

# Offshore wind farm optimisation: a comparison of performance between regular and irregular wind turbine layouts

Maaïke Sickler<sup>1</sup>, Bart Ummels<sup>1,2</sup>, Michiel Zaaijer<sup>3</sup>, Roland Schmehl<sup>3</sup>, and Katherine Dykes<sup>4</sup>

<sup>1</sup>Ventolines B.V., P.J. Oudweg 4, 1314 CH Almere, the Netherlands

<sup>2</sup>Faculty of Civil Engineering and Geosciences, Delft University of Technology, Stevinweg 1, 2628 CN Delft, the Netherlands

<sup>3</sup>Faculty of Aerospace Engineering, Delft University of Technology, Kluyverweg 1, 2629 HS Delft, the Netherlands

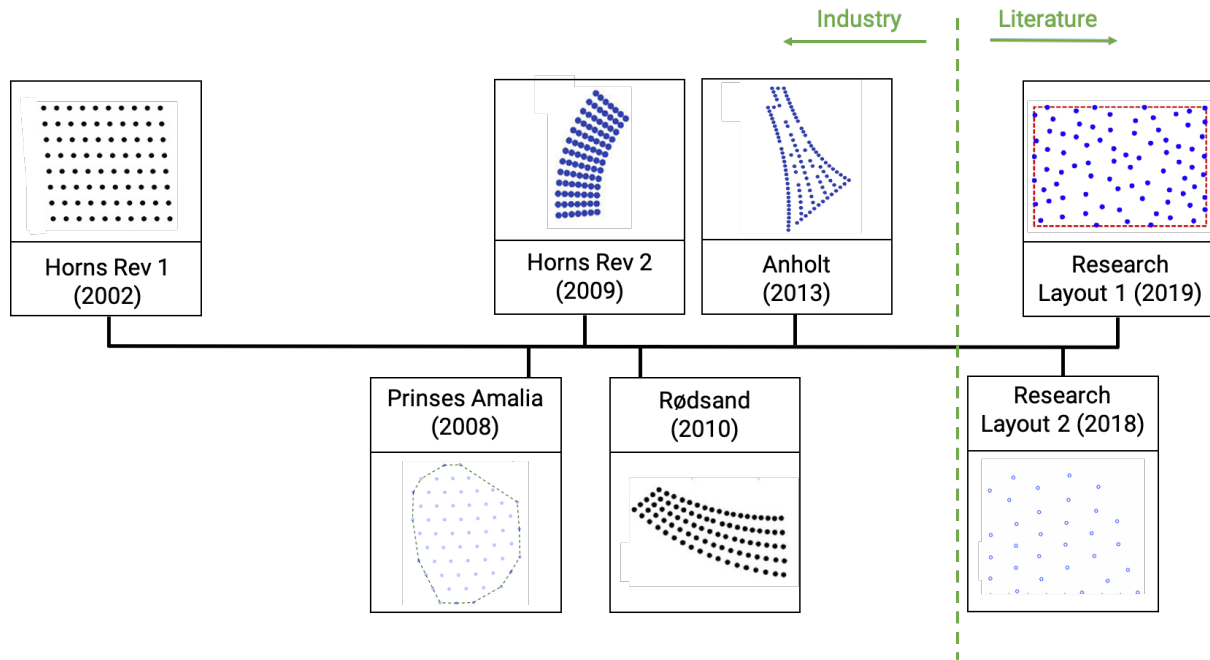
<sup>4</sup>DTU Wind Energy, Frederiksborgvej 399, 4000 Roskilde, Denmark

**Correspondence:** Roland Schmehl (r.schmehl@tudelft.nl)

**Abstract.** Layout optimisation is essential for improving the overall performance of offshore wind farms. During the past 15 years, the use of yield optimisation algorithms has resulted in a transition from regular to more irregular farm layouts. However, since the layout affects many factors, yield optimisation alone may not maximise the overall performance. In this paper, a comparative case study is presented to quantify the effect of the wind farm layout on the overall performance of offshore wind farms. The case study was performed to investigate two performance indicators: power performance, using yield calculations with WindPRO and wake-induced tower fatigue, using the Frandsen model. It is observed that irregular wind farm layouts have a higher annual energy production compared to regular layouts. Their power production is also more persistent (less sensitive) to wind direction, improving predictability and thus market value of power output. However, one turbine location in the irregular layout has a 24% higher effective turbulence level, leading to additional tower fatigue. As a result, fatigue-driven tower designs would require increased wall thicknesses, which would result in higher capital costs for all turbine locations. It is demonstrated in this study that layout optimisation using a minimum inter-turbine spacing effectively resolves the induced wake issue while maintaining high-yield performance.

## 1 Introduction

The share of wind energy in the electricity market is rapidly increasing (Musgrove, 2009; International Energy Agency (IEA), 2022). Offshore wind farms pose fewer geographical and social constraints than onshore wind farms, which leads to larger design spaces. The performance of an offshore wind farm indicates how efficient the system is at achieving its main objective (Tao and Finenko, 2016). Examining operational wind farms, a development of farm layouts over time can be recognised. Earlier wind farms show regular patterns such as the wind farms Horns Rev 1 (2002) (Akay et al., 2014) and Prinses Amalia (2008) (Stanley and Ning, 2019). Newer and larger wind farms show more variation in patterns such as the wind farms Horns Rev 2 (2009) (Ostachowicz et al., 2016) and Rødsand (2010) (Nygaard, 2014), and partial irregularity such as Anholt (2013) (Ostachowicz et al., 2016) and many more. A number of desktop optimisation studies even suggest fully irregular wind farms such as Research Layout 1 and 2 (Charhouni et al., 2019; Karouani and Elhoussaine, 2018) which are obtained from existing research as shown in Figure 1.



**Figure 1.** Development of wind farm patterns over time. Left of the green dashed line are wind farm layouts operational in industry (Akay et al., 2014; Stanley and Ning, 2019; Ostachowicz et al., 2016; Nygaard, 2014), while right of this line are optimised layouts from literature studies (Karouani and Elhoussaine, 2018; Charhouni et al., 2019).

Sanchez Perez Moreno (2019) investigated the preliminary design of the layout, electrical collection system, and support structures of an offshore wind farm using two different optimisation approaches. The sequential approach neglects the interaction between the three selected performance characteristics, while precisely this is taken into account in the multidisciplinary design analysis and optimisation (MDAO) approach. The two approaches were used to optimise the total system levelised cost of energy (LCOE) of a regular and an irregular farm layout. The study focussed on the comparison of the two approaches and the interaction effects, not comparing the performance of the different geometric patterns. Chen et al. (2015) used a multi-objective genetic algorithm (GA) to maximise the wind farm efficiency and minimise its cost applying real wind conditions. Investigating one regular and three irregular layouts with identical total geographical area, the comparison suggested that irregular geometric patterns may perform better than regular layouts, yet no final conclusion was drawn in the study. The goal of maximising the energy extraction while minimising the cost was also pursued by Charhouni et al. (2019) comparing regular and irregular wind farm layouts. The resulting power, capacity factor and efficiency were all higher for the irregular layout, although it should be noted that a constant wind speed and direction was considered. For general validity of this conclusion, the different layout options need to be investigated also at variable wind speed and direction.

Three observations can be made for comparisons of wind farms with regular and irregular layouts conducted to date. First, the performance indicators for wind farms are not well-defined in the literature. An overview of all possible indicators and how

they affect the overall performance is lacking. Also, the degree to which these indicators are influenced by the geometry of the wind farm is not investigated.

Second, the effects of optimised wind farm layouts on all performance indicators are either unknown or only partially investigated in the literature. The existing studies which include regular and irregular wind farm layouts focus on the performance of the optimisation tools. The aim of these optimisation studies is not to compare the overall performance of the regular and irregular wind farms.

Third, an optimisation of ~~the farm layout an existing regular wind farm pattern~~ inherently leads to an ~~irregular pattern~~ increase in irregularity, as shown by ~~most optimisation studies in the literature~~ optimisation studies (Grady et al., 2005; Marmidis et al., 2008; DuPont et al., 2012; Shakoor et al., 2016). This is only logical given the enormous design space of irregular patterns with many local optima compared to regular patterns. A particle swarm optimisation (PSO) or genetic algorithm (GA) is, for example, unlikely to find a regular pattern. Based on the nature of the optimisation algorithms many studies are naturally biased toward irregular wind farm layouts.

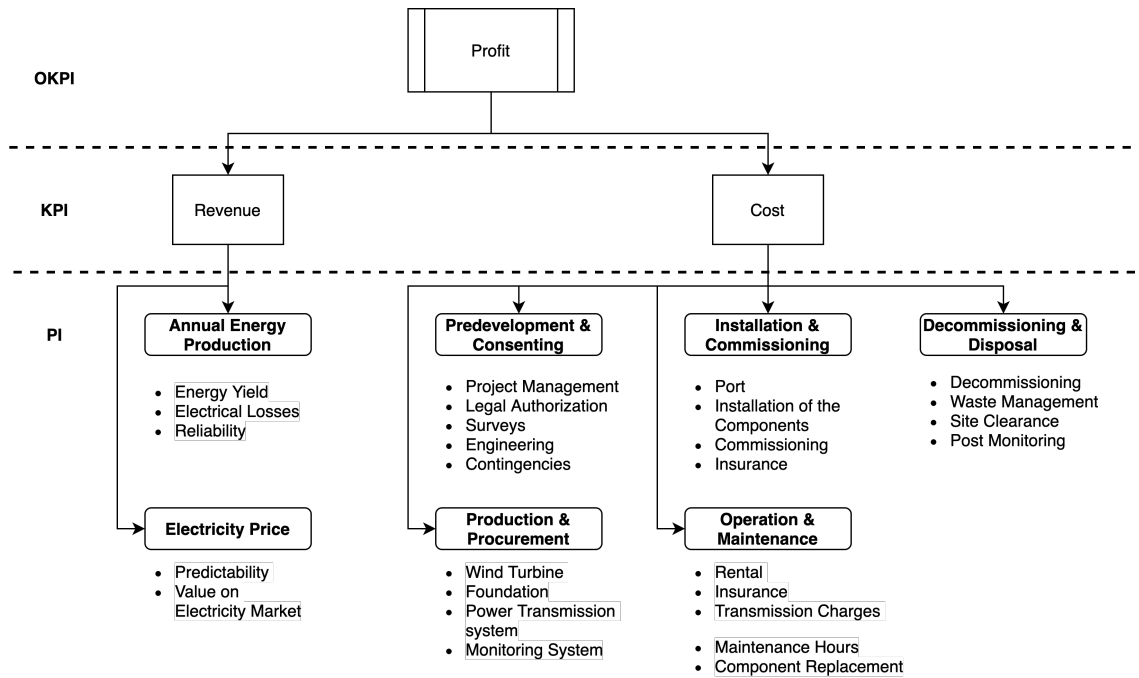
The objective of this paper is thus to quantify the effect of regular and irregular offshore wind farm layouts on selected performance indicators by means of a comparative case study using state-of-the-art simulation tools and models. The paper is based on the graduation project of the first author (Sickler, 2020) and is structured as follows. In Section 2, the selection of performance indicators is described. In Section 3, the power production of the different layouts is assessed and in Section 4 the wake-induced tower fatigue of the different layouts. In Section 5, the general applicability of the results is investigated with a sensitivity analysis of the performance indicators for the Borssele wind farm. Conclusions are presented in Section 6.

## 2 Selection of performance indicators

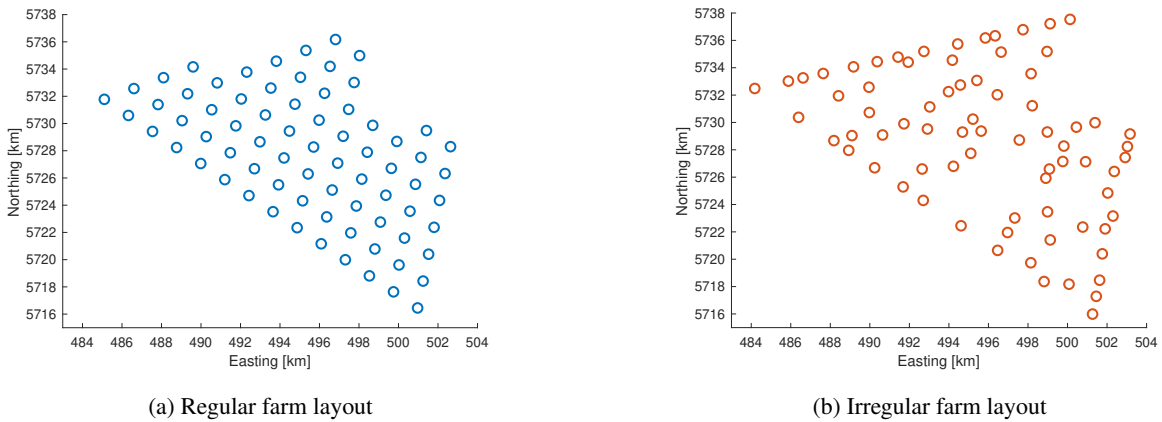
All performance indicators by which a wind farm has been assessed so far were inventorised using, among others, the works of Gonzalez et al. (2017) and Shafiee et al. (2016). The indicators were divided into ~~four levels~~ three levels with the third level containing sub-categories, as shown in Figure 2. To incorporate changes in energy price, instead of using the LCOE as an overarching key performance indicator, profit (positive net present value) was selected (Nissen and Harfst, 2019).

~~A~~ To direct the research, a multi-criteria decision analysis ~~based on~~ was performed based on these criteria: (1) affected by wind farm layout, (2) feasibility to research, (3) site independence, and (4) technical nature ~~resulted in~~. This resulted in the selection of five sub-performance indicators. ~~These were grouped into two performance indicator groups: (1) Power performance, including, which were grouped as to represent 'Power Performance' (yield/wake losses, predictability and value on the electricity market, and (2) Wake induced tower fatigue, including) and 'Wake-Induced Tower Fatigue' (wind turbine cost and, component replacement cost).~~

To assess the performance of these indicator groups for the different layout categories, the regular and irregular farm layouts depicted in Figure 3 were selected from the work of Sanchez Perez Moreno (2019). For both layouts, the IEA Wind Task 37 reference wind turbine with 10 MW rated power and a rotor diameter of 190.8 m was used (Bortolotti et al., 2019). The degree of irregularity was quantified mathematically with (1) the sum of the distance to surrounding turbines in a radius of 10 rotor



**Figure 2.** Breakdown of performance indicators. OKPI = overarching key performance indicator, KPI = key performance indicator, PI = performance indicator consisting of with itemised sub-performance indicators (Sickler, 2020).



**Figure 3.** Regular and irregular wind farm layouts from Sanchez Perez Moreno (2019) consisting of 74 turbines with a rated power of 10 MW at Borssele.

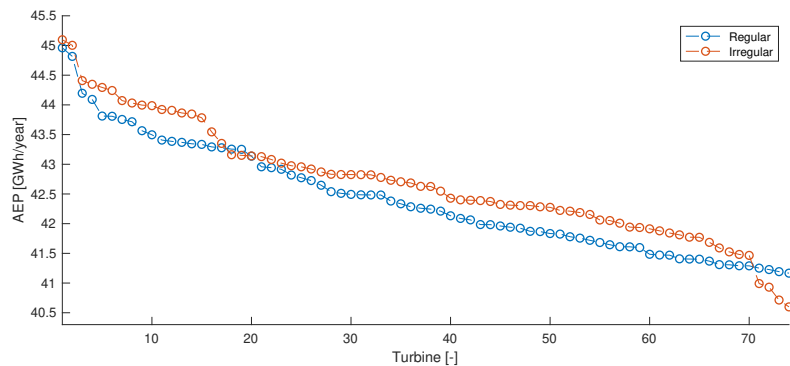
diameters (10 RD) for each turbine and (2) the minimum inter-turbine spacing. The number of turbines with the same unique sum of distances to their surrounding turbines with a tolerance of 0.001 RD was 66 for the regular wind farm layout and only

5 for the irregular farm layout. The minimum inter-turbine spacing was 2.73 RD for the irregular wind farm layout compared to 8.88 RD for the regular wind farm.

The following two sections will present the analyses of performance indicator groups (1) and (2), respectively.

### 3 Performance indicator group (1): power performance

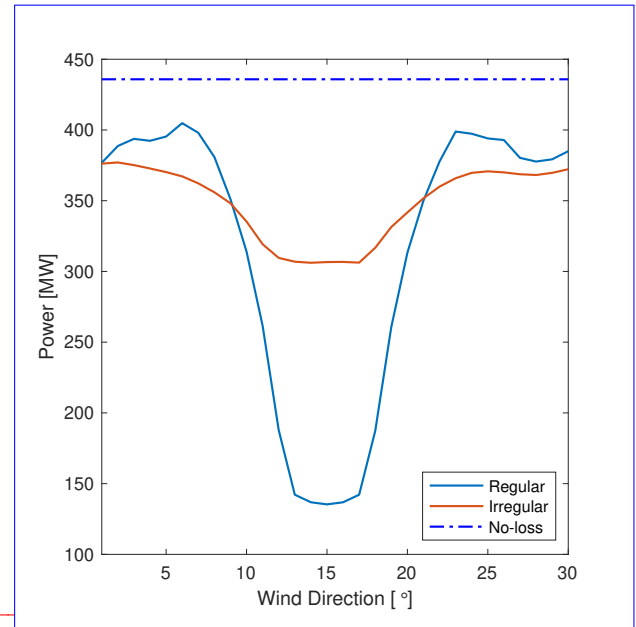
The annual energy production (AEP) was analysed in WindPRO, computing the absolute difference between regular and irregular wind farm layouts. The wind climate imported to WindPRO was obtained from Riezebos et al. (2015). The data was extrapolated to hub height using the power-law wind profile with a power exponent  $\alpha$  of 0.08. The WindPRO calculation shows a higher AEP of approximately 0.66% for the irregular wind farm layout, corresponding to approximately €700 000 according to the average European Power Exchange (EPEX) price in the Netherlands between 2007 and 2020. The individual turbine performance shows that the difference in AEP is not caused by the outliers (best-performing and worst-performing turbines) but by the average-performing turbines in the wind farm. Relating the performance and positions shows that the distribution of the lower performing turbines is more evenly spread for the regular wind farm than for the irregular wind farm as becomes apparent from Figure 4.



**Figure 4.** Individual turbine AEP for the regular and irregular wind farm layouts arranged from high performance to low performance (Sickler, 2020).

Figure 5 shows the persistence of power to wind direction, i.e. the extent to which power production varies with wind direction, measured in degrees, for a certain wind speed. The maximum power drop is quantified as the maximum uninterrupted decrease of power for an increase or decrease in wind direction. This maximum power drop decreases by 73.7 % for the irregular wind farm compared to the regular wind farm layout. The orientation of turbine rows in the wind farm with regular layout is driving for the angle at which the power drops occur as well as for their magnitude. More turbines in a row correspond to a larger power drop. It is expected that a wind farm layout with a higher persistence to wind direction will lead to a decrease in prediction errors. This will likely result in lower imbalance costs. A rough estimation based on historical imbalance cost

data shows that the imbalance cost would amount to approximately 1.6 % of the AEP revenue. The difference between the  
95 imbalance cost of the regular and irregular wind farm would then become visible within this 1.6 %.



**Figure 5.** ~~Regular farm layout~~ Power output of wind farms with regular and irregular layouts at a wind speed of 9.5 m/s as functions of wind direction, zoomed in on the wind directions with the largest power drops (Sickler, 2020).

~~Irregular farm layout~~ Power output of wind farms with regular and irregular layouts at a wind speed of 9.5 m/s as functions of wind direction, zoomed in on the wind directions with the highest power drops.

The analysis for persistence to wind direction was executed using a constant mean wind speed of 9.5 m/s. This simplification likely overestimates the power drops as a function of wind direction because the time-dependent change of wake losses in the wind farm was not included. Additionally, the wind speed is just below the rated power, which means that the wake losses play a significant role. For higher wind speeds (+15 m/s and above) the effect of wake losses ~~diminishes or even disappears completely.~~  
100 is reduced or disappears.

Based on the analysis and assumptions in this section, the irregular wind farm layout performs better for all three sub-performance indicators analysed: the energy yield, predictability, and value in the electricity market. The importance and value of persistence to wind direction will increase as the impacts of wind power on power system operation increase with the very large growth foreseen in the next decades. The ~~indicator~~ indicator predictability and value in the electricity market do require a  
105 much more extensive analysis for proper quantification.

#### 4 Performance indicator group (2): wake-induced tower fatigue

The layout of a wind farm and the wind environment determine to what degree downstream turbines are affected by the wakes of upstream turbines. Especially for offshore farms, these wake effects are driving for the wind turbine fatigue loading (Thomsen and Sørensen, 1999). With low terrain roughness and low ambient turbulence intensities, the effect of wakes is higher than in  
 110 onshore wind farms. Multiple studies confirm that one of the fundamental parameters which determine the wall thickness of the tower design is fatigue (Igwemezie et al., 2018; Frandsen, 2007; Thomsen and Sørensen, 1999; Frohboese and Schmuck, 2010). Therefore, the layout of the farm will affect the cost of the towers.

Interestingly, while monopile foundation designs are optimised for individual locations within an offshore wind farm, typically only a single tower design is applied based on the turbine location with the highest turbulence intensity. Therefore a  
 115 single, high-turbulence turbine location within a project impacts the wall thickness of all towers of that project, which implies a high-cost multiplication factor.

The effective turbulence intensity was quantified using the Frandsen model, which implies that the structural load ranges vary linearly with the turbulence intensity (Frandsen, 2007). The model was used to determine the damage-equivalent bending moment<sup>1</sup> at the tower bottom,  $M_{YT,DEL}$ , as a function of the varying wind and wake conditions in the farm. The bending  
 120 moment is then related to the damage-equivalent stress  $\sigma_{DEL}$  and the tower wall thickness  $t$  via the following equation

$$\sigma_{DEL} \propto \frac{M_{YT,DEL}}{t}. \quad (1)$$

To maintain a constant damage-equivalent stress, the wall thickness of the tower thus needs to increase proportionally to the damage-equivalent load. This can be translated to an increased wall thickness required to support the increased load

$$t_{new} = t_{old} \left( \frac{I_{eff}}{I_a} \right), \quad (2)$$

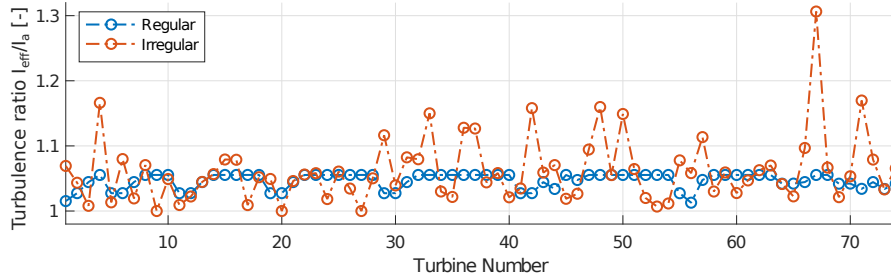
125 where  $I_a$  is the ambient turbulence intensity and  $I_{eff}$  the effective turbulence intensity that can be evaluated as

$$I_{eff}(\bar{U}_a) = \left[ \int_0^{2\pi} p(\theta|\bar{U}_a) I^m(\theta|\bar{U}_a) d\theta \right]^{\frac{1}{m}}. \quad (3)$$

In this equation,  $p$  is the probability of a certain wind direction occurring at hub height,  $\theta$  is the wind direction,  $\bar{U}_a$  is the mean wind speed at hub height,  $I$  is the turbulence intensity in the wake, which consists of the ambient turbulence intensity and the wake-added turbulence intensity, and  $m$  is the Wöhler exponent of the material determined by the SN-curve. The effective  
 130 turbulence intensity is driven by the minimum inter-turbine spacing in the wind farm. To compare the impact of the layout, the effective turbulence intensity was calculated for the individual turbines in the regular (blue) and irregular (red) wind farm layouts using a Wöhler exponent  $m = 4$ . The result is shown in Figure 6.

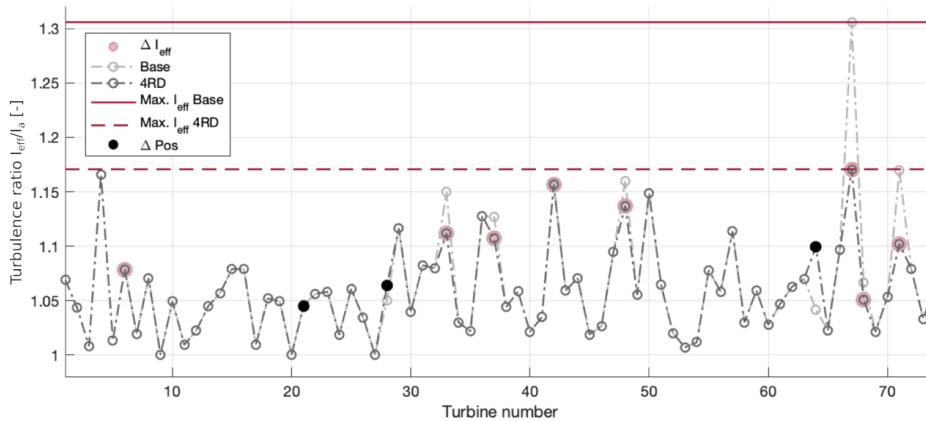
As expected, the effective turbulence intensity levels are more constant for the regular wind farm layout. This means that wake-induced tower fatigue is similar for all turbines. For the irregular layout, however, a single outlier (in this case, turbine  
 135 67) can significantly increase tower steel for the entire project.

<sup>1</sup>The damage-equivalent load is a load with constant amplitude and fixed frequency causing the same damage the actual variation of loads over a lifetime.



**Figure 6.** Effective to ambient turbulence intensity ratio  $I_{eff}/I_a$  for the different turbines in wind farms with regular (blue) and irregular (red) layouts due to wake-added turbulence using the Frandsen model (Sickler, 2020).

Conveniently, an irregular layout has a higher potential of increasing the minimum inter-turbine spacing. By strategically relocating a limited number of turbines, the wake-induced turbulence of those turbines (and thereby the tower design of all turbines) can be optimised, effectively resolving the issue. One of the turbines for each of the turbine pairs with inter-turbine spacing less than 4 RD is manually moved to satisfy a 4 RD separation constraint to show the result in wake-induced turbulence. The result is shown in Figure 7, resulting in a decrease of 10.4% of the maximum effective turbulence in the wind farm. This in turn results in a cost decrease which can go up to millions of euros depending on the steel price and number of turbines.



**Figure 7.** Effective to ambient turbulence intensity ratio  $I_{eff}/I_a$  of the original and increased inter-turbine spacing wind farm layout. The re-positioned turbines are denoted with a filled black dot. The turbines which are not re-positioned, but do experience a change in effective turbulence, are highlighted in red. The maximum effective turbulence value is indicated with the horizontal red lines for the respective layouts (Sickler, 2020).

The AEP is found to increase with +0.043% (increasing) for the 4RD spacing compared to the 2.73RD spacing. This means both the KPI's maximum effective turbulence intensity and the AEP perform better with an increased spacing.



## 5 General applicability of results

145 ~~The performance indicator group analyses in the first part of this study were performed for the Borssele wind farm with the original 10 MW IEA Wind Task 37 reference wind turbines. In this section, the global effect of the farm layout was investigated using sensitivity studies and additional layout cases with both MDAO and WindPRO. The sensitivity analysis served~~ presented in this section serves as a method to predict the outcome of ~~the performance indicator group results for a change in rotor diameter size or wind climate~~ results:

- 150
- Annual energy production
  - Maximum power drop
  - Standard deviation power per wind direction
  - Maximum effective turbulence, and
  - Standard deviation of the effective turbulence

155 To assess the general applicability of the findings, alternative sets of regular and irregular wind farm layouts are explored. The cases are re-analysed with a reduced rotor diameter and a uniform, unidirectional wind rose are implemented to analyse the effect of the extreme wind rose cases. While this may not inform about the global effects of different layouts, it ~~provided~~ provides a first step toward evaluating the general trends ~~of their effects. To assess this global effect of different layouts, the effect of other optimised wind farm layouts on the performance indicator group results was quantified. The results of the sensitivity studies are shown on.~~

160

### 5.1 Rotor Diameter

To study the sensitivity to the turbine size, the rotor diameter of ~~the left hand side of the red dashed line in , and the additional layout case studies are shown on the right of this line. The changes to the conditions and layouts are explained in the discussion of the results~~ IEA Wind Task 37 reference wind turbine was down-scaled from 190.8 to 178.3 m. It is expected that the impact

165 on relative performance for the irregular wind farm layout to the regular layout would be small. Indeed, the difference is calculated to be a percentage point change of 0.03 % (an AEP increase of 0.66 % and 0.63 %, respectively).

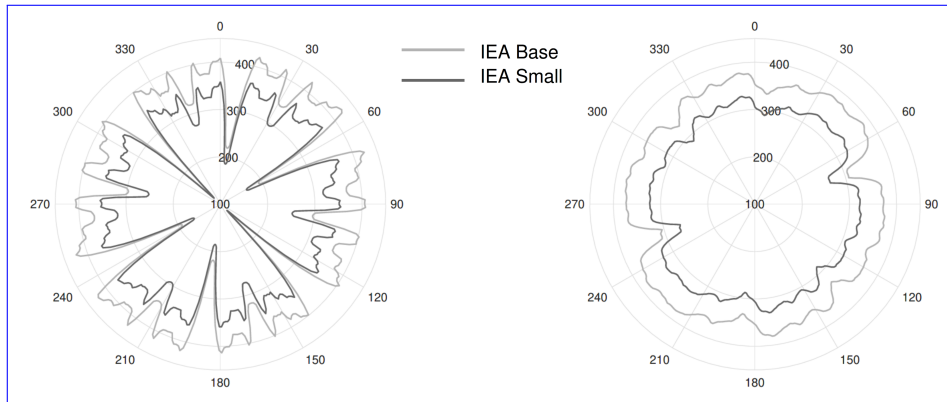
For persistence to wind direction it is found the irregular wind farms perform better than their regular counterpart independent for a smaller rotor diameter, with minor decrease of 0.3% and 0.4% for the maximum power drop and standard deviation respectively. This is small compared to the significant change of rotor area (-13%). The results of the power output are shown

170 in Figure 8 below.

~~To study the sensitivity to the turbine size, the rotor diameter of the IEA Wind Task 37 reference wind turbine was down-scaled from 190.8 to 178.3 m. Comparing the two layouts then shows that the relative sub-performance indicator results between the irregular and regular layouts are only marginally affected by this size change. Following, the sensitivity to the~~

For effective turbulence, a higher sensitivity to changes in the rotor diameter is found, at 5.5 % and 3.5% respectively. This

175 can be explained when considering that the wake model used, Frandsen, includes turbines within a radius of 10 RD around each turbine. So, a smaller rotor diameter results in fewer neighboring turbines being considered in the calculation, resulting in significantly lower results for effective turbulence.



**Figure 8.** Absolute percentage points change obtained from the sensitivity (left Power output in MW as a function of wind direction for the red-dashed-line(a) Regular and additional case studies (right of the dashed red line b) -The absolute percentage points change are computed based on the Irregular wind farm layout pair relative performance compared to with the base layout pair performance IEA Base (light-grey) and IEA Small (dark-grey) turbines, with a mean wind speed of 9.5 m/s (Sickler, 2020).

Overall, assessing the rotor diameter sensitivity results it can be observed that the difference in performance of the wind rose was investigated, considering uniform and unidirectional wind roses. The farms with irregular layout compared to the wind farms with regular layout is very similar regardless of the turbine rotor diameter selected. However, although not changing the overall conclusion regarding irregular vs. regular layouts, turbulence intensity is found to be impacted more significantly by the rotor size than the power performance results.

## 5.2 Wind Rose

A uniform wind rose and a single direction wind speed of 9.5 m/s in the prevailing wind direction have been used to investigate the sensitivity of the performance indicator group results to changes in the wind rose was no longer negligible. Especially the results for the sub-performance indicator effective turbulence changed significantly between the Borssele and results to the uniform wind rose climate. The percentage point change computed comparing the percentage point difference between the uniform and single direction wind speed results to the Base Case results in -0.23 % and -0.99 % for the uniform and single direction wind speed respectively.

It should be noted that the wind farm layout is not optimised for changes in input parameters, which is not realistic. WindPRO was utilised to develop an additional wind farm layout for the Borssele case study. Two additional optimisations for a In the analysis of persistence to wind direction, the wind farm is subjected to two different wind speeds to assess their effect on the obtained results. The wind speeds selected are 8 m/s and 12 m/s respectively. The difference in percentage point difference when comparing the irregular and regular wind farms show -0.68% and -1.85% compared to the base mean wind speed case. Also, the effective turbulence intensity is analysed for the uniform wind rose distribution. The sensitivity of the maximum effective turbulence and standard deviation of the effective turbulence are both found to be relatively high compared to the

other previous sensitivity studies. With a percentage point change of 10.1 % and 9.9 %, the wind climate distribution is found to significantly change in rotor diameter showed that the farm layout does not change significantly as a function of this input change. On the other hand, the changes of the wind rose altered the optimised wind farm layout significantly the effective turbulence results. Overall, the sensitivity of the results to changes in wind climate is significant, in particular the results regarding the effective turbulence for a (very large) change in the wind rose. Still, the irregular layout outperforms the regular one.

Finally, the-

### 5.3 Layout

205 Finally, a second set of regular and irregular turbine patterns was used from the same study by Sanchez Perez Moreno (2019), and an optimisation in WindPRO was performed for the Base Case area, number of turbines, wind speed distribution and rotor diameter. These MDAO- and WindPRO-optimised farm layout pairs were compared. The aim of performing these additional case studies was to assess the global effect of these wind farm layouts on the performance indicator group results. We observed that the relative behaviour of the layout pairs (Base, MDAO, and WindPRO) is very similar. ~~The largest difference is in the-~~

210 ~~The annual energy output difference in percentage points difference compared to the base case is found to be 0.38% and 0.01% for the WindPRO and MDAO cases respectively. Comparing the persistence to wind direction for the standard deviation, the irregular wind farm layouts showed better performance for both the maximum power drop and standard deviation of the power output as a function of wind direction. This sub-performance indicator result strongly depends on the size of the wind farm with regular layout~~ Corresponding to a difference in percentage change of 12.4 % and 41.6 % for the maximum power  
215 ~~drop, and 8.6% and 68.1% for the standard deviation of the power output per wind direction.~~

~~Different analysis methods were implemented to assess the global effect of the wind farm-~~ The effective turbulence intensity comparative analysis for the MDAO and WindPRO layouts show a percentage point change of 5.9 % and 1.7%. Overall, the effective turbulence intensity results for the additional wind farm layouts indicate that the trend found in Chapter 4 applies for a different set of regular vs. irregular layouts as well.

220 The global sensitivity study performed with the additional layout case studies is shown on the right of this line. The changes to the conditions and layouts are explained in the discussion of the results below.

The conclusions drawn from this sensitivity study appear to be more generally applicable for irregular patterns. It is found that for different layout ~~on the performance indicator group results-~~ It was found that regardless of the changes in layout cases, wind ~~rose or roses and~~ rotor radius, the absolute inter-pair results ~~are identical as to which layout outperforms the other-~~ For  
225 ~~example, in the base case, the irregular wind farm was found to perform worse on the-~~ show the irregular layout outperforming the regular one except for maximum effective turbulence. ~~The same negative behaviour was found with respect to the regular wind farm layout for a change in rotor diameter, wind climate and also for alternative wind farm layouts-, which is worse for irregular layouts and which can be explained very well.~~

## 6 Conclusions

230 ~~Irregular~~ Based on the work done in this paper, it is found that irregular wind farm layouts outperform regular layouts regarding energy production, as overall wake losses are reduced. In the performed case study, an overall yield increase of 0.66% was found for the chosen layout pair. A notable finding ~~was that the irregular layout also increases~~ is that irregular layouts also increase the persistence to wind direction, which means that the power output is less sensitive to fluctuations in wind direction. ~~The~~ For the case study done, the maximum power drop of the irregular layout is roughly one-third of the maximum power drop observed in the regular layout. This characteristic of irregular layouts improves the predictability of the power output, reducing the impact of wind forecasting errors on power system operation and potentially increasing the value of power in the electricity market. The actual benefit of an irregular layout compared to a regular one, ceteris paribus, will vary between the actual layouts compared.

~~However, irregular layouts may increase the overall tower steel use~~ A drawback of irregular layouts is that the turbulence intensity for some turbines may be higher. Using the Frandsen model, the irregular layout is found to generate 14 to 24% higher worst-case wake-induced turbulence levels. This results in higher fatigue loads, increases in tower wall thickness and therefore higher steel costs. Since typically only one wind turbine tower design is used per project, this effect may be significant at the project level. By increasing the minimum spacing, the worst-case turbulence intensity is reduced by 10.4%, bringing the worst-case wake-induced turbulence within the range of the regular layout. This conclusion has general validity since irregular layouts inherently have at least a few turbines positioned with limited spacing. Although the use of irregular wind farm patterns increases energy yield, improving the performance of the wind farm as a whole requires caution to inter-turbine spacing to limit the negative effect of increased fatigue-loading.

*Author contributions.* MS and BU wrote the original draft. MZ, RS and KD were involved in the revision of the work.

*Competing interests.* There are no competing interests.

## 250 References

- Akay, B., Ragni, D., Ferreira, C. S., and Bussel, G. J. W. V.: Experimental investigation of the root flow in a horizontal axis wind turbine, *Wind Energy*, 17, 1093–1109, <https://doi.org/10.1002/we.1620>, 2014.
- Bortolotti, P., Tarres, H. C., Dykes, K. L., Merz, K., Sethuraman, L., Verelst, D., and Zahle, F.: IEA Wind TCP Task 37: Systems Engineering in Wind Energy - WP2.1 Reference Wind Turbines, Technical Report NREL/TP-5000-73492, National Renewable Energy Lab. (NREL),  
255 Golden, CO, USA, <https://doi.org/10.2172/1529216>, <https://www.osti.gov/biblio/1529216>, 2019.
- Charhouni, N., Sallaou, M., and Mansouri, K.: Realistic wind farm design layout optimization with different wind turbines types, *International Journal of Energy and Environmental Engineering*, 10, 307–318, <https://doi.org/10.1007/s40095-019-0303-2>, 2019.
- Chen, Y., Li, H., He, B., Wang, P., and Jin, K.: Multi-objective genetic algorithm based innovative wind farm layout optimization method, *Energy Conversion and Management*, 105, 1318–1327, <https://doi.org/10.1016/j.enconman.2015.09.011>, 2015.
- 260 DuPont, B., Cagan, J., and Moriarty, P.: Optimization of Wind Farm Layout and Wind Turbine Geometry Using a Multi-Level Extended Pattern Search Algorithm That Accounts for Variation in Wind Shear Profile Shape, in: *ASME 2012 International Design Engineering Technical Conferences and Computers and Information in Engineering Conference*, vol. Volume 3: 38th Design Automation Conference, Parts A and B, Chicago, Illinois, USA Chicago, Illinois, USA, <https://doi.org/10.1115/DETC2012-70290>, 2012.
- Frandsen, S. T.: Turbulence and turbulence- generated structural loading in wind turbine clusters, Technical Report Risoe-R-1188, Risoe  
265 National Laboratory, 2007.
- Frohboese, P. and Schmuck, C.: Thrust coefficients used for estimation of wake effects for fatigue load calculation, in: *European Wind Energy Conference and Exhibition 2010*, pp. 1–10, Warsaw, Poland, [http://proceedings.ewea.org/ewec2010/allfiles2/207\\_EWEC2010presentation.pdf](http://proceedings.ewea.org/ewec2010/allfiles2/207_EWEC2010presentation.pdf), 2010.
- Gonzalez, E., Nanos, E. M., Seyr, H., Valldecabres, L., Yürüşen, N. Y., Smolka, U., Muskulus, M., and Melero, J. J.: Key Performance  
270 Indicators for Wind Farm Operation and Maintenance, *Energy Procedia*, 137, 559–570, <https://doi.org/10.1016/j.egypro.2017.10.385>, 2017.
- Grady, S. A., Hussaini, M. Y., and Abdullah, M. M.: Placement of wind turbines using genetic algorithms, *Renewable Energy*, 30, 259–270, <https://doi.org/10.1016/j.renene.2004.05.007>, 2005.
- Igwemezie, V., Mehmanparast, A., and Kolios, A.: Materials selection for XL wind turbine support structures: A corrosion-fatigue perspec-  
275 tive, *Marine Structures*, 61, 381–397, <https://doi.org/10.1016/j.marstruc.2018.06.008>, 2018.
- International Energy Agency (IEA): *Wind Electricity*, <https://www.iea.org/reports/wind-electricity>, 2022.
- Karouani, Y. and Elhoussaine, Z.: Toward an intelligent traffic management based on big data for smart city, in: *Innovations in Smart Cities and Applications*, edited by Ben Ahmed, M. and Boudhir, A., vol. 37 of *SCAMS 2017. Lecture Notes in Networks and Systems*, pp. 502–514, Springer, Cham, [https://doi.org/10.1007/978-3-319-74500-8\\_47](https://doi.org/10.1007/978-3-319-74500-8_47), 2018.
- 280 Marmidis, G., Lazarou, S., and Pyrgioti, E.: Optimal placement of wind turbines in a wind park using Monte Carlo simulation, *Renewable Energy*, 33, 1455–1460, <https://doi.org/10.1016/j.renene.2007.09.004>, 2008.
- Musgrove, P.: *Wind Power*, no. 9780521762380 in Cambridge Books, Cambridge University Press, <https://ideas.repec.org/b/cup/cbooks/9780521762380.html>, 2009.
- Nissen, U. and Harfst, N.: Shortcomings of the traditional “levelized cost of energy” [LCOE] for the determination of grid parity, *Energy*,  
285 171, 1009–1016, <https://doi.org/10.1016/j.energy.2019.01.093>, 2019.

- Nygaard, N. G.: Wakes in very large wind farms and the effect of neighbouring wind farms, *Journal of Physics: Conference Series*, 524, 012 162, <https://doi.org/10.1088/1742-6596/524/1/012162>, 2014.
- Ostachowicz, W., McGugan, M., Schröder-Hinrichs, J. U., and Luczak, M.: MARE-WINT: New materials and reliability in offshore wind turbine technology, Springer Cham, <https://doi.org/10.1007/978-3-319-39095-6>, 2016.
- 290 Riezebos, H. J., Hasselaar, R., Raaijmakers, T., and Vermaas, T.: Site Studies Wind Farm Zone Borssele: Morphodynamics of Borssele Wind Farm Zone, Tech. rep., Deltares, [https://english.rvo.nl/sites/default/files/2015/02/SiteStudiesWindFarmZoneBorssele\\_MorphodynamicsofBorsseleWindFarmZone.pdf](https://english.rvo.nl/sites/default/files/2015/02/SiteStudiesWindFarmZoneBorssele_MorphodynamicsofBorsseleWindFarmZone.pdf), 2015.
- Sanchez Perez Moreno, S.: A guideline for selecting MDAO workflows with an application in offshore wind energy, Ph.D. thesis, Delft University of Technology, <https://doi.org/10.4233/uuid:ea1b4101-0e55-4abe-9539-ae5d81cf9f65>, 2019.
- 295 Shafiee, M., Brennan, F., and Espinosa, I. A.: A parametric whole life cost model for offshore wind farms, *International Journal of Life Cycle Assessment*, 21, 961–975, <https://doi.org/10.1007/s11367-016-1075-z>, 2016.
- Shakoor, R., Hassan, M. Y., Raheem, A., and Rasheed, N.: Wind farm layout optimization using area dimensions and definite point selection techniques, *Renewable Energy*, 88, 154–163, <https://doi.org/10.1016/j.renene.2015.11.021>, 2016.
- Sickler, M.: Offshore Wind Farm Optimisation: A Comparison of Performance between Regular and Irregular Wind Turbine Layouts, Master's thesis, Delft University of Technology, <http://resolver.tudelft.nl/uuid:c7d52141-1218-4754-bf16-8cbb1a46fee0>, 2020.
- 300 Stanley, A. P. and Ning, A.: Coupled wind turbine design and layout optimization with nonhomogeneous wind turbines, *Wind Energy Science*, 4, 99–114, <https://doi.org/10.5194/wes-4-99-2019>, 2019.
- Tao, J. Y. and Finenko, A.: Moving beyond LCOE: impact of various financing methods on PV profitability for SIDS, *Energy Policy*, 98, 749–758, <https://doi.org/10.1016/j.enpol.2016.03.021>, 2016.
- 305 Thomsen, K. and Sørensen, P.: Fatigue loads for wind turbines operating in wakes, *Journal of Wind Engineering and Industrial Aerodynamics*, 80, 121–136, [https://doi.org/10.1016/S0167-6105\(98\)00194-9](https://doi.org/10.1016/S0167-6105(98)00194-9), 1999.