Combining wake redirection and derating strategies in a **load-constrained** wind farm **load-constrained** power maximization

Alessandro Croce¹, Stefano Cacciola¹, and Federico Isella¹ ¹Department of Aerospace Science and Technology, Politecnico di Milano, Milano, Italy **Correspondence:** Alessandro Croce (alessandro.croce@polimi.it)

Abstract. Power derating and wake redirection are two wind farm control techniques proposed in the last decade as means for increasing the overall wind farm power output. While derating operations are associated with a limited gain in terms of farm energy harvesting and with a decrease in turbine loading levels, farm controls based on wake redirection proved, both in silico and experimental tests, to entail significant increases in the overall wind farm power output. However, according to wake redirection strategies, the upstream wind turbines may typically operate at large yaw misalignment angles, and the possible increase in loads that the machines may experience in such conditions represents a source of concern when it comes

to testing this control on existing farms that are not specifically designed for prolonged misaligned operations. In this work, it is first demonstrated that a suitable derating level can compensate for the increase in the rotor loads associated with large

misalignment angles. Secondarily, two load-constrained wind farm controls based on a combination of wake redirection and
derating are proposed with the aim of maximizing the overall farm output while maintaining unaltered the design load envelope of the wind turbines operating within the controlled wind farm.

1 Introduction

5

Maximizing the power harvested by wind energy systems and minimizing the associated cost of the energy represent two of the most important goals in the development of any industrial wind energy project. In the last decade, the optimization paradigm has moved from turbine (?) to farm level (??). The concept of wind farm control refers to the synergistic control of all wind turbines within a farm with the goal of maximizing the overall power output, as opposed to the maximization of the single-machine output.

Among all possible techniques that have been proposed as wind farm controls, e.g. wake redirection (?), steady axial induction (?) or dynamic induction control (??), the one that wake redirection (WR) has proved to be highly effective as means

20 of increasing the for increasing wind farm energy harvestingis the wake redirection (WR). According to WR technique, the upstream turbine is intentionally yawed so as to deflect its wake out of downstream rotors. Clearly, away from downstream rotors, at the expense of possible load increase due to operations at large yaw misalignment may be detrimental in terms of the loading exerted on the turbine(??).

As reported in a recent review paper related to the flow control applied to wind farm optimization (?), quantifying the impacts of wind farm control on turbine structural loads represents a critical area of investigation.

In fact, modern wind turbines are designed with the aim of minimizing the associated cost of energy by looking for a good balance between aerodynamic performance and reliability of the structural components (?). The international Standards, e.g. ????, provide the guidelines for the design including a list of design load cases (DLC) to be considered for quantifying fatigue and ultimate loads, as well as maximum structural deflection. An already existing turbine could have been designed without

30

considering the possible impact of wind farm control on design loads. Consequently, in the case of WR control, the loads and displacements arising from prolonged vawed operations may be a source of concern when it comes to testing or applying a wind farm control technique to already existing farms.

As argued in ???, operating at large yaw misalignment angles, for an isolated (not-waked) turbine, can entail increased design loads, with severity depending on several parameters, such as wind velocity, turbulence intensity, and shear layer.

- To cope with this issue, wind farm control definitions employed in real farms often considered strong limitations in the 35 allowable misalignment angles. For example, in a testing campaign reported in ? the misalignment misaligned turbines were persistently yawed by 20 deg clockwise for wind coming from a specific sector. In another field campaign, ? employed the so-called "one-sided wake redirection", where only clockwise yaw offsets are allowed. The reason for such a technique lies in the fact that, according to a preliminary study on misalignment-induced loads (?), clockwise yaw misalignment angles are
- associated with a lower impact in terms of loads. 40

A notable exception to the persistent application of the "one-sided wake redirection" technique to real wind farms is represented by the testing campaign presented in ?, in which both negative and positive misalignment angles were employed. However, the maximum misalignment assigned to turbines was limited to 20 deg, and the Authors acknowledged that loads were not considered even if they may play a prominent role.

45

In this paper, we consider the combination of wake redirection and steady derating controls, that are techniques, integrated in a load-constrained wind farm control.? acknowledged that while wake redirection can be associated with an increase in the loading status of the turbine, derated operations may entail load reduction.

Clearly, the The combination of the aforementioned strategies is not new, as witnessed by the work of ? and ? that proposed combined wind farm control with the aim of balancing power harvesting and fatigue loads at wind farm level. Both contributions suggested that, while wake redirection is exploited for power maximization, derated operations can be optimized so as

to achieve a two-fold goal: decreasing fatigue of the turbines and adjusting to decrease turbine fatigue and adjust the overall power output to match power the demand.

In this paper, we follow a different methodology that is mainly based on the use of a suitable derating level to compensate for the possible increase in loads induced by yawed operations.

55

50

Next, from the map computed in the previous step, the derating level that compensates for the increase in design indicators induced by misalignment is computed. Such a compensating derating level is likely a nonlinear function of the misalignment

In particular, the methodology considers three steps. At first the maximum design loads and blade tip deflections, not only fatigue, are computed for different combinations of the derating level and misalignment angles. In the preliminary investigation, performed in this paper, only the isolated turbine is considered.

60 angle and can be viewed as a load constraint, that defines a **safe envelope region** in which combined operations, derated and misaligned, do not lead to <u>increase increased</u> design loads and blade deflections.

Finally, two open-loop combined and load-constrained controls are proposed by exploiting the safe envelope.

The first is an optimal combined approach in which the derating levels and the misalignment angles of all turbines within the farm are computed so as to optimize the farm power subject to the constraint that the turbine operations be inside the safe envelope.

The second one is a sub-optimal combined control, that only optimizes the misalignment angles without considering load limitations. Afterward, the derating for The derating of all turbines is computed then computed, outside the optimization loop, by projecting the obtained misalignment on the loads-constraint load-constraint function.

The controls were tested in a simulation environment, through Floris simulations (?) of two-turbine and nine-turbine 70 wind farms.

Both approaches proved effective in increasing the overall farm production, featuring power gains mildly lower than the ones associated with standard unconstrained wake redirection methodologies. <u>Moreover, thanks-Thanks</u> to the proposed open-loop controls, it is not necessary to impose strong limitations on yaw misalignment angles, such as one-sided policies, as the load constraint automatically ensures load protection.

75 Moreover, the load-constrained combination of wake redirection and derating, as it is formulated in this work, can be easily employed in both open- and closed-loop wind farm control algorithms, even if here only open-loop controls are considered.

The paper is divided into three sections. Firstly, Sec. ?? is devoted to the description of the process used for defining the safe envelope and to the formulation of the load-constrained combined control. Secondarily, In Sec. ?? the reference wind turbine and the farm modeling are presented. This section includes also the details about the strategy employed to render derated

80 operations. Sec. ?? deals with the results of all analyses performed to evaluate the load constraint of a 10MW reference wind turbine and to quantify the performance of the proposed controls. Finally, Sec. ?? concludes the paper by summarizing the main findings of the work.

2 Methodology

65

In this section, the methodology followed to define the load-constrained wind farm control combining wake redirection and turbine derating will be detailed.

Such a process considers three consecutive steps. At first, in Sec. ??, a parametric analysis is performed in order to quantify the impact of the combination of yaw misalignment and derating operation on the different design loads of a wind turbine. Secondarily, from the output of the previous analysis, one has to identify the **safe envelope region**, i.e. the region comprising all those combinations of yaw misalignment and derating which are not associated with an increase in the design loads with respect

90 to the reference condition with null misalignment and null derating. Finally, a load-constrained control can be formulated with the goal of finding the optimal wind farm output only-within the safe-envelope region. Figure **??** <u>qualitatively</u> illustrates this conceptin a <u>qualitative way</u>. At first, left plot, one evaluates the increase (or decrease) of different indicators (such as ultimate and fatigue loads as well as blade deformations) due to derated or yawed operations. Then, middle plot, for all considered indicators, the combinations of derating and yaw misalignment associated with null impact are obtained, generating multiple constraint lines. At last, right plot, all constraints are merged together to define the safe envelope region, i.e. the region in the plane derating–versus–misalignment that satisfies all the constraints.

95

100

Clearly, in order to keep any turbine of the wind farm within its safe envelopeoperating below or at its design loads, a wind farm control should seek the maximum power output controller should maximize the overall power within the safe envelope of each turbine belonging to the farm, combining this way derated and misaligned operationsall turbines, thereby combining derating and wake redirection.



Figure 1. Sketch of the process for defining the safe envelope. Left (blue) block: qualitative contour plots of the increase in all design indicators (e.g. fatigue and ultimate loads or maximum displacements) in terms of misalignment and derating. Middle (orange) block: definition of the constraint function for each indicator, i.e. derating level that compensates for the possible increase in the specific load or displacement entailed by the misalignment. Right (green) block: combination of all load-specific constraints to define the **safe envelope region**.

The forthcoming sections **??** and **??**, will better detailed detail the definition of the misalignment-derating constraint and the load-constrained maximization of the overall wind farm output, respectively.

2.1 Definition of the misalignment-derating constraint through the analysis of fatigue and ultimate loads

As already discussed in the introduction, a parametric study of the impact of derated and yawed operations on ultimate and 105 fatigue loads and maximum blade tip deflection of the isolated wind turbine is first analyzed. The behavior of downstream 105 machines is not considered in this work and, clearly, this represents a limitation of the present analysis. The proposed approach 106 is then to be viewed as a preliminary investigation on the possibility to combine of combining wake redirection and derating 107 farm control strategies to keep wind turbines operating within their load limits. The findings that will be detailed in Sec. ?? 108 apply to the sole turbines belonging to the front row of the farm but, clearly, an extension to downstream machines can be 110 certainly done providing that a simulator of fatigue and ultimate indicators for all turbines of the farm is available.

The parametric analysis for the isolated turbine takes into account a subset of the well-known list of design load cases (DLC) (see <u>IEC, 2005, ?</u>. Sect. 7.4), that are reported in Tab. ??. Such a shortlist was, chosen according to the findings of ?, which highlighted the most impacting cases in terms of rotor loads of the same turbine model considered in this work, i.e. the INNWIND.EU reference 10-MW machine (?). Possible farm control failure modes are not considered within DLC2.x, because it is reasonable to think that supervisors of farm operations can be implemented so as to disengage the farm control if

malfunctions are detected, in order to minimize their impact on the operations of the single turbines

Table 1. Definition of the DLCs considered in the analyses. NTM: normal turbulence model; ETM: extreme turbulence model; ECD: extreme coherent gust with direction change; EWS: extreme wind shear; EOG: extreme operating gust; EWM: extreme wind speed model.

DLC	Wind	Wind	Horizontal	Fault	Safety	Performance
	Туре	speed	Misalignment	Fault	Factor	indicator
1.1/1.2	NTM	$V_{\mathrm{in}}:V_{\mathrm{out}}$	-	-	1.35	Fatigue and Ultimate
1.3	ETM	$V_{\mathrm{in}}:V_{\mathrm{out}}$	-	-	1.35	Ultimate
1.4	ECD	$V_{\rm r}, V_{\rm r}\pm 2, V_{\rm out}$	-		1.35	Ultimate
2.2 PR	NTM	$V_{\mathrm{in}}:V_{\mathrm{out}}$	-	Pitch Runaway	1.1	Ultimate
2.3	EOG	$V_{ m r}, V_{ m out}$	-	Grid Loss	1.1	Ultimate
6.2	EWM	$V_{ m ref}$	$-180:180 \deg$	Grid Loss	1.1	Ultimate
6.3	EWM	$V_{ m ref}$	$-20:20 \deg$	-	1.1	Ultimate

The DLC list should be repeated for different couples of turbine yaw misalignment angles and derating levels.

The misalignment angle ϕ corresponds to the angle between the wind direction and the projection of the rotor axis on a horizontal plane. A positive value of the misalignment angle is, in this work, associated with a counterclockwise rotation of the rotor seen from above. Consequently, the turbine experiences positive value misalignment if the wind velocity, viewed by an

observer located on the rotor center and looking in front of the turbine, has a lateral component coming from the right side.

120

115

The derating ξ , on the other side, is defined as the ratio between the power reduction and the reference one in the same wind condition. Accordingly,

$$P_{\rm der}(V) = (1 - \xi) P_{\rm nom}(V), \tag{1}$$

125 where P_{nom} is the nominal power, P_{der} is the derated one and V is the wind velocity.

Fatigue and ultimate loads for all turbine sub-components are then stored in look-up tables generating an overall map related to the variation of the design indicators as functions of the typical wind farm control parameters (i.e. yaw misalignment and derating).

- It is expected that, independently of the turbine type and of its location within the farm, derated operations will entail a general reduction in maximum and fatigue loads. On the other side, yawed operations may increase the overall loading status of the machine with respect to the reference condition associated with null yaw misalignment and null derating. The left block in Fig. ?? provides a sketch of what one could expect from such a sensitivity analysis: all different design loads (fatigue and ultimate loads or maximum displacement) feature a complex behavior (typically non-linear and discontinuous) in terms of derating levels and misalignment angles, that can be quantified numerically.
- 135

140

150

5 Starting from this consideration, one can infer that given a specific load of interest, it is possible to find a derating level for each yaw misalignment angle that compensates for the possible increase in the design loads.

To this end, consider the *j*th generic design indicator (e.g. maximum displacement, fatigue, or ultimate load) associated with the *i*th turbine within the farm, named $y_{j_i}(\xi_i, \varphi_i)$ function of the turbine misalignment and derating. For all y_{j_i} one can find a compensating derating level by imposing the equality between the design indicator and those associated with the reference condition, as

$$y_{j_i}(\xi_i,\varphi_i) - y_{j_i}(0,0), \quad i = 1, \dots, N_{\text{turb}}; \ j = 1, \dots, N_{\text{ind}};$$
⁽²⁾

where ξ_i and φ_i are respectively the derating and misalignment angle of the *i*th turbine, N_{turb} is the number of the turbine within the farm, N_{ind} is the number of design indicators considered, while $y_{j_i}(0,0)$ refers to the design indicator of the reference conditions with $\xi_i = \varphi_i = 0$.

145 The function that solves Eq. (??) is named $f_{j_i}^{\text{cnstr}}$ and links the yaw misalignment angles with the load-compensating derating $\xi_{j_i}^{\text{cnstr}}$ as

$$\xi_{j_i}^{\text{cnstr}} = f_{j_i}^{\text{cnstr}}(\phi_i).$$
(3)

The left and middle blocks of Fig. ?? qualitatively depict this process: from the map of the increase in the value of interested design loads and displacements in terms, functions of misalignment and derating, one can easily extract the constraint function $f_{j_i}^{\text{cnstr}}(\phi_i)$ seeking for the null increase. Notice that each load is expected to feature different constraint functions.

Once the load-specific constraints $f_{j_i}^{\text{cnstr}}$ of the *i*th turbine of the farm are determined for all indicators of interest, these are to be combined to define the overall turbine constraint function g_i^{cnstr} , by selecting the most limiting constraints for each misalignment as

$$g_i^{\text{cnstr}}(\phi_i) = \max_j \left(f_{j_i}^{\text{cnstr}}(\phi_i) \right).$$
(4)

The right block of Fig. ?? qualitatively shows how to combine the different load-specific constraints, into an overall one. Clearly, for For each turbine in the farm, the constraint function g_i^{cnstr} splits the domain derating-misalignment into two regions. The first one, indicated with the green texture in Fig. ??, is the **safe envelope region** where all combinations of derating and yaw misalignment do not entail an increase in any of the design loads and displacements with respect to the reference conditions. Such a region can be mathematically indicated as

160
$$\xi_i \ge g_i^{\text{cnstr}}(\phi_i)$$
. (5)

It is expected that larger misalignment angles imply higher derating levels to compensate for possible increases in design indicators.

Then, a second region, when $\xi_i < g_i^{\text{cnstr}}(\phi_i)$, comprises all combinations of misalignment and derating, where at least one load-specific constraint is violated, implying that it is possible that the *i*th turbine may experience an increase in that design load or displacement.

165

From a practical point of view, assuming that a turbine was designed and certified for standard operations with limited yaw misalignment angles, when it comes to implementing a farm control logic based on wake redirection, in order to keep the machine within its safe envelope, one has to simply enforce a certain level of derating when the turbine is subject to important yawed operations. Notice that this approach represents an interesting alternative to employing one-side wake steering

170 policies or, in general, imposing strong limitations on the possible yaw misalignment angles, such as those used in many field applications of the wind farm control based on wake redirection (?). In fact, it is not important to avoid a turbine working at misalignment angles potentially dangerous for its structural integrity, but rather to limit the increase in the machine loading status, a task that can be also accomplished by unloading the turbine through a suitable derating level.

Before describing possible uses of the safe envelope region within the synthesis of wind farm control, it is worthwhile 175 clarifying some aspects.

First of all, the process described in this section to define the safe-envelope region could lead to a constraint curve excessively limiting. In fact, the DLC list, which is typically employed to design turbines, also considers extreme events and faults. Consequently, operating for a limited time outside the safe envelope does not necessarily imply a structural failure of the turbine. For example, if one expects that a too-large maximum tip deflection may be experienced at a large yaw misalignment

- 180 during a coherent gust with extreme direction change (DLC 1.4), operating at that misalignment angle is not dangerous unless this extreme event happens. Clearly, such a risk is avoidable if the wind farm operator has one or more systems that allow the super-controller to measure and predict such extreme events in advance (e.g. a LIDAR). Moreover, the constraint curve, as it is defined in Eq. (??), applies to the turbine operations no matter the wind speed and turbulence. This fact could be limiting as the ultimate loads are typically experienced around the rated speed. Consequently, yawed operations at low speeds are seldom
- to be considered problematic. Clearly, a more thorough analysis could be performed so as to evaluate possible dependencies of the safe region with respect to wind velocity, <u>direction</u> and turbulence intensity. This improvement of the process, although interesting, falls outside the scope of the paper, which is aimed at proposing a possible way of combining derating and wake redirection control in a load-constrained algorithm.

Being saidthis That being said, the proposed approach, based on a combination of derating and misalignment, even without

- 190 considering wake redirection, even in its simplest form without wind speed and TI dependency, results is less restrictive than imposing strong limitations on the misalignment range such as those due to other envelope protection alternatives, such as the one-sided wake steering, because the large and very large yaw angles, potentially dangerous, are not which may impose strong limitations on the misalignment angles. In fact, all potentially dangerous yaw angles do not need to be excluded but simply associated with a higher reached providing a suitable level of derating. It is expected that a more sophisticated definition of the safe envelope region (e.g. including speed and TI dependency) may lead to improvement in the effectiveness of the proposed
- solution.

2.2 Load-constrained maximization of wind farm power output based on wake redirection and derating strategies

In this section, we will consider the definition of a wind farm control based on wake steering and derating, which includes also the load constraints as defined in Eq. (??).

200 Three different optimal setpoint definitions are considered. The first refers to the classical wake redirection <u>control control c</u>

205 2.2.1 Reference wake redirection control

Consider a generic steady wind farm control steady-state wind farm controller based on the single wake redirection and unbounded, i.e. without considering the limitations entailed by structural issues. In this case, the control in its simplest definition consists in finding the yaw misalignment setpoints for each turbine of all turbines belonging to the farm so as to maximize the produced power. To this end, let us collect the yaw angle ϕ of all turbines in an array Θ^{ref} , as

210
$$\Theta^{\text{ret}} = \{\phi_1, \phi_2, \dots, \phi_N\},$$
 (6)

where N is the number of turbines in the farm, and on Similarly, the ambient characteristics, i.e. wind speed V, turbulence intensity TI and direction ϕ_{wind} , in are collected into an array p, as,

$$\boldsymbol{p} = \{V, \mathrm{TI}, \phi_{\mathrm{wind}}\},\tag{7}$$

The optimal control set-points related to the reference wake redirection strategy Θ_{opt}^{ref} are computed by maximizing the overall farm power *P* as

$$\boldsymbol{\Theta}_{\mathrm{opt}}^{\mathrm{ref}} = \arg\left(\max\left(P\left(\boldsymbol{\Theta}^{\mathrm{ref}};\boldsymbol{p}\right)\right)\right),\tag{8}$$

where

$$P\left(\boldsymbol{\Theta}^{\mathrm{ref}};\boldsymbol{p}\right) = \sum_{i} P_{i}\left(\boldsymbol{\Theta}^{\mathrm{ref}};\boldsymbol{p}\right)$$
(9)

is the overall farm power, i.e. the sum of the power of the single turbines P_i with i = 1 : N. Clearly, the power of the single turbines P_i and, in turn, the overall farm power, depends on the vaw angles of all turbines Θ and the ambient conditions p.

- Usually, problemProblem (??) requires a non-linear optimization, typically usually gradient-based, with a number of optimization variables equal to the number of turbines belonging to the farm. For very large farms the optimization could be computationally expensive, especially if sophisticated simulation tools, such as those based on computation fluid dynamics, are used. For this reason, engineering or surrogate wind farm models can be employed to estimate the overall power as suggested by ? and ?. Moreover, in order to limit the number of optimization parameters it is also possible to apply the vaw control
- to a limited number of turbines, for example, those which mostly affect the overall power output, as proposed by ?.

Obviously, since no bounds for the misalignment angles have been considered, it is possible that one or more turbines experience increases in their design loads and displacements.

2.2.2 Optimal load-constrained control combining wake redirection and derating

230 To cope with the possible increase in loads due to misaligned operations, it is proposed an optimal load-constrained control is proposed, that combines derating and wake redirection, exploiting the constraint function defined in Eq.(??).

To this end, the array of optimization variables is extended by adding the derating level of all turbines, as in Θ^{comb} ,

$$\boldsymbol{\Theta}^{\text{comb}} = \{\phi_1, \phi_2, \dots, \phi_N, \xi_1, \xi_2, \dots, \xi_N\},\tag{10}$$

where ξ_i is the derating level of the *i*th turbine of the farm.

235

5 The load-constrained optimal combined control set-points for all machines are then computed by solving the following constrained maximization problem,

$$\boldsymbol{\Theta}_{\text{opt}}^{\text{comb}} = \arg\left(\max\left(P\left(\boldsymbol{\Theta}^{\text{comb}}; \boldsymbol{p}\right)\right)\right), \quad \text{s.t.} \quad \xi_i \ge g_i^{\text{cnstr}}(\phi_i), \quad i = 1, \dots, N_{\text{turb}}.$$
(11)

The proposed methodology has some specific advantages with respect to other control techniques developed for a similar aim. Firstly, contrary to the method considered by **?**, it does not require the construction of a surrogate model from costexpensive CFD simulations that would also result invariably dependent on the farm configuration and on the selected scenarios employed to train the surrogate model itself. Secondarily, with respect to what was also proposed by **?**, we also include the ultimate loads and displacements in the analysis. In fact, the sizing of many turbine sub-components is driven by ultimate rather than fatigue loads and, as witnessed by **?** and **?**, only the modification of such ultimate indicators has an effect on the design of the system.

245 2.2.3 Sub-optimal constrained and combined control

<u>Clearly, the The</u> solution of problem (??) requires also also requires the evaluation of the constraint for each wind turbine belonging to the farm, and its linearization in case gradient-based optimization techniques are employed. Moreover, the number of optimization parameters is doubled with respect to that of the unconstrained problem in Eq. (??).

In order to limit the number of optimization parameters, one can employ a sub-optimal algorithm that considers the load

- constraint in a practical and straightforward way starting from the setpoint obtained with the standard wake redirection control. The idea comes from the fact that, as it will be demonstrated in Sec. ??, in terms of optimal misalignment angle the optimal yaw misalignment angles ϕ_{opt} , the solutions of problems ?? and ??are really, are similar for the majority of the analyzed cases. Along with a misalignment angle, the solution of the optimal combined problem features also also features a specific level of derating, which is needed to maintain the turbine operation within its safe envelope. From this consideration, one can
- easily devise a different setpoint definition that optimizes the sole misalignment angles without imposing the constraint, as it is done in the reference case object of Sec. ??. Subsequently, the level of derating for each turbine is computed a posteriori as the minimum one that is needed to satisfy the constraint in Eq. (??). It is expected that this process will generate sub-optimal set-points compliant with the load constraint and associated with a limited reduction marginally lower increase in farm power with respect to than that associated with the optimal combined case.
- 260

To this end, one may define the array with the variable to-be-optimized in the sub-optimal case, Θ^{constr} , exactly as it was defined in the reference wake redirection control

$$\boldsymbol{\Theta}^{\text{constr}} = \boldsymbol{\Theta}^{\text{ref}} = \{\phi_1, \phi_2, \dots, \phi_N\}.$$
(12)

The optimal problem, as in the reference case, is formalized through an unconstrained optimization, as

$$\boldsymbol{\Theta}_{\text{subopt}}^{\text{constr}} = \arg\left(\max\left(P\left(\boldsymbol{\Theta}^{\text{constr}}; \boldsymbol{p}\right)\right)\right),\tag{13}$$

that yields the sub-optimal set-points for all misalignment angles of all turbines.

Finally, the constraint is imposed for all turbines by finding the minimum derating level that satisfies Eq. (??). Such a derating level can be computed, as

$$\xi_{\text{subopt}_{i}}^{\text{constr}} = g_{i}^{\text{cnstr}} \left(\phi_{\text{subopt}_{i}}^{\text{constr}} \right), \quad i = 1, \dots, N_{\text{turb}}, \tag{14}$$

where $\phi_{\text{subopt}_i}^{\text{constr}}$ is the misalignment angle of the *i*th turbine computed through Eq. (??), while $\xi_{\text{subopt}_i}^{\text{constr}}$ is the related derating 270 level, evaluated to satisfy the load constraint. Notice also that the "greater-or-equal" symbol in Eq. (??) is now substituted by a simple "equal" sign, to emphasize that the derating is computed to bring the turbine operation on the onset of its safe envelope.

In order to show what we could typically expect from the three control techniques, a qualitative plot is depicted in Fig. ??. The behavior of the control methodology, hitherto expected, will be subsequently deeply analyzed in the result section (Sec. ??). The scheme refers to a hypothetical contour plot of the increase of the overall power related to a simple two-turbine farm for

- 275 a generic wind condition. The horizontal and vertical axes are associated respectively with the misalignment angle and the derating level of the upstream machine, representing the sole optimization variables, since the downstream turbine will not modify its operating condition. The contour is typically non-symmetric and may feature one or more local maxima. Moreover, too-high levels of derating may entail also a reduction in the overall power output. As wake redirection is typically more efficient in increasing overall farm output than steady derating, the absolute maximum is expected to be found in a condition with
- a specific misalignment and null derating. Consequently, we may envision that the solution of the reference wake redirection



Figure 2. Qualitative definition of the control set-points for the three techniques in the case of a simple two-turbine farm, where only misalignment ϕ_1 and derating ξ_1 of the upstream turbine are optimized. Contour plot: generic increase in the overall power as a function of ϕ_1 and ξ_1 . Solid red line: load constraint. Square marker: unconstrained optimum related to the reference wake redirection control. Circle marker: combined and constrained optimum. × marker: sub-optimum optimum.

problem coincides with the absolute maximum as indicated by the square marker. Clearly, this behavior depends on the specific case: as it will be shown in Sec. ??, it is possible to find the absolute maximum for non-null derating, especially when extremely reduced spacings are considered. On that plot, one may superimpose Superimposed to the contour plot of the farm power increase, as in Fig. ??, one can draw the load constraint, emphasizing what we previously called "safe envelope region"
(see Eq. ??). The lower bounds of the safe envelope region are reported as a solid red line. The solution of the load-constrained and combined control seeks the optimum in the upper part of the plot, where the constraint is satisfied. In general, imposing derating on the upstream machine, when it is yawed to deflect its wake out of downstream rotors, entails a reduction of the overall power output. This means that often, but not always, the optimal set-point of the contour line with the highest power increase. This point is marked in the plot with a circle. Finally, the sub-optimal case is simply derived by projecting the solution of the reference wake redirection on the constraint, yielding the sub-optimal set-point in correspondence with the × marker.

As it will be demonstrated later on, the difference between the solution of the combined and sub-optimal control is typically marginal, as well as the performance of the two techniques in terms of overall farm power increase. Hence, one could in principle define the operative setpoints of the turbines in a sub-optimal turbine's operative setpoints through a simpler optimization sub-optimal algorithm without a strong detrimental impact on the overall power output.

295

3 ResultsDefinition and modeling of the reference wind turbine and farm

3.1 Definition and modeling of the reference wind turbine and farm

The study object of this work considers the 10 MW INNWIND.EU model. This turbine is an upwind pitch-regulated machine of a diameter equal to about 178 m, which is described in **?**. The model was implemented in the general-purpose multibody 300 software Cp-Lambda (**??**). Turbine flexible elements, such as the blades, the tower, and the shaft, are implemented through a nonlinear, kinematically exact beam formulation with fully-populate cross-sectional stiffness matrices (**?**). Rotor aerodynamics is rendered through the classical blade element momentum theory. Lifting lines are used for modeling blade aerodynamic forces and moments, as well as for reproducing the drag of the nacelle and the tower. Hub- and tip-losses and tower shadow are also considered. The overall modeling of the aerodynamics implemented in Cp-Lambda was also recently validated against field 305 data coming from a 2.3 MW wind turbine with a diameter of 80 meters in sheared and yawed inflow conditions (**?**).

The turbine model considers also a first-order dynamic model for the generator and a second-order one for pitch actuators. The control of the turbine in operating conditions all operating conditions, including derated operations, is managed by the POLI-Wind controller and is based on a linear quadratic regulator (LQR), as described in ? and ?. Such an LQR controller is

based on the linearization of the torque balance equation about the trimming conditions, a task that is easy to be performed

- 310 providing the availability of the At first, the turbine operating points can be computed from the standard $C_p \lambda$ curves. The LQR, being model-based, results to be extremely flexible in managing also the derating. In fact, as functions of the wind speed and the derating level. A linear model is extracted by linearizing the model about different reference conditions, that are derived so as to generate a desired derating level, one automatically obtains the new control gains, without modifying the architecture of the control torque balance equation about all these operating points and then used within the LQR algorithm
- 315 for automatically computing the control gains. Thereby, the LQR control technique automatically provides for control gains suitably scheduled for all wind speeds and all derating levels, without the need for hand-tuning.

In particular, in derated conditions, the operating point of the turbine was found by modifying only the pitch settings leaving unaltered the tip-speed ratio with respect to the nominal case at the same wind speed. Hence, for all wind speeds from the cut-in to cut-out, the pitch setting, realizing the desired derating level β_{derat} , was found by solving the following equation

320
$$\frac{1}{2}\rho V^3 SC_p(\lambda_{\text{nom}},\beta) = (1-\xi)P_{\text{nom}}(V),$$
 (15)

where ρ is the air density, λ_{nom} is tip-speed-ratio associated with the nominal case, β the pitch settings and $C_p(\lambda, \beta)$ are the well-known $C_p - \lambda$ look-up table. Given β_{derat} and λ_{nom} for all desired derating levels, it is also possible to evaluate the thrust coefficients, by simply interpolating the thrust coefficient look-up table, $C_t(\lambda, \beta)$.

Finally, misalignment angles are reproduced in the simulation by rotating the nacelle. Control architecture and gains are not modified in yawed conditions with respect to the reference, i.e. aligned, case.

Idling, faults, startup and shutdown maneuvers, and, more in general, all the non-operating conditions and the transition among the different operating states, are managed by the POLI-Wind Supervisor (?).

The analyzed wind farms are modeled through the software FLORIS (FLOW Redirection and Induction in Steady State), jointly developed by NREL and TUDelft (?). This software features a multitude of engineering wake models, which can be

330 employed to characterize the steady flow within the farm. The turbines are included in the farm according to their power and thrust coefficients defined as functions of the wind speed. The outputs of all turbines and, in turn, the overall farm power production are computed according to the mean flow at each rotor location. In this work, the Gaussian wake model and wake combination based on kinetic energy were employed.

Within FLORIS, the impact of misalignment on wake deflection is included in the wake models, whereas derating can be rendered by modifying the power and thrust coefficients of each turbine.

In this work, we did not develop a dedicated formulation for capturing the impact of derating on wake behavior, but we simply relied on the wake model already implemented in FLORIS, which is based on the treatment of ?. In such a model, the turbine thrust coefficient C_T affects multiple wake characteristics including speed deficit, lateral displacement of wake center, in-wake turbulence intensity, and the downstream location associated with the onset of the far-wake region. Having said this,

340 derating a turbine indirectly affects its wake through the variation of the thrust coefficient associated with the lower power coefficient. For this reason, the Bastankhan and Porté-Agel model is considered adequate, at least for the scope of our work, to capture the combined and mutual impact of derating and misalignment on wake behavior.

Dynamical variations of wind direction, derating, and misalignment are not considered.

4 **Results**

345 4.1 Definition of the load constraint and of the safe envelope region

The DLC list in Tab. ?? was simulated with the reference 10 MW turbine model so as to evaluate fatigue and ultimate loads as well as maximum blade tip deflections for all combinations of five yaw misalignment angles $(0, \pm 15, \pm 25)$ deg and five derating levels (0, 2.5%, 5.0%, 10%, 15%).

- Clearly, the DLC6.n series was considered only for the nominal case with null misalignment and null derating, as it refers to a non-operative phase where any farm control is not active. Since this case can result in design loads, however, it is critical to take this into account in this scenario as well. This, in general, raises another general issue regarding the impact of a wind farm controller on ultimate loads or other indicators: if design loads came from not-controlled conditions (e.g. parking) or from conditions where the wind farm control does not operate (at high winds, for example), then clearly this constitutes a condition that can allow the controller to operate without any constraints.
- 355

In this analysis, only wind farm controls scheduled with respect to the sole wind speed are considered, and an upper limit for its activation equal to 15 m/s is imposed, no matter the turbulence intensity (TI), as it was already done by ?.

Finally, notice that the list in Tab. ?? refers to a selection from the whole cases prescribed by the Standards (?). In fact, only the most impacting DLCs were considered on the basis of previous analysis on the same machine, reported in detail in ?.

in In order to present the idea, in this paper only rotor loads are taken into account, neglecting the impact of wake redirection
 and derating on tower and hub loads. However, the very same process can be extended to other turbine sub-components, without any modifications.

Figure ?? shows the two most affecting ultimate indicators related to the blade. The blade-root combined ultimate load and the maximum blade tip deflection are displayed respectively on the left and on the right. Both plots present the percentage variation of such indicators as functions of the misalignment and the derating. In order to evaluate the maximum blade tip deflection, we considered the displacements of all three blades within an azimuthal segment of 60 deg around the tower position, so as to capture only those conditions exposed to the risk of a blade-tower strike.



370



Figure 3. Percentage variation of blade root combined load (left) and maximum blade tip deflection (right) as functions of misalignment and derating, taken with respect to nominal condition (i.e. null misalignment and derating)

Qualitatively, both Both plots feature similar trends: significant increases are experienced at higher misalignment angles. Furthermore, as expected, even small derating levels entail sensible reductions in the indicators, such that it is even possible to fully compensate for the increments caused by large misalignment angles. Notice also how the plots are non-symmetric as the maximum increases in blade root combined loads are experienced for negative misalignment angles, while the blade tip deflection is highest for negative ones. Quantitatively, at -25 deg the derating level that compensates for the increase in blade root loads is slightly higher than 5% (see left plot of Fig. ??), whereas at +25 deg the increase in maximum blade deflection is compensated by a derating slightly less than 5% -(see right plot of Fig. ??). Such values are apparently limited and compatible with turbine standard operating conditions.

Figure ?? shows the DLC type reporting the ultimate indicators for blade root combined load (left) and maximum blade tip deflection (right). Notice how the cases associated with ultimate loads and displacements may vary on the basis of the chosen parameters. This represents further evidence that a global overview of all operative regimes of the turbines is needed to evaluate the actual impact of the farm-controlled operations on the design drivers.



Blade root combined load

385

Maximum blade tip deflection

Figure 4. DLC types associated with the ultimate indicators for blade root combined load (left) and maximum blade tip deflection (right) as functions of misalignment and derating.





Fatigue loads, on the other side, seem less impacted by the misalignment, as can be noticed in Fig. ?? showing the cumulated
DEL for blade root flapwise. The maximum percentage increase is limited, i.e. less than 2%, and is experienced only for positive and large misalignment angles. Here again, as As in the previous analyses, it can be clearly noticed the positive impact of derating on loads can be clearly noticed.

From the maps of the variation of the design indicators, one can easily find the specific constraint functions defined in Eq. (??) by numerically solving Eq. (??). Dealing with the solution of Eq. (??), the maps associated with loads and displacements were linearly interpolated.



Figure 6. Constraint function definition for blade root combined ultimate load, maximum blade tip deflection, and blade root flapwise fatigue load.

Figure ?? displays the constraint functions, i.e. the derating level that compensates for the possible increase in loads and displacements induced by misalignment, for the three analyzed quantities (square markers: blade root combined ultimate load; circle markers: maximum blade tip deflection; triangle marker: blade root flapwise fatigue load).

As it can be easily seen from the graph, for this machine, the most constraining function is associated with the blade root 390 combined ultimate load, while the fatigue of the blade root flapwise features an inactive constraint, as it is associated with lower derating levels for all misalignment angles. The constraint associated with the maximum blade tip deflection, on the other side, is active only for the highest positive misalignment angles.

Finally, the overall constraint function, visualized by a dashed thick line, can be simply extracted from load-specific constraints by taking the maximum derating level as defined in Eq. (??).

395

To cover the range of misalignment angles outside the bounds of the performed analyses, i.e. (± 25) deg, the overall constraint function was linearly extrapolated.

4.2 Optimal load-constrained farm control for different inflow conditions, spacing, and overlaps

In this section, the performance of the reference, combined, and sub-optimal controllers is evaluated in terms of the overall power output of a simple two-turbine wind farm. The analyses were made for different inflow conditions, defined in terms of

400

wind speed V and turbulence intensity TI, and different geometries of the farm, defined in terms of the spacing s between the turbines and the lateral offset y_h of the downstream machine. Figure ?? offers an easy-to-interpret visual representation of the

farm geometry parameters. In particular, we considered all combinations of the following parameters,

Wind speed :
$$V = (7, 10, 11.4, 12, 12.5, 13, 14) \text{ m/s},$$

Turbulence intensity: TI = (2%, 6%, 10%),

Spacing:
$$s = (3D, 4D, 5D, 6D, 7D),$$

Lateral Offset : $y_h = (\pm 1D, \pm 0.75D, \pm 0.5D, \pm 0.25D, 0);$

for a total number of 945 cases. The range of wind speed, between 7 and 14 m/s, was chosen so as to focus on the region
 where the farm control is expected to be highly effective. In fact, below 7 m/s its impact is mild due to low speed, whereas above 14 m/s the control becomes ineffective as the low thrust coefficients, characterizing the upstream turbine, entail a small speed deficit inside the wake. Clearly, a comprehensive analysis for design purposes of for the evaluation of the control impact of large farms should consider a wider range, extended especially towards the cut-in speed.

(16)

The optimal load-constrained solutions of Eq. (??) and of the sub-optimals one of Eq. (??) presented here below, have been 410 computed in MATLAB, by solving the constrained optimization problem with a gradient based gradient-based algorithm (i.e. *fmincon*) coupled with the wind farm solver Floris (?).



Figure 7. Top view of the simple two-turbine farm with the most important geometry parameters, i.e. spacing s and lateral offset y_h . The lateral offset is positive if the downstream turbine is on the right with respect to wind direction if viewed from above.

At first, consider a reference case with wind velocity V = 14 m/sV = 11.4 m/s, corresponding to the rated speed, TI = 6%, spacing s = 5D, being with D being the rotor diameter, and lateral spacing $y_h = 0$ representing a full wake impingement.

Figure **??** shows the contour plot of the farm power gain as a function of the upstream misalignment and derating. The overall constraint function, a solid red curve, is superimposed on the contour, splitting the domain into two regions, where the



Figure 8. Contour plot of the overall power output of the two-turbine farm with s = 5D, $y_h = 0$ and at V = 11.4 m/s and TI = 6%. Red solid line represents the overall constraint function. Optimal control setpoints are also visualized as a square marker (reference wake redirection, only misalignment), circle marker (combined and constrained control) and × marker (sub-optimal control).

Table 2. Optimal setpoint and power gain. Two-turbine wind farm with s = 5D and $y_h = 0$, at V = 11.4 m/s and TI = 6%.

	Misalignment	Derating	Power increase
	\deg	%	%
Combined	22.5	2.6	3.9
Suboptimum	24.6	2.9	3.8
Reference WR	24.6	0.0	5.4

constraint is satisfied (i.e. the safe envelope) and where it is not. Moreover, Tab. ?? summarizes the control set-points and the associated power gains for the three control strategies.

The standard unconstrained wake redirection control finds the optimum at about 24.6 deg and obviously with null derating, outside the safe envelope, with a net increase in the farm output of 5.4%. The optimum found according to the combined strategy, on the other hand, features a slightly lower misalignment (i.e. 24.6 deg) and a mild level of derating (i.e. 2.6%). Notice that this set-point lays exactly on the constraint line. As expected, the inclusion of the constraint into the optimization strategy entails a reduction of the power gain of about 1.5 percentage points. In any case, the gain associated with the combined strategy, 3.9%, still remains significant. Consequently, derating the upstream machine, while it is yawed, to fulfill the load constraint, reduces but does not annihilate the effectiveness of the wake redirection.

425 An important discussion should be made concerning the sub-optimal approach. As said in Sec. ??, combined and reference wake redirection strategies typically feature similar optimal misalignment angles. This fact is clearly visible in the results shown in Fig. ?? and Tab. ??, providing preliminary evidence of the rationale behind the sub-optimal control.

The analyzed case shows that, in the sub-optimal control, the derating set-point of the upstream machine (i.e. 2.9%) is higher than that of the combined strategy as a result of the higher optimal misalignment angle. The However, the gain increment in

- 430
- the sub-optimal control case (i.e. 3.8%, however, results to be) appears to be only marginally lower than the one associated with the combined one equal to 3.8% that of the combined control approach equal to 3.9%. The fact that the two controls are characterized by similar performance could favor the use of the simpler simplest strategy, the sub-optimal one, especially in larger farms when the turbinesto be controlled are much more farms containing a large number of turbines.

Table 3. Optimal set-point and power gain. Two-turbine wind farm with s = 5D and $y_h = 0.5D$, at V = 10.0 m/s and TI = 6%.

	Misalignment	Derating	Power increase		
	\deg	%	%		
Optimal combined	18.6	2.38	7.53		
Suboptimal combined	19.1	2.39	7.52		
Reference WR	19.1	0.0	8.72		

Table 4. Optimal setpoint and power gain. Two-turbine wind farm with s = 7D and $y_h = -0.5D$, at V = 11.4 m/s and TI = 6%.

	Misalignment	Derating	Power increase		
	\deg	%	%		
Optimal combined	-15.2	3.3	6.3		
Suboptimal combined	-17.2	3.7	6.1		
Reference WR	-17.2	0.0	7.9		

435

Tables ?? and ?? report the optimal parameters and gains for two other cases. The first one refers to a condition with wind speed $V = 10.0 \,\mathrm{m/s}$ and TI = 6% with spacing equal to 5D and lateral offset equal to 0.5D corresponding to a partial wake impingement on the left side of the downstream rotor. The second case is characterized by wind speed $V = 11.4 \,\mathrm{m/s}$ and TI = 6% with spacing equal to 7D and lateral offset equal to -0.5D, corresponding now to an impingement on the right side of the downstream machine.

440

From both tables, one can immediately notice that the same conclusions, that were derived for the case related to the full impingement scenario (see Fig. ?? and Tab. ??), are still valid. In particular, the optimal misalignment for the combined control is slightly lower in modulus than the one related to the reference wake redirection control and features a significant power gain even if lower than the one related to the unconstrained case. The difference in power gain is about 1.5 percentage points.

On the other side, sub-optimal control performs similarly to the combined one, a with marginally lower power gains, i.e. less than 0.2 percentage points. This last remark demonstrates again that sub-optimal control represents a valuable strategy.



Figure 9. Contour plot of the overall power output of the two-turbine farm with s = 3D, $y_h = 0$ and at V = 11.4 m/s and TI = 6%. The red solid line represents the overall constraint function. Optimal control set-points are also visualized as a square marker (reference wake redirection, only misalignment), circle marker (combined and constrained control), and × marker (sub-optimal control).

Table 5. Optimal set-point and power gain. Two-turbine wind farm with s = 3D and $y_h = 0$, at V = 11.4 m/s and TI = 6%.

	Misalignment	Derating	Power increase		
	\deg	%	%		
Optimal combined	4.6	2.6	1.1		
Suboptimal combined	7.2	1.2	0.8		
Reference WR	7.2	0.0	0.1		

445 A last case was also considered to show how the three controllers might behave differently in extreme cases, such as those related to very tight spacing. To this end, Fig. ?? and Tab. ?? reports report the results of an analysis with a spacing s = 3D, lateral offset $y_h = 0$, at V = 11.4 m/s and TI = 6%.

In this case, the pure wake redirection is not as effective as in the previous conditions as the close spacing between the turbine does not allow the wake to actually move away from the downstream rotor. Derating strategy, on the other hand, appears to be

450

more effective. In this extreme situation, the optimal combined control outperforms the standard wake redirection and features optimal misalignment angles noticeably lower, i.e from $7.2 \deg$ to $4.6 \deg$. As a consequence of that, the differences in the performance between combined and sub-optimal controls are quite evident.

Clearly, especially for all unusual cases such as the previous example with 3D spacing, a question arises over the validity of the employed steady wake model and the impact of derating on wake characteristics. In fact, it is well-known that steady wake modeling may overestimate the impact of the variation of axial induction on wake development. This said, the obtained increase in power output associated with derating, even in this rather extreme case, does not deviate too far from wind tunnel or field test observations (????).

455



Figure 10. Histograms representing the number of occurrences associated with the differences between the power gains associated with the difference between the percentage gain associated with reference wake redirection control γ^{ref} and that related to the combined one γ^{ref} . Right plot: difference between the percentage gain associated with the optimal combined control γ^{comb} and that related to the sub-optimal one γ^{subopt} . Vertical dashed lines indicate the range associated with the 60%, 85%, and 95% of the occurrences.

An overall analysis of the differences in the performance of the three controls, considering the whole set of 945 analyzed conditions, was also performed with the aim of analyzing this procedure applied to this specific wind farm in more detail.

- 460 Figure ?? displays the histograms representing the number of occurrences associated with specific differences in terms of power gain between the reference wake redirection and the optimal combined controls, on the left, and between combined and sub-optimal controls, on the right. The number of occurrences is reported in the *y*-axis while the difference in the power gains is in the *x*-axis.
- From the left plot of Fig. ??, it is possible to verify that the overall impact of the load constraint on the power output is 465 in general limited, as the difference between the percentage gain associated with reference control γ^{ref} and that related to the combined one γ^{ref} is quite limited for the majority of the analyzed cases. As indicated by the vertical dashed lines, the difference between the gains of the two strategies is below 0.8 percentage points for the 60% of the cases, below 2 percentage points for the 85% of the cases, and below 2.75 percentage points for the 95% of the cases. Negative values in the *x*-axis of the left plot in Fig. ?? refer to those extreme conditions with spacing equal to 3*D*, for which the optimal combined control 470 outperforms the reference one.
 - 21

The difference between combined and sub-optimal controls is even less marked, as witnessed by the right plot of Fig. **??**. For the 95% of the cases, the power gain of the sub-optimal control is lower than that of the combined one for at most 0.4 percentage points.

4.3 Evaluation of control performance for a nine-turbine wind farm.

475 In order to evaluate and compare, in a more complex scenario, the behavior the robustness of the controls, described in Sec. ??, a-in a more realistic scenario, a nine-turbine farm is considered. The goal of the present example is to simply verify that the increased number of optimization variables and the introduction of the constraints do not lead to a problem that is difficult to resolve as the number of turbines grows.

480

The farm layout is organized such that the farm is square-shaped with three rows and three columns spaced by 5 D. The farm is also oriented so as to have the diagonals aligned in the North-South and East-West directions, respectively. The direction the wind is blowing from is indicated with ϕ_{wind} . When $\phi_{wind} = 0 \deg$ the wind is blowing from the North, whereas when $\phi_{wind} = 90 \deg$ it is blowing from the East.

The wind farm layout is represented in Fig. ??, where also the turbine numbering is reported.



Figure 11. Generic nine-turbine wind farm layout

Two relevant conditions are considered. The first considers and inflow with speed V = 9 m/s and direction $\phi_{\text{wind}} = 0 \text{ deg}$, 485 i.e. coming from the North. The second one refers to the same speed but to a different direction, $\phi_{\text{wind}} = 90 \text{ deg} \phi_{\text{wind}} = 45 \text{ deg}$, representing the most impacting condition, being associated with minimum distance between upstream and downstream rotors and with full impingement levels.

In this analysis, it is assumed that the constraint function $g_i^{\text{constr}}(\phi_i)$ stays the same for all turbines, independently of the location within the farm, as

$$490 \quad g_{\ell}^{\text{constr}}(\phi_{\ell}) = g_{\kappa}^{\text{constr}}(\phi_{\kappa}), \quad \forall (\ell; \kappa) \in (1, \dots, N_{\text{turb}}; 1, \dots, N_{\text{turb}})$$

$$(17)$$

Notice that, when the wind is coming from the North, the inner turbine WT#5 is inside the wake of WT#1 and influences through its wake the performance of WT#9. Hence, it is both waked and performing a control action. The hypothesis in Eq. (??) for this turbine (and similarly for any inner turbine) should be then carefully evaluated. We expect that for fatigue loads the assumption of free-stream flow is strong, but can be acceptable for the evaluation of the ultimate loads and displacements, that, in the case at hand, represent the active constraints.

Tables **??** and **??** display the results of the two analyses, reporting, along with the turbine-specific and overall power gains, the derating and the misalignment angle of all machines, for all controls.

495

Table 6. Wind farm analysis at V = 9 m/s and $\phi_{\text{wind}} = 0 \text{ deg. } \phi_i$ and ξ_i : misalignment angle in deg and derating level of the *i* turbine; γ : overall farm power gain in percentage. The behavior of WT#4, WT#7, and WT#8 is respectively equal to that of WT#2, WT#3 and WT#6. The performance of WT#8 is equal to that of WT#6.

	WT	`#1	WT#2		WT#3		WT#5		WT#6		WT#9		Overall power gain
	ϕ_i	ξ_i	γ										
Optimal combined	22.9	2.6	21.5	2.4	0	0	19.4	2.4	0	0	0	0	4.4
Suboptimal combined	25.1	2.9	22.9	2.6	0	0	19.3	2.4	0	0	0	0	4.3
Reference WR	25.1	0	22.9	0	0	0	19.3	0	0	0	0	0	5.7

Table 7. Wind farm analysis at V = 9 m/s and $\phi_{\text{wind}} = 45 \text{ deg}$. ϕ_i and ξ_i : misalignment angle in deg and derating level of the *i* turbine; γ : overall farm power gain in percentage. The behavior of WT#2 and WT#3 is equal to that of WT#1. The behavior of WT#5 and WT#6 is equal to that of WT#4. The behavior of WT#8 and WT#9 is equal to that of WT#7.

	WT#1		WT#4		W	Г#7	Overall power gain
	ϕ_i	ξ_i	γ_i	ϕ_i	ξ_i	γ_i	γ
Optimal combined	25.5	3.1	23.8	3.0	0	0	14.7
Suboptimal combined	28.4	3.5	24.6	2.9	0	0	14.7
Reference WR	28.4	0	24.6	0	0	0	17.8

From the results obtained considering the nine-turbine wind farm, one can derive the same conclusions related to the simpler cases, analyzed in Sec. ??. In particular, the optimal combined control features lower optimal misalignment in the upstream turbines with respect to than those associated with the reference control. The inclusion of the load constraint entails a mild

reduction in the optimal farm output, without, in any case, jeopardizing the effectiveness of the wake redirection strategy. Finally, with respect to the performance of the sub-optimal control is similar to that of the optimal combined control, the sub-optimal oneperforms similarly one, with a negligible reduction in the gain potentially achievable.

5 Conclusions and outlook

515

530

- 505 In this paper, we first presented a parametric analysis related to the impact of the combination of derating and misalignment angles on the design indicators (i.e. fatigue and ultimate loads, and maximum displacements) of an isolated multi-MW wind turbine. The parametric analysis, thanks to the fact that derating entails a general reduction in the loading status of the turbine, was then used for deriving a safe envelope region, i.e. a region where the combination of the two parameters is not associated with an increase in any of the machine design indicators. The safe envelope can be easily formulated in terms of the minimum
- 510 derating level needed to compensate for possible increases in design indicators due to yawed operations. From the performed analyses, such compensating derating was expressed as a nonlinear function of the sole misalignment angle, neglecting possible dependencies on wind speed and turbulence intensity.

Finally, two novel wind farm control techniques, based on a combination of wake redirection and derating, are proposed. The main idea is to exploit a combined use of derating and misalignment to optimize farm production while maintaining all the turbines in the farm within the respective save envelope region.

In a combined approach, the turbine operation set-points, in terms of derating and misalignment, are defined so as to maximize the farm power subject to the constraint that the operation of all turbines be inside the safe envelope. In a suboptimal approach, the load constraint is directly imposed on the optimal misalignment angles defined by the standard wake redirection control.

520 The entire procedure, from the computation of the safe envelope region to the definition of the load-constrained controls, was tested in a simulation environment using a 10MW reference turbine model and two simple reference farms, made by two and nine turbines.

From the results shown in this paper, as well as from extensive practice on the same topic, the following conclusions can be derived.

525 – Derating the turbine when it is yawed has the advantage of reducing the impact that misaligned operations may have on turbine design indicators. In particular, not only blade fatigue loads are reduced but also ultimate loads and maximum blade tip deflections.

- With a simple parametric study, it is possible to find a derating level, function of the misalignment angles, that is able to compensate for the possible increase in the design indicators entailed by the yawed operations. In this study, the compensating derating level resulted to be quite small, of the order of a few percentage points.

24

- When tested on simple two-turbine and nine-turbine farms the optimal combined control performs as expected. Clearly, a penalty of a few percentage points in the power gain is experienced as a result of the imposition of the load constraint. However, the optimal combined farm control remains highly effective in increasing the overall power output.
- With extremely low spacing, i.e. 3D, the optimal combined control outperforms the standard wake redirection. This was due to the fact that for such reduced spacing the derating is more effective than the wake redirection technique.
- The sub-optimal control, interestingly, features a performance in terms of overall power gain, really similar to that of the
 optimal combined control, and requires an optimization with fewer variables.
- With the proposed controls it is no more could be no longer necessary to limit the yaw misalignment angle of the upstream turbine or to employ "one-sided wake steering" methodology to limit the impact on loads due to large yaw operations. The "derating vs misalignment" constraint automatically ensures that the turbine operates within its load limits.

Clearly, the work object of this paper represents a preliminary investigation and much is to be done before this technique may reach maturity.

The most important improvement of the analysis deals with the tuning of the steady wake model. Even if the farm power

- 545 output increases, obtained in the present analyses, do not significantly differ from the expectation based on the current literature, it is certainly possible that different wake parameters or different turbine types could lead to quantitatively different results. However, a dramatic loss of effectiveness of the load-constrained combined control is not expected in different scenarios. In terms of extension of the proposed control strategy, one can easily list multiple opportunities.
- Firstly, the definition of the safe envelope region should include a dependency on wind speed and, possibly, turbulence
 intensity. This may improve the effectiveness of the optimal combined control, that, as it is implemented in this work, considers
 the load constraint also at low speeds, which are typically associated with a minor impact on the loading status of the machine.
 Secondarily, it will be important to include in the formulation also fatigue and ultimate loads of the downstream machines.
 In fact, the constraint function was here computed only for the upstream turbine in out-of-wake conditions. This will be investigated in further research activities.
- 555 Moreover, we considered only rotor loads and displacement in the definition of the safe envelope. One should evaluate also the constraints related to other measurements such as tower and hub moments.

Last, the proposed methodology, with a few modification_modifications in the tools used, may be used to further analyze employed to further analyze the combination of other wind farm control techniques (i.e. dynamic induction controls).

Finally, the inclusion of the proposed controls in a turbine design framework is certainly an extension of interest.

All the aforementioned extensions and possibilities are currently under investigation.

535

540

Data availability. The data used for generating all figures will be made available for download through a data sharing platform, e.g. Zenodo, in the final revised version of this paper.

Code and data availability. The linked Matlab-Python tool implementing the combined controls can be made available upon request.

Author contributions. All authors provided fundamental inputs to this work through discussions, feedback, and analyses of the obtained

565 results. AC and SC devised the main idea of the load-constrained controls and wrote the manuscript, AC supervised the research activities. FI performed the Floris analyses.

Competing interests. AC is member of the editorial board of Wind Energy Science.

Acknowledgements. The Authors gratefully acknowledge Gianluca Dadda, M.Sc., for his contribution to the preparation of the multibody aero-servo-elastic simulations of the design load cases for the reference 10MW wind turbine combining wake redirection and derating.

570 References

- Annoni, J., Gebraad, P. M., Scholbrock, A. K., Fleming, P., and v. Wingerden, J.-W.: Analysis of axial-induction-based wind plant control using an engineering and a high-order wind plant model., Wind Energy, 19, 1135—1150, 2016.
- Archer, C. L. and Vasel-Be-Hagh, A.: Wake steering via yaw control in multi-turbine wind farms: Recommendations based on large-eddy simulation, Sustainable Energy Technologies and Assessments, 33, 34–43, https://doi.org/https://doi.org/10.1016/j.seta.2019.03.002, 2019.
- 575 Bak, C., Zahle, F., Bitsche, R., Kim, T., Yde, A., Henriksen, L. C., Hansen, M. H., Blasques, J. P. A. A., Gaunaa, M., and Natarajan, A.: The DTU 10-MW Reference Wind Turbine Project Site, Tech. rep., DTU, https://orbit.dtu.dk/en/publications/the-dtu-10-mw-reference-windturbine, 2013.
 - Bastankhah, M. and Porté-Agel, F.: Experimental and theoretical study of wind turbine wakes in yawed conditions, Journal of Fluid Mechanics, 806, 506–541, https://doi.org/10.1017/jfm.2016.595, 2016.
- 580 Bauchau, O. A.: Flexible Multibody Dynamics, vol. 176 of *Solid Mechanics and Its Applications*, Springer Netherlands, 1 edn., 2011. Boorsma, K.: Power and loads forwind turbines in yawed conditions — Analysis of field measurements and aerodynamic predictions, Tech. Rep. ECN-E–12-047, ECN – Energy reserach Center of the Netherlands, 2012.
 - Boorsma, K., Schepers, G., Aagard Madsen, H., Pirrung, G., Sørensen, N., Bangga, G., Imiela, M., Grinderslev, C., Meyer Forsting, A., Shen, W. Z., Croce, A., Cacciola, S., Schaffarczyk, A. P., Lobo, B., Blondel, F., Gilbert, P., Boisard, R., Höning, L., Greco, L., Testa,
- 585 C., Branlard, E., Jonkman, J., and Vijayakumar, G.: Progress in the validation of rotor aerodynamic codes using field data, Wind Energy Science, 8, 211–230, https://doi.org/10.5194/wes-8-211-2023, 2023.
 - Bortolotti, P., Bottasso, C. L., and Croce, A.: Combined preliminary-detailed design of wind turbines, Wind Energy Science, 1, 71-88, https://doi.org/10.5194/wes-1-71-2016, 2016.

Bossanyi, E.: Combining induction control and wake steering for wind farm energy and fatigue loads optimisation, Journal of Physics:

- Conference Series, 1037, 032 011, https://doi.org/10.1088/1742-6596/1037/3/032011, 2018.
 Bossanyi, E. and Ruisi, R.: Axial induction controller field test at Sedini wind farm, Wind Energy Science, 6, 389–408, https://doi.org/10.5194/wes-6-389-2021, 2021.
 - Bottasso, C., Croce, A., Nam, Y., and Riboldi, C.: Power curve tracking in the presence of a tip speed constraint, Renewable Energy, 40, 1–12, https://doi.org/https://doi.org/10.1016/j.renene.2011.07.045, 2012.
- 595 Bottasso, C., F., C., and A., C.: Multi-disciplinary constrained optimization of wind turbines, Multibody System Dynamics, 27, 21–53, https://doi.org/10.1007/s11044-011-9271-x, 2022.
 - Bottasso, C. L. and Croce, A.: Cp-Lambda user manual, Tech. rep., Dipartimento di Scienze e Tecnologie Aerospaziali, Politecnico di Milano, Milano, Italy, 2009–2018.
 - Bottasso, C. L., Croce, A., Savini, B., Sirchi, W., and Trainelli, L.: Aero-servo-elastic modeling and control of wind turbines using finite
- element multibody procedures, Multibody Systems Dynamics, 16, 291–308, 2006.
 - Bottasso, C. L., Croce, A., Riboldi, C. E. D., and Salvetti, M.: Cyclic pitch control for the reduction of ultimate loads on wind turbines, Journal of Physics: Conference Series, 524, 012 063, https://doi.org/10.1088/1742-6596/524/1/012063, 2014.
 - Campagnolo, F., Tamaro, S., Mühle, F., and Bottasso, C. L.: Wind Tunnel Testing of Combined Derating and Wake Steering, IFAC-PapersOnLine, 56, 8400–8405, https://doi.org/10.1016/j.ifacol.2023.10.1034, 22nd IFAC World Congress, 2023.
- 605 Croce, A., Cacciola, S., and Sartori, L.: Evaluation of the impact of active wake control techniques on ultimate loads for a 10 MW wind turbine, Wind Energy Science, 7, 1–17, https://doi.org/10.5194/wes-7-1-2022, 2022.

- Croce, A., Cacciola, S., Montero Montenegro, M., Stipa, S., and Praticó, R.: A CFD-based analysis of dynamic induction techniques for wind farm control applications, Wind Energy, 26, 325–343, https://doi.org/https://doi.org/10.1002/we.2801, 2023.
- Damiani, R., Dana, S., Annoni, J., Fleming, P., Roadman, J., van Dam, J., and Dykes, K.: Assessment of wind turbine component loads under yaw-offset conditions, Wind Energy Science, 3, 173–189, https://doi.org/10.5194/wes-3-173-2018, 2018.
- Debusscher, C. M. J., Göçmen, T., and Andersen, S. J.: Probabilistic surrogates for flow control using combined control strategies, Journal of Physics: Conference Series, 2265, 032 110, https://doi.org/10.1088/1742-6596/2265/3/032110, 2022.

610

- Doekemeijer, B. M., van der Hoek, D., and van Wingerden, J.-W.: Closed-loop model-based wind farm control using FLORIS under timevarying inflow conditions, Renewable Energy, 156, 719–730, https://doi.org/https://doi.org/10.1016/j.renene.2020.04.007, 2020.
- 615 Doekemeijer, B. M., Kern, S., Maturu, S., Kanev, S., Salbert, B., Schreiber, J., Campagnolo, F., Bottasso, C. L., Schuler, S., Wilts, F., Neumann, T., Potenza, G., Calabretta, F., Fioretti, F., and van Wingerden, J.-W.: Field experiment for open-loop yaw-based wake steering at a commercial onshore wind farm in Italy, Wind Energy Science, 6, 159–176, https://doi.org/10.5194/wes-6-159-2021, 2021.
 - Fleming, P., King, J., Dykes, K., Simley, E., Roadman, J., Scholbrock, A., Murphy, P., Lundquist, J. K., Moriarty, P., Fleming, K., van Dam, J., Bay, C., Mudafort, R., Lopez, H., Skopek, J., Scott, M., Ryan, B., Guernsey, C., and Brake, D.: Initial results from a field campaign
- 620 of wake steering applied at a commercial wind farm Part 1, Wind Energy Science, 4, 273–285, https://doi.org/10.5194/wes-4-273-2019, 2019.
 - Frederik, J. A., Weber, R., Cacciola, S., Campagnolo, F., Croce, A., Bottasso, C., and van Wingerden, J.-W.: Periodic dynamic induction control of wind farms: proving the potential in simulations and wind tunnel experiments, Wind Energy Science, 5, 245–257, https://doi.org/10.5194/wes-5-245-2020, 2020.
- 625 Gebraad, P., Thomas, J. J., Ning, A., Fleming, P., and Dykes, K.: Maximization of the annual energy production of wind power plants by optimization of layout and yaw-based wake control, Wind Energy, 20, 97—107, 2017.
 - Gebraad, P. M. O., Teeuwisse, F. W., van Wingerden, J. W., Fleming, P. A., Ruben, S. D., Marden, J. R., and Pao, L. Y.: Wind plant power optimization through yaw control using a parametric model for wake effects—a CFD simulation study, Wind Energy, 19, 95–114, https://doi.org/10.1002/we.1822, 2016.
- 630 Germanischer Lloyd: Guideline for the Certification of Wind Turbines, Tech. rep., Germanischer Lloyd Industrial Services GmbH, Brooktorkai 18, 20457 Hamburg, Germany, 2010.
 - Howland, M. F., Lele, S. K., and Dabiri, J. O.: Wind farm power optimization through wake steering, Proceedings of the National Academy of Sciences, 116, 14 495–14 500, https://doi.org/10.1073/pnas.1903680116, 2019.

Hulsman, P., Andersen, S. J., and Göçmen, T.: Optimizing wind farm control through wake steering using surrogate models based on high-

- fidelity simulations, Wind Energy Science, 5, 309–329, https://doi.org/10.5194/wes-5-309-2020, 2020.
 - Kim, H., Kim, K., Paek, I., Bottasso, C. L., and Campagnolo, F.: A Study on the Active Induction Control of Upstream Wind Turbines for total power increases, Journal of Physics: Conference Series, 753, 032 014, https://doi.org/10.1088/1742-6596/753/3/032014, 2016.
 - IEC 61400-1 Ed.3.: Wind Turbines Part 1: Design requirements, Tech. rep., Garrad Hassan and Partners Ltd, St Vincent's Works, Silverthorne Lane - Bristol BS2 0QD, UK, 2004.
- 640 Meyers, J., Bottasso, C., Dykes, K., Fleming, P., Gebraad, P., Giebel, G., Göçmen, T., and van Wingerden, J.-W.: Wind farm flow control: prospects and challenges, Wind Energy Science, 7, 2271–2306, https://doi.org/10.5194/wes-7-2271-2022, 2022. NREL: FLORIS. Version 1.0.0, https://github.com/NREL/floris, 2019.
 - Riboldi, C. E. D.: Advanced control laws for variable-speed wind turbines and supporting enabling technologies, Ph.D. thesis, Politecnico di Milano, 2012.

645 Services, G.L. I.: Guideline for the Certification of Wind Turbines, Tech.rep.

van der Hoek, D., Kanev, S., Allin, J., Germanischer Lloyd Industrial Services GmbH, Brooktorkai 18, 20457 Hamburg, Germany, 2004. Bieniek, D., and Mittelmeier, N.: Effects of axial induction control on wind farm energy production - A field test, Renewable Energy, 140, 994–1003, https://doi.org/https://doi.org/10.1016/j.renene.2019.03.117, 2019.