



1 Towards Smart Blades for Vertical Axis Wind Turbines: Different 2 Airfoil Shapes and Tip Speed Ratios

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8 **Abstract.** Future wind turbines will benefit from state-of-the-art technologies that allow them to not only operate efficiently in any
 9 environmental condition, but also to maximize the power output and cut the cost of energy production. Smart technology, based
 10 on morphing blades, is one of the promising tools that could make this possible. The present study serves as a basis for identifying
 11 morphing airfoils as functions of azimuthal angle and tip speed ratio for vertical axis wind turbines. The focus of this work is on
 12 the combined analysis of three airfoil shape-defining parameters, namely the maximum thickness t/c and its chordwise position
 13 xt/c as well as the leading-edge radius index I . A total of 126 airfoils are generated. The analysis is based on 630 high-fidelity
 14 transient CFD simulations, validated with three experiments. The results show that with increasing λ , the optimal maximum
 15 thickness decreases from 24% c to 10% c , its chordwise position shifts from 35% c to 22.5% c , while the corresponding leading-edge
 16 radius index remains at 4.5. The results show an average improvement of nearly 0.06 in C_p for all the values of λ .

17 **Keywords.** Smart rotor design; Morphing airfoil; Shape adaptation; wind energy; Computational fluid dynamics (CFD).

18 Nomenclature

α	Angle of attack [°]	k	Reduced frequency, $\Omega c/2V_{ref} \approx c/2R$ [-]
α_{ss}	Static stall angle [°]	L	Lift [N]
θ	Azimuth angle [°]	M	Turbine moment [Nm]
λ	Tip speed ratio, $R\Omega/U_\infty$ [-]	n	Number of blades [-]
ν	Kinematic viscosity of air [m ² /s]	P	Turbine output power [W]
σ	Solidity, nc/d [-]	q	Dynamic pressure [Pa]
Ω	Turbine rotational speed [rad/s]	R	Turbine radius [m]
A	Turbine swept area, $h.d$ [m ²]	Re_c	Chord-based Reynolds number, $cU_\infty\sqrt{1+\lambda^2}/\nu$ [-]
c	Airfoil chord length [m]	r_{LE}	Airfoil leading-edge radius [% c]
C_d	Drag coefficient, D/qA [-]	T	Turbine thrust force [N]
C_f	Skin friction coefficient, D/qA [-]	t/c	Airfoil relative maximum thickness [%]
C_l	Lift coefficient, L/qA [-]	U_∞	Freestream velocity [m/s]
C_m	Moment coefficient, $M/(qAR)$ [-]	U	Instantaneous streamwise velocity [m/s]
C_p	Turbine power coefficient, $P/(qAU_\infty)$ [-]	V	Instantaneous lateral velocity [m/s]
C_T	Turbine thrust coefficient, $T/(qA)$ [-]	$V_{tan,n}$	Dimensionless instantaneous tangential velocity, $(ucos(\theta)+vsin(\theta))/U_\infty$ [-]
D	Drag [N]	V_{rel}	Relative velocity [m/s]
h	Turbine height [m]	xt/c	Dimensionless chordwise-position of airfoil maximum thickness [%]
I	Airfoil leading-edge radius index [-]	TI	Turbulence intensity [%]

19 1. Introduction

20 1.1 State of the art

21 Morphing technology has the potential to improve the performance of flying bodies by adapting their shape to different operational
 22 conditions. This can result in improved aerodynamic efficiency and the release of unwanted stresses [1, 2]. Nature has given birds



23 the capability of continuous morphing to generate enough lift for various flight maneuvers. These bio-inspired sources served
24 as models for possible morphing vehicles and provided the pioneering researchers with a new method of improving aerodynamic
25 efficiency [3]. However, because of the technological limitations of the day, it was not possible to reach the level of smooth shape-
26 changing capabilities as seen in birds. This led to the development of shape-changing by using ailerons, slats, flaps or variable
27 sweep [1]. Nowadays, advances in smart technologies have enabled such needs to be satisfied. Wing morphing is used in the
28 aerospace industry to improve the aerodynamic efficiency and adaptability of aircraft [4-8], helicopters [9-12], micro air vehicles
29 [13-17] and unmanned air vehicles [18-21]. In contrast, the blades of wind turbines operate at relatively low wind speeds with a
30 low level of risk. Nevertheless, morphing technology can still be of benefit for wind turbine purposes without the challenges that
31 must be overcome in aerospace applications (e. g., increasing weight and complexity) [22]. For horizontal axis wind turbines
32 (HAWTs), the impact of morphing blades on load control has been studied by [23-33].

33 The angle of attack α of a vertical axis wind turbine (VAWT) blade varies periodically between positive and negative values.
34 Through this quasi-sinusoidal variation of α , it exceeds the static stall angle, α_{ss} , and the blade undergoes unsteady separation,
35 resulting in the occurrence of dynamic stall and hysteresis effects on aerodynamic loads [25, 34-37]. When a turbine is operating
36 at low λ , it benefits from the early stages of dynamic stall; that is, the performance of the blade increases due to an overshoot in
37 lift coefficient C_l ; however, the overall power output is affected negatively by the consequential sudden drop in C_l [38, 39]. This
38 sophisticated aerodynamics makes the development of a single optimal airfoil for VAWTs a challenging process.

39 To this date, the performance of VAWTs, which very often use airfoils used in the helicopter industry [40, 41], has been studied
40 for airfoil parameters as proposed in [42-46]. More recently, a few studies have been conducted to improve VAWTs performance
41 via optimizing the airfoil [47-49]. This dependency of VAWT performance on airfoil shape means that the design of morphing
42 blades, which can adapt their shapes to variables such as azimuthal angle θ and λ is worth pursuing. In other words, as the airfoil
43 morphs into a new geometry due to changes in azimuthal position or wind speed, the separation point will move to an optimal
44 coordinate. As a result, flow detachment can be reduced or delayed to higher α , and severe dynamic stall can be controlled or even
45 avoided in the case of unsteady separation at low λ , resulting in improved aerodynamic and power performance [39, 50].

46 Detailed analysis of the literature shows that the majority of studies focused on morphing trailing edges. For example, experimental
47 [51] and numerical [52] studies show that morphing the trailing edge results in significant power regulation and aerodynamic load
48 reduction. In another work [53] a deformable trailing edge was discovered to improve the power output of VAWTs. [50] showed
49 that morphing aileron improves the aerodynamic performance of VAWTs. In a numerical study, it was found that the airfoil
50 parameters have a substantial impact on the power performance of VAWT operating in the dynamic stall regime [39].

51 Despite the existence of this reported literature, several shape-defining parameters have received much less attention. Such
52 parameters are hypothesised to have an influence on boundary layer events and the resultant aerodynamic loads. Therefore, a
53 parametric analysis of these variables, with their potential to morph, would provide fundamental knowledge towards designing
54 morphing blades for smart VAWTs.

55 1.2 Objectives

56 The present work follows the objectives below:

- 57 i. To pave the road towards smart blades for VAWTs, having the capability of adaptation to different operational conditions.
- 58 ii. To provide a set of generalizable conclusions from 630 transient simulations for 126 identical airfoils, generated with
59 different values of maximum thickness t/c , chordwise position of maximum thickness xt/c , and leading-edge radius index I
60 at 5 different tip speed ratios λ ; and thus, understand the impact of different morphing blade scenarios on the turbine power
61 performance C_P as well as the thrust performance C_T .



62 The reference airfoil is chosen from the symmetric modified NACA four-digit series. The morphing airfoils are generated through
 63 changing the combination of the three aforementioned parameters. An unsteady Reynolds-Averaged Navier-Stokes (URANS)
 64 approach, validated with experimental data, will be used for the analysis. The results will provide a set of optimal airfoils at each
 65 λ , as well as each azimuth angle, and thus, making a conceptual step towards designing morphing blades for VAWTs.

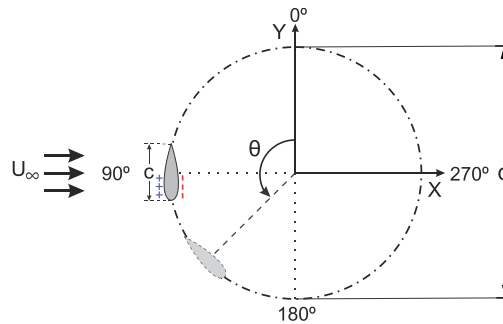
66 1.3 Paper outline

67 The paper is organized as follows: Sect. 2 presents the computational settings and parameters for the simulations. The solution
 68 verification and validation studies are also included. Sect. 3 introduces the generated airfoil shapes. In Sect. 4, the results are
 69 presented in two scenarios. Sect. 5 and 6 are devoted to the discussion and conclusions.

70 2. Computational settings and parameters

71 2.1 Reference turbine characteristics

72 A single-bladed Darrieus H-type VAWT was chosen as the reference case for this study (see Table 1 and Fig. 1). The turbine is a
 73 simplified representation of the original one used by [54]. That is, the turbine shaft and spokes are removed, and there is only one
 74 blade. Note that the conclusions are not significantly affected by these components. The reader is referred to our earlier works [55,
 75 56] where it is shown that for low solidity VAWTs, the power performance is almost independent of the shaft and number of
 76 blades. Therefore, such a simplified turbine model can effectively reduce the computational costs of the huge number of simulations
 77 (i. e., 630 transient simulations) for the present work and, at the same time, provide reliable results. Refs. [56, 57] are used to select
 78 the rest of the geometrical and operational characteristics of the reference turbine.



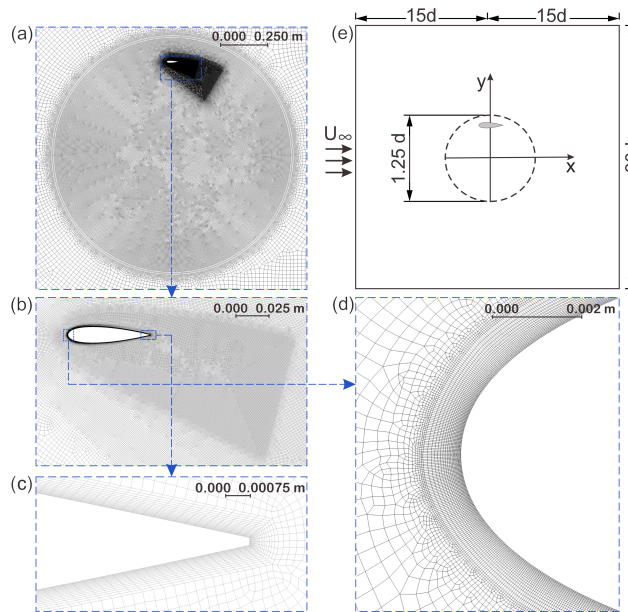
79
 80 **Figure 1: The reference turbine (not to scale). (+): airfoil pressure side and (-): suction side for $0^\circ \leq \theta < 180^\circ$.**

81 **Table 1: Characteristics of the reference turbine.**

Turbine type	Darrieus H-type
N	1
D	1 m
σ	0.06
Airfoil shape	NACA0018-6.0/3.0 (i.e., baseline NACA0018)
	$t/c = 18\%$; $I = 6.0$; $xt/c = 30\%$
Blade/Spoke connection point	$c/2$
U_∞	9.3 m/s
Λ	2.5, 3.0, 3.5, 4.5, 5.0
Ω	46.5, 55.8, 65.1, 83.7, 93.0 rad/s
C	0.06 m
$Re_c [\times 10^5]$	1.03, 1.20, 1.40, 1.76, 1.95
TI	5%

82 2.2 Computational settings

83 The commercial flow solver ANSYS Fluent v2019R2 is employed for the 2D incompressible URANS simulations coupled with
 84 the four-equation transition SST turbulence model. The simulations are solved using second-order spatial/temporal discretization
 85 and the SIMPLE pressure-velocity coupling scheme. The computational domain, grid, and boundary conditions are summarized
 86 in Table 2. The schematic of the computational domain and the computational grid and its subregions are shown in Fig.2.
 87 The turbulence model is selected based on our previous findings [58-60]. Best-practice guidelines for the CFD simulations of
 88 VAWTs are used to select the domain size, the azimuthal increment, and the convergence criterion [61]. The corresponding
 89 absolute time-step values are $3.75339546 \times 10^{-5}$ s, $3.12782955 \times 10^{-5}$ s, $2.68099676 \times 10^{-5}$ s, 2.0852197×10^{-5} s and $1.70608885 \times 10^{-5}$
 90 s for $\lambda = 2.5, 3.0, 3.5, 4.5$ and 5.5 , respectively. With the selected $d\theta = 0.1$, 3600 time-steps per turbine revolution are achieved. A
 91 total number of 20 revolutions, i.e., 72,000 time-steps, are simulated before the results of the present study are obtained at the 21st
 92 turbine revolution. Under these conditions, the statistical convergence of the transient simulations is ensured. In each case, a
 93 number of 20 iterations per time-step is performed so that the scaled residuals stay $< 10^{-5}$.



94
 95 **Figure 2. (a-d) the grid; and (e) schematic of the computational domain (not to scale).**

96 **Table 2: Details of computational domain, grid, and boundary conditions.**

Computational domain (see Fig. 2e)	$30d \times 30d$ (d: turbine diameter)
Computational grid (see Fig. 2a-d)	Cell type: quadrilateral Cell No.: 302,815 No. of cells around the airfoil circumference: 800 $y_{max}^+ < 2.5$
Boundary conditions	Inlet: uniform normal velocity (Turbulence length scale = d); Outlet: zero static gauge pressure;

97 **2.3 Solution verification and validation**

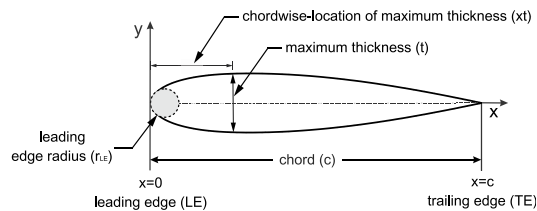
98 The domain type is selected based on our earlier studies, where the difference between 2D and 2.5D URANS simulations was
 99 found to be insignificant [57]. A grid convergence analysis using uniformly-doubled grids has been performed and documented in
 100 Ref. [62], which for brevity is not repeated here. Three experimental studies with different test conditions are used to validate the
 101 CFD simulations. The different geometrical and operational characteristics of the turbines used in the experiments led to dissimilar

102 conclusions [25, 54, 63], ensuring a high level of confidence in the accuracy of the CFD simulations. However, the reader is
 103 referred to Ref. [59] for more detailed descriptions of the validation studies.

104 3. Morphing airfoil shapes

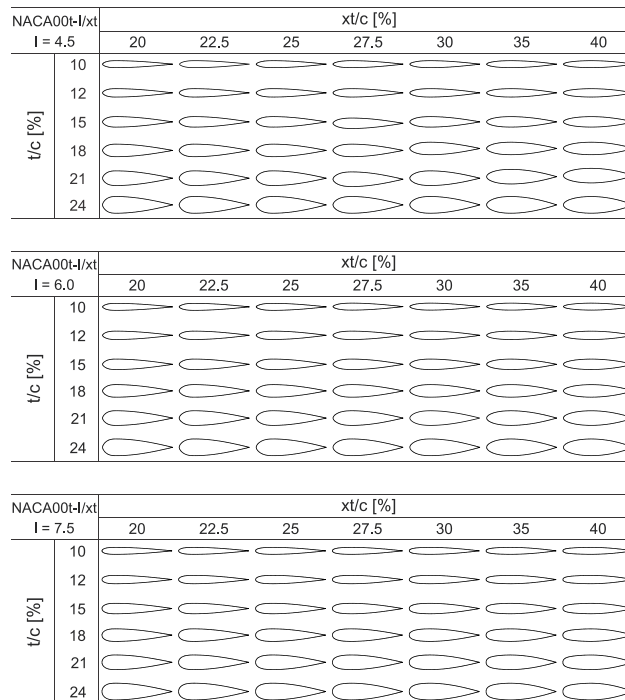
105 Figure 3 shows a schematic drawing of the symmetric modified NACA 4-digit airfoil and the selected shape-defining parameters
 106 for this study. These parameters are morphed within their most common regimes as follows:

- 107 (i) relative maximum thickness (t/c): 10, 12, 15, 18, 21 and 24%;
- 108 (ii) relative chordwise position of maximum thickness (xt/c): 20, 22.4, 25, 27.5, 30, 35 and 40%;
- 109 (iii) index of leading-edge radius (I): 4.5, 6.0 and 7.5.



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Figure 3: Defining parameters of the symmetric airfoil.



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Figure 4: Studied airfoil shapes.

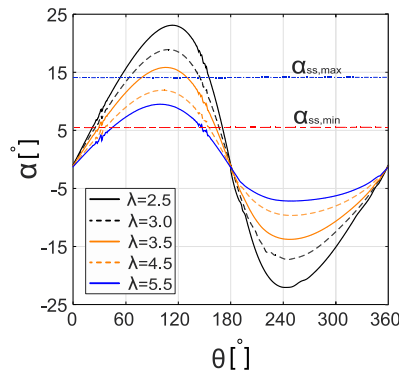
114 Note that any value of I out of the selected range results in a too sharp or too blunt leading edge. The analysis is based on 126
 115 airfoil shapes (see Fig. 4). The modification of the airfoil coordinates and the related equations are documented in Ref. [39]. The
 116 focus of this study is on symmetric airfoils with zero camber. The morphing airfoils are designated as the $NACA00t/c - I / xt/c$.
 117 The first symbol from left to right, i.e., t/c , represents the maximum thickness in %c; the second one, I , shows the index of leading-
 118 edge radius (with one decimal precision); and the third one, xt/c , is the chordwise position of the maximum thickness in 10th of the



119 chord with two decimal precision. For example, the NACA0024-4.5/3.50 has a maximum thickness of $t/c = 24\%$, located at $xt/c =$
120 35% , and a leading-edge radius index of $I = 4.5$.

121 4. Results

122 The results are presented in two scenarios, namely, morphing airfoils as functions of λ (Sect. 4.1), and $d\theta$ (Sect. 4.2). In Sect. 4.3
123 the performance of the morphing airfoils from the first scenario is compared with that of the reference airfoil. A coupled analysis
124 is performed at different λ of 2.5, 3.0, 3.5, 4.5 and 5.5. Figure 5 depicts the variation of α as the turbine passes through its last
125 revolution. Note that the higher the value of λ is, the more limited the variation of α is. For $\lambda = 2.5, 3.0$ and 3.5 the variation of α
126 exceeds the α_{ss} for all the studied airfoils, while at higher $\lambda = 4.5$ and 5.5 , not for all the studied airfoils the same event is observed.
127 The reader is referred to [57], where the method of calculating the α from the CFD results is provided in detail.



128
129

Figure 5: α versus θ for different λ . The $\alpha_{ss,min}$ and $\alpha_{ss,max}$ are based on Xfoil.

130 4.1 Morphing the airfoil shape-defining parameters

131 To derive the optimal airfoil for each λ , the combination of the t/c_{opt} , xt/c_{opt} , and I_{opt} , corresponding to the turbine $C_{P,max}$ is
132 determined. Sect. 4.1.1 to 4.1.3 are devoted to the discussions on individual morphing, and Sect. 4.1.4, presents an overall view on
133 the combined morphing of the aforementioned parameters.

134 4.1.1 Morphing the maximum thickness (t/c)

135 Figure 6 shows the impact of morphing t/c on the turbine C_P for the studied range of xt/c , I and λ . Figure 7 shows the instantaneous
136 moment coefficient C_m versus θ for selected t/c and xt/c . It can be observed that:

137 *Regarding the lowest value of $I = 4.5$ (see Fig. 6a – e and Fig. 7):* Generally speaking, the trend of $C_P - t/c$ for different λ is similar,
138 except for some noticeable differences. That is, by increasing λ , the C_P shows higher sensitivity to t/c . This is reflected as higher
139 $|\Delta C_P|$ and can be due to the following reasoning: by morphing t/c , the pressure gradient changes over the airfoil; therefore, the
140 transition point, the separation and stall characteristics, and eventually the resultant aerodynamic loads also change. However,
141 when the flow is fully separated in the post-stall regime, morphing t/c has no longer significant impact on C_P . By increasing λ , and
142 thus, more limited variation of α , the blade passes over a range of fewer azimuth angles in the post-stall regime (see Fig. 5). Due
143 to this, morphing the t/c is influential within a wider range of effective θ . This can be recognized by the improved C_P for higher λ .
144 At $\lambda = 2.5$, the C_P follows a polynomial trend for $xt/c \leq 30\%$, and a monotonic upward trend for $xt/c \geq 35\%$. Nevertheless, with the
145 exception of $xt/c \leq 22.5\%$ at $\lambda = 5.5$, where the C_P monotonically decreases by increasing t/c , the trend remains polynomial for
146 different values of xt/c at the studied range of λ . That is, by positive morphing of t/c , the C_P experiences an initial growth to its

147 maximum value at t_{opt}/c , followed by a reduction for $t/c > t_{opt}/c$. This can be recognized from the C_m plots, where by morphing t/c
 148 to its optimal value at t_{opt}/c , the sudden drop in $C_{m,max}$, which indicates the instant of moment stall, is observed at higher θ ; the
 149 consequent fluctuation is alleviated, and the overall value of C_m increases, thus, making consistency with the highest C_P at t_{opt}/c
 150 for a fixed xt/c (see Fig. 7a-i for selected xt/c). This can be attributed to the following observations from the skin friction, lift, and
 151 drag coefficients (C_f , C_l , and C_d): when the turbine is operating at low values of $\lambda \leq 3.5$, increasing t/c from 10% to t_{opt}/c , changes
 152 the stall type from leading-edge stall and thin-airfoil stall for $t/c \leq 12\%$ to trailing-edge stall for moderate- and high-thickness
 153 airfoils with $t/c \geq 15\%$; an earlier formation of laminar separation bubble (LSB) and trailing-edge separation (TES) is observed;
 154 TES-LSB merging (i. e., full-flow separation) is discovered to occur at higher azimuth, indicating a more extended favorable
 155 pressure gradient for t_{opt}/c ; the dynamic stall characteristics (i. e., jump in lift and drag coefficients, and post-stall load fluctuation)
 156 are significantly reduced; and the deviation in lift and drag, which indicates the onset of dynamic stall, shifts to higher azimuth.
 157 However, an earlier stall is found to occur for $t/c > t_{opt}/c$ due to more pronounced earlier merging of TES-LSB. This is reflected by
 158 lower C_P and $C_{m,max}$ for $t/c > t_{opt}/c$ (see Figs. 6a-c and 7a-i). Note that the monotonic growth in $C_P - t/c$ for $xt/c \geq 35\%$ at $\lambda = 2.5$
 159 can also be explained with the aforementioned reasoning, yielding the $C_{P,max}$ at the highest thickness of $t_{opt}/c = 24\%$ (see Fig. 6a).
 160 For brevity, the skin friction, lift, and drag coefficients are not presented here.

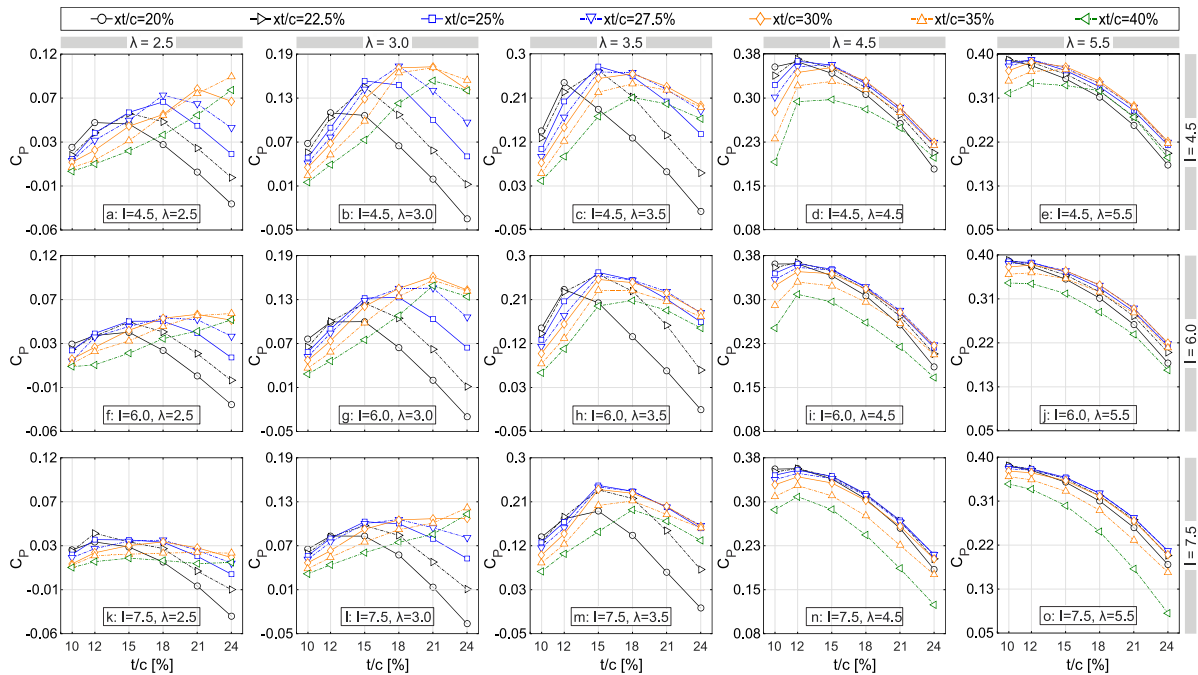


Figure 6: Impact of morphing t/c on the turbine C_P at different xt/c and λ .

163 Table 3 shows the t_{opt}/c , corresponding to each xt/c (i. e., $t_{opt,xt/c}$) at different λ . The t_{opt}/c corresponding to each λ is indicated by a
 164 star sign. It can be seen that by increasing xt/c , which means a longer favorable pressure gradient on the blade, a higher thickness
 165 is needed for the airfoil to be optimal. Note that, increasing λ , influences the shape of the optimal airfoil by decreasing its thickness.
 166 In other words, the higher λ is, the thinner the optimal airfoil is. This is consistent with the findings documented in [45, 64], where
 167 it shows the superior performance of thick airfoils at low λ . This may be attributed to the turbine operational regime as follows:
 168 When the turbine goes into regimes with higher λ and more pronounced reduction in the variation of α , higher values of C_l at lower
 169 α is of most impact on the turbine C_P . Therefore, thinner airfoils with a higher lift curve slope outperform the thicker ones with a



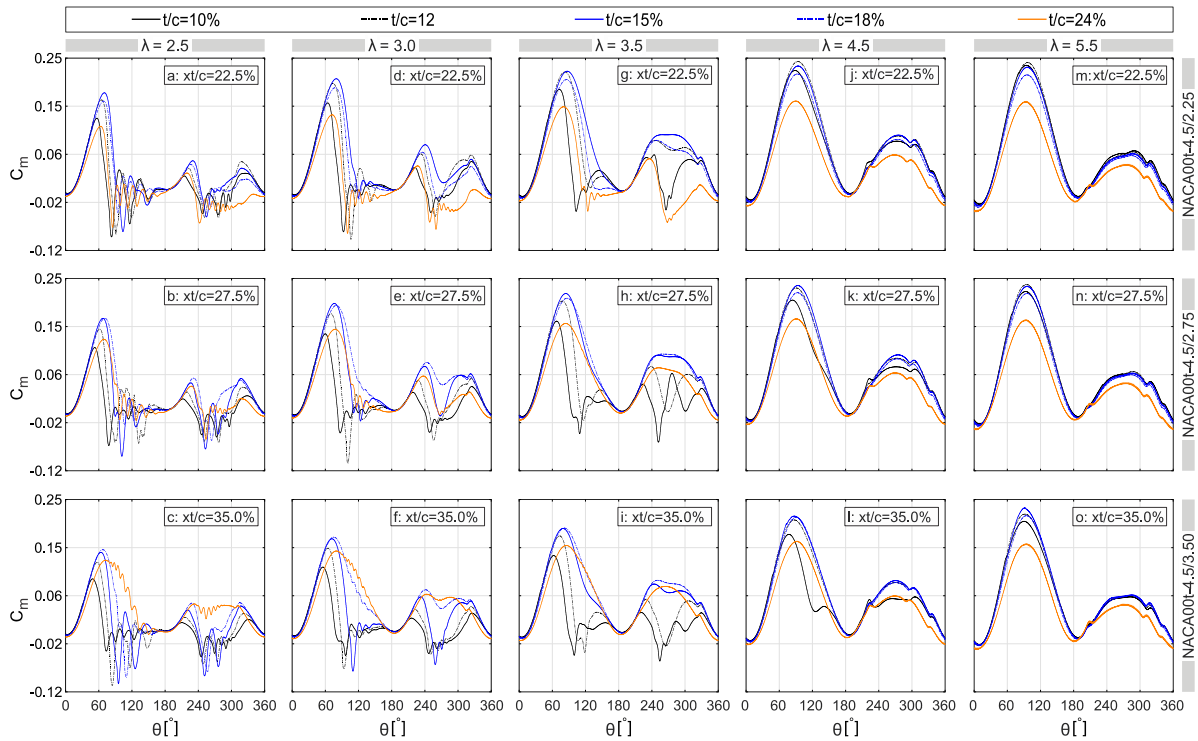
170 lower slope of the $C_l - \alpha$. Eventually, this results in less pronounced sensitivity of the t_{opt}/c to xt/c , and shifting the peak in $C_P - t/c$
 171 (i. e., t_{opt}/c) towards the lowest $t/c = 10\%$ and 12% in the non-dynamic stall regime with $\lambda \geq 4.5$ (see Table 3). The analysis also
 172 shows a drag increment for thicker airfoils at $\lambda = 4.5$ and 5.5 , which is a result of the earlier formation of LSB and TES. This is
 173 consistent with the reduction in C_P and $C_{m,max}$ for $t/c > t_{opt}/c$ (see Figs. 6d-e and 7j-o). Note that for $xt/c \leq 22.5\%$ at $\lambda = 5.5$ the same
 174 reasoning results in a monotonic decrease of C_P , yielding the $C_{P,max}$ at the lowest thickness of $t/c = 10\%$.
 175 Regarding the moderate and highest values of $I = 6.0$ and 7.5 (see Fig. 6f-j and 6k-o): The overall trend for C_P is very similar to
 176 that of the lowest $I = 4.5$; however, it shows comparatively lower values of $|\Delta C_P|$, especially for $\lambda \leq 3.5$. The impact of morphing
 177 the r_{LE} on the turbine C_P is separately discussed in detail in Sect. 4.1.3; therefore, it is not included here.

178

Table 3. $t_{opt,xt}/c$ for different values of xt/c and λ ($I = 4.5$).

λ	20	22.5	25	27.5	30	35	40	xt/c [%]
2.5	12	15	18	18	21	24*	24	$t_{opt,xt}/c$ [%]
3.0	12	15	15	18*	21	21	21	
3.5	12	15	15*	15	18	18	18	
4.5	12	12*	12	15	15	15	15	
5.5	10	10*	12	12	12	15	12	

* t_{opt}/c at the corresponding λ



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Figure 7: Impact of morphing t/c on the turbine C_m for selected xt/c and t/c at different λ .

181

4.1.2 Morphing the chordwise position of maximum thickness (xt/c)

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Figure 8 shows the variation of the turbine C_P versus xt/c at the studied range of t/c , I , and λ . Figure 9 shows the instantaneous moment coefficient C_m versus azimuth for selected xt/c and t/c . It can be seen that:

183



184 Regarding the lowest value of $I = 4.5$ (see Fig. 8a-e): The overall trend of $C_P - xt/c$ for different λ is very similar, except for the
 185 following differences. By increasing λ , the turbine C_P shows higher $|\Delta C_P|$. This is due to the similar reasoning discussed earlier in
 186 Sect. 4.1.1, and summarized as follows: morphing the xt/c results in changing the boundary layer and stall characteristics. On the
 187 other hand, increasing λ is associated with lower variation of α , i.e., a more limited azimuthal range of the post-stall regime. As a
 188 result, the impact of morphing xt/c becomes significant over a wider range of θ , resulting in improved C_P .
 189 For $t/c \leq 12\%$ in the dynamic stall regime with $\lambda \leq 3.5$, the C_P monotonically decreases by morphing the xt/c , yielding the $C_{P,max}$
 190 with the lowest xt/c of 20% (see Fig. 8a-c). However, apart from $t/c = 10\%$ at $\lambda = 4.5$, where C_P monotonically decreases, the trend
 191 for thin airfoils changes to polynomial at $\lambda \geq 4.5$ (see Fig. 8d-e). In other words, by morphing xt/c from 20% to 40%, the C_P grows
 192 to its maximum value at xt_{opt}/c , before decreasing for $xt/c > xt_{opt}/c$. On one hand, the monotonic behavior of C_P for thin airfoils at
 193 low λ can be explained based on the observations of the skin-friction coefficient C_f as follows: The dynamic stall for $t/c \leq 12\%$ is
 194 preceded by either (i) gradual extension of the LSB towards the trailing edge (thin-airfoil stall), or (ii) a sudden upstream
 195 propagation of the TES (leading-edge stall). Morphing the xt/c to higher values results in either an earlier downstream extension
 196 of the LSB, or an earlier formation and abrupt-upstream propagation of the TES; and consequently, an advanced stall on the blade.
 197 This is evident from the C_m plots for $t/c = 12\%$ (see Fig. 9a-c), where the abrupt drop in $C_{m,max}$ occurs at a lower θ , indicating an
 198 earlier moment stall due to increasing the xt/c . The overall lower values of C_m for higher xt/c justify the monotonic reduction in C_P .
 199 This can also be recognized from the C_l and C_d plots, where by increasing xt/c , the deviation in lift and drag coefficients occurs at
 200 lower azimuth, signaling an earlier dynamic-stall onset. For brevity, the C_f , C_l , and C_d plots are not presented here.

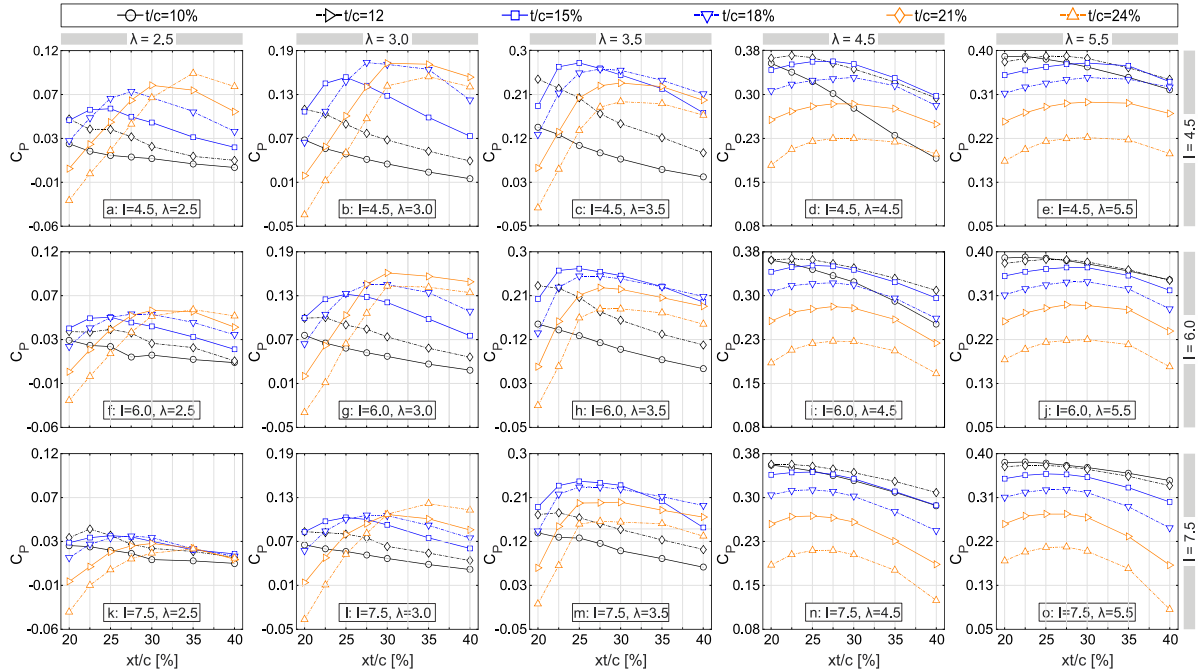


Figure 8: Impact of morphing xt/c on the turbine C_P at different t/c and λ .

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203 On the other hand, the polynomial trend of C_P for thin airfoils at $\lambda \geq 4.5$ (i. e., non-dynamic stall regime) can be recognized from
 204 the C_m plots. For example, by morphing xt/c from 20% to $xt_{opt}/c = 25\%$ for $t/c = 12\%$ $\lambda = 5.5$, the $C_{m,max}$ slightly increases before
 205 decreasing for $xt/c \geq 27.5\%$ (see Fig. 8e). This can be explained by the skin-friction coefficient C_f , where it shows an earlier
 206 formation and upstream propagation of the TES, and thus, an earlier stall for $xt/c > xt_{opt}/c$. Note that, when the adverse effects of

207 dynamic stall are suppressed at $\lambda \geq 4.5$, increasing xt/c shows a marginal positive impact on the C_P for thin airfoils, reflecting a
 208 polynomial trend of C_P versus xt/c . However, the value of t/c for thin airfoils plays a more crucial role in this regime. This can be
 209 observed from the sharp downward trend of $C_P - xt/c$ for $t/c = 10\%$ at $\lambda = 4.5$, while it changes to a polynomial trend for $t/c =$
 210 12% . This may be attributed to the more pronounced formation and propagation of TES, and thus, an earlier stall due to increasing
 211 xt/c for $t/c = 10\%$. However, the trend of $C_P - xt/c$ for t/c of 10% remains polynomial at $\lambda = 5.5$, showing less sensitivity to TES at
 212 higher λ . For brevity, C_f contour plots are not presented here.

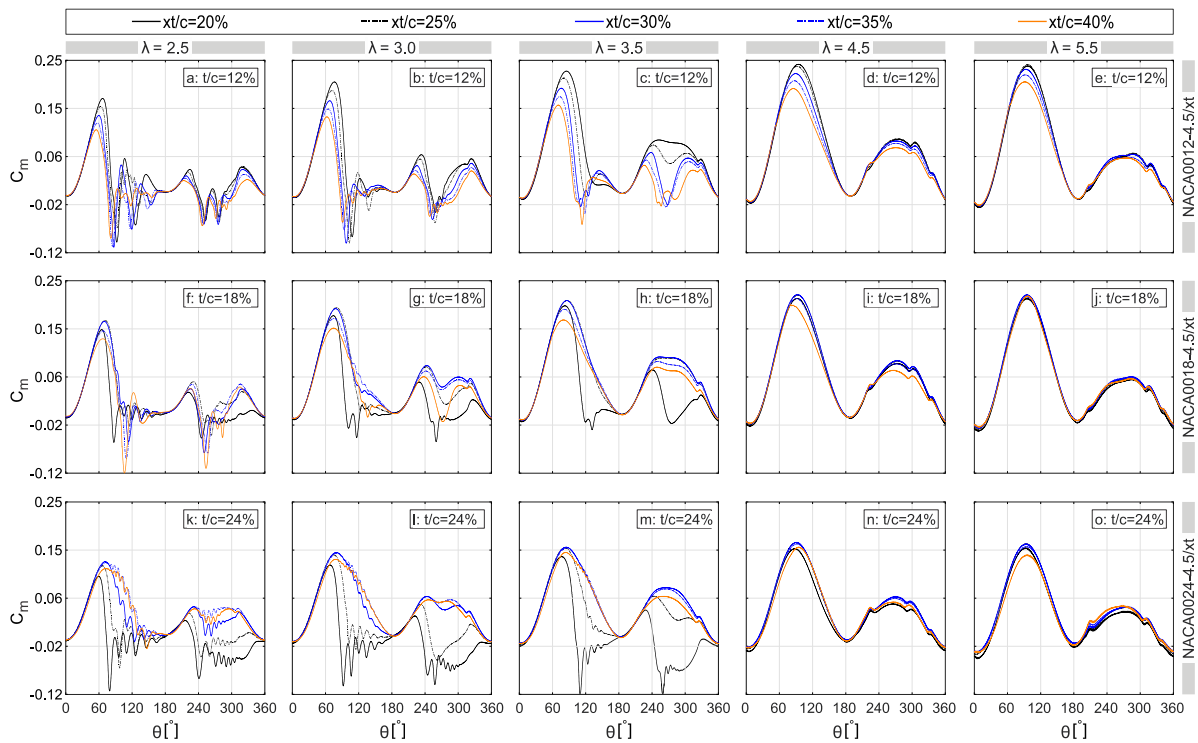


Figure 9: Impact of morphing xt/c on the turbine C_m for selected t/c and xt/c at different λ .

215 For the medium- and high-thickness airfoils (i.e., $t/c \geq 15\%$), the turbine C_P polynomially increases with xt/c (see Figs. 8a-e). As
 216 previously discussed in Sect. 4.1.1, this polynomial trend is a consequence of thicker-airfoil stall type, which is triggered by the
 217 formation of a flow reversal near the trailing edge [65-68]. Therefore, when xt/c morphs to its optimal value, the adverse pressure
 218 gradient becomes less severe, resulting in improved stall characteristics. This can be recognized by either dynamic stall alleviation
 219 at low values of $\lambda \leq 3.5$, or a postponed stall at non-dynamic stall regimes with $\lambda \geq 4.5$. Table 4 gives the $xt_{opt,t/c}$ (i. e., the $xt_{opt,c}$ at
 220 each t/c) in terms of $C_{P,max}$ for each λ . The corresponding $xt_{opt,t/c}$ for different λ is indicated by a star sign. For $\lambda \leq 3.5$, by increasing
 221 t/c , the $xt_{opt,t/c}$ also increases. However, by increasing λ from 2.5 to 3.5, and thus, encountering a comparatively lighter dynamic
 222 stall and more limited variation of α , the $xt_{opt,t/c}$ and its corresponding t/c decrease (see also Fig. 8). The reason for the
 223 outperformance of thin airfoils at higher λ is explained earlier in Sect. 4.1.1. Nevertheless, in the dynamic stall regime, the
 224 outperformance of moderate to high values of xt/c for thicker airfoils at a fixed λ is readily apparent from the turbine C_m for selected
 225 $t/c = 18\%$ and 24% (see Fig. 9f-h and k-m). It can be seen that increasing xt/c to its optimal value results in an increase in the C_m
 226 curve peak, a delay in the sudden drop of $C_{m,max}$, less pronounced subsequent fluctuations, and higher values of C_m in the turbine
 227 downwind quartile. This is due to either alleviated dynamic stall, and is more pronounced for $t/c = 24\%$ (see Fig. 9k-m). A further



228 increase in $xt/c > x_{top}/c$, is found to have a negative effect on C_m and finally leads to an earlier stall. This can be explained by the
 229 C_f contour plots, where increasing xt/c higher than x_{top}/c promotes the formation of LSB and TES, and results in an earlier full-
 230 flow separation and drop in $C_{l,max}$. Please note that for better illustration, the C_m plots are not presented for all the studied values of
 231 xt/c . For $\lambda \geq 4.5$, by morphing xt/c for $t/c \geq 15\%$, the C_P shows less sensitivity to xt/c and the corresponding x_{top}/c changes
 232 marginally (see Fig. 8d-e and Table 4). This is consistent with the turbine C_m plots for selected $t/c = 18\%$ and 24% , where the
 233 $C_{m,max}$ and the azimuth of moment stall are almost invariant to xt/c (see Fig. 9i-j and Fig. 9n-o).
 234 Regarding the moderate and highest values of $I = 6.0$ and 7.5 (see Fig. 8f-j and 8k-o): The $C_P - xt/c$ shows a similar trend to that
 235 of $I = 4.5$. However, in dynamic stall regime (i.e., $\lambda \leq 3.5$), the turbine C_P shows a considerably smaller $|\Delta C_P|$, especially for higher
 236 xt/c . On the other hand, in non-dynamic stall regime with $\lambda \geq 4.5$, a marginal reduction in $|\Delta C_P|$ is observed. However, the $C_P - xt/c$
 237 shows more pronounced sensitivity to morphing xt/c for the moderate and thick airfoils.

238

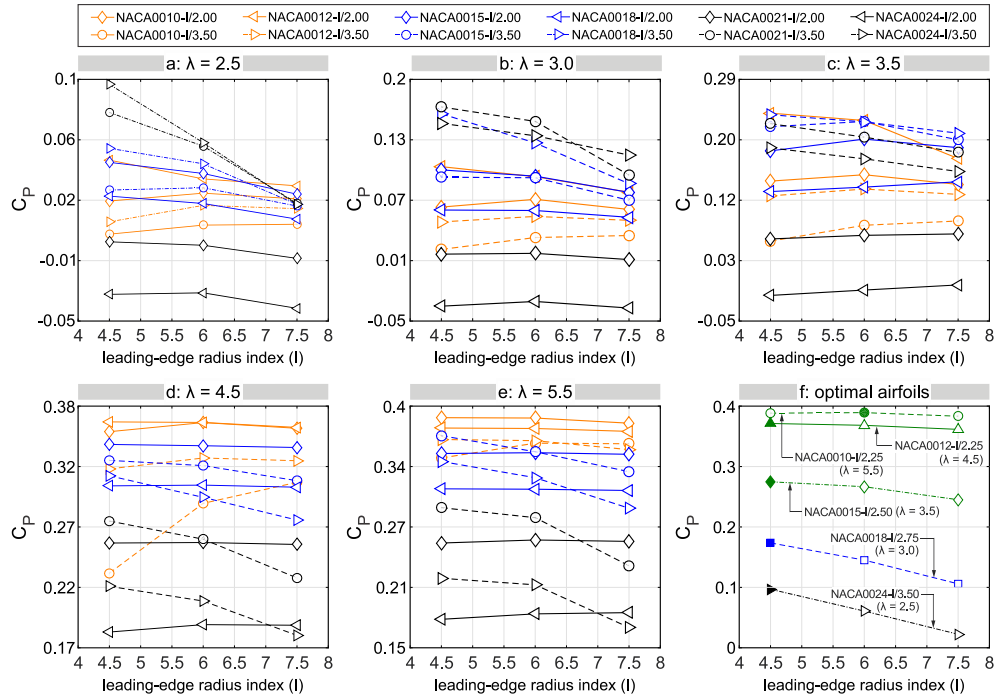
Table 4. x_{top}/c for $I = 4.5$ at different t/c and λ .

$\lambda \backslash t/c$ [%]	10	12	15	18	21	24	x_{top}/c [%]
2.5	20	20	25	27.5	30	35*	
3.0	20	20	25	27.5*	30	35	
3.5	20	20	25*	27.5	30	30	
4.5	20	22.5*	27.5	30	27.5	27.5	
5.5	22.5*	25	30	30	30	30	
* x_{top}/c at the corresponding λ							

239 4.1.3 Morphing the leading-edge radius (r_{LE})

240 Figure 10 shows the impact of morphing r_{LE} on the C_P for selected and optimal airfoils at different λ . Figure 11 shows a comparison
 241 of the $C_P - xt/c$ for different I and selected values of t/c . The analysis is grouped based on the maximum thickness as follows:
 242 Regarding the thin airfoils ($t/c = 10\%$ and 12%) (see Fig. 10 and 11a-e): regardless of xt/c , the turbine C_P is marginally influenced
 243 by the r_{LE} . This can be attributed to the low dependency of thin airfoils and the relevant aerodynamic loads on r_{LE} , which is due to
 244 the geometrical constraints imposed by the airfoil thickness. It can be observed that by increasing the index of r_{LE} for different xt/c
 245 at $\lambda \leq 3.5$, C_P slightly changes; this minimal difference is in line with the corresponding C_m plots for $t/c \leq 12\%$. This can also be
 246 recognized from the skin friction, lift, and drag coefficients by the negligible changes in the characteristics of boundary layer
 247 events, including LSB and TES, and consequently the onset of dynamic stall and $C_{d,max}$. Due to the large volume of the results, the
 248 C_m , C_l , C_d , and C_f plots are not presented here. For $\lambda \geq 4.5$, except for the NACA0010-I/3.5, where increasing r_{LE} has the most
 249 influence on C_P , the aerodynamic loads and the turbine C_m show even less sensitivity to r_{LE} . Note that this is the regime in which
 250 the dynamic stall is no longer encountered and thin airfoils outperform the rest of the airfoils. The impact of r_{LE} on the turbine C_P
 251 for the optimal thin airfoils at $\lambda \geq 4.5$ is shown in Fig. 10f. Figures 12d and e show the corresponding C_m plots.
 252 Regarding the moderately-thick airfoils ($t/c = 15\%$ and 18%) (see Fig. 10 and 11f-j): overall, the turbine C_P shows higher
 253 dependency and sensitivity to r_{LE} . The higher dependency is due to the less severe geometrical constraints imposed by the
 254 moderately thick airfoils. Thus, morphing the r_{LE} noticeably modifies the airfoil shape and thereby influences the aerodynamic
 255 loads. The higher sensitivity is reflected by the noticeable monotonic reduction of C_P for most of the xt/c values. This significant
 256 decrease can be recognized from the C_m plots, where the curve peak drops by morphing the leading edge to more blunt shapes (i.
 257 e., higher r_{LE}). This may be due to the promoted LSB and TES characteristics, which result in higher $C_{d,max}$ for larger r_{LE} . For $\lambda \leq$
 258 3.0, the more prominent sensitivity is observed within the range of $22.5\% \leq xt/c \leq 35\%$; however, the C_P shows less sensitivity to
 259 r_{LE} for $\lambda = 3.5$, corresponding to a lighter dynamic stall regime (see Fig. 11f-h). Note that the moderately thick airfoils show
 260 superior performance over the thin and thick airfoils at $\lambda = 3.0$ and 3.5 (i. e., the NACA0018-4.5/2.75 and NACA0015-4.5/2.5,
 261 respectively). Figure 10f and Figs. 12b and c show the impact of morphing r_{LE} on the turbine C_P and C_m for the optimal airfoils at

262 $\lambda = 3.0$ and 3.5 . When the turbine goes into the non-dynamic stall regime with $\lambda \geq 4.5$, the range of xt/c within which the index of
 263 leading-edge radius is the most influential, shifts downstream to $30\% \leq xt/c \leq 40\%$ (see Fig. 11i and j).

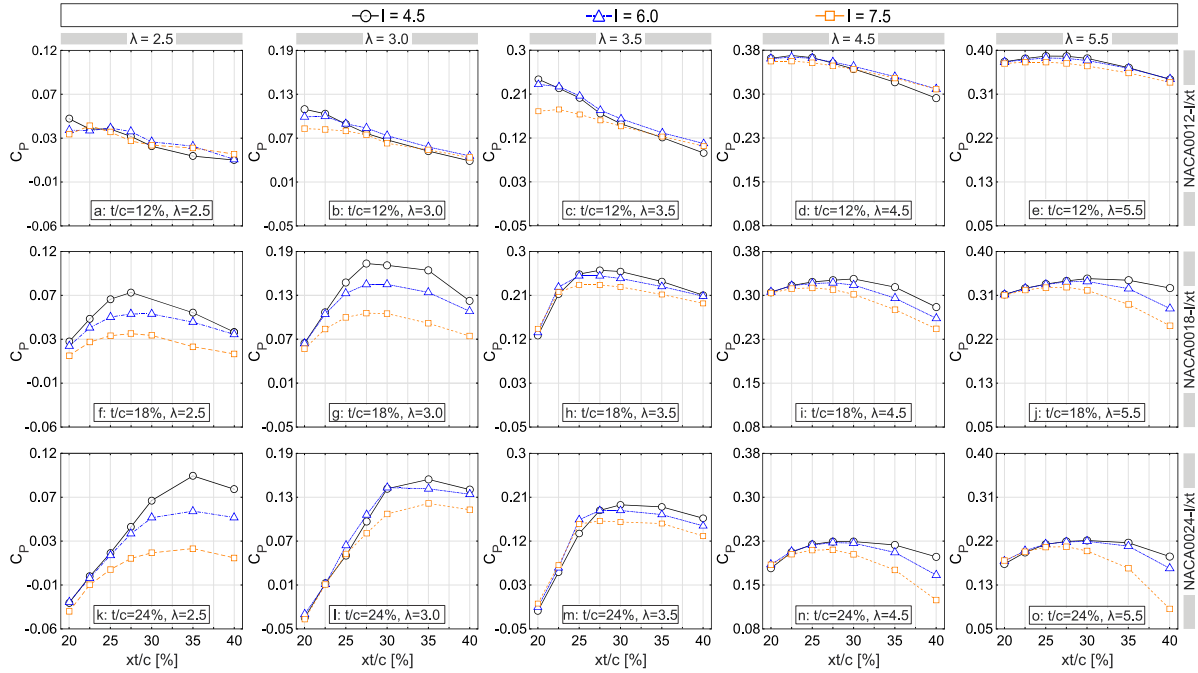


264

265 **Figure 10: Impact of morphing r_{LE} on the C_P for (a-e) selected, and (f) optimal airfoils at different λ . Filled symbols represent the**
 266 **optimal airfoils corresponding to each λ .**
 267

268 Regarding the thick airfoils ($t/c = 21\%$ and 24%) (see Fig. 10 and 11k-o): the analysis shows that at $\lambda = 2.5$, thick airfoils
 269 significantly surpass other airfoils in terms of power performance (see Fig. 10). Aside from the following differences, the overall
 270 trend of $C_P - xt/c$ is quite similar to that of moderately thick airfoils: C_P values are more sensitive to r_{LE} at $\lambda = 2.5, 4.5$ and 5.5 , but
 271 less so at $\lambda = 3.0$ and 3.5 (see Fig. 11k-o). By increasing the r_{LE} , the C_P values experience a monotonic reduction, especially for
 272 thick airfoils with $xt/c \geq 30\%$ at $\lambda = 2.5$, where the variation of I is the most influential on C_P . For example, the overall reduction
 273 of C_P for the NACA0024-I/3.50 at $\lambda = 2.5, 3.0, 3.5, 4.5$ and 5.5 is 77%, 21%, 17%, 19% and 23%, respectively. This can be
 274 recognized from the C_m plots, where the C_m values decrease dramatically in both upwind and downwind quartiles, the C_m curve
 275 peak drops, and the post-stall C_m fluctuation gets more significant (see Fig. 12a). This is due to earlier formations of the LSB and
 276 TES, and thus a higher $C_{d,max}$. Thick airfoils with low xt/c show marginal sensitivity to r_{LE} at different λ . The corresponding C_m
 277 plots show approximately the same azimuth of moment stall for different I . For brevity, the C_m plots are only presented for the
 278 NACA0024-I/3.50, which is the optimal airfoil at $\lambda = 2.5$ (see Fig. 12a).

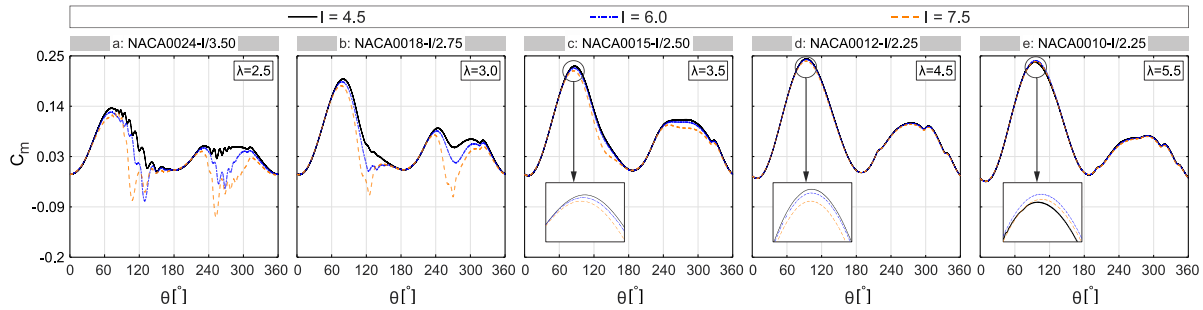
279 Overall, at $\lambda \leq 3.5$, the xt_{opt}/c belongs to the range of xt/c , which corresponds to the highest sensitivity of C_P to r_{LE} . For example,
 280 the optimal airfoil at $\lambda = 2.5$ (i. e., the NACA0024-4.5/3.5) has $xt/c = 35\%$ that fits in the range of $30\% \leq xt/c \leq 40\%$, within which
 281 the impact of r_{LE} is the most significant. This is while the xt_{opt}/c for $\lambda \geq 4.5$ (i. e., $xt/c = 22.5\%$) does not belong to such a range of
 282 xt/c (i. e., $xt/c \geq 30\%$). In addition, the most noticeable improvement in C_P due to morphing the r_{LE} occurs at $\lambda = 2.5$, where the
 283 dynamic stall deeply affects the aerodynamic and power performance of the blade. Nevertheless, by increasing λ and thus,
 284 alleviating or avoiding the dynamic stall, the aerodynamic loads are less affected by the r_{LE} .



285

286

Figure 11: Comparison of the turbine C_p versus xt/c for different I and λ .



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Figure 12: Impact of morphing r_{LE} on the turbine C_m for the combination of t_{opt}/c and x_{top}/c at different λ .

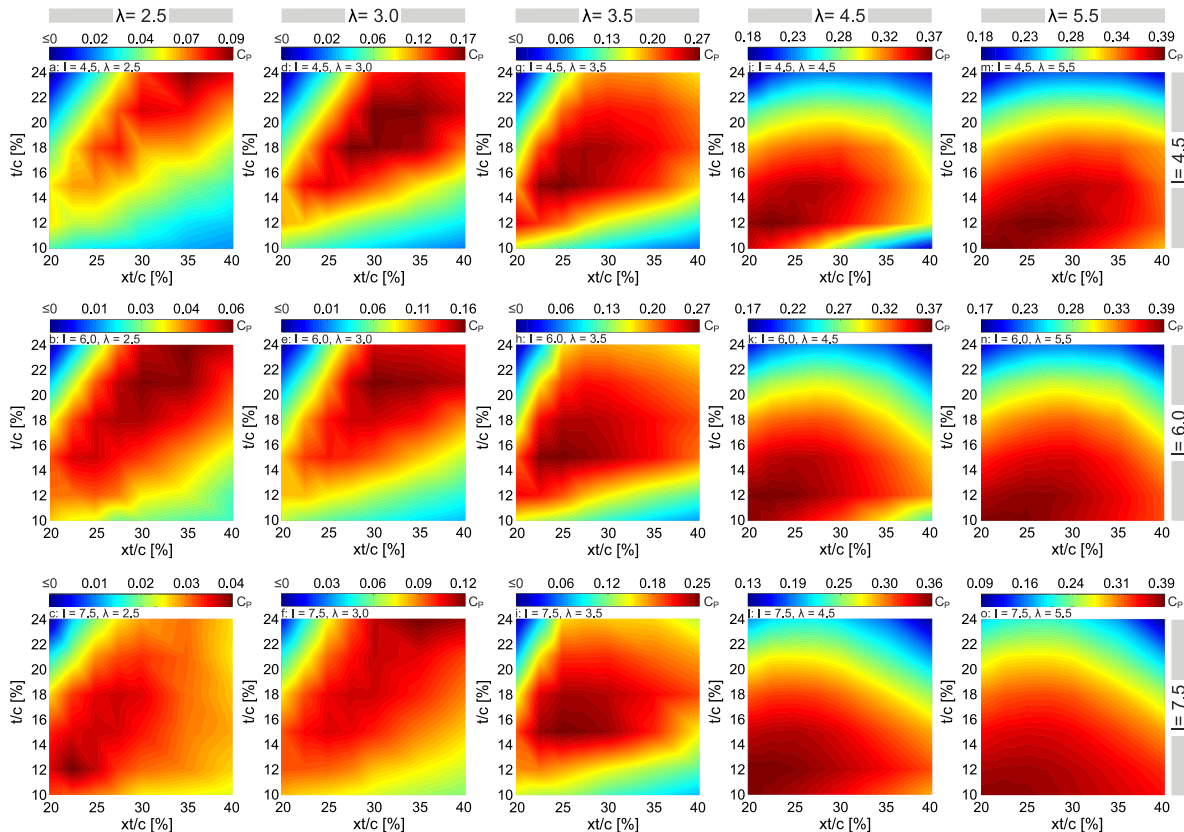
289 4.1.4 Combined morphing of the airfoil shape-defining parameters

290 Morphing the airfoil shape-defining parameters is thought to have a fully coupled impact on the turbine C_p . Thus, it is of high
 291 importance to study the impact of their combined morphing on the turbine C_p and C_T . Figure 13 shows the variation of C_p in t/c –
 292 xt/c space for different I and λ . Except for $\lambda = 5.5$, where the combination of t_{opt}/c and x_{top}/c is achieved by the moderate $I = 6.0$,
 293 the $C_{p,max}$ corresponds to the smallest $I = 4.5$ for $\lambda \leq 4.5$.

294 For $\lambda = 2.5$ and $I = 4.5$, the global optimum occurs by a set of high t/c and xt/c (i.e., NACA0024-4.5/3.50). For higher $I = 6.0$,
 295 although the combination of t_{opt}/c and x_{top}/c remains invariant, the local optimum area is found to morph into thin airfoils with low
 296 xt/c . For $I = 7.5$, the morphing airfoil changes to a thin airfoil with low xt/c , while experiencing lower C_p . The variation of optimal
 297 airfoil shape-defining parameters for different λ and the resultant airfoils at each λ are illustrated in Fig. 14.

298 At $\lambda = 3.0$, the local region of $C_{p,max}$ shows less sensitivity to I , shifting between moderate and high values of t/c and xt/c (see Fig.
 299 13d-f). However, similar to that of $\lambda = 2.5$, the overall range of C_p values narrows down with increasing I . For $\lambda = 3.5$, the local
 300 optimum region remains nearly the same at moderate values of t/c and xt/c for different I (see Fig. 13g-i); while for higher values

301 of $\lambda \geq 4.5$, it stays approximately independent of I , shifting marginally between low values of t/c and xt/c (see Fig. 13j-o). This
 302 implies that, by increasing λ , the local optimum region is less sensitive to I . In other words, the higher λ is, the less dependent the
 303 local optimum is on I . Overall, by increasing λ the local region of optimal airfoil shapes changes from the combination of high
 304 values of t/c and xt/c for $\lambda = 2.5$ to moderate t/c and xt/c for $\lambda = 3.0$ and 3.5 , and low values of t/c and xt/c for $\lambda \geq 4.5$.



305
 306

Figure 13: Turbine C_p in $t/c - xt/c$ space. Each contour plot is based on 42 simulations. Colormaps are in different range.

307 It is observed that in designing morphing blades, single-parameter studies will not provide the overall picture and could lead to
 308 unreliable results. The contour plots give a conceptual view of the optimal regions in terms of the airfoil shape-defining parameters,
 309 with which the resultant airfoils have their most efficient performance; and also, the inefficient regions of the turbine C_p , which
 310 must be avoided.

311 Figure 15 shows the turbine C_T in $t/c - xt/c$ space. It is interesting to observe that for low $\lambda \leq 3.5$ there is no coincidence between
 312 the optimal regions of C_T and C_p contours; while for $\lambda \geq 4.5$, these two regions overlap. By increasing λ , the optimal region extends
 313 marginally towards higher t/c and xt/c , while also experiencing higher values of C_T . The noncongruent region of $C_{p,max}$ and $C_{T,max}$
 314 at low values of λ is different from what is observed in the case of HAWTs. That is, the maximum power output of a HAWT occurs
 315 where the highest thrust load is exerted by the turbine blade on the flow. This led to a correlation between the optimal regions of
 316 C_p and C_T . In contrast, the results of the present study show that for VAWTs, the same phenomenon only occurs at high values of
 317 $\lambda \geq 4.5$, where the turbine goes into non-dynamic stall regimes with more limited variations of α . Therefore, when designing
 318 morphing blades for VAWTs, the C_T values corresponding to high values of λ are of more importance compared to those of lower
 319 λ , where dynamic stall is expected to occur.

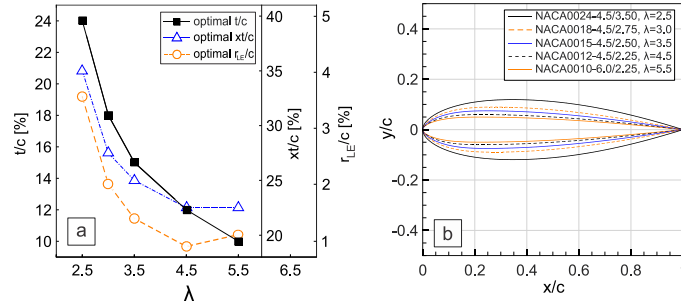


Figure 14. (a): variation of morphing airfoil shape-defining parameters and (b): morphing airfoils at different λ .

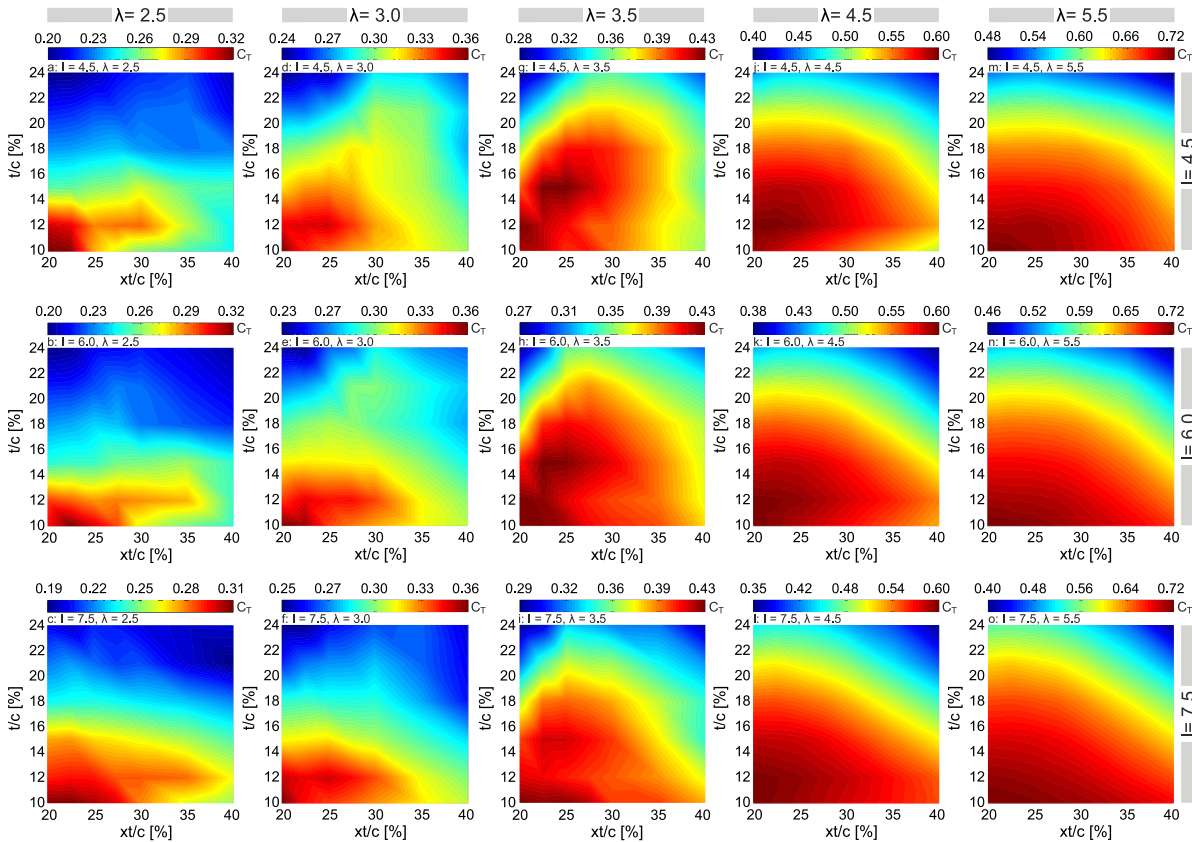
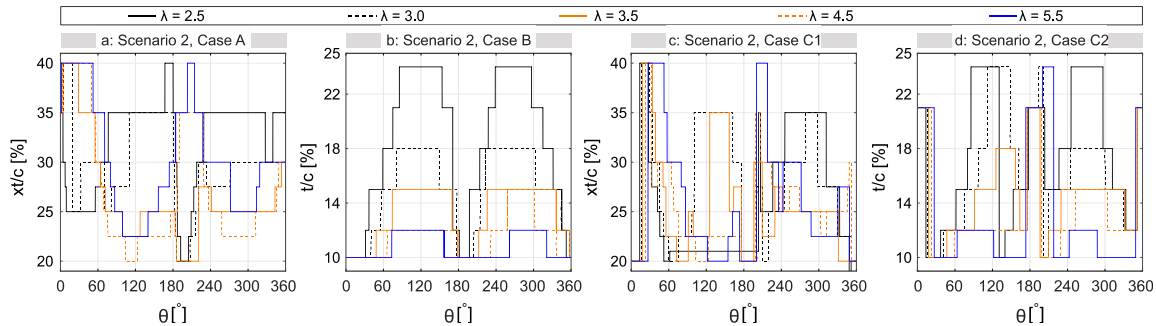


Figure 15: Turbine C_T in $t/c - xt/c$ space. Each contour plot is based on 42 simulations. Colormaps are in different range.

4.2 Towards a morphing blade

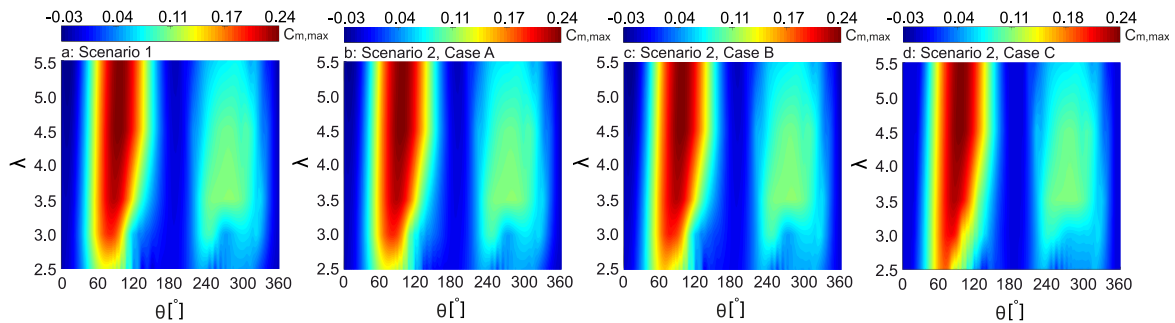
This section provides an overview of the turbine power gain due to different morphing scenarios, namely a fixed optimal airfoil for each λ (scenario 1), as already discussed in Sect. 1; and an optimal airfoil for each $d\theta$, as discussed in the following Sect. (scenario 2). Figure 16 shows the variation of t/c and xt/c versus azimuth for scenario 2. Figure 17 shows the corresponding $C_{m,max}$ for each scenario in $\lambda - \theta$ space. Note that scenario 2 is divided into three cases, namely cases A, B and C. In cases A and B, the t_{opt}/c and xt_{opt}/c of the already identified optimal shapes for each λ are kept fixed and distributions of xt/c and t/c versus θ , corresponding to $C_{m,max}$, are extracted, respectively. In case C, the combination of t_{opt}/c and xt_{opt}/c , corresponding to $C_{m,max}$ at each $d\theta$ is selected and kept fixed, and distributions of xt_{opt}/c (i.e., case C1) and t_{opt}/c (i.e., case C2) versus azimuth are extracted,

332 respectively. Note that $I_{opt} = 4.5$ remains invariant for $\lambda \leq 4.5$ and changes to $I_{opt} = 6.0$ only at $\lambda = 5.5$. For the sake of clarity and
 333 analysis, $I_{opt} = 4.5$ is assumed to be constant throughout the studied range of λ , introducing the NACA0012-4.5/2.50 as the optimal
 334 airfoil at $\lambda = 5.5$. The absolute difference between the $C_{P,max}$ values for optimal airfoils with $I = 4.5$ and 6.0 at $\lambda = 5.5$ is 0.0005.



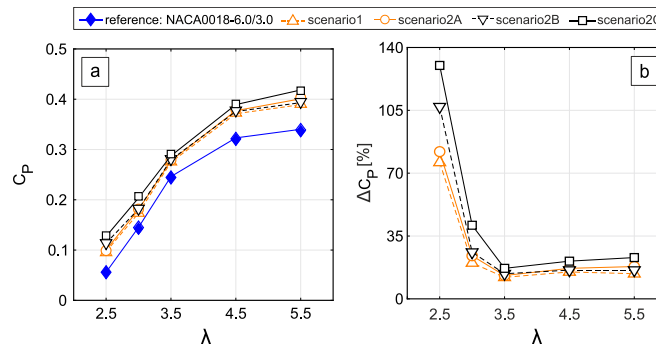
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Figure 16: Morphing (a) xt/c and (b) t/c versus azimuth for fixed t_{opt}/c and xt_{opt}/c corresponding to each λ ; morphing (c) xt_{opt}/c and (d) t_{opt}/c vs azimuth for fixed t_{opt}/c and xt_{opt}/c corresponding to each $d\theta$.



338
 339

Figure 17: Turbine C_m in $\lambda - \theta$ space for different morphing scenarios.



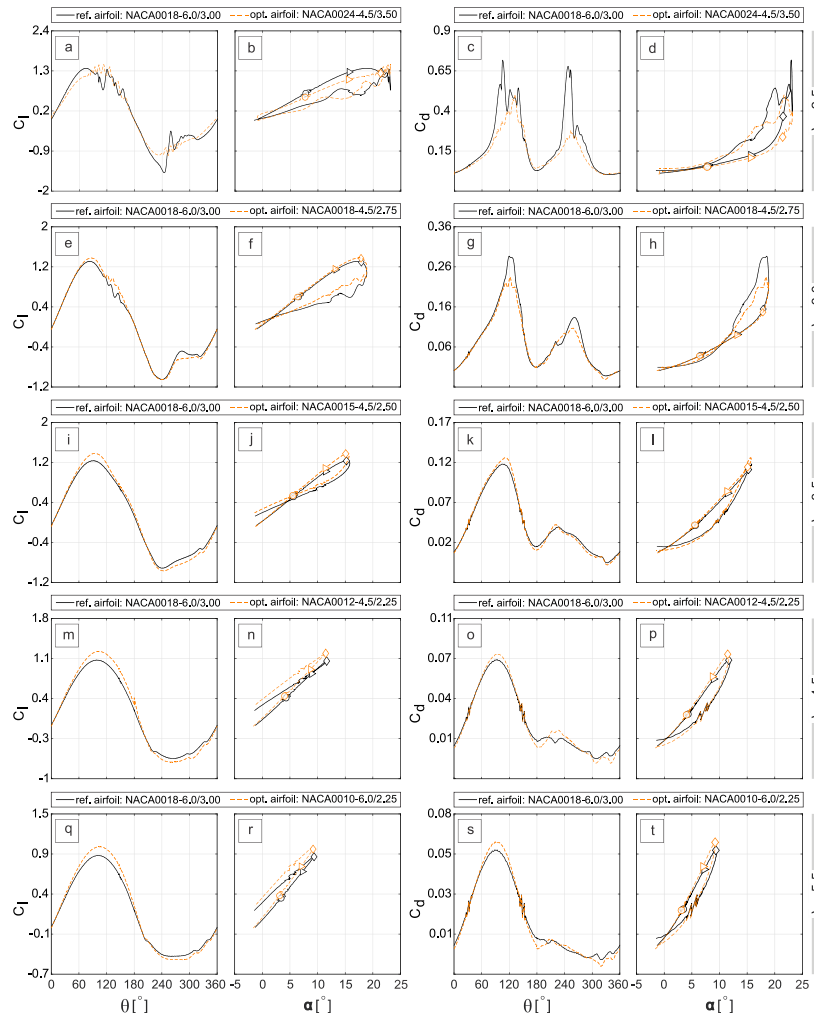
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 341

Figure 18: Variation of (a): Turbine C_p and (b): power gain due to different scenarios of a morphing blade at different λ .

342 Figures 16a and 17b show the results for scenario 2, case A. Note that the results correspond to the $C_{m,max}$ at each $d\theta = 0.1^\circ$. It can
 343 be observed that xt/c shows almost the same level of sensitivity to θ for different λ (see Fig. 15 a). Fig. 17b shows the overall view
 344 of the $C_{m,max}$ as the blade section rotates and morphs at different λ . Obviously, the maximum torque is obtained around $\theta = 90^\circ$ for
 345 different λ . The higher torque generated in the upwind quartile is due to the unperturbed upstream wind profile, while the less
 346 pronounced $C_{m,max}$ in the downwind quartile is due to the lower wind velocity and blade-wake interaction.

347 For scenario 2, case B, the observed trend for $t_{opt}/c - \theta$ is quite similar at different λ , except for a noticeable difference; that is, the
 348 higher λ is, the less sensitive the variation of t_{opt}/c to θ is. By increasing λ , and thus, decreasing the xt_{opt}/c , thinner airfoils outperform
 349 the thicker ones. The turbine $C_{m,max}$ shows negligible changes (see Figs. 16b and 17b). The observations for scenario 2C1 and C2

350 are almost similar to those of cases A and B, respectively. However, there are some narrow ranges of θ at the beginning, middle,
 351 and end of the turbine rotation disk, where noticeable differences exist. The resulting $C_{m,max}$ in $\lambda - \theta$ space differs slightly from the
 352 other scenarios (see Fig. 17d).
 353 Figure 18 shows the turbine C_P and the power gain due to different scenarios for a morphing blade versus the reference case at
 354 different λ . By increasing λ from 2.5 to 3.5, the power gain significantly decreases. Nevertheless, for $\lambda \geq 4.5$ it marginally increases.
 355 The more pronounced ΔC_P at low λ is due to alleviating the dynamic stall by using a morphing blade. The averaged improvement
 356 in C_P due to scenarios 1, 2A, 2B, and 2C ($\overline{\Delta C_P}$) over the studied range of λ is 0.04, 0.045, 0.047, and 0.06, respectively.

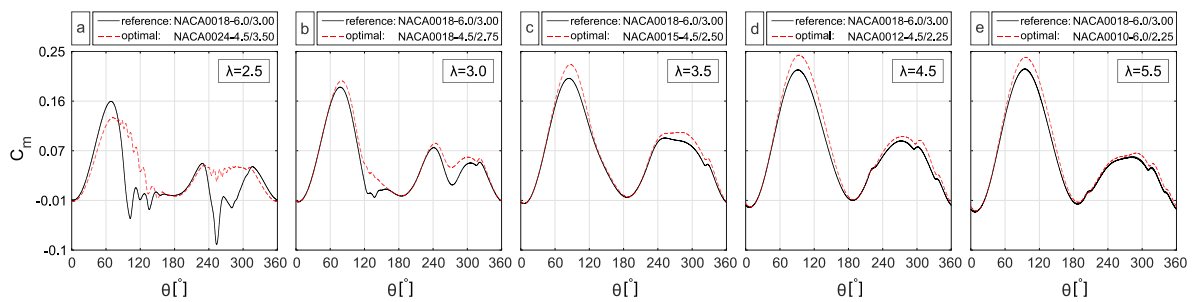


357
 358 **Figure 19:** C_l and C_d versus θ and α for the reference and morphing airfoils at different λ (\circ : $\theta = 60^\circ$; \triangleright : $\theta = 120^\circ$; \diamond : $\theta = 180^\circ$).

359 **4.3 Aerodynamic analysis of the morphing airfoils**

360 Figure 19 gives a comparison of the turbine aerodynamic loads (namely, C_l and C_d) versus θ and α for the reference and morphing
 361 airfoils. The results correspond to scenario 1, where an optimal airfoil is identified for each λ . In general, the morphing airfoils
 362 have higher $C_{l,max}$ compared to that of the reference case. For $\lambda = 2.5$, the morphing airfoil shows an obvious reduction in drag

363 jump both in upwind and downwind quartiles and reduced post-stall fluctuation. These are the reflections of the significantly-
 364 alleviated dynamic stall. Table 5 gives the $C_{l,max}$ and $C_{d,max}$ values for the reference and morphing airfoils at different λ . It can be
 365 seen that for $\lambda = 3.0$ and 3.5 , where the turbine goes into a lighter-dynamic stall regime, the morphing airfoil shows higher $C_{l,max}$
 366 with less severe post-stall fluctuation and lower $C_{d,max}$ with less substantial drag jump. For $\lambda \geq 4.5$ (i. e., non-dynamic stall regime),
 367 although the morphing airfoils show higher values for both the $C_{l,max}$ and $C_{d,max}$, the increase in $C_{l,max}$ is more dominant than that
 368 of the $C_{d,max}$ (see also Table 5). Figure 20 shows the turbine C_m for the reference and morphing airfoils at each λ . Other than a
 369 reduction for $0^\circ \leq \theta \leq 80^\circ$ at $\lambda = 2.5$, the turbine C_m is found to improve moderately due to the morphing airfoils at the studied
 370 range of λ , indicating higher turbine C_p .



371
 372 **Figure 20: Turbine C_m for the reference and morphing blades at different λ (scenario 1).**

373 **Table 5. Estimated $C_{l,max}$ and $C_{d,max}$ for the morphing and reference airfoils at different λ (scenario1).**

λ	2.5		3.0		3.5		4.5		5.5	
load coefficient	$C_{l,max}$	$C_{d,max}$	$C_{l,max}$	$C_{d,max}$	$C_{l,max}$	$C_{d,max}$	$C_{l,max}$	$C_{d,max}$	$C_{l,max}$	$C_{d,max}$
reference	1.37	0.716	1.31	0.29	1.23	0.118	1.07	0.076	0.93	0.064
morphing	1.47	0.503	1.38	0.24	1.38	0.126	1.23	0.082	1.05	0.059
Difference [%]	+7	-29.8	+5	-17	+12	+6.7	+15	+8	+13	+8.5

374 **5. Discussion**

375 The present work includes a wide range of λ , where the turbine goes into different operational regimes of light-, deep-, and non-
 376 dynamic stall regimes. The aim of the analysis is to highlight the power gain of VAWTs due to different scenarios of a morphing
 377 blade. It is suggested to continue this work for the rest of important geometrical parameters, such as camber and its position along
 378 the chord, which describe the airfoil asymmetry and have the potential to morph.

379 The symmetric modified NACA 4-digit airfoil series is chosen as a basis for the morphing airfoils. The airfoils are generated by
 380 setting the three main defining parameters, i.e., t/c , xt/c and r_{LE} .

381 The results prove the usefulness of the morphing technique to improve the power performance of VAWTs as the main objective
 382 of this work. Also, the structural strength of the blade could be another important objective that must be considered while designing
 383 morphing blades for VAWTs. It is found that this objective is also satisfied, and the blade structural limitations are met. This is
 384 due to the fact that the morphing airfoil changes from a thin airfoil for the highest λ , corresponding to low wind speeds and
 385 aerodynamic loads, to a more robust thick airfoil for the lowest λ , where the lack of strength and stiffness can cause blade failure,
 386 and thus, the blade needs to withstand the aerodynamic loads and to avoid the resultant deflections. However, technical
 387 considerations related to the complexity of the electromechanical actuators for the morphing blade must be taken into account. The
 388 required actuators need to be chosen such that they can meet the displacement requirements at the corresponding response times



389 and rotational speeds. In addition, it is of particular importance to consider the cost factor and feasibility of such a system and also
390 to estimate the difference between the power required to drive the actuators and the resulting turbine power gain.

391 6. Conclusions

392 Incompressible URANS simulations, validated with experiments, are used to study the impact of different scenarios of a morphing
393 blade on the power and thrust performance of a VAWT. Three main airfoil shape-defining parameter, namely t/c , xt/c and I , are
394 chosen and morphed as functions of λ and θ to determine the optimal airfoils in terms of C_P in a wide range of λ .

395 The main conclusions are as follows:

- 396 - For each λ , there exists a morphing airfoil shape, corresponding to the turbine $C_{P,max}$. At the lowest $\lambda = 2.5$, the morphing
397 airfoil is defined with $t/c = 24\%$, $xt/c = 35\%$ and $I = 4.5$ (i.e., the NACA0024-4.5/3.5). In comparison to the baseline airfoil
398 (i.e., the NACA0018-6.0/3.0), this airfoil has a smaller leading-edge radius; and a higher maximum thickness, which is found
399 to shift downstream of the default point by 5%.
- 400 - By increasing λ , the combination of t_{opt}/c and xt_{opt}/c morphs to lower values; however, it shows less dependency on r_{LE} . For
401 $\lambda = 3.0, 3.5, 4.5$, and 5.5 , the optimal airfoil morphs to NACA0018-4.5/2.75, NACA0015-4.5/2.50, NACA0012-4.5/2.25 and
402 NACA0010-6.0/2.25, respectively.
- 403 - Regarding the morphing airfoil as a function of θ , the highest average improvement in the turbine C_P is due to scenario 2C,
404 where the combination of t_{opt}/c and xt_{opt}/c , corresponding to the turbine $C_{m,max}$ at each $d\theta$, is selected and kept fixed.
- 405 - The improvement in C_P due to morphing blade becomes more pronounced for low values of λ , where the adverse effects of
406 dynamic stall, i.e., jump in aerodynamic loads and post-stall loads fluctuation, are mitigated by morphing airfoils.

407 The presented work not only highlights the strong relevance of the gain in turbine C_P to a morphing blade scenario but also
408 emphasizes the combined morphing of the airfoil shape-defining parameters. That is, single-parameter morphing will not result in
409 the highest power improvement of VAWTs. Other important considerations, such as morphing the rest of the geometrical
410 parameters, are yet to be determined. Therefore, the present study could be a significant stride towards future studies on designing
411 advanced morphing blades for smart VAWTs.

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