

1     **Effect of scour on the fatigue life of offshore wind turbines and**  
2             **its prevention through passive structural control**

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4     Yu Cao<sup>1</sup>, Ningyu Wu<sup>2</sup>, Jigang Yang<sup>2</sup>, Chao Chen<sup>1,3\*</sup>, Ronghua Zhu<sup>3,4\*</sup>, Xugang Hua<sup>1</sup>,

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6     <sup>1</sup>Key Laboratory for Bridge and Wind Engineering of Hunan Province, College of Civil  
7     Engineering, Hunan University, Changsha, China

8     <sup>2</sup>Hebei Construction Investment Offshore Wind Power Co., Ltd., Tangshan, China

9     <sup>3</sup>Yangjiang Offshore Wind Laboratory, Yangjiang, China

10    <sup>4</sup>Ocean College, Zhejiang University, Hangzhou, China

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\*Corresponding author: steinchen@hnu.edu.cn, zhu.richard@zju.edu.cn

## 16 **Abstract**

17 Offshore wind turbine (OWT) support structures are exposed to the risk of fatigue  
18 damage and scour, and this risk can be effectively mitigated by installing structural  
19 control devices such as tuned mass dampers (TMDs). However, time-varying scour al-  
20 tering OWTs' dynamic characteristics has an impact on the TMD design and fatigue  
21 life, which was rarely studied before. In this paper, a simplified modal model is used to  
22 investigate the influence of scour and a TMD on the fatigue life evaluation of a 5 MW  
23 OWT's support structure, and a traditional method and a newly developed optimization  
24 technique are both presented to obtain TMD parameters. This optimization technique  
25 aims at finding optimal parameters of the TMD which maximizes the fatigue life of a  
26 hotspot at the mudline, and effect of time-varying scour can be considered. This study  
27 assumes the TMD operates in the FA direction, and the vibration in the SS direction is  
28 uncontrolled. Results show that scour can decrease the fatigue life by about 24.1%, and  
29 the TMD can effectively suppress vibration and increase the fatigue life. When the  
30 scour depth reaches 1.3 times the pile diameter, the TMD with a mass ratio of 1% can  
31 increase the fatigue life of OWT's support structure by about 64.6%. Further, it is found  
32 that the fatigue life can be extended by 25% with the TMD optimized by the proposed  
33 optimization technique, compared to that with the traditionally optimized TMD which  
34 does not take the change of dynamic characteristics into account.

35 **Keywords:** scour, offshore wind turbine, structural control, modal analysis, fatigue life.

36

## 37 **1 Introduction**

38 With the continuous development of large-size fixed-bottom OWTs, local scour  
39 and scour protection of pile foundation have become a common issue (L. Wang et al.,  
40 2020; X. Wang et al., 2019; F. Zhang et al., 2022). Scour have a significant impact on  
41 dynamic characteristics, vibration magnitudes, and thus fatigue life of OWTs under  
42 wind and wave loads. On the one hand, the action of currents and waves causes local  
43 scour pits around pile foundations, which reduces the burial depth of pile foundations.  
44 This phenomenon usually causes a reduction in natural frequencies of OWTs and  
45 changes in other dynamic characteristics, possibly leading to resonance, large ampli-  
46 tude stress cycles and fatigue damage when one of natural frequencies is close to the  
47 rotational frequency of the blades (Sørensen and Ibsen, 2013). On the other hand,

48 current scour protection measures cannot completely avoid scour and have their own  
49 shortcomings. For example, armouring protection has the disadvantages that the pro-  
50 jectile cannot be accurately cast in complex sea conditions and is easy to be washed  
51 away (G. Wang et al., 2023; F. Zhang et al., 2023). Flow-altering protection has the  
52 disadvantages of high cost and changing the dynamic characteristics of the foundation  
53 (Tang et al., 2023). As offshore structures, wind turbines are vulnerable to corrosion  
54 from seawater, which makes the fatigue problem worse (Amirafshari et al., 2021). Thus,  
55 the scour-induced changes in dynamic characteristics and risk in resonance inevitably  
56 induce a further increase in fatigue damage and deserve in-depth research (Mayall et  
57 al., 2018).

58 Many researchers have studied the effect of scour on fatigue damage accumulation  
59 in OWTs. For instance, Tempel et al. (2006) investigated the frequency and fatigue of  
60 piles under different scour depths and concluded that scour has a little effect on the  
61 natural frequencies but a great effect on fatigue damage. Zhang et al. (2021) found that  
62 scour depth has a significant influence on monopile impedance. Rezaei et al. (2018)  
63 showed that scour leads to an increase in the maximum bending moment of the mono-  
64 pile and a shortening of the fatigue life. To mitigate the fatigue damage in OWTs, in-  
65 stalling structural control devices is an effective way. It was demonstrated that TMDs  
66 have a positive effect on reducing vibration amplitudes of wind turbine systems (Lack-  
67 ner and Rotea, 2011a; Dinh and Basu, 2015; Lu et al., 2023; Aydin et al., 2023). Dai et  
68 al. (2021) conducted a shaker experiment using a scaled wind turbine model and  
69 showed that the installed TMD can suppress the vibration of the structure more effec-  
70 tively considering soil-structure interaction (SSI).

71 In the previously mentioned studies, researchers have individually investigated the  
72 effect of scour on structural vibration and fatigue, and the structural control by TMDs  
73 for OWTs. However, in practice, the effect of scour combining structural control via  
74 TMDs could have a significant impact on OWTs' fatigue life. Moreover, whether con-  
75 sidering scour could influence the design of TMDs, and TMDs with different parame-  
76 ters can also have an impact on fatigue damage accumulation.

77 The purpose of this study is to explore the effect of scour on the fatigue life of  
78 wind turbine structures and the control effect of TMD on the fatigue life of wind turbine  
79 structures under scour conditions. The authors use a 5 MW single-pile wind turbine as  
80 a case study to carry out related research. In this study, ABAQUS is used to establish a

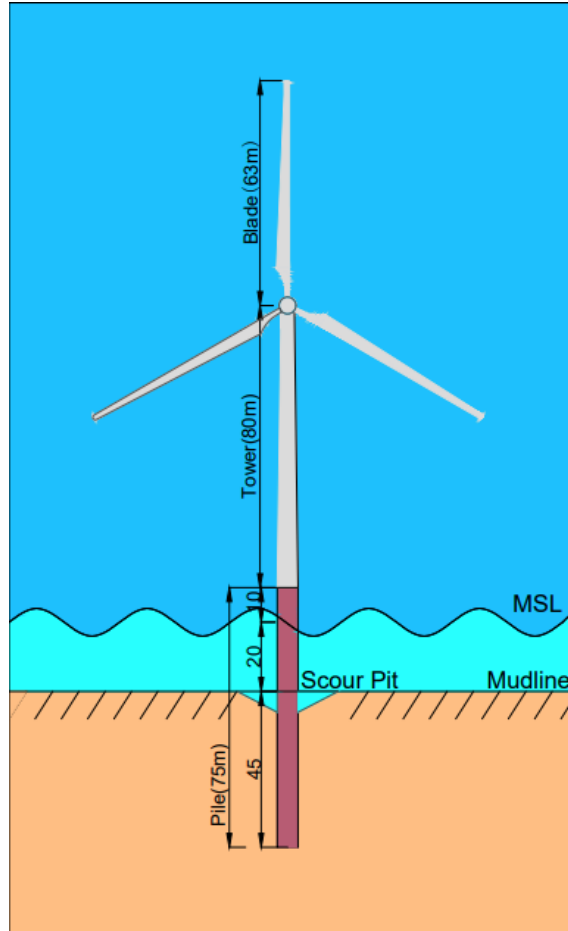
81 detailed SSI model with different scour depths. A finite element model considering  
82 wind loads and TMD was established in MATLAB, and the scour effect is considered  
83 by establishing a relationship with the ABAQUS model by means of the equivalent  
84 stiffness matrix. And the finite element model is simplified to a modal model for fast  
85 prediction of fatigue life. The TMD operates in the FA direction and does not work in  
86 the SS direction. This study investigates the effect of different scour depths on the per-  
87 formance of the TMD and the fatigue life of a 5 MW OWT's support structure including  
88 a tower and a monopile foundation, and the optimization of the TMD's parameters con-  
89 sidering time-varying scour depths to maximum fatigue life is also presented. This  
90 study provides some knowledge of the effects of the time varying scour and the TMD  
91 on the fatigue life of wind turbines, as well as a new TMD design method targeting at  
92 enhancing fatigue resistance. The rest of the paper is organized as follows: Section 2  
93 introduces the numerical models used in the research. Section 3 introduces the tradi-  
94 tional TMD design method and the newly developed parameter optimization method.  
95 Section 4 describes the load cases for the fatigue analysis, the analysis results of this  
96 study and the TMD parameter optimization results. Section 5 concludes the study.

## 97 **2 Model description**

### 98 **2.1 Finite element model and implementation of tuned mass damper**

99 An FE model of a monopile-supported OWT installed with a TMD is established  
100 in MATLAB. This model contains a flexible tower, a rotor-nacelle assembly (RNA),  
101 and an external TMD, considering the foundation flexibility. The model is based on the  
102 widely used NREL 5MW reference OWT, and its detailed properties are shown in Ta-  
103 ble 1. Three-dimensional beam elements are used to create the FE model and the theo-  
104 retical basis is the standard Euler-Bernoulli beam theory. The wind turbine tower is  
105 divided into 18 beam elements, and the monopile between the mudline and the mean  
106 sea level (MSL) are divided into 4 beam elements. A convergence test by comparing  
107 the first natural frequencies shows that 22 beam elements are sufficient. Each element  
108 node has 6 degrees of freedom (DOFs) corresponding to the translational and rotational  
109 motions in different directions. The mass matrix and stiffness matrix in the equation of  
110 motion of the OWT structure can be obtained given the material properties. The damp-  
111 ing matrix is applied by means of Rayleigh damping, and the combined damping ratio  
112 of soil damping and structural damping is assumed to be 1% (Chen and Duffour, 2018).  
113 The Rayleigh mass and stiffness coefficients  $\alpha_1$  and  $\alpha_2$  are defined by  $\alpha_1 = \alpha_2 =$

114  $\frac{\zeta_c}{2\omega + \frac{1}{\omega}}$ .  $\omega$  is the natural frequency of the first fore-aft mode, and  $\zeta_c$  is the combined  
 115 damping ratio. The RNA is represented by a lumped mass at the tower top.



116

117 Fig. 1. Schematic of NREL 5MW wind turbine and scour effect

118 The TMD is mounted on the top of the tower, and the effect of the TMD is consid-  
 119 ered by adding its mass, damping, and stiffness terms at relevant positions in the local  
 120 mass, damping, and stiffness matrices of the beam element representing the tower top.

121 The equation of motion of the OWT main structure is:

$$\begin{aligned} \mathbf{M}_s \ddot{\mathbf{U}}_s + \mathbf{C}_s \dot{\mathbf{U}}_s + \mathbf{K}_s \mathbf{U}_s + \mathbf{C}_T (\dot{\mathbf{U}}_s - \dot{\mathbf{U}}_T) + \mathbf{K}_T (\mathbf{U}_s - \mathbf{U}_T) \\ = \mathbf{F}_{\text{wind}} + \mathbf{F}_{\text{wave}}, \end{aligned} \quad (1)$$

122 where  $\mathbf{M}_s$ ,  $\mathbf{C}_s$ ,  $\mathbf{K}_s$  are the mass, damping and stiffness matrices of the main structure.

123  $\mathbf{C}_T$ ,  $\mathbf{K}_T$  are matrices with same dimensions containing  $c_T$ ,  $k_T$ ,  $\mathbf{C}_T = \begin{bmatrix} 0 & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & c_T \end{bmatrix}$ ,  $\mathbf{K}_T =$

124  $\begin{bmatrix} 0 & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & k_T \end{bmatrix}$ .  $\mathbf{U}_s$  is the displacement vector of the main structure,  $\mathbf{U}_s = \begin{bmatrix} u_{s-1} \\ \vdots \\ u_{s-top} \end{bmatrix}$ .

125  $\mathbf{U}_T$  is the displacement vector containing  $u_T$ ,  $\mathbf{U}_T = \begin{bmatrix} 0 \\ \vdots \\ u_T \end{bmatrix}$ .  $\mathbf{F}_{wind}$ ,  $\mathbf{F}_{wave}$  are the aerody-

126 namic and wave load vectors. The equation of motion for the TMD can be represented  
127 by

$$m_T \ddot{u}_T + c_T (\dot{u}_T - \dot{u}_{s-top}) + k_T (u_T - u_{s-top}) = 0, \quad (2)$$

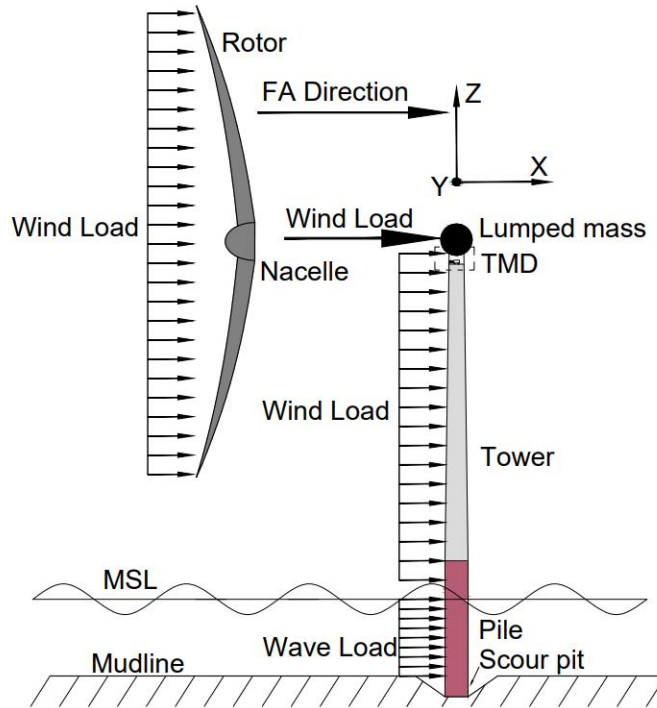
128 where  $m_T$ ,  $c_T$ ,  $k_T$  are the mass, damping and stiffness of the TMD,  $u_T$ ,  $u_{s-top}$  are the  
129 displacement of the TMD and the displacement of the top node. The modelling of SSI  
130 is realized by an equivalent stiffness matrix, which will be introduced in detail subse-  
131 quently in Section 2.3.

132 Table 1. Basic properties of the NREL 5MW reference OWT (J. Jonkman et al.,  
133 2009; Rezaei, 2017)

Number of blade	3
Rotor diameter	126 m
Tower length	80 m
Tower diameter	3.87–6.00 m
Tower thickness	28–38 mm
Pile length	75 m
Pile penetration depth	45 m
Pile diameter	6 m
Pile thickness	80 mm
Hub height from MSL	92.4 m
Turbine mass	350000 kg
Blade mass	17740 kg
Rated wind speed	12.1 m/s

134 Wind loads were calculated using modified unsteady blade element momentum  
135 (BEM) theory (Branlard, 2017; B. J. Jonkman and Buhl, 2006) with Prandtl and Glauert  
136 corrections. Ignoring the iterative loop (Chen, Duffour, Fromme, et al., 2021) in the  
137 steady-state BEM code, the instantaneous aerodynamic forces were calculated for each  
138 time step within the time integration. The turbulent wind field was generated using the  
139 Kaimal spectrum according to the wind field parameters of IEC 61400-3 (2019) as-  
140 suming moderate turbulence intensity. It should be noted that the aerodynamic loads

141 from the rotor applied at the tower top were calculated using an aerodynamic force  
 142 linearization technique previously developed by authors (Chen, Duffour, Fromme, et  
 143 al., 2021; Chen et al., 2020). This technique divides the aerodynamic loads into two  
 144 parts. The first part is the quasi-steady aerodynamic force calculated by BEM theory,  
 145 which does not consider the influence of tower top motion. The second part considers  
 146 the effect of aerodynamic damping by introducing an additional aerodynamic damping  
 147 matrix. The adoption of this technique is to enable the development of the simplified  
 148 modal model for rapid fatigue calculation, which will be introduced in detail in Sub-  
 149 section 2.4. To represent the influence of controller in the OWT, a standard relationship  
 150 (J. Jonkman et al., 2009) between the mean wind speed, rotor rotation speed and blade  
 151 pitch angles, which represents the OWT's normal operational conditions, are adopted  
 152 throughout the wind loading calculation.



153

154

Fig. 2 Schematic of wind turbine load application

155

Wave loads were calculated using the Morison equation, which includes viscous  
 156 drag and inertial forces:

$$\mathbf{F}_{\text{wave}} = \frac{1}{2} \rho_w D_{\text{pile}} C_d |\dot{\mathbf{u}}_w| \dot{\mathbf{u}}_w + \frac{\pi}{4} \rho_w D_{\text{pile}}^2 C_m \ddot{\mathbf{u}}_w, \quad (3)$$

157 where  $\dot{\mathbf{u}}_w$  and  $\ddot{\mathbf{u}}_w$  are the velocity and acceleration of water particles,  $C_d$  is the drag  
 158 coefficient,  $D_{pile}$  is the diameter of the monopile between the mean sea level and the  
 159 mudline,  $C_m$  is the inertia coefficient and  $\rho_w$  is the density of water.  $C_d$  and  $C_m$  were  
 160 chosen as 1 and 2 respectively as the recommended values in Shirzadeh et al (2013).  
 161 The wave profiles were obtained through the superposition of wave components, com-  
 162 bining linear wave theory and JONSWAP spectra (Klaus et al., 1973). The application  
 163 of wind and wave loads is shown in Fig. 2.

## 164 2.2 Scour modelling in ABAQUS

165 Using solid elements to model pile-soil interaction (S. Dai et al., 2021; Fard et al.,  
 166 2022; Ma and Chen, 2021; Zdravković et al., 2015) is usually considered to be more  
 167 accurate than the p-y curve method (Liang et al., 2018; Song and Achmus, 2023) and  
 168 the equivalent embedding method (Shahmohammadi and Shabakhty, 2020; Bergua et  
 169 al., 2022). The solid element method can also reduce the influence of empirical formula  
 170 on the results. Therefore, the solid element method is used to establish the wind turbine  
 171 scour model. The wind turbine scour model established in ABAQUS contains soil, pile  
 172 foundation, tower, and the RNA is replaced by a concentrated mass located at the top  
 173 of the tower. The diameter of the soil body is selected as 20 times of the pile diameter,  
 174 the soil under the pile foundation is selected as 2.5 times of the pile diameter, and the  
 175 total height of the soil body is 60 m. The soil body is made of homogeneous dense  
 176 sandy soil, and the piles and tower are made of steel. The material parameters of the  
 177 soil body, pile and tower are shown in Table 2 below:

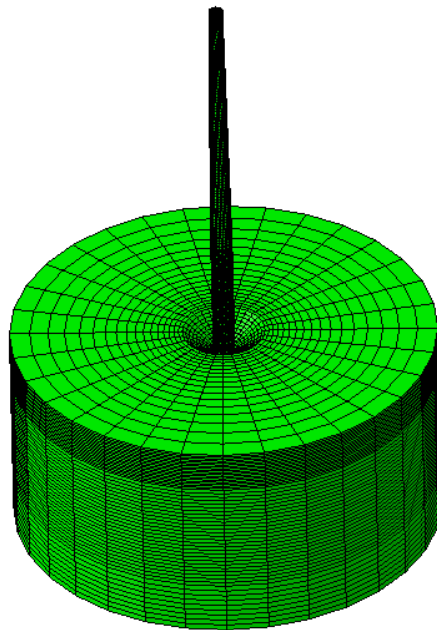
178 Table 2. Soil, pile and tower material parameters

Type	Weight $\gamma$ (kN/m <sup>3</sup> )	modulus of elasticity $E_S$ (MPa)	Poisson's ratio $\nu$	Internal friction angle $\varphi$ (°)	Expansion angle $\psi$ (°)	Cohesion $c$ (kPa)
Soil	19	80	0.3	35	23	0.1
Pile	78.5	215	0.25	-	-	-
Tower	85	215	0.25	-	-	-

179 The Mohr-Coulomb model is used for the soil, and the pile, tower, and nacelle are  
 180 assumed to be elastic as they are much stiffer than the soil and do not deform plastically  
 181 for the normal operational conditions. The pile and tower are connected by a binding  
 182 relationship. The normal contact between the pile and soil adopts the hard contact, and  
 183 the tangential contact adopts the friction penalty function. The relative sliding friction



184 factor at the interface,  $\mu$  is equal to  $\tan(0.75 \varphi)$ , where  $\varphi$  is the internal friction angle.  
185 The pile-soil contact is in the form of frictional contact, where mutual contact pairs are  
186 established between the pile and the soil, including the contacts between the pile bottom  
187 surface and the soil, between the outside surface of the pile and the soil, and the inside  
188 surface of the pile and the soil core. The frictional contact between pile bottom surface  
189 and soil is omitted due to the small area of the contact surface. These frictional contacts  
190 all adopt the face-to-face contact, and the contact discretization method adopts the face-  
191 to-face discretization method, considering the large stiffness of the main surface and  
192 small stiffness of the slave surface. The perimeter of the soil body is translationally  
193 constrained, and the bottom surface of the soil adopts a fixed constraint. The eight-node  
194 linear brick element (C3D8R) is used to model the pile and soil, and the mesh division  
195 is realized by arranging seeds as shown in Fig. 2. The whole model is set up by adopting  
196 the modelling method of “element birth and death”, which realizes the operation of  
197 initial soil stress balance and sets up contacts and other related steps by killing and  
198 activating relevant elements.



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Fig. 3. Pile-soil interaction modelled by ABAQUS

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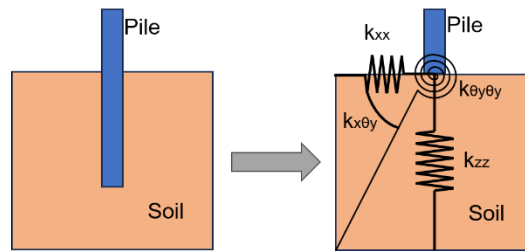
The scour conditions can be represented by a deep conical pit around the pile under the long-term action of the waves and currents. According to the specification of Det Norske Veritas (DNV) (2014b), the radius of the pit surface formed by scour,  $R$ , can be related to the depth of the scour pit by

$$R = \frac{D}{2} + \frac{S}{\tan\varphi}, \quad (4)$$

205 where  $D$  is the diameter of the pile,  $S$  is the scour depth, and  $\varphi$  is the angle of internal  
 206 friction of the soil.

### 207 2.3 Equivalent stiffness matrix method

208 It is necessary to consider the effect of scour in the FE model in MATLAB. An  
 209 equivalent stiffness matrix method is adopted in the FE model to consider the flexibility  
 210 induced by SSI. The 6 DOFs of node at the mudline are assumed to be constrained by  
 211 a series of coupled springs, and the stiffnesses of the coupled springs form a  $6 \times 6$  stiff-  
 212 ness matrix. For one specific stiffness term used in the FE model, for instance the one  
 213 relevant to the lateral displacement in the fore-aft (FA) direction, the value of the stiff-  
 214 ness term can be found from the relationship between the reaction force at the mudline  
 215 and the pile top displacement (Jung et al., 2015). The equivalent stiffness schematic of  
 216 the pile-soil interaction in the FA direction for the OWT is shown in Fig. 4.



217

218 Fig. 4. Equivalent stiffness schematic of pile-soil interaction in the FA direction

219 According to the principle of virtual displacement and with the DOFs in the other  
 220 directions constrained, a unit displacement or rotation was first applied in one direction,  
 221 and then the reaction force in that direction can be known. The equivalent stiffness in  
 222 that direction can be subsequently calculated by the relationship between the displace-  
 223 ment and reaction force. Using the same approach, the stiffness terms corresponding to  
 224 the remaining five DOFs were calculated. The stiffness terms in all the six DOFs to-  
 225 gether form all the diagonal terms of the soil stiffness matrix. With the diagonal terms  
 226 known, the off-diagonal stiffness terms can be found by applying a unit displacement  
 227 in one direction and looking at the reaction force in the other concerned direction, with  
 228 the other four DOFs constrained. Using the same principle, the off-diagonal terms can  
 229 also be found from the relationship between the displacements and reaction forces,

230 which ultimately results in a 6×6 stiffness matrix (Bergua et al., 2021; Pedersen and  
 231 Askheim, 2021):

$$\mathbf{F}_{\text{soil}} = \begin{Bmatrix} F_x(t) \\ F_y(t) \\ F_z(t) \\ M_x(t) \\ M_y(t) \\ M_z(t) \end{Bmatrix} = \begin{bmatrix} k_{xx} & 0 & 0 & 0 & k_{x\theta y} & 0 \\ 0 & k_{yy} & 0 & k_{y\theta x} & 0 & 0 \\ 0 & 0 & k_{zz} & 0 & 0 & 0 \\ 0 & k_{\theta xy} & 0 & k_{\theta x\theta x} & 0 & 0 \\ k_{\theta yx} & 0 & 0 & 0 & k_{\theta y\theta y} & 0 \\ 0 & 0 & 0 & 0 & 0 & k_{\theta z\theta z} \end{bmatrix} \begin{Bmatrix} u_x(t) \\ u_y(t) \\ u_z(t) \\ \theta_x(t) \\ \theta_y(t) \\ \theta_z(t) \end{Bmatrix} \quad (5)$$

$$= \mathbf{K}_{\text{soil}} \mathbf{u}_{\text{soil}},$$

232 where  $\mathbf{K}_{\text{soil}}$  is the equivalent soil stiffness matrix,  $\mathbf{u}_{\text{soil}}$  is the displacement vector, and  
 233  $\mathbf{F}_{\text{soil}}$  is the reaction force vector. The equivalent soil stiffness matrix ignores the nonlin-  
 234 earity in the force-displacement relationship. This approach is suitable for fatigue anal-  
 235 ysis, as in normal operation conditions the deformation of the soil around the monopile  
 236 is relatively small and the nonlinearity in soil stiffness is very weak. The 6×6 soil stiff-  
 237 ness matrix obtained from ABAQUS is imported to the FE model in MATLAB. This  
 238 modelling method possesses the advantages of the increase in accuracy brought by the  
 239 scour model in ABAQUS with solid elements, and the fast calculation speed and con-  
 240 venience in applying wind and wave loads brought by the usage of the FE model in  
 241 MATLAB.

#### 242 2.4 Rapid fatigue evaluation method

243 The established FE model in MATLAB can generate dynamic responses of the  
 244 OWT, considering wind and wave loads and scour effect. However, a comprehensive  
 245 fatigue life prediction in time domain needs to consider a large number of environmen-  
 246 tal states and load cases, so simulation efficiency is very important. Moreover, the TMD  
 247 design optimization requires much more dynamic response time series. The FE model  
 248 is not fast enough in this case. Therefore, a simplified modal model is developed from  
 249 the FE model in MATLAB following the method develop in Ref. (C .Chen et al., 2021).  
 250 The total aerodynamic forces from the rotor applied on the tower top node are linearized  
 251 to the sum of a term corresponding to the forces for an assumed rigid tower, plus a term  
 252 proportional to the tower top linear and angular velocities. The hydrodynamic forces  
 253 are linearized by ignoring the relatively small monopile vibrations. The details for force  
 254 linearization can be found in the authors' previous studies (Chen, Duffour, Fromme, et  
 255 al., 2021). Since the dynamic responses of the OWT are mainly dominated by the first

256 two bending vibration modes, the FE model is reduced into a 4-DOF simplified modal  
 257 model by considering only the first two bending modes in the FA and side-side (SS)  
 258 directions respectively. The development of the simplified 4-DOF modal model is  
 259 briefly introduced as follows. Denoting the mass matrix and stiffness matrix of the  
 260 OWT as  $\mathbf{M}$  and  $\mathbf{K}$  including the TMD and the lumped soil stiffness matrix, the un-  
 261 damped vibration mode matrix  $\mathbf{\Psi}$  can be obtained directly through eigen analysis. Ac-  
 262 cording to relationship  $\mathbf{u} = \mathbf{\Psi}\alpha$  and multiplying the transpose of the undamped vibra-  
 263 tion matrix  $\mathbf{\Psi}^T$  with the equation of motion, the following equation is obtained:

$$\mathbf{\Psi}^T \mathbf{M} \mathbf{\Psi} \ddot{\alpha} + \mathbf{\Psi}^T \mathbf{C} \mathbf{\Psi} \dot{\alpha} + \mathbf{\Psi}^T \mathbf{K} \mathbf{\Psi} \alpha = \mathbf{\Psi}^T \mathbf{F}. \quad (6)$$

264 Then rewrite the above equation as

$$\bar{\mathbf{M}} \ddot{\alpha} + \bar{\mathbf{C}} \dot{\alpha} + \bar{\mathbf{K}} \alpha = \bar{\mathbf{F}}, \quad (7)$$

265 where  $\alpha$  is the general coordinate vector,  $\bar{\mathbf{M}}$  is the modal mass matrix,  $\bar{\mathbf{C}}$  is the modal  
 266 damping matrix,  $\bar{\mathbf{K}}$  is the modal stiffness matrix,  $\bar{\mathbf{F}}$  the modal load matrix. Truncating  
 267 Eq. (6) by only considering the first two bending modes, the FE model is reduced to a  
 268 4-DOF modal model, which can be used for a rapid fatigue analysis. The dynamic re-  
 269 sponses of the OWT can be obtained by modal superposition after solving the general  
 270 coordinate vector by time integration. In the 4-DOF simplified modal model, the cross-  
 271 section stress at any height can be calculated from the calculated node displacements.  
 272 According to the dynamic stress extraction method provided by Pelayo et al. (Pelayo et  
 273 al., 2015), the cross-section stress  $\sigma_z(t)$  at any moment at a given location can be ob-  
 274 tained by:

$$\sigma_z(t) = -E(\mathbf{N}^{e''}(z)\mathbf{u}_x^e(t)x + \mathbf{N}^{e''}(z)\mathbf{u}_y^e(t)y), \quad (8)$$

275 where  $\mathbf{u}^e$  is the nodal displacement vector at the cross section,  $E$  is the material elastic  
 276 modulus, and  $\mathbf{N}^e$  is the elemental shape function vector of FE model,  $x$  and  $y$  are the  
 277 positions within the section at the height  $z$  of the tower. After cyclic counting the stress  
 278 time series using the rainfall counting method, the fatigue damage at the hotspot can be  
 279 evaluated by utilizing the Palmgren-Miner rule based on the S-N fatigue calculation  
 280 method. The S-N curve for steel under water can be obtained by the following equation  
 281 considering the thickness effect in DNV (2014a):

$$\log N = \log \bar{a} - m \cdot \log \left[ \Delta \sigma \left( \frac{t}{t_{\text{ref}}} \right)^k \right], \quad (9)$$

282 where  $N$  is the number of cycles to failure,  $\Delta \sigma$  is the stress range.  $\Delta \sigma$  is calculated from  
 283 the nominal stress  $\Delta \sigma_{\text{nominal}}$  by the equation  $\Delta \sigma = \text{SCF} \cdot \Delta \sigma_{\text{nominal}}$ , SCF is the stress  
 284 concentration factor.  $m$  is the negative inverse slope of the S-N curve, and  $\log \bar{a}$  is the  
 285 intercept between the  $\log N$  axis and the S-N curve,  $t_{\text{ref}}$  is the reference thickness for  
 286 welded joints,  $t$  is the thickness at which cracks may grow. And  $t = t_{\text{ref}}$  is used for  
 287 thickness less than  $t_{\text{ref}}$ . When  $t$  is larger than  $t_{\text{ref}}$ ,  $t$  is the actual thickness of the pile.  $k$   
 288 is the thickness exponent of fatigue strength. For pile joints,  $t_{\text{ref}} = 25\text{mm}$ . According  
 289 to the DNV code, a bilinear S-N curve is usually used for offshore structures subjected  
 290 mainly to typical wind and wave loads, using the Class E structural detail S-N curve  
 291 shown in Table 3.

292 Table 3 Class E structural detail S-N curves

$N \leq 10^6$		$N \geq 10^6$		$k$	$t$ (mm)	SCF
$m_1$	$\log \bar{a}_1$	$m_2$	$\log \bar{a}_2$			
3.0	11.610	5.0	15.350	0.2	80	1.13

293 For variable amplitude stresses, the fatigue damage index is calculated using the  
 294 Palmgren-Miner summation rule:

$$D_k = \sum_{i=1}^{N_c} \frac{n_i}{N_i}, \quad (10)$$

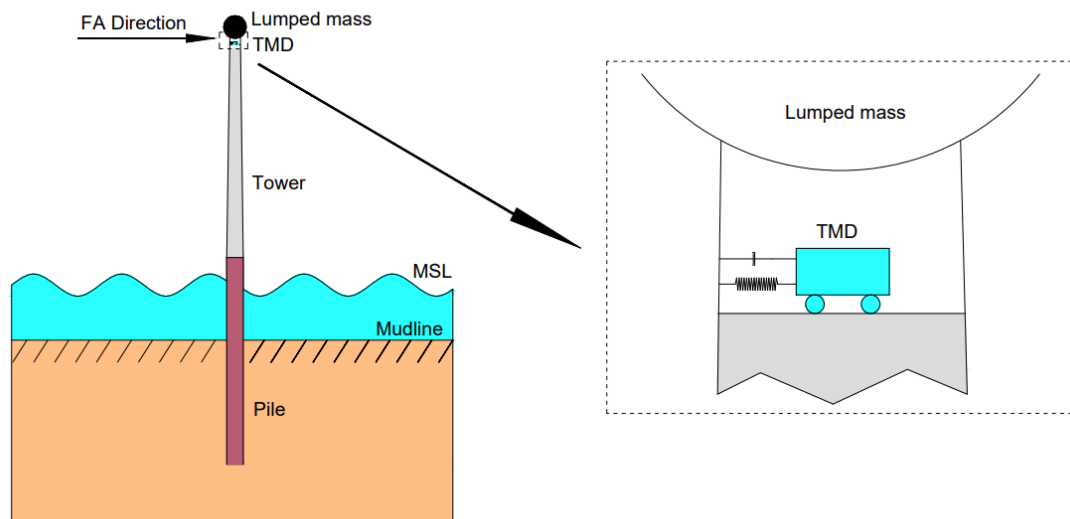
295 where  $N_c$  is the total number of bins,  $n_i$  is the number of cycles in  $i^{\text{th}}$  stress bin,  $N_i$  is  
 296 the number of cycles to failure for the  $i^{\text{th}}$  stress range, and  $D_k$  is the total fatigue dam-  
 297 age index. The ‘‘rainflow’’ function in MATLAB is adopted for rainflow counting.  
 298 When a stress time history is given, this function can automatically obtain the  $i^{\text{th}}$  stress  
 299 range and the corresponding cycle number  $n_i$ , and  $N_c$  is the total number of stress  
 300 ranges. Fatigue failure occurs at the hotspot when the fatigue damage index reaches  
 301 unit 1.

### 302 3 Damper design and optimisation method

303 Installing damping devices can efficiently reduce the vibration amplitudes of  
 304 OWTs so that their service life can be greatly prolonged. Using TMDs as passive

305 control devices is most widely used to control the vibration of OWT support structures.  
 306 Usually, most of TMDs are designed according to the dynamic characteristics of the  
 307 OWTs determined in the preliminary design stage, without considering the changes in  
 308 dynamic properties possibly caused by scour and soil degradation. However, in the real  
 309 environment, scour can cause the dynamic characteristics of OWTs to change, which  
 310 perhaps makes installed dampers become less effective or even completely ineffective.  
 311 Therefore, it is a great significance to consider the change in dynamic properties caused  
 312 by scour on the TMD design. The following two subsections first introduce the tradi-  
 313 tional TMD design method considering constant dynamic characteristic in the initial  
 314 state, and then an optimal parameter searching method for the design of TMDs is pre-  
 315 sented considering the effect of scour and fatigue life evaluation.

### 316 3.1 TMD design in initial state



317

318 Fig. 5. Schematic diagram of TMD arrangement in the tower tube

319 As the dominant vibration mode of the OWT structure in operation is the first  
 320 bending mode, the largest vibration amplitude occurs at the tower top and installing the  
 321 TMD at the tower top is most effective. Therefore, the TMD is installed inside the steel  
 322 tube at the tower top to mainly control the vibration in the FA direction, as shown in  
 323 Fig. 5. And the TMD can be aligned with the FA direction by rotating the damper.  
 324 Accordingly, the initial design of the TMD is mainly carried out based on the dynamic  
 325 properties for the first-order mode. The initial design is conduct based on the assump-  
 326 tion that the monopile foundation is not scoured.

327 Numerous studies have shown that a TMD can effectively suppress the vibration  
328 of a main structure when the mass ratio of the TMDs to the main structure is 1%-2%  
329 (Lackner and Rotea, 2011b; R. Zhang et al., 2019). After determining the mass ratio of  
330 the TMD to the OWT structure, according to the classic TMD optimization theory  
331 proposed by Den Hartog (1957), the optimal frequency ratio of the TMD to the OWT  
332 structure is

$$\alpha_{\text{opt}} = \frac{1}{1 + \mu}. \quad (11)$$

333 The optimal damping ratio for the TMD can be calculated by

$$\xi_{\text{opt}} = \sqrt{\frac{3\mu}{8(1 + \mu)}}, \quad (12)$$

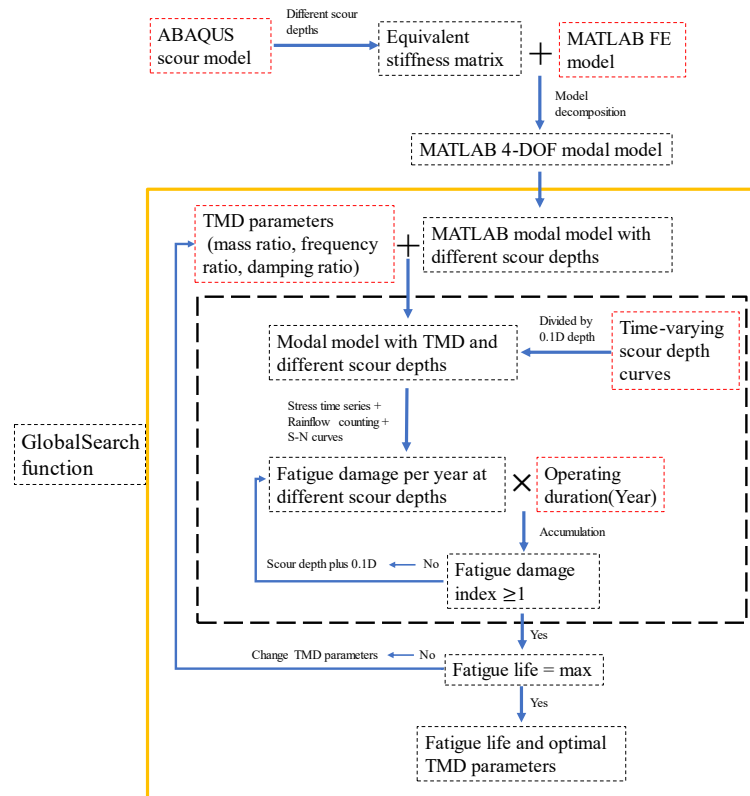
334 where  $\mu$  is the mass ratio of the TMD to the OWT structure,  $\alpha_{\text{opt}}$  is the optimal fre-  
335 quency ratio of the TMD to the OWT structure and  $\xi_{\text{opt}}$  is the optimal damping ratio  
336 of the TMD.

337 Considering that excessive mass will lead to increased construction costs and dif-  
338 ficulties and changes in the inherent characteristics of the original structure, the mass  
339 ratio of the TMD system to the main structure is first selected to be 1%. Moreover,  
340 previous studies have found that TLCD with a mass ratio of 1% and TMD with a mass  
341 ratio of 2% can effectively suppress vibration (Colwell and Basu, 2009; Lackner and  
342 Rotea, 2011b; R. Zhang et al., 2019). According to Den Hartog's optimization theory  
343 for the initial TMD design, it can be determined that the optimal frequency ratio of the  
344 TMD to the main structure is 0.99, and the optimal damping ratio of the TMD is 0.061.  
345 When the OWT support structure is not scoured, the first-order modal mass of the struc-  
346 ture is 440350 kg, and the first-order modal frequency is 0.265 Hz. Therefore, accord-  
347 ing to the initial design parameters, the mass, stiffness coefficient and damping coeffi-  
348 cient of the TMD system are 4403.5 kg, 11,952 N/m and 885 Ns/m respectively.

### 349 3.2 Fatigue-based damper optimisation technique

350 After scour occurs around the monopile foundation, the burial depth of the mono-  
351 pile and natural frequencies of the OWT gradually change. The vibration mitigation  
352 effect of the TMD designed based on the dynamic parameters in the initial state can be

353 reduced, which may lead to the increase of fatigue damage of the OWT support struc-  
 354 ture. Therefore, when designing the TMD, considering the influence of the time-vary-  
 355 ing scour can enhance the performance of the TMD and thus result in a longer fatigue  
 356 life of the support structure.



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Fig. 6. Flowchart of TMD fatigue-life-based optimization technique

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Here a fatigue-life-based optimization technique (FOT) to find optimal parameters of the TMD is developed in MATLAB as shown in Fig. 8. In this technique, the frequency ratio, mass ratio and damping ratio of the TMD are set as the optimal parameters to search, and the fatigue life is the optimization objective. When considering the time-varying scour process, the time-varying scour depth curve is first divided into a number of scour depths with an increment of 0.1d. For each scour depth, the fatigue damage is calculated respectively and then the total fatigue damage in a particular duration can be summarised. When the scour pit becomes deeper, the fatigue damage accumulates and finally reaches unit 1 which denotes the end of fatigue life. The simplified 4-DOF modal model incorporating scour modelling is used to generate the stress time series. The optimization problem is formed so that the optimal parameters of the TMD correspond to the longest fatigue life of the OWT support structure. The GlobalSearch function in MATLAB was used to solve the optimization problem. In the TMD optimization



372 process, the mass ratio of TMD is first set to 1%, and only the parameter frequency  
 373 ratio and damping ratio are optimized. Subsequently, in order to understand the optimi-  
 374 zation effect of TMD when the value of TMD mass ratio is not fixed, a mass ratio  
 375 optimization interval is given, so the mass ratio becomes a variable within the optimi-  
 376 zation interval.

## 377 4 Results

### 378 4.1 Environmental states and load cases

379 In this study, fatigue analyses are performed under 22 environmental states pro-  
 380 vided by Tempel (2006), taking into account both operational and parked conditions.  
 381 These 22 environmental states are shown in Table 4. In operating conditions, the wind  
 382 turbine bears the aerodynamic load of the rotating rotor and the wind load of the tower,  
 383 and the wind load on the rotor is calculated using the BEM theory. In parked conditions,  
 384 the wind turbine mainly bears the aerodynamic load on the tower, and the aerodynamic  
 385 damping is very small. The aerodynamic loading on the blades is calculated by directly  
 386 looking at the aerodynamic loading coefficient table given the local attack angles. The  
 387 wind and wave loads are assumed to be always in the same direction to simplify the  
 388 analysis. When the mean wind speeds are above the cut-in wind speed and below the  
 389 cut-out wind speed, a 95% wind turbine availability is assumed following the setting  
 390 in Ref (Velarde et al., 2020), meaning that the OWT does not produce power for 5%  
 391 when the mean wind speeds are in the operating range. For a particular set of mean  
 392 wind speed, wave period and wave height, six different random seed numbers are used  
 393 to generate different wind fields and wave profiles to reduce the influence of random-  
 394 ness. To obtain the stress time histories at the mudline, a 700s simulation for each ran-  
 395 dom seed was conducted and the response in the first 100 seconds was deducted to  
 396 eliminate the effect of initial transient vibration. (Capaldo and Mella, 2023; Stieng and  
 397 Muskulus, 2020).

398 Table 4. Environmental states, adopted from Tempel (van der Tempel, 2006).

State	V <sub>w</sub> (m/s)	T <sub>z</sub> (s)	H <sub>s</sub> (m)	P <sub>State</sub> (%)	State	V <sub>w</sub> (m/s)	T <sub>z</sub> (s)	H <sub>s</sub> (m)	P <sub>State</sub> (%)
1	4	3	0.5	3.95	12	14	5	2	3.26
2	4	4	0.5	3.21	13	16	4	2	1.79
3	6	3	0.5	11.17	14	16	5	2.5	3.1
4	6	4	0.5	7.22	15	18	5	2.5	1.74

5	8	3	0.5	11.45	16	18	5	3	0.8
6	8	4	1	8.68	17	20	5	2.5	0.43
7	10	3	0.5	5.31	18	20	5	3	1.14
8	10	4	1	11.33	19	22	5	3	0.4
9	12	4	1	5.86	20	22	6	4	0.29
10	12	4	1.5	6	21	24	5	3.5	0.15
11	14	4	1.5	4.48	22	24	6	4	0.1

399 In Table 4,  $V_w$  is the wind speed,  $T_z$  is the zero-crossing wave period,  $H_s$  is the  
400 wave height, and  $P_{state}$  is the probability of environmental state. To investigate the ef-  
401 fect of scour and installation of the TMD on the fatigue damage accumulation, six load  
402 cases (LCs) are selected as shown in Table 5. LC 1 is used as the reference case, and  
403 other cases are distinguished by different scour and TMD settings. For LC 4 to LC 6,  
404 the initial design of the TMD with the mass ratio of 1% is used.

405

Table 5. Load case definition

LC number	TMD condition	Scour condition	LC number	TMD condition	Scour condition
LC 1	No	No Scour	LC 4	Enable	No Scour
LC 2	No	Time-varying	LC 5	Enable	Time-varying
LC 3	No	Maximum	LC 6	Enable	Maximum

406 When considering the time-varying scour depth, for a particular time  $t$ , the time-  
407 varying scour depth  $S$  can be predicted by the equation provided by Nakagawa et al.  
408 (1976):

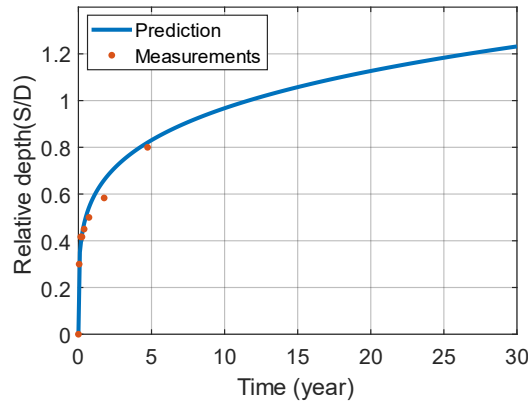
$$S = \left(\frac{t}{t_1}\right)^{0.22} D, \quad (13)$$

409 where  $D$  is the diameter of the monopile,  $t_1$  is the reference time and can be calculated  
410 by

$$t_1 = 29.2 \cdot \frac{D}{\sqrt{2} \cdot u} \cdot \left(\frac{\sqrt{\Delta \cdot g \cdot d_{50}}}{\sqrt{2} \cdot u - u_c}\right)^3 \cdot \left(\frac{D}{d_{50}}\right)^{1.9}. \quad (14)$$

411  $u$  is the tidal velocity and taken as 0.5 m/s,  $u_c$  is the critical shear velocity and taken as  
412 0.37 m/s,  $g$  is the acceleration of gravity and taken as 9.8 m/s<sup>2</sup>,  $d_{50}$  is grain size of sea  
413 sand and taken as 0.2 mm. The parameter  $\Delta = \frac{\rho_s}{\rho_w} - 1$ , where  $\rho_s$  is density of sand and  
414 taken as 2.65 g/cm<sup>3</sup>,  $\rho_w$  is density of water and taken as 1 g/cm<sup>3</sup>. Rudolph et al.

415 (Rudolph et al., 2016) provided the sea state and measured the scour depth for the North  
 416 Sea where the monopile N7 is located. The measured scour depth was fitted well for  
 417 the first five years based on the time-varying scour depth prediction equation shown in  
 418 Eq. (13). Therefore, the data from the North Sea site can represent a typical ocean en-  
 419 vironment with time-varying scour and is used for the correlation analysis in this study.



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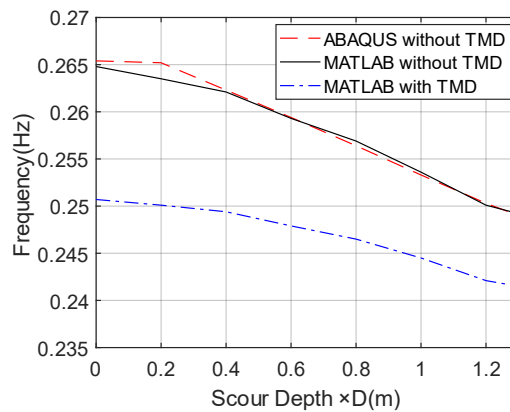
421 Fig. 7. Time-varying scour depth curve for pile N7 in the North Sea

422 When conducting analysis with the time-varying scour, an increment of scour  
 423 depth equal to  $0.1D$  is used. At one particular scour depth, the fatigue damage is calcu-  
 424 lated and then the total fatigue damage during a longer period with a changing scour  
 425 depth can be obtained by damage accumulation. According to the specification of DNV,  
 426 the maximum depth of a local scour pit formed around a pile foundation is 1.3 times  
 427 the diameter of the pile. Therefore, it is assumed that the local scour pit has a maximum  
 428 scour depth of  $1.3D$  at which the scour process achieves equilibrium.

#### 429 4.2 Scour influence on natural frequencies

430 The scour of the soil around the monopile has an important effect on the natural  
 431 frequencies of the OWT. For different scour depths, the first natural frequencies ob-  
 432 tained the by the models in ABAQUS and MATLAB are compared in Fig. 8. It shows  
 433 the increase in the scour depth leads to a decrease in the first natural frequency of the  
 434 OWT. The first natural frequency is  $0.265$  Hz when no scour occurs, and the natural  
 435 frequency is reduced to  $0.248$  Hz when the depth of the scour pit reaches the maximum  
 436 depth. The first natural frequency is reduced by  $6.42\%$  due to the maximum scour depth.  
 437 It shows that the natural frequency nearly monotonically decreases with the increase of  
 438 the scour depth. The installation of TMD also influences the natural frequency of the  
 439 OWT main structure. The TMD with a mass ratio of  $1\%$  makes the first natural

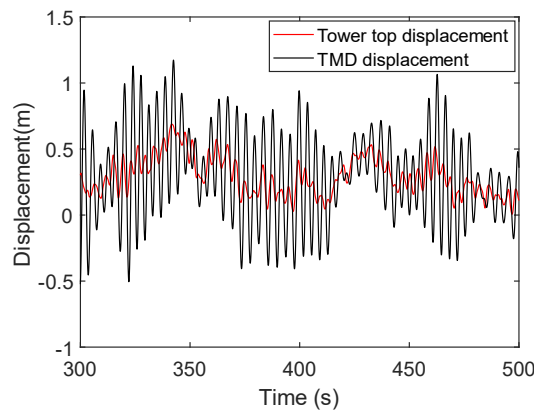
440 frequency of the OWT main structure reduces to 0.251 Hz when no scour occurs, mean-  
 441 ing that the natural frequency is reduced by 5.28%.



442

443 Fig. 8. Relationship between wind turbine natural frequency and scour depth

444 In the TMD design process, the feasible displacement should be considered. The  
 445 smaller the mass ratio of TMD is, the larger the feasible displacement is required. The  
 446 22nd environmental state corresponds to the greatest vibration responses of the wind  
 447 turbine tower top due to large wind speed variations and lower aerodynamic damping,  
 448 and the stroke of the TMD could be the largest. As shown in the Fig. 9, the relative  
 449 displacement between the TMD and the tower top is much less than the inner diameter  
 450 of the wind turbine tower top in the 22nd environmental state. It shows that the stroke  
 451 of the TMD is sufficient when the mass ratio of TMD is 1%.



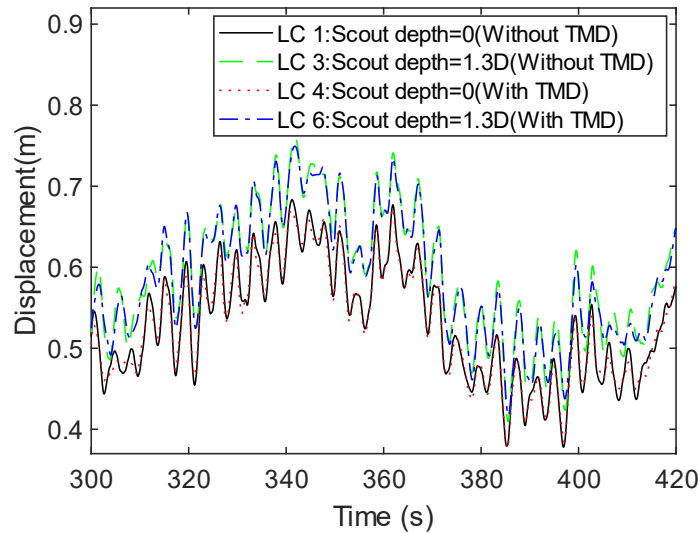
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453 Fig. 9 Displacement of tower top and TMD under the 22nd environmental state

454 **4.3 Dynamic response analysis**

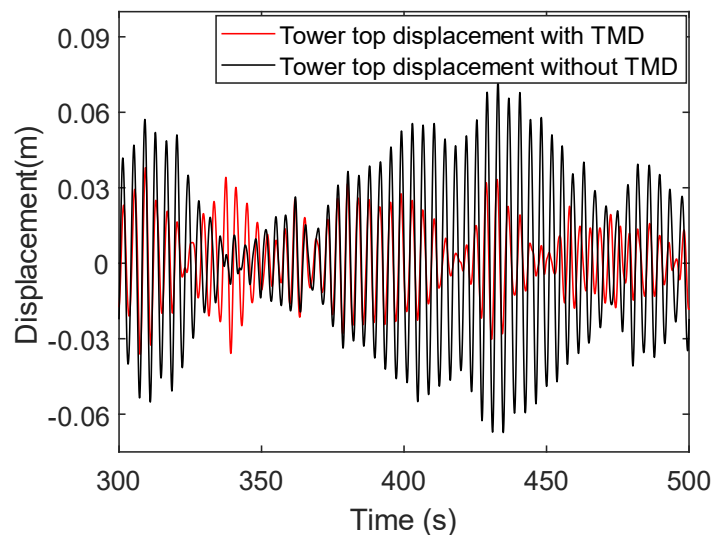
455 When the OWT in the operating state is under the 9th environmental state which  
 456 corresponds to the rated wind speed of 12 m/s, a comparison for the tower top displacements  
 457 is made for LC 1, LC 3, LC 4 and LC 6, as shown in Fig. 10. These displacements

458 are obtained from the FE model in MATLAB described in Subsection 2.1. By compar-  
 459 ing the displacements from 300 seconds to 420 seconds for LC 1 and LC 4, it can be  
 460 found that the displacement amplitudes of the tower top decreases when the TMD is  
 461 installed. It is known that the aerodynamic damping is large when the OWT is operating  
 462 under the rated wind speed, so it is normal that the vibration mitigation effect of the  
 463 TMD is less significant in this case.



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465 Fig. 10. Dynamic response of wind turbine under wind-wave coupled loads for four  
 466 operating conditions



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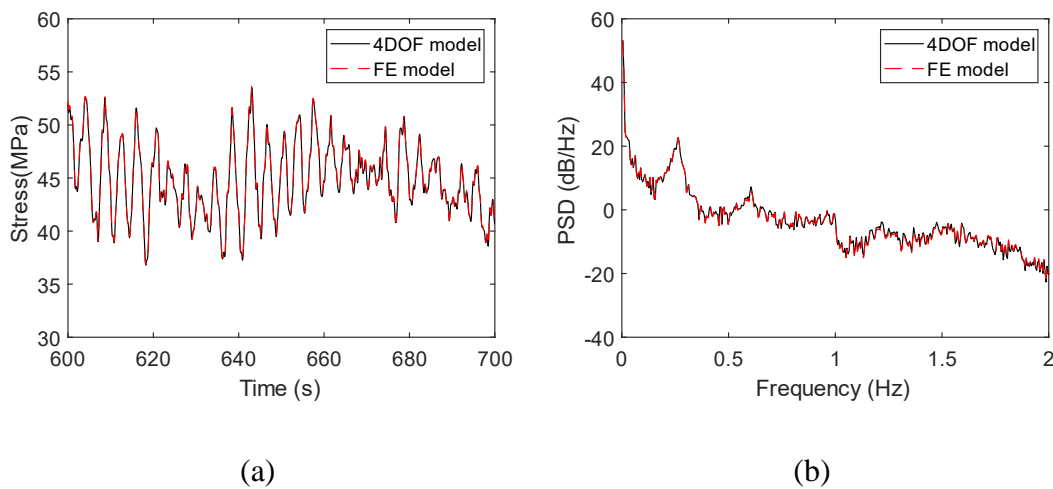
468 Fig. 11 The displacement response of wind turbine tower under the parked condition  
 469 with 3 m/s wind speed

470 The effect of the TMD is more prominent for parked conditions with less aerody-  
 471 namic damping. As shown in the Fig. 11, the vibration mitigation effect of the TMD is  
 472 more significant under the parked condition with 3 m/s wind speed. Moreover, by com-  
 473 paring the displacement responses for LC 1 and LC 3, it can be found that the average  
 474 of the displacement at the tower top increases when the scour depth reaches 1.3D. This  
 475 is because scour makes the OWT support structure become more flexible.

#### 476 4.4 Fatigue calculation results

477 In Subsection 2.4, it is mentioned that in the process of fatigue life analysis, the 4-  
 478 DOF simplified modal model is used to greatly save the calculation time. The accuracy  
 479 test of the 4-DOF modal model in generating dynamic responses is first present in this  
 480 subsection. Under the turbulent wind field with a turbulence intensity of 11.9% and an  
 481 average wind speed of 12 m/s, the FE model and the 4-DOF simplified modal model  
 482 are used to calculate the stress responses at the mudline for 10 minutes.

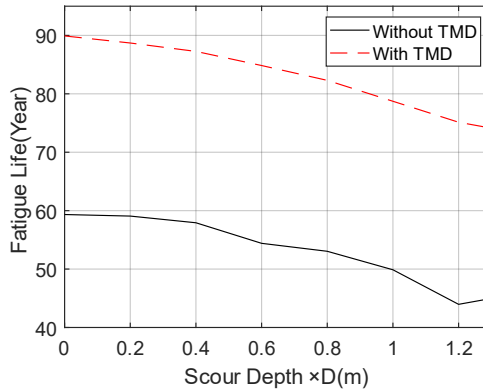
483 As shown in Fig. 12, the stress responses from these two models are very close,  
 484 confirming good accuracy of the 4-DOF modal model. The fatigue damage caused by  
 485 the FE model in 10 min is  $2.108 \times 10^{-7}$ , and the fatigue damage caused by the 4-DOF  
 486 model in 10 min is  $2.1 \times 10^{-7}$ , with an error of 0.05%. Moreover, the calculation time  
 487 of the 4-DOF simplified modal model is only about 1/55 of that of the FE model, which  
 488 shows that the 4-DOF simplified modal model is adequate to replace the FE model  
 489 when conducting fatigue life prediction.



490 Fig. 12. Comparison of stresses at the mudline from the FE model and the 4-DOF  
 491 model in time domain (a) and frequency domain (b)

492 The 4-DOF simplified modal model is used to conduct fatigue life prediction for  
493 the OWT support structure under LC 1 to LC 6. A 10 min simulation for each random  
494 seed of six different random seed numbers conducted to obtain the stress time histo-  
495 ries at the mudline. The location of the hotspot used to evaluate fatigue damage is se-  
496 lected at the point where the maximum stress is reached, and this point is in the support  
497 structure cross section at the mudline. Although the location in the monopile where the  
498 moment reaches its maximum value can be below the mudline, the location at the mud-  
499 line is picked for simplicity. Further, as the SSI is modelled in the FE model by an  
500 equivalent soil stiffness matrix, it is unstraightforward to obtain the internal forces at  
501 the cross sections below the mudline. Given the stress time series at the selected hotspot,  
502 the corresponding fatigue damage is calculated. Then the fatigue damage for the set of  
503 mean wind speed, wave period and wave height in 10 min is obtained by averaging the  
504 fatigue damage for all the six random seeds. For all the 22 environment states, the 10  
505 min fatigue damage are calculated, and the fatigue life is predicted according to  
506 Palmgren-Miner sum rule by combing these calculated fatigue damage and the occur-  
507 rence probabilities of the environmental states.

508 For different scour depths, the fatigue life of the OWT considering both operating  
509 and parked conditions is predicted with or without TMD installation, and the results are  
510 shown in Fig. 13. It is shown that an increase in scour depth leads to a decrease in  
511 fatigue life, and an increasing fatigue life reduction rate can be observed when the scour  
512 depth increases. When no scour occurs and the TMD is not installed on the OWT, the  
513 OWT's fatigue life is 59.3 years, and the fatigue life drops to 45.0 years when consid-  
514 ering the maximum scour depth of 1.3 D. There exist some uncertainties in the fatigue  
515 life prediction process due to the generation of random wind field and wave profile. It  
516 should be noted that the predicted fatigue life is much longer than the normally adopted  
517 OWTs' design fatigue life of 25-30 years. This can be explained by the following rea-  
518 sons. First, the maximum moment of the OWT support structure is not at the cross  
519 section at the mudline where the selected hotspot is located. Second, the complex wind  
520 and wave directionality during the OWT's lifetime is simplified, which would influence  
521 the fatigue calculation result. Third, many other operation conditions such as starting  
522 up, shutting down phases are not considered in this study, which can also have an im-  
523 pact on the fatigue damage accumulation. Moreover, the installation of the TMD greatly  
524 extends about 51.8% of the OWT support structure's fatigue life.



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Fig. 13. Fatigue life of wind turbine with different scour depths

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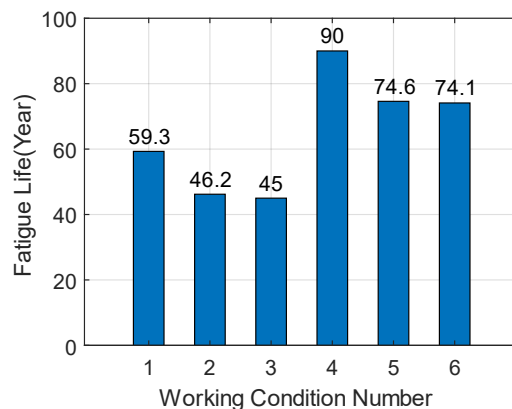
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The fatigue life prediction results of the OWT were obtained for all the six LCs, as shown in Fig. 14. The fatigue life from the reference case LC 1, 59.3 years, is regarded as the reference fatigue life. It shows that the fatigue life decreases by 14.3 years, or about 24.1%, when the scour depth is set as the maximum value of 1.3D without applying the TMD, compared to the reference fatigue life. When considering the time-varying scour, the fatigue life decreases by about 22.1% from the reference value. When comparing the results for LC 1 and LC 4, it shows the installation of the TMD results in a significant increase in the fatigue life of the OWT, with an increase in fatigue life of about 30.7 years, which is about 51.8%. In LCs with the TMD installed, the fatigue life in LC 6 decreases by about 17.7% when the scour depth reaches 1.3 D, compared to the result in LC 4. But the fatigue life in LC 6 is still 1.25 times of the reference fatigue life, which indicates that the imposition of TMD can effectively increase the fatigue life of the OWT by reducing vibration amplitudes.

540



541

Fig. 14. Fatigue life of the wind turbine under six operating conditions



542 **4.5 Fatigue calculation with optimized TMD**

543 To compare the optimization effect and speed up the optimal parameter search  
 544 process, the mass ratio of TMD is first kept as 1%. Before the optimization, the param-  
 545 eter ranges of the frequency ratio and damping ratio need to be defined. The optimal  
 546 frequency of the TMD is usually close to the resonance frequency of the main structure,  
 547 so the range of the frequency ratio was chosen to be from 0.8 to 1.1 for optimization.  
 548 As the optimal damping ratio could vary in a relatively larger range, the range of the  
 549 damping ratio for optimization is chosen to be from 1% to 30%. The optimization of  
 550 the TMD is also conducted with the mass ratio not fixed. A range of the mass ratio from  
 551 0.001 to 0.1 is used to optimize the TMD so that the influence of the mass ratio can be  
 552 evaluated.

553 Table 6. Optimization of TMD parameters

Optimization method	Mass ratio range	Time-varying scour	Optimal mass ratio	Optimal frequency ratio	Optimal damping ratio	Fatigue life (Year)
Initial (LC 5)	0.01	Use	0.01	0.99	0.061	74.6
FOT	0.01	Use	0.01	0.94	0.050	93.2
FOT	0.001-0.1	Use	0.097	0.92	0.150	133.2

554 The optimal parameters obtained by FOT as well as the predicted fatigue life are  
 555 listed in Table 6. The fatigue life for LC 5 and the parameters of the initially designed  
 556 TMD are also shown in Table 6 for comparison. It shows that when the mass ratio is  
 557 fixed at 1%, the optimal frequency ratio is 0.94, the optimal damping ratio is 5%, and  
 558 the final fatigue life is 93.2 years. Compared to the fatigue life with initially optimized  
 559 TMD using the traditional method without considering scour, the fatigue life is in-  
 560 creased by 18.6 years or about 25%. It indicates that the parameter search in the opti-  
 561 mization process is correct and it is better to use the TMD parameter search method to  
 562 design the TMD after obtaining the time-varying scour curve. When the mass ratio  
 563 range is taken from 0.1% to 10%, the optimal mass ratio of the TMD is 9.7%, the fre-  
 564 quency ratio is 0.92, the damping ratio is 15%, and the final fatigue life is 133.2 years.  
 565 In this case, the fatigue life of the OWT is significantly increased mainly due to the  
 566 large mass ratio. However, in practice, it might be uneconomic to implement a TMD  
 567 with such a large mass ratio.

## 568 5 Conclusions

569 This study establishes a rapid numerical model which can consider the effect of  
570 scour and installation of a TMD, and the TMD operates only in the FA direction. The  
571 model is simplified by using concentrated mass instead of RNA and ignores the non-  
572 linearity of the equivalent stiffness matrix. The established model is used to investigate  
573 the influence of scour and the installed passive structural control device on the OWT's  
574 natural frequencies and fatigue life through 22 environmental states. An optimization  
575 technique is also developed to find optimal parameters of the TMD considering time-  
576 varying scour. Moreover, it shows that the vibration amplitude of the OWT can be ef-  
577 fectively reduced by the TMD. On the one hand, results show that the TMD reduces  
578 the vibration amplitude of the tower top. On the other hand, when the scour depth  
579 reaches 1.3D, the wind turbine support structure becomes more flexible, with the dis-  
580 placement of the tower top increased without TMD.

581 In addition, the fatigue calculation results show that installation of the TMD sig-  
582 nificantly extends the fatigue life of the OWT, but scour can cause a reduced perfor-  
583 mance of the TMD. It is found that when the initially designed TMD does consider  
584 scour and the scour-induced natural frequency reduction during the OWT's lifetime, its  
585 performance is not as good as the TMD optimized by the developed FOT in terms of  
586 fatigue life enhancement. Given a mass ratio of 1%, the fatigue life can be extended by  
587 25% with the TMD optimized by FOT. This is because FOT can consider the effect of  
588 time-varying scour. This study only performs the analysis with scour, but other factors  
589 such as soil degradation can also alter the dynamic characteristics of OWTs and thus  
590 have some influence on structural control devices' performance and fatigue life evalu-  
591 ation. Additionally, during OWTs' lifetime, the properties of installed TMDs can also  
592 change, making the evaluation of TMDs' performance and OWTs' fatigue life more  
593 complicated. These factors are worthwhile investigating in the future.

## 594 6 Competing interests

595 The contact author has declared that none of the authors has any competing inter-  
596 ests.

## 597 7 Acknowledgements

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