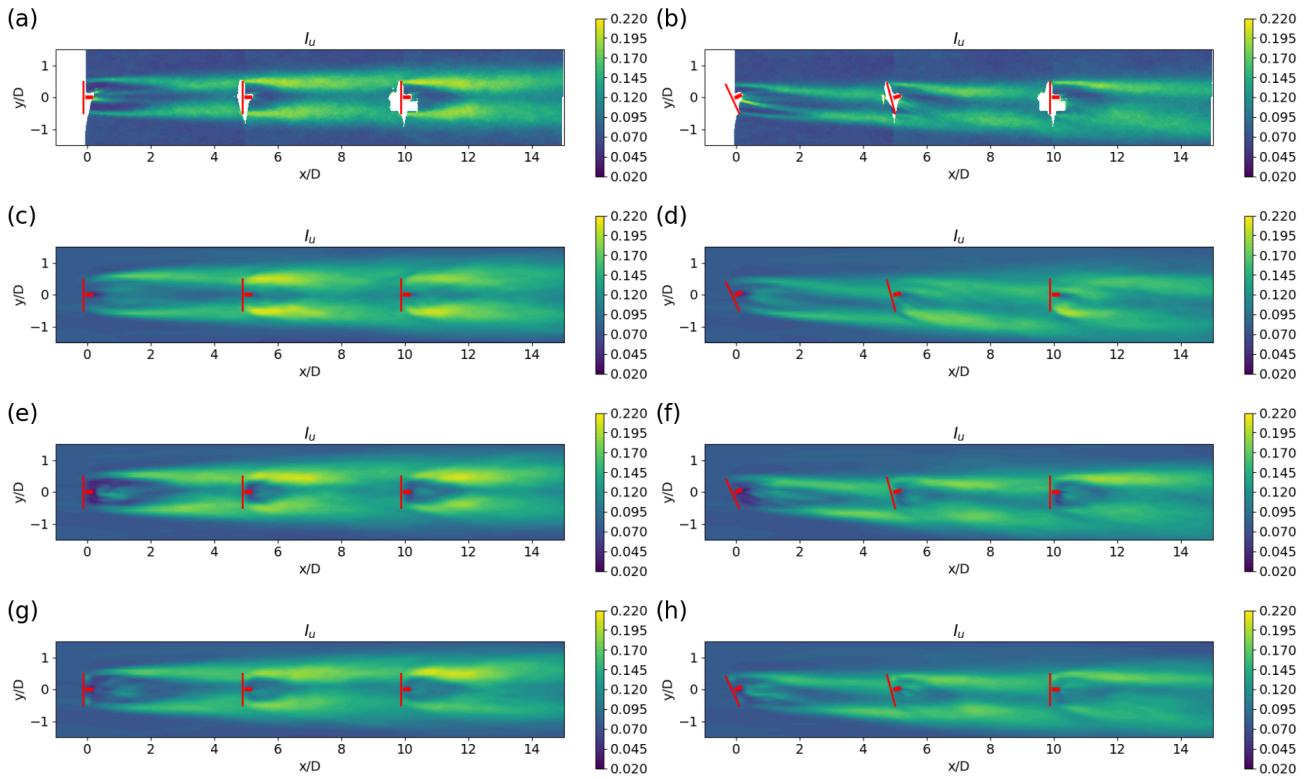
Figure 10. Top-view contours of the turbulence intensity I_u in the $x - y$ plane at hub height obtained from the wind-tunnel experiments, LES using the ADM-std, ADM-BE and ALM. The lateral offset of the turbines is zero (Cases 1 and 2). **(a)** Experiment, $\gamma = (0°, 0°, 0°)$; **(b)** Experiment, $\gamma = (25°, 15°, 0°)$; **(c)** the ADM-std, $\gamma = (0°, 0°, 0°)$; **(d)** the ADM-std, $\gamma = (25°, 15°, 0°)$; **(e)** the ADM-BE, $\gamma = (0°, 0°, 0°)$; **(f)** the ADM-BE, $\gamma = (25°, 15°, 0°)$; **(g)** the ALM, $\gamma = (0°, 0°, 0°)$; **(h)** the ALM, $\gamma = (25°, 15°, 0°)$.

~~As~~ Fig. 14 shows the simulated and measured power of the three-turbine array in Cases 1 to 4 specified in Table 1. Fig. 15 shows the corresponding errors of the simulated power with respect to the measured power for each turbine. The power outputs and the errors are normalised by the measured power of the first turbine of the array in zero yaw. Using the data shown in Fig. ~~??, the~~ 14 and 15, we further compute the normalised total power error of the three-turbine array in Cases 1 to 4 (Fig. 16) and use it as the metric to evaluate
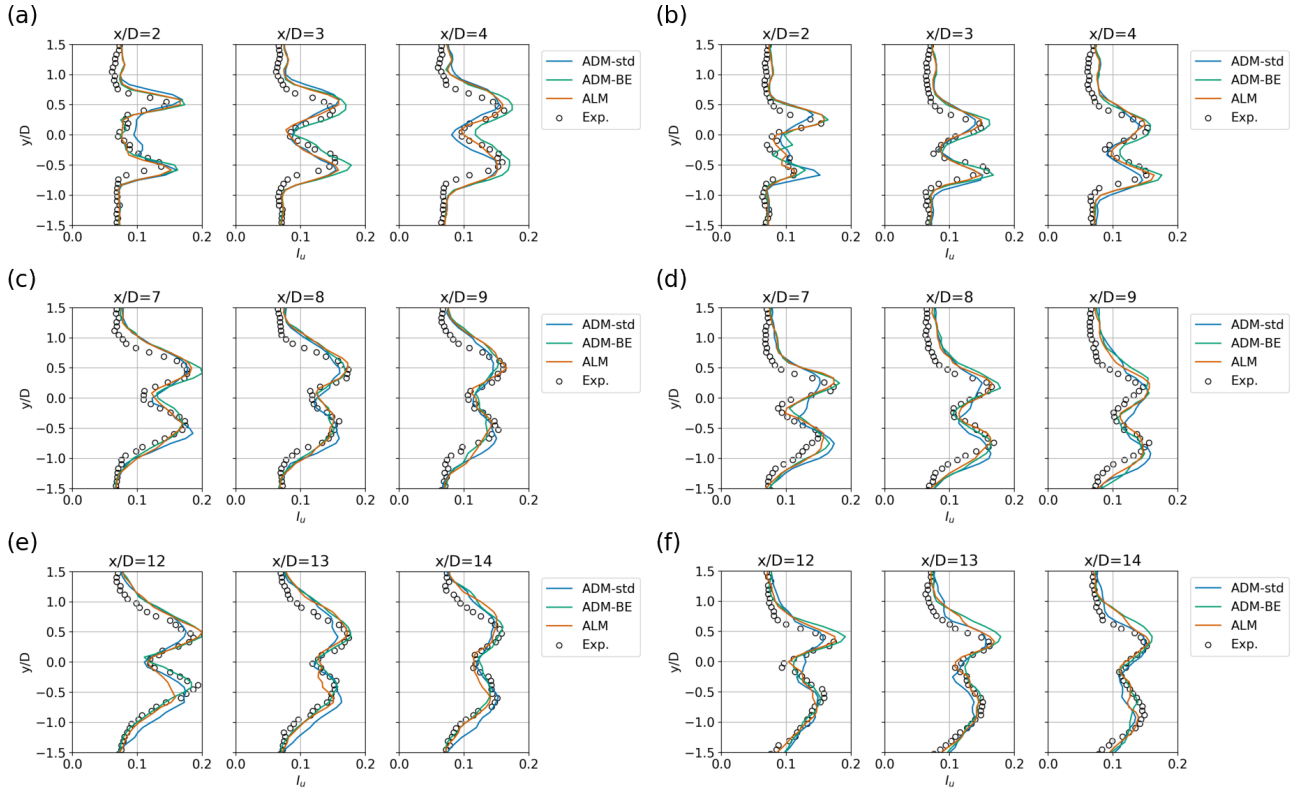
Figure 11. Profiles of the streamwise turbulence intensity I_u in the $x-y$ plane at hub height obtained from the wind-tunnel experiments, LES using the ADM-std, ADM-BE and ALM. **(a)** WT 1, $\gamma = (0°,0°,0°)$; **(b)** WT 1, $\gamma = (25°,15°,0°)$; **(c)** WT 2, $\gamma = (0°,0°,0°)$; **(d)** WT 2, $\gamma = (25°,15°,0°)$; **(e)** WT 3, $\gamma = (0°,0°,0°)$; **(f)** WT 3, $\gamma = (25°,15°,0°)$.
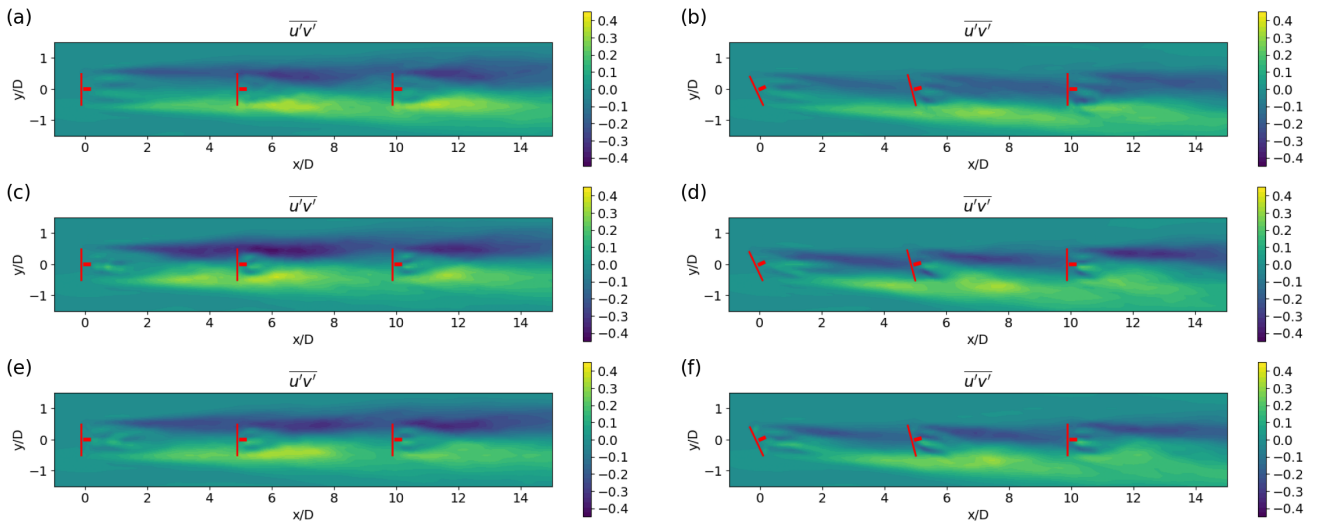
Figure 12. Top-view contours of the ~~turbulent~~ turbulence flux $\overline{u'v'}$ (m²/s²) in the $x-y$ plane at hub height obtained from LES using the ADM-std, ADM-BE and ALM. The lateral offset of the turbines is zero (Cases 1 and 2). **(a)** the ADM-std, $\gamma = (0°,0°,0°)$; **(b)** the ADM-std, $\gamma = (25°,15°,0°)$; **(c)** the ADM-BE, $\gamma = (0°,0°,0°)$; **(d)** the ADM-BE, $\gamma = (25°,15°,0°)$; **(e)** the ALM, $\gamma = (0°,0°,0°)$; **(f)** the ALM,
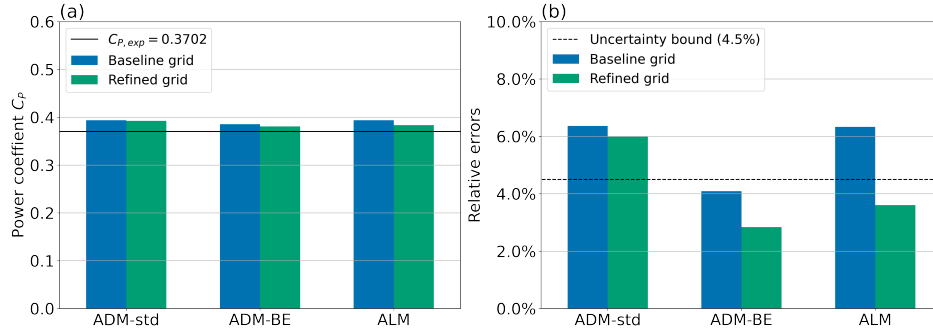
Figure 13. (a) Power coefficients of the first turbine in the turbine array in zero yaw. The black solid line marks the measured power coefficient. (b) Relative errors of the power coefficient compared to the power measurement. The black dashed line marks the uncertainty bound of the power measurement.

the predictions of different parametrisations. This metric is defined as the L^1 norm (the summation of absolute values) of the power error of each turbine in the array, normalised by the total measured power in each case:

$$\tilde{\epsilon}_{tot} = \frac{\sum_{i=1}^{3} |\epsilon_i|}{\sum_{i=1}^{3} P_{i,exp}}, \quad |\epsilon_i| = |P_{i,sim} - P_{i,exp}|. \tag{10}$$

We find that the ADM-BE, which explicitly resolves the torque, and therefore the power, yields more accurate power predictions than ~~than~~ the ADM-std. The ~~inaccuracies~~ errors in the ADM-std results ~~are largely~~ can be attributed to the basic formulation of the model. Firstly, the model assumes a uniform thrust force distribution on the rotor. As we have shown in Fig. 8 and 9, due to the ~~fact that the~~ inaccuracy of the uniform force assumption, the ADM-std yields shifted maximum velocity deficit trajectories compared to the measurements. Such errors in the wake velocity distribution affect the power prediction. Secondly, the ADM-std computes the power indirectly using an estimated inflow velocity reconstructed from the local disk-averaged velocity based on 1D momentum theory (Eq. 6 and 7) and a pre-determined power ~~output is calculated using the power~~ curve. Since ~~that~~ the power curve is obtained from ~~wind turbines operating in homogeneous inflow and zero-yaw conditions~~ the measurements of a turbine facing an undisturbed inflow, it is expected to be less accurate ~~when the wind turbine operates in partial wake or yawed conditions~~ for turbines in yawed and waked conditions. Moreover, the difference between the inflow velocity reconstructed from the local disk-averaged velocity and the hub-height velocity used to normalise the power curve also introduces some errors to the power prediction. In certain scenarios, the errors originating from the aforementioned factors can cancel with each other, but overall we observe larger total errors in the power predictions of the ADM-std than the ADM-BE. ~~It is also found~~

We also find that, in general, the ADM-BE outperforms the ALM, even if both of them are torque-resolving parametrisations. This is consistent with previous studies ~~(Martinez et al., 2012; Martínez-Tossas et al., 2017) that have shown that~~ (Martinez et al., 2012; Martínez-Tossas et al., 2015) showing that the power prediction from the ALM is more sensitive to the ~~smearing kernel used to project the localised blade-induced forces on the Cartesian mesh grid, compared to the ADM~~ mesh resolution than the ADM-BE. As a result, the ALM usually fails to yield ~~good power predictions in the typical mesh resolution (~ 10~~ satisfactory power prediction in the simulation employing a grid resolution with less than 30 grid points along the rotor diameter ~~) used in simulations of wind farm flows (Stevens et al., 2018)~~ (Draper and Usera, 2015; Martínez-Tossas et al., 2015; Stevens et al., 20 .

4   Summary

In this study, we validate an LES framework with different wind turbine force parametrisations (the ADM-std, ADM-BE and ALM) ~~for the prediction of the~~ to predict the flow through a three-turbine array. The simulations are set to match existing wind tunnel experiments for which flow and power measurements are available for different turbine lateral offsets (with respect to the wind direction) and different active yaw control strategies.

Comparisons with wind tunnel measurements show that LES with wind turbine models that capture the local distribution of the turbine-induced forces (the ADM-BE and ALM) provide reasonably accurate predictions of the streamwise mean velocity ~~deficit~~ and the streamwise turbulence intensity in the wakes of the three wind turbines for all the considered conditions of lateral offset and yaw control. In contrast, the wake flows simulated with the standard actuator disk model (the ADM-std) show a lateral shift with respect to the measurements when the turbines are exposed to partial wake con-
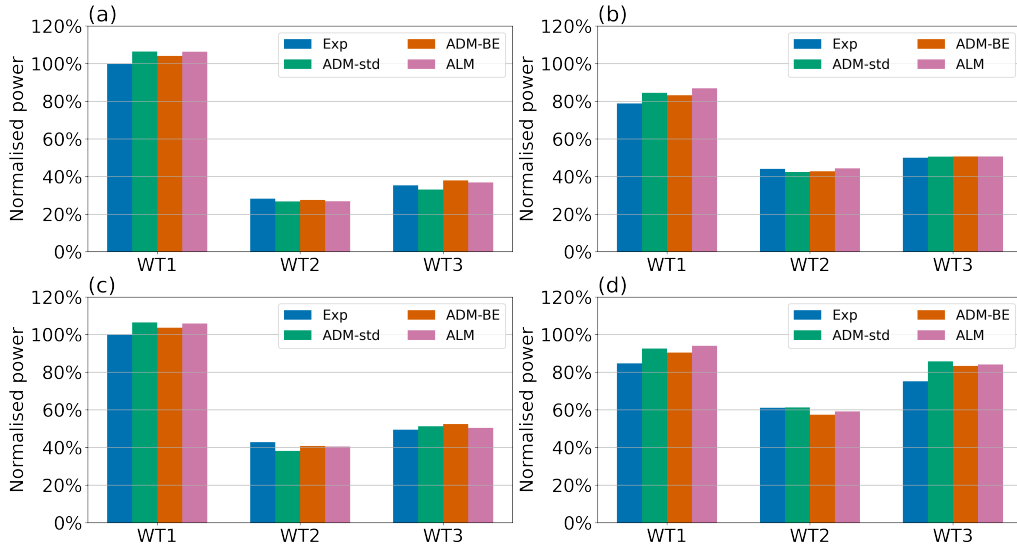
Figure 14. Normalised power outputs in (a) Case 1: $\gamma = (0°, 0°, 0°)$, zero offset; (b) Case 2: $\gamma = (25°, 15°, 0°)$, zero offset; (c) Case 3: $\gamma = (0°, 0°, 0°)$, $D/3$ offset; (d) Case 4: $\gamma = (20°, 20°, 0°)$, $D/3$ offset. The power outputs are normalised by the measured power of the zero-yawed first turbine of the turbine array.
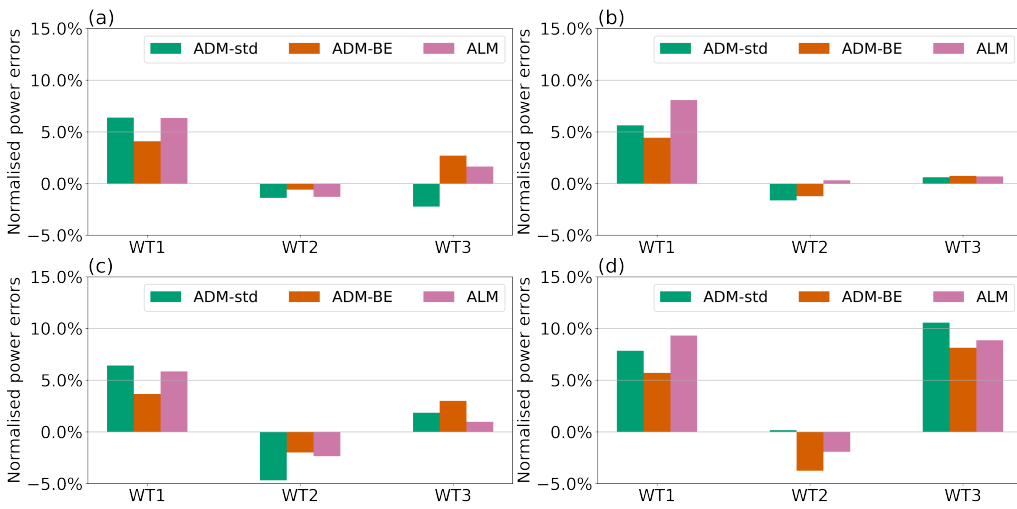
Figure 15. Normalised power errors in (a) Case 1: $\gamma = (0°, 0°, 0°)$, zero offset; (b) Case 2: $\gamma = (25°, 15°, 0°)$, zero offset; (c) Case 3: $\gamma = (0°, 0°, 0°)$, $D/3$ offset; (d) Case 4: $\gamma = (20°, 20°, 0°)$, $D/3$ offset. The power outputs are normalised by the measured power of the zero-yawed first turbine of the turbine array.
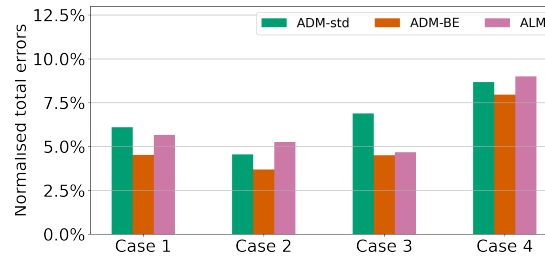
Figure 16. Normalised total power errors of the three-turbine array. The errors are normalised by the total measured power of the wind turbine array in each case. Case 1: $\gamma = (0°, 0°, 0°)$, zero offset; Case 2: $\gamma = (25°, 15°, 0°)$, zero offset; Case 3: $\gamma = (0°, 0°, 0°)$, $D/3$ offset; Case 4: $\gamma = (20°, 20°, 0°)$, $D/3$ offset.

ditions produced by either lateral offset of the turbines or/and active yaw control. This is due to the fact that the assumption of ~~homogeneous~~ uniform thrust force made by the ADM-std hinders the model from capturing the ~~non-homogeneous~~ non-uniform force distribution experienced by the rotor and, consequently, the correct wake velocity ~~deficit~~ distribution under partial wake conditions. Moreover, ~~the standard ADM-std yields the largest inaccuracies in the power output predictions~~ we find that LES using the ADM-BE yields overall better power predictions than the ADM-std and the ALM in the cases considered in this study. The ADM-BE is found to be better suited for the conditions of turbine yawing and partial wake overlapping than the ADM-std, due to the fact that ~~it is based on the power curve, which is not reliable under non-homogeneous inflow conditions (e.g., under partial wake conditions). The two torque-resolving models (the~~ ADM-BE ~~and ALM) are found to provide more accurate power predictions, with the~~ computes the power from the torque that is explicitly resolved on the rotor. The ADM-BE ~~showing less sensitivity to errors associated with the smearing kernel used to project the forces on the grid .~~ is also found to be more computationally efficient than the ALM, as the ALM requires finer grid resolution to produce satisfactory power predictions.

From the ~~aforementioned results~~ results mentioned above, we conclude that the ADM-BE provides a good balance between accuracy and computational cost for the simulation of wind farm flows~~under different conditions, including partial wake and active yaw control~~. In our future research, we plan to apply the validated LES framework to investigate optimal AYC strategies under different atmospheric conditions, e.g., turbulence intensity and atmospheric stability. Furthermore, since the ~~turbine forces are explicitly resolved by the~~ ADM-BE and ALM explicitly resolve the turbine forces, the LES framework could also be applied to study structural loads in wind farms subjected to AYC.

Data availability. The dataset is available on Zenodo (Lin and Porté-Agel, 2022)

Author contributions. ML contributed to the conceptualisation, curation, formal analysis, investigation, methodology, software, visualisation and writing (original draft). FPA contributed to the conceptualisation, supervision, software, funding acquisition, project administration and writing (review & editing).

Competing interests. The authors declare that they have no conflict of interest.

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Appendix A: Grid sensitivity of flow statistics

Here we present results from a grid sensitivity analysis carried out to investigate the influence of grid resolution on the results obtained with LES. Fig. A1 shows the hub-height profiles of the mean velocity and turbulence intensity in the wake behind a yawed turbine ($\gamma = 25°$) obtained from the measurements and the simulations using the ADM-std, the ADM-BE and the ALM. The simulations are carried out on the baseline grid specified in Sec. 2.4 and a refined grid ($\times 2$ refinement in x, y and z directions from the baseline grid). Overall, we find that simulation results converge and agree reasonably well with the measurements when the grid is refined.
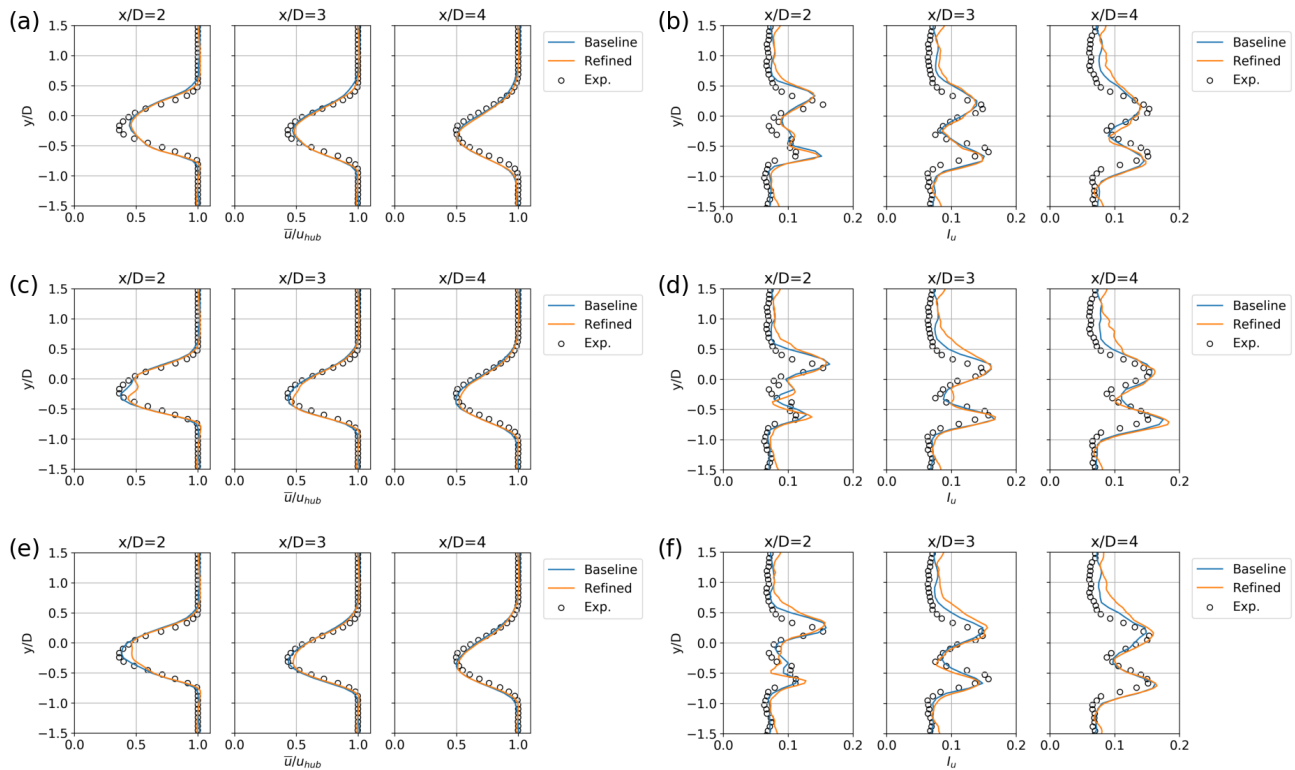
Figure A1. Profiles of the normalised streamwise mean velocity (left column) and turbulence intensity (right column) in the $x - y$ plane at the hub height, obtained from the wind-tunnel experiments and the LES at different grid resolution. **(a)** and **(b)**: the ADM-std; **(c)** and **(d)**: the ADM-BE; **(e)** and **(f)**: the ALM. The yaw angle of the wind turbine is $25°$

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