Overall quality:

Interesting work, the case study is relevant and the proposed procedure has been well described. The text is quite clear and easy to follow.

Thank you very much for taking the time to evaluate our manuscript. Your comments are much appreciated.

In this file, the black colored text is your comments. We have done our best to response/answer all your comments, which is given as green colored text.

Because both reviewers are asking to get more explanation on why we have focused on the 2-3 h fluctuations and not other frequency ranges, this has been elaborated on in the text. In addition, one additional subsection is included, discussing potential smoothing effect at other frequency ranges (subsection 4.5, see end of this document).

However, I see two important points to improve:

The authors should elaborate on why the frequency interval from 1/2 h⁻¹ to 1/3 h⁻¹ has been selected for the optimization instead of larger periods (e.g. 1-2 days) or a wider range of frequencies (e.g. from daily to 1/2 h⁻¹). This choice should be carefully motivated since it is at the article's core. One could argue that the 2-3h period falls right within the spectral gap of typical wind variations at a site and therefore relatively low variability is expected in that range. Valid arguments justifying the frequency range selection should be presented already in the introduction (e.g. around lines 31 or 59) and then renewed in the discussion sections (e.g. around lines 157 and 237).

Your comment makes much sense. Arguments are added around line 31. And again, shortly mentioned around lines 157 (Method>Optimization Method) and 237 (discussion).

• The authors should present at least a hypothesis for why the optimization provides a limited benefit compared to an even distribution of the capacity. Moreover, it would be nice to see some comments about what would be expected if the same methodology was applied to different case studies.

To answer your comment, the following discussion is added to section 4.2. (The end of section 4.2 has been removed to a separate subsection (4.2.1)):

The reduction of the 5th and 95th percentiles and standard deviations of the hourly step-change functions are 2% or less for the three optimized cases. It may be speculated that the observed limited hourly smoothing effect is because the improvement that the optimization adds is small compared to the smoothing that already occurred by considering the equally weighted spatially distribution of the wind farms.

To investigate this further, small wind farm portfolios in the region are examined, by looking at combinations of three wind farms. With the combination of the southernmost site and the two clustered northernmost sites, optimized wind farm capacity distribution places around 27% of the total power capacity of the wind farm portfolio at each of the northernmost sites and almost 47% at the southernmost site. The distribution is logical, with lower capacities at both of the clustered wind farm sites, and higher capacity at the distant site. If the two clustered sites were fully correlated on 2-3 hourly scale while the distant site was uncorrelated, the capacity distribution is expected to be 25%, 25%, and 50%, respectively, which is close to what is observed for this set-up. For the optimized portfolio with this set-up, the 5th and 95th percentiles and the standard deviation of the hourly power output step-change function are 4-5% lower compared to if the wind power capacity were to be equally distributed over the three sites. Comparing the optimized wind farm portfolio to a portfolio where 40% of the total wind power capacity are placed at each of the two northernmost wind farms and 20% at the southernmost wind farm – a rather illogical distribution in terms of spatially smoothing of the power capacity – the optimized wind farm portfolio contains 12-13% lower 5th and 95th percentiles and standard deviation. Indicating that the power capacity distribution of the wind farms matters.

Going back to case I (all fourteen favorable wind farm sites in the region), although the optimized portfolio has only limited effect on the smoothing effect compared to the portfolio where the power capacities are equally distributed, comparing the overall power outputs of the optimized distribution of case I to the power output of the equally distributed capacity of case III with the constrain of the given boundary conditions, the 5th and 95th percentiles and the standard deviation of the hourly step-change function are 4% lower. Likewise, by comparing the power output of the optimized distribution of case I to a set-up where 11% of the total wind power capacity is placed at the four closest clustered sites as well as at the two northernmost sites, and 4.5% at the rest of the sites (with the intent to distribute the capacity of the wind farms poorly), the 5th and 95th percentiles and the standard deviation of the hourly step-change function are 6% and 8% lower, respectively. Indicating that the wind power capacity distribution matters.

It is expected that the results would be different for other case studies. The magnitude of the smoothing due to spatial distribution of wind farm capacities depends on the magnitude of the coherences and the details of the shape of the PSD curves. Other locations with e.g. simpler terrain are expected to have larger coherencies. On the other hand, larger regions have the advantage to be able to scatter wind farms to a larger extend.

Specific comments:

- Title: "... to minimize the overall power fluctuations ..." maybe it would be better to rephrase it a bit, e.g. with something like: "... minimize the power fluctuation at selected frequencies ..." This more accurate. Thank you for your suggestion. The title is being changed to: "Optimization of wind farm portfolio to minimize the overall power fluctuations at selected frequencies a case study for the Faroe Islands"
- Abstract: "The focus is mainly on the smoothing effect in highest resolvable frequencies." it would be nice to add a brief explanation for why these frequencies are relevant.

The following is added to the sentence: "The focus is mainly on the smoothing effect in the 1-3 hourly scale, where the coherency between wind farm power outputs is expected to be dependent on how the regional weather travels between local sites, making optimizations of wind farm portfolios relevant – in oppose to a focus on either lower or

higher frequencies in the scale of days or minutes, respectively, where wind farm power output time series are expected to be either close to fully coherent due to the same weather conditions covering a small region or not coherent as the turbulence for separate wind farm locations are expected to be uncorrelated. Results show that an optimization of ..."

• Abstract: "decrease the 1-3 hourly fluctuations considerably" – it would be better to be more quantitative.

Understood. That was actually the intent of the last line in the abstract. For clarification, more information is added. The end of the abstract is changed to the following:

"However, choosing optimized combinations of the individual wind farm site locations decreases the 1-3 hourly fluctuations considerably. For example, selecting a portfolio with four wind farms (out of the fourteen pre-defined wind farm site locations) results in 15% lower 5th and 95th percentiles of the hourly step change function when choosing optimal wind farm combinations compared to choosing the worst wind farm combinations. For an optimized wind farm portfolio of seven wind farms, this number is 13%. Optimized wind farm portfolios consist of distant wind farms, while the worst portfolios consist of clustered wind farms."

- •Line 94 The authors should explain why that height was selected. Is it the turbine's hub height? Yes. This height is chosen, because all currently operating wind turbines in the Faroe Islands have a hub height of 45 m a.g.l. (this explanation is added in the revised version). (Additional information: currently constructed wind farms/future planned wind farms consist of/will consist of taller wind turbines. This information is not considered in this study, but instead, given as future study suggestions at the end of the manuscript).
- Line 96 Please motivate the choice of this turbine and give at least some minimum specifics like the hub height and the rated power.

OK. Additional information is added to this paragraph (but the hub height is added to the paragraph above):

"The wind speed time series are modeled to power output time series using the power curve of an Enercon E-44 wind turbine with storm control function (Enercon, 2012), having a rated power of 0.9 MW. This turbine model is chosen because most of the currently operating wind turbines in the Faroe Islands are of the type Enercon E-44 (25 out of 28 turbines)."

• Line 108 – Please indicate the overall duration of the signal and the chunks. The following paragraph is added:

"The length of the chunks is a compromise between the accuracy of the PSD estimates (smaller chunks, i.e., more chunks) and the frequency resolution and the lowest resolvable frequency (longer chunks). In this study, a length of 256 data points is chosen (10 days and 16 hours), giving a number of 135 overlapping chunks for two-year hourly time series. The PSD estimates will therefore be generated for frequencies between $(256 \text{ h})^{-1}$ (Thus, including PSD estimates for the 3-4 day period of the time scale of migratory low-pressure systems at mid and high latitudes) and the Nyquist frequency of $(2 \text{ h})^{-1}$, with a resolution of $(256 \text{ h})^{-1}$."

- Line 210 It would be nice to link this to the findings of previous studies. This sentence is added: "These characteristics are similar to results observed by e.g. Katzenstein et al. (2010) and Beyer et al. (1993), who analyzed the variability of interconnected wind power time series, spatially dispersed in the area of Texas and northwest Germany, respectively."
- Line 269 The paragraph on future work is a bit superficial. Possibly it should be extended or at least better argumented. Agreed. Initially, we suggested two future works. Now the outlook focuses only on the first suggestion, with more details and argument for why this given future work is interesting.

Technical corrections:

- The labels or at least the captions of the PSD plots should specify what quantity is considered and its physical dimensions (or if normalized it should be mentioned). Also, I think that adding gridlines to the plots would help their interpretability.
 - Grid lines are added to all figures (excluding the maps). All time series are normalized with respect to the installed wind power capacity (except in the appendix). All the captions for these figures now mention that they represent "hourly wind power output time series per installed capacity $\left(\frac{P}{P_{inst}}\right)$ ". And $\left(\frac{P}{P_{inst}}\right)$ " is added to the label of all PSD plots.
- •I could find several typos and a few small mistakes in the use of English. I will only list a few here, but please check the manuscript thoroughly before submitting the revised version. Thank you. The below typos have been corrected, and so are additional typos and mistakes found when going through the manuscript again.
- Abstract: "5th and 95th percentiles" specify "of the hourly step-change functions". Thanks! "of the hourly step-change functions" is now specified in the abstract.
- Line 37 extent Thanks, this is now corrected
- Line 42 recent Thanks, this is now corrected
- Line 58 geography Thanks, this is now corrected
- Line 60 is available I cannot find this in the manuscript
- Line 162 constraint Thanks, this is now corrected
- Line 210 pronounced Thanks, this is now corrected
- Line 270 planned Thanks, this is now corrected

4.5 A note on the coherency between pairs of wind farm power output data at various frequency ranges

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The focus of this wind farm optimization study has been to minimize the two-three hourly fluctuations of the overall power output time series. As argued in the Introduction, and observed in the results, optimized wind farm portfolios yield less fluctuations at these frequencies. For longer periods, longer that a few days, results in section 4.3 established that there were limited smoothing effect for any wind farm combinations in the region. The focus of this subsection is on the smoothing effect for frequencies in between these two.

High wind speeds are associated with high standard deviations, thus high spectral values, as the integral of the spectral values over frequency equals about half of the variance of the time series. And since the spectral values are higher for lower the frequencies, in the considered frequency range, it can be expected that the PSD with the smallest spectral values at the lower frequencies are correlated to time series with smaller standard deviations and smaller wind speeds, thus smaller capacity factors. This is not desirable, as minimizing the fluctuations of the overall wind power output time series should not be at the cost of lower power production. Therefore, instead of looking at the PSD, this subsection will focus on the coherence function between pairs of wind turbine power output time series.

There is a connection between the coherency between time series and the smoothing effect of their combined time series.

The higher the coherence, the less the smoothing. For a coherence value of one, there will be no smoothing of the combined time series, while a coherence of zero means that the time series are uncorrelated, and the fluctuations of the combined time series will be less with respect to produced power.

Fig. 10 displays the squared coherence functions for all possible site-pairs of turbine power output time series, out of the fourteen favourable wind farm locations locations marked in Fig. 2, with respect to inter-site distances. At the lower frequencies, the coherences are high, consistent with that the same weather systems travel across the entire region. As the frequencies increase, the coherence values decrease, which is why from figure 7 in subsection 4.3, it was observed that the smoothing effect from combining wind farms is more evident for the higher frequencies. Another general characteristics that can be observed from Fig. 10 is that the closer the inter-site distances are, the higher their coherence value are, consistent with that the wind flow has had less time to change when traveling between two closer wind farm sites, which is why in subsection 4.4, optimized wind farm portfolio are combinations of distant wind farms.

To examine the potential smoothing effect for fluctuations at selective periods when combining wind farm power output time series, the average squared coherences between selected frequency ranges are extracted from Fig. 10 and displayed in Fig. 11 with respect to inter-site distances between site-pairs. As expected, the same general characteristics can be observed: higher coherence values for closer wind farms, higher coherence values at lower frequencies, and decreasing coherence values with increasing frequencies. The average squared coherence values for $\frac{1}{3h} < f < \frac{1}{2h}$ decrease rapidly with inter-site distance and are already below 0.02 for all pair of time series having inter-site distances larger than 10 km. This means that in order to minimize the 2-3 hourly fluctuations of aggregated wind farm power output time series, all wind farms in the portfolio should be placed at least 10 km apart from each other. In order to do so in a small region, and at the same time include several wind farms in the

portfolio, most of the spatial area in the region has to be utilized. Although comparable less, the average squared coherence for $\frac{1}{9h} < f < \frac{1}{6h}$ also decrease rapidly with inter-site distances, reaching a value around 0.05 for an inter-site distance of 30 km. This means that there are still possibilities for a maximum smoothing effect of 6-9 h hourly fluctuations for optimized wind farm portfolios consisting of a few wind farms, having in mind that the largest inter-site distances are around 90 km.

The squared coherence values for $\frac{24}{3h} < f < \frac{1}{16h}$ and $\frac{1}{72h} < f < \frac{1}{48h}$ decrease comparably more slowly with frequency, and the values are scattered. The lowest squared coherence values for $\frac{24}{3h} < f < \frac{1}{16h}$ and $\frac{1}{72h} < f < \frac{1}{48h}$ are 0.16 and 0.36, respectively. Although, a smoothing effect at these frequencies should be observed for combinations of two time series with low coherence values, combining more that a couple of wind farms in a wind farm portfolio is assumed to have limited smoothing effect for the these frequency ranges in the given region. And optimized wind farm portfolios consisting of more than a couple of wind farms are speculated to be determined by the standard deviation of the power output time serious at the expense of the total power production, rather than the combination of wind farms with low coherence values. The trend of the decrease of the squared coherence values with inter-site distance is is observable. By extrapolating, it is expected that optimized wind farm portfolios consisting of multiple wind farms could have a high daily smoothing effect at larger regions without the expense of total power production.

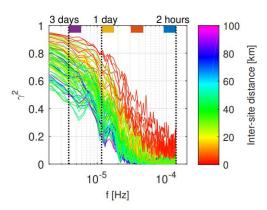


Figure 10. Squared coherence functions for all possible sitepairs out of the fourteen turbine power output time series, placed at the favourable wind farm locations marked in Fig. 2 (a total of 91 pairs). The colors of the coherence functions represent the distances in km between site-pairs, see colorbar. The four colors marked at the top of the figure are added to mark the frequency ranges considered in Fig. 11.

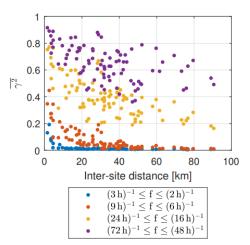


Figure 11. The average squared coherence for frequencies between $(3 \text{ h})^{-1}$ and $(2 \text{ h})^{-1}$ (blue color), $(9 \text{ h})^{-1}$ and $(6 \text{ h})^{-1}$ (red color), $(24 \text{ h})^{-1}$ and $(16 \text{ h})^{-1}$ (yellow color), and $(72 \text{ h})^{-1}$ and $(48 \text{ h})^{-1}$ (purple color), with respect to inter-site distance for all site-pairs considered in figure 10. The considered frequency ranges are marked in figure 10.