Load case selection for finite element simulations of wind turbine pitch bearings and hubs

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Abstract. Finite element simulations of large rolling bearings and structural parts are an indispensable tool in the design of wind turbines. Unlike simpler structures or smaller bearings in rigid environments where analytical formulas suffice, wind turbine components require a more comprehensive approach. This is because analytical formulas often fall short in predicting load distributions and stresses, leading to inadequate designs. However, due to the complexity of the finite element models and number of operational loads cases involved, it's necessary to strike a balance between achieving realistic results and keeping computational times manageable. This study focuses on the selection of load cases for simulations of pitch bearings and hubs of wind turbines. The models for these contain the hub, the pitch bearings, the inner parts of three blades, and any necessary interface parts. The simulation results allow the calculation of static and fatigue strength. Given the complexity of the problem, with each rotor blade having six degrees of freedom, five types of loads, and the pitch angle, ~~the potential combinations of loads~~ their potential combinations would result in an unmanageably high number of required simulations. The present work ~~exploits relationships between load components and the rotor position by means of stacked data binning to reduce the number of load cases needed for fatigue calculations. It uses the standard deviation of supposedly dependent signals to determine necessary number of bins. The IWT 7.5-164 reference turbine and three commercial turbines serve as the basis for case studies which include exemplary finite element simulations~~ assumes that binning of one or more degrees of freedom into sufficiently small bins results in the other degrees of freedom showing negligible variation. Defining the values for these binned degrees of freedom thus gives the values for the others and reduces the number of combinations drastically. The validity of this approach is verified by the standard deviations of the unbinned degrees of freedom and by exemplary stress calculations of a pitch bearing ring. The blade's azimuth angle and bending moments of one blade root allow determining the loads at all three blade roots and ~~allow determination~~ thus the derivation of stress-time series with 384 simulations of a full rotor with a reasonable degree of confidence.

1 Introduction

Pitch bearings of wind turbines are slewing bearings which connect each rotor blade with the rotor hub (Hau, 2017). There are several commercially available design types for these bearings, as listed in (Stammler, 2020). Bearings can fail for various reasons as described in ISO 15243 (ISO, 2017). Rolling contact fatigue and structural fatigue of the rings are among those and are driven by stress cycles. Hubs are the structural centerpiece of wind turbine rotors, providing the linkage between the three

blades and the turbine's drive train. Similar to the pitch bearing ring, the structural integrity of hubs is influenced by stress cycles, which drive fatigue (Hau, 2017).

Aero-elastic simulations of wind turbines provide the load time-series at various positions, such as the rotor blade roots (Burton et al., 2011; Hau, 2017). In order to assess the lifespan of individual components, it is necessary to establish a relationship between the applied loads and the resulting stresses. This involves calculating the nonlinear dependencies between these variables. Finite element (FE) simulations derive these relations for each calculated load case. In theory it is possible to use FE simulations with the loads at each discrete time step of the input data. This approach would yield time series data of stresses, which could then be utilized for analytical fatigue calculations. Menck et al. (2020) state a duration of 25 min for one simulation of a model containing one rotor blade and bearing. Based on this, hundreds of thousands of load cases for a full rotor would ~~results~~ result in several years of computational time on a similar machine. ~~would~~ Doing so is not possible within reasonable computing times and a reduction of load cases for the simulations is therefore necessary.

Aside from the definition of load cases, the selection of a model type is another crucial aspect for a FE simulation. This study covers full rotors with three blades. The load and stress distributions of pitch bearings and hubs are influenced by the loads the three rotor blades transfer to their roots. It is assumed that the stress distribution in one pitch bearing is influenced by the loads of the other pitch bearings by load transfer through the hub.

Chen and Wen (2012) simulated a double-row four-point contact ball bearing that is used as pitch bearing in a 1.5 MW wind turbine. They used a model with three rotor blade roots but did not elucidate on the selection of load cases.

To the best knowledge of the authors, the only approaches for load case selection published in literature are limited to the determination of load cases for one blade root, i.e. one pitch bearing:

- Characterise and simplify the input load time series by means of rainflow counts and use the reduced data to define load cases for the FE. Use the results, which again have the form of rainflow count results, to calculate fatigue.

- Use the extreme operating loads. Evenly spread load steps in between those and calculate the results for these load cases. Interpolate between the results to obtain stress time-series and apply rainflow counts to calculate fatigue.

Both approaches will result in inaccurate results in comparison to FE simulations of each time step of the input data. The extent of the inaccuracies depends on the number of load cases simulated and the turbine configuration.

Becker et al. (2017) describe a process as per the first of the abovementioned approaches where the input load time series are first processed into rainflow counts which then give the load cases for the FE simulations. To account for the complex behavior of large bearings, the bearings circumference is split into several sections, for each of which the rainflow counts are done. Stammler et al. (2018) did 126 simulations with a rotor of a 3 MW turbine with variations of pitch angles and bending moments. They evaluated the load distribution in one pitch bearing, kept the pitch angles of the other bearings constant and the loads at the other bearings at one third of the loads of the primary bearing. They did not elucidate on the reasons for the load case selection. The load distribution in the pitch bearing was shown to be dependent on the interfaces. Menck et al. (2020) used a one-third rotor with rotational symmetric boundary conditions to reduce the computational effort in comparison to a full rotor. They ran 358 simulations on this model and varied the pitch angle and the resulting bending moment and its angle as per

60   the second approach. With a regression of the resultant rolling body loads they obtained time series of rolling body loads and calculated the fatigue life of the bearing raceways. In particular for comparably weak hub structures, Becker and Jorgensen (2023) stated the need of full rotor simulations for pitch-bearing damage modes which are driven by edgewise loads of the blades. They also point to the need of taking into account flapwise moments and combinations of the individual moments for comprehensive assessments.
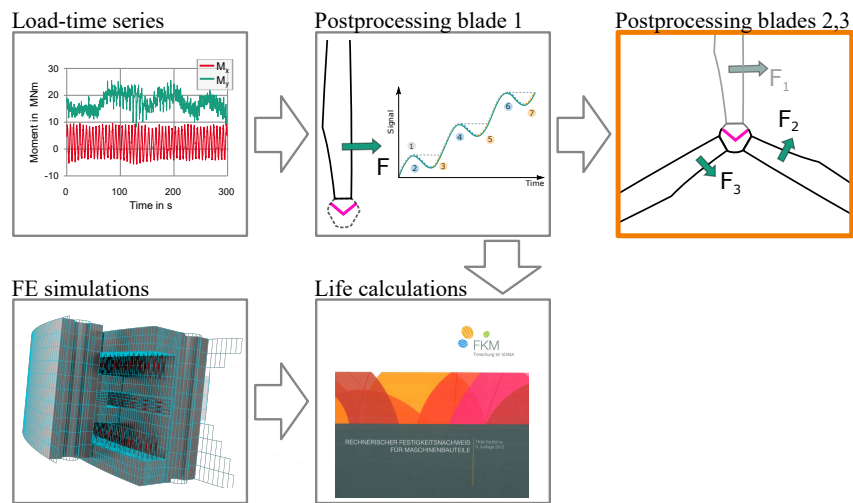
Figure 1. Flowchart of load case selection with preceding rainflow count
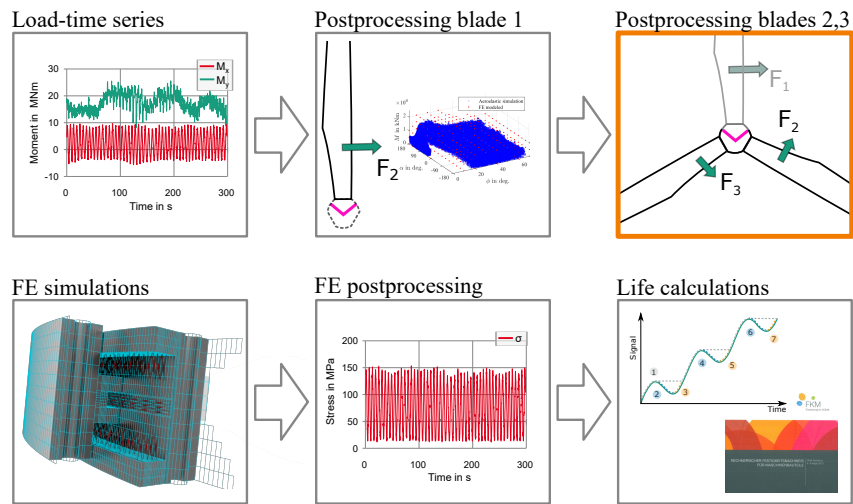
Figure 2. Flowchart of load case selection with preceding interpolation and stress-time series creation

65   Figures 1 and 2 summarize the two published approaches as flow charts. Figure 1 depicts the approach by Becker et al. (2017). The input load time series (upper left box) are processed by rainflow counts of the loads of an arbitrarily selected blade one (upper center box). These are then used for finite element simulations of the pitch bearings and their interfaces (lower left box). As the load cases already are given in form of rainflow counts, the FE-results can be used directly for fatigue calculations. The FKM guideline contains methods for such calculations (lower center box, FKM (2012)). Becker et al. (2024) apply the

70   FKM guideline for static and fatigue bearing ring strength. The selection of the loads of the other blades (upper right box in orange) is not explained in the publications.

Figure 2 depicts the approach by Stammler et al. (2018) and Menck et al. (2020). The input loads (upper left box) are processed evaluated to obtain the ranges of each ~~signal~~load component. In between the extreme values, a grid of load cases is created (upper center box). These are then used for finite element simulations of the pitch bearings and their interfaces (lower

75   left box). The results need additional postprocessing by interpolation to obtain stress-time series (lower center box). A rainflow count of these time series is then used for fatigue calculations (lower right box). The selection of the loads of the other blades (upper right box in orange) is either omitted or not explained in detail in the publications.

To the authors' knowledge, there is a notable gap in the existing literature regarding a comprehensive exploration of load case selection specifically for pitch bearing simulations involving three rotor blades, highlighted by the orange boxes in Figure

80   1 and 2 flow charts. Furthermore, there appears to be a lack of published works addressing load case selection for rotor hubs. The central inquiry driving this study is to understand to which ~~extend~~ extent the loads of one rotor blade bearing are correlated or affected by the loads of the other blade bearings or the rotor position.

The remainder of this article begins with Section 2, which introduces definitions for the following sections, the necessary data input, and the methods which are applied to determine dependencies. The data input for the case studies includes aero-

85   elastic simulation time series of the IWT7.5-164 reference turbine and three commercial turbines. Section 3 covers the results of the case studies and shows which relationships are useful for the load case selection. The final discussion and conclusions then summarizes the findings of this work.

2   Definitions and methods

2.1   Coordinate systems

90   Pitch bearing loads in this study use the Cartesian coordinate system shown in Figure 3, left, with the exception of the pitch angle θ, which is positive on clockwise, i.e. opposite to the right-hand rule. This convention is industry standard, and most turbine simulation time series follow it. Although the coordinate system does not rotate with the pitch angle, the term flapwise bending moment refers to $M_{y,\mathrm{B}}$ and the term edgewise bending moment to $M_{x,\mathrm{B}}$ in the following. Strictly speaking, $M_{y,\mathrm{B}}$ is only a pure flapwise moment if the pitch is at $0°$. Flapwise bending moments are the result of wind thrust, whereas edgewise

95   bending moments are mostly dominated by gravitational forces. Hub center loads and blade azimuth angle in this study use the coordinate system shown in Figure 3, right.
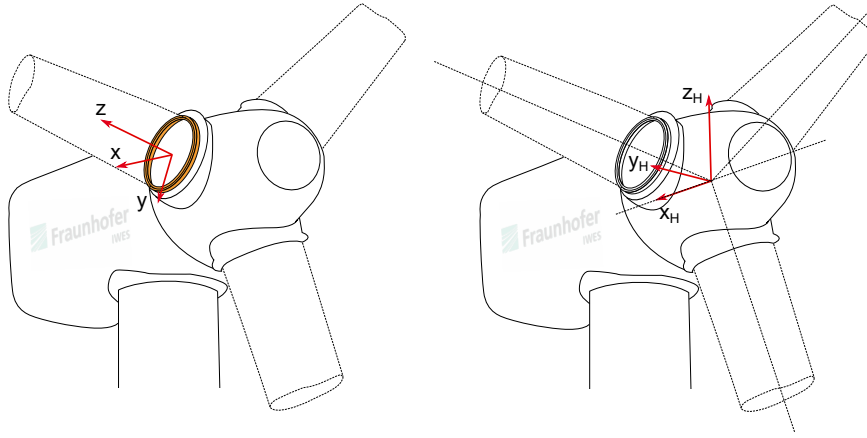
Figure 3. Pitch bearing coordinate system (fixed to rotor hub, left); hub coordinate system (right) (Stammler, 2020)

The blade azimuth angle $\Phi_{r,B}$ is defined in Figure 4. Note that the $0°$ position is arbitrarily chosen. As long as it is consistent throughout the data set, any other position can serve as $0°$.
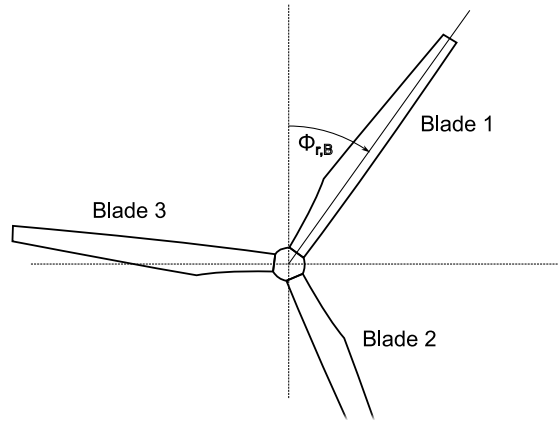
Figure 4. Blade azimuth angle $\Phi_{r,B}$

The three blades have the arbitrarily chosen numbers one, two, and three which are consistent throughout the simulation data set. The numbers increase clockwise seen from the incoming wind direction. $\Phi_{r,B}$ refers to blade one. Blade one is also called primary blade in the following, blade two and three secondary blades.

2.2 Input data and signal selection

The time-series output of aero-elastic simulations is the input for the present work. Time-series output can contain numerous signals. Becker et al. (2017); Stammler et al. (2018); Menck et al. (2020); Becker and Jorgensen (2023); Becker (2024) all use

the edgewise and flapwise bending moments $M_{x,\mathrm{B}}$ and $M_{y,\mathrm{B}}$ to describe the load cases of one pitch bearing. The use of the combined bending moments $M_{\mathrm{xy,B}}$ and their load angle β is equivalent to the use of $M_{x,\mathrm{B}}$ and $M_{y,\mathrm{B}}$. Stammler et al. (2018); Menck et al. (2020) also include the pitch angle θ.

The input data for finite element simulations with three blades thus needs pitch angles θ, blade root bending moments $M_{x,\mathrm{B}}$ and $M_{y,\mathrm{B}}$, and forces $F_{x,\mathrm{B}}$, $F_{y,\mathrm{B}}$, and $F_{z,\mathrm{B}}$ for all three blades. The need for the inclusion of pitch angles ~~bases upon~~ is based on the results of Stammler et al. (2018) and Menck et al. (2020), who show the load distribution in a blade bearing to be dependent on the non-rotationally symmetric stiffness profile of the rotor blade. At constant blade root loads, different pitch angles can thus cause different load distributions on its circumference. While the aforementioned signals suffice to build finite element simulations, the introduction of additional signals for the selection of load cases might render more meaningful relations between the load components. The blade's azimuth angle $\Phi_{\mathrm{r,B}}$ and the out-of-plane rotor moment $M_{\mathrm{y,H}}$ are included as additional signals. $\Phi_{\mathrm{r,B}}$ is strongly related to the dominant 1p-component of all $M_{x,\mathrm{B}}$. The out-of plane rotor moments might help to narrow relations between the individual $M_{y,\mathrm{B}}$.

2.3 ~~Calculation of missing time series signals~~

~~While the blade root loads of all three blades and the pitch angle of the primary blade are essential to perform the tasks laid out in the later sections of this work, the absence of other signals can be accepted as they can be derived from the aforementioned signals. This might be necesssary when the input data sets do not contain all signals and cannot be recreated in a convenient fashion.~~

- ~~Pitch angles of secondary blades~~

  ~~Although modern turbines can have individual pitch control and differing pitch angles between the blades, it is permissible to assume same pitch angles on all three blade roots. In comparison to the larger angle changes performed by the collective pitch to control the turbine's power, the smaller travels of the individual pitch have a negligible cross-influence between the individual blade roots.~~

- ~~Out-of-plane rotor moments~~

  ~~The out-of-plane rotor moments $M_{\mathrm{y,H}}$ and $M_{\mathrm{z,H}}$ in a fixed frame of reference can be calculated from the individual flapwise blade root moments. This assumes $\Phi_{\mathrm{r,B}}$ as per Figure 4.~~

$$M_{\mathrm{y,H}} = M_{\mathrm{y,B,1}} \cdot cos(\Phi_{\mathrm{r,B}}) - cos\left(\Phi_{\mathrm{r,B}} + \frac{2}{3}\pi\right)(M_{\mathrm{y,B,2}} + M_{\mathrm{y,B,3}})$$

$$M_{\mathrm{z,H}} = M_{\mathrm{y,B,1}} \cdot sin(\Phi_{\mathrm{r,B}}) - sin\left(\Phi_{\mathrm{r,B}} + \frac{2}{3}\pi\right)(M_{\mathrm{y,B,2}} + M_{\mathrm{y,B,3}})$$

- Blade azimuth angle

  As the edgewise bending moments of the rotor blades are dominated by gravitational forces, the 1p component of $M_{x,\mathrm{B}}$ links directly to the blade azimuth angle $\Phi_{\mathrm{r,B}}$. An algorithm to obtain $\Phi_{\mathrm{r,B}}$ can be outlined as follows for each time series file:

- Define $0°$ position for $\Phi_{\mathrm{r,B}}$, e.g. at local maximum of the first derivative of $M_{x,\mathrm{B}}$

- Apply low pass filter to $M_{x,\mathrm{B}}$ to eliminate high frequency components

- If necessary, calculate derivative of $M_{x,\mathrm{B}}$

- Identify local maxima or minima

- Check for consistency, i.e. remove extreme values in unrealistic proximity to each other from the analysis

- For each space between extreme values: calculate linearly increasing vector ranging from $0°$ to $360°$ or 0 to 2π for the time steps from one extreme value to the next

- Paste the resulting vector at the corresponding positions into a new $\Phi_{\mathrm{r,B,calc}}$ signal in the file

- For a leading or trailing incomplete rotation of the rotor, use portions of the adjacent full vector This algorithm reproduces speed changes between full rotor revolutions, but not within a revolution. It is essentially equivalent to taking the inverse sine of the 1p-component of the edgewise bending moment observed at one of the blade roots.

2.3 Data binning and mean value evaluation

The relations between different load signals are evaluated with the help of data binning (bin counts). The relation between each time-series file duration and the period it represents of the turbine design life is expressed by multipliers. A multiplier quantifies the number of repetitions of each time-series file to reach the design life of the turbine. One or more signals are assumed to be independent and the other signals are assumed to be dependent on them. For each equidistant bin of the independent signal(s), all assumed dependent signals are evaluated for their mean value and standard deviation. Mean value and standard deviation are weighted by the multipliers. The use of the standard deviation implies the assumption of a normal distribution of the signal values around the mean value, which is not necessarily the case. Yet, it allows a good comparison between different data binning with different bin numbers.

In case of more than one assumed independent signal, the bin counts are stacked. For each bin of the first signal, all bins of the second signal are counted. Table 1 lists an example structure of such a result for two independent signals and two dependent signals. The result values are arbitrarily chosen. The first signal is split into two and values are taken from the later case study, but limited to two bins for the first and three bins for the second signal into three bins, resulting in a total of six bins. The first signal is $\Phi_{\mathrm{r,B}}$ and the second signal $M_{y,\mathrm{B},1}$. The first two columns contain a normalized bin range for the values the bin range of these two signals. The third column contains the number of values within that range time spent in the bin within the turbine

life. The columns for the dependent signals then contain their mean values ('mean') and standard deviations ('std'). In the context of the present work, the mean values are the input values of the FE simulations for all values of signal one and two in the respective bin range.

Table 1. Example output of data binning

Independent signals			Dependent signals			
$\Phi_{r,B}$ **in** $^\circ$	$M_{y,B,1}$ **in kNm**	**Time in bin in h**	$M_{x,B,2}$ **mean**	$M_{x,B,2}$ **std**	$M_{y,B,2}$ **mean**	$M_{y,B,2}$ **std**
67.5 – 90	14,169 – 16,189	1,186	-614	791	13,850	1,868
67.5 – 90	16,189 – 18,028	1,075	-248	803	15,463	1,683
67.5 – 90	18,028 – 20,227	373	-78	756	16,383	1,323
90 – 112.5	14,169 – 16,189	1,194	-2,614	679	13,780	1,964
90 – 112.5	16,189 – 18,028	1,011	-2,250	700	15,379	1,753
90 – 112.5	18,028 – 20,227	384	-2,101	621	16,101	1,366

The standard deviations of dependent signals are combined by weighted means to a single standard deviation for all bins and normalized against the maximum value of $M_{y,B,1}$ of the data set. The number of bins of the independent signals is increased until the standard deviation of dependent signals converges or until a finer resolution of bins is unreasonable.

2.4 Finite element simulations

The verification of the assumption of cross-influences between the pitch bearings and the load case selection method needs finite element simulations. This work uses a bearing model as described in Graßmann et al. (2023) in a full rotor model. A full rotor contains three blades, blade bearings, the hub, part of the main shaft, and all necessary interface parts such as stiffener plates. The bearing model uses non-linear springs to represent the rolling bodies and connects these via force-distributed constraints to the raceways. The bearing rings including the bolt holes are represented with 3D-elements. The hub and all other interfacing steel parts are represent with 3D-elements as well. The modelling approach is validated in Graßmann et al. (2023) with experimental results. The deviations between measured and simulated tangential ring deformations are below 10%. Further validation is not part of the present work. The three blades are modelled according to Menck et al. (2020) with shell elements except for the root section which consists of 3D elements. Finite element simulations within the frame of the present work serve two targets:

– Verify initial assumption of the influence of secondary blade bearing loads on the stress distribution on blade bearing one (see Section 3.2).

– Relate standard deviation of the data binning for outer loads with deviations of the stress values in the bearings (see Section 3.4).

A rotor model which considers only one rotor blade and introduces symmetry conditions on its boundaries is called a one-third rotor model (see left of Figure 5). A comparison between full and one-third model results delivers the verification of cross-influences of the three blades. As the model for this work was initially set up as a full rotor and only a limited number of simulations are done, a one-third rotor behavior is achieved by loading all three blades with the same load. For convenience, this model is designated one-third rotor model in the following.
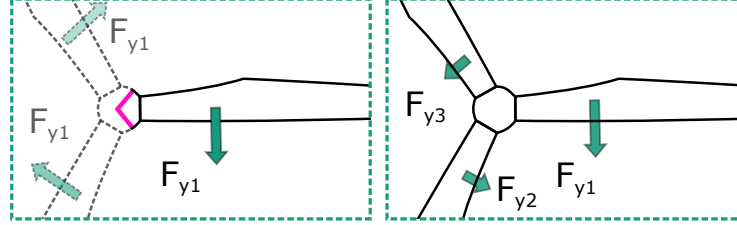
Figure 5. One-third rotor model (left) , full rotor model (right)

3 Case studies

3.1 Input data and scenario

The IWT7.5-164 is a nearshore reference wind turbine (Sevinc et al., 2014). The authors used time series data of this turbine in previous works, see (Stammler et al., 2019; Stammler, 2020). Table 2 lists the main properties of the turbine. The simulation time series, taken from Requate et al. (2020), contain all signals listed above which makes the calculation of additional signals as described in Section A unnecessary for this case study. The data set comprises 156 files of the DLC1.1 with mean wind speeds from 3 to 25 m/s. Figure 6 shows the generator output power over momentary wind speed in x-direction of the hub coordinate system of Figure ~~??~~ 3 with calculated mean values.

Figure 7 shows an exemplary time series of the turbine simulation data at 11 m/s mean wind speed and gives a first impression of the characteristics of the individual signals. The turbine is in power production mode. The top row shows the $M_{y,\mathrm{B}}$ and $F_{x,\mathrm{B}}$ of all three blades, the next row $M_{x,\mathrm{B}}$, $F_{y,\mathrm{B}}$, and $F_{z,\mathrm{B}}$ of all three blades. Signals pertaining to the same blade are displayed in the same color. Bending moments are the thick lines, forces the thin and dashed lines. The blade's azimuth angle is depicted in the third row and the two tilting moments $M_{y,\mathrm{H}}$, green, and $M_{z,\mathrm{H}}$, orange, of the rotor in the last row. The flapwise blade moments and the rotor moment about its horizontal axis appear more stochastic than the edgewise moments and the connected forces. Edgewise bending moments and radial forces have a sine characteristic with a phase angle shift of 120° between them. Relating these signals either to each other or to the rotor azimuth angle seems a promising approach.

Figure 8 further supports the close relation of $\Phi_{\mathrm{r,B}}$ and $M_{x,\mathrm{B}}$. The blue areas contain all data points of the input data, with the full red line as the mean value and the dashed lines as the boundaries of the 95%-quantile. The orange vertical lines have a 120° spacing and allow easier visual comparison of the three plots.

Table 2. Main characteristics of the IWT7.5-164, from (Stammler, 2020)

Property	Symbol	Value	Unit
Hub height	h_{hub}	119.3	m
Specific power (per swept area)	ψ_{rotor}	355	W/m^2
Cut-in wind speed	V_{in}	3	m/s
Rated wind speed	V_{r}	11	m/s
Cut-out wind speed	V_{out}	25	m/s
Minimum rotational speed	Ω_{min}	5	rpm
Rated rotational speed	Ω_{r}	10	rpm
Rated tip speed	$V_{\text{tip,r}}$	85.9	m/s
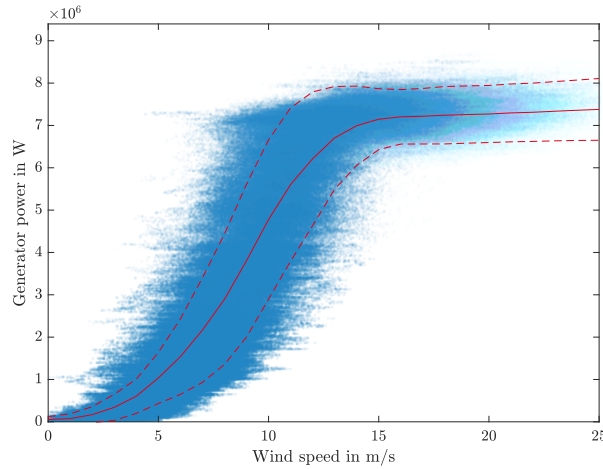
Figure 6. Generator power over wind speed from simulation data set, red line: mean value, red dashed lines: 95%-quantile

In addition to the IWT7.5-164 as a reference turbine, time series of three commercial turbines are part of the case studies. All time series are the result of aero-elastic simulations. The turbines are both onshore and offshore with rated outputs between 2 and 15 MW. The time series include power production load cases from cut in to cut out wind speed of the turbines. The time series were chosen due to their availability. Due to their commercial nature, further details on turbines and loads are subject to confidentiality agreements and cannot be disclosed. In the context of the present work, they serve to confirm the results are not limited to the specific design of the IWT7.5-164.

The finite element simulations are done with a full rotor model of one of the commercial turbines. Again, details of the design cannot be disclosed. This rotor model was selected because the structural design of the components is far more detailed
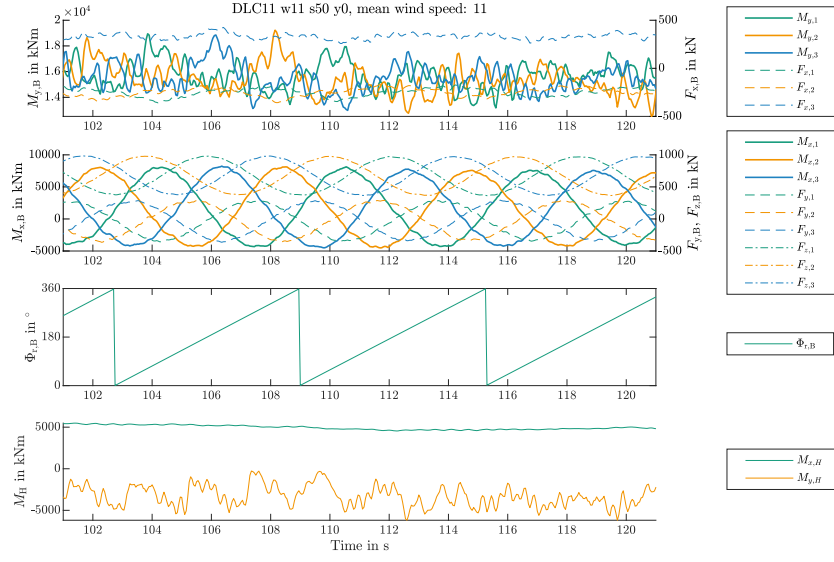
Figure 7. Time series of IWT7.5-164 at 11 m/s
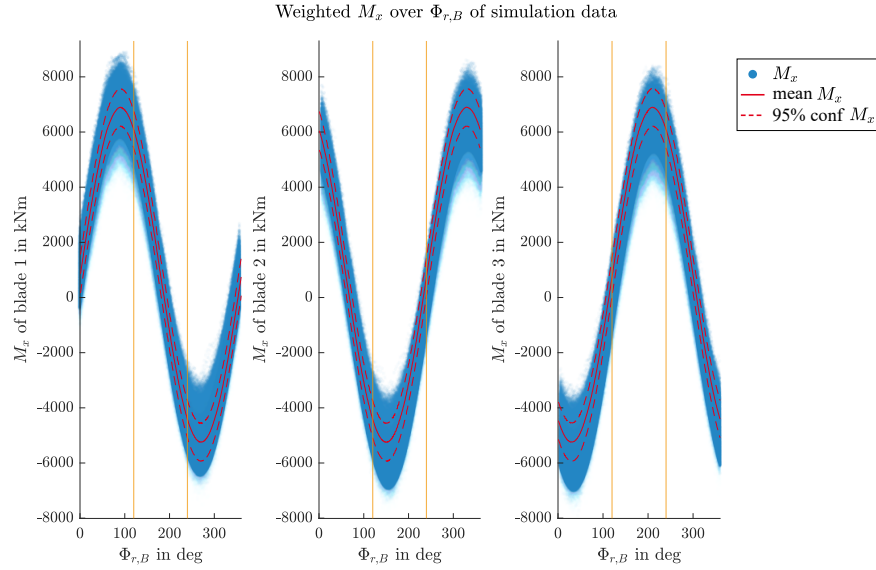
Figure 8. Weighted $M_{x,\mathrm{B}}$ of all blades over $\Phi_{\mathrm{r,B}}$, red line: mean value, red dashed lines: 95%-quantile

215 than typically in reference turbines and the authors deemed the obtained results to be closer to state-of-the-art turbines than those achievable with IWT7.5-164 components.

3.2 Finite element simulation of one rotation

To verify the central assumption of cross-influences between the individual pitch bearing loads, the first set of finite element simulations comprises one exemplary rotor rotation in twelve steps. This rotation is simulated with a full and a one-third rotor
220 model.

Stress cycles in the outer ring drive its structural fatigue. Locations with high stress amplitudes and a high number of stress cycles are most prone to fatigue. Their identification is a critical part of the design process and is not within the scope of the present work. Instead, a locations with high stress amplitudes is selected and then used for comparative analyses. These locations are the outer ring bolt holes at two distinct circumferential positions. These are on the positive and negative y-axis of
225 the pitch bearing coordinate system and experience high stress dynamics due to the M_x edgewise loads.

The left part of Figure 9 shows a simulated stress distribution in an outer ring bolt hole with higher values in red and lower values in blue. The stresses are tangential or hoop stresses. In case of the outer ring, they are tensile stresses. The right part is a concept sketch of the bearing. The front shows a section with ~~with~~ the outer ring on the left and the inner ring on the right. The outer ring attaches to the hub and the inner ring to the blade of the turbine. The shown bearing is a four-point contact ball
230 bearing with a contact angle of $45°$. A blade root bending moment such as M_x causes axial loads on the bearing rings. The rolling bodies turn these into a combined radial and axial load which pushes the outer ring to the outside and the inner ring towards the bearing center. As the inner ring is pushed to the bearing center, it gets compressed. The deformations are usually smaller than on the outer ring and the compressive stresses are less critical for fatigue. The outer ring, however, experiences tensile hoop stresses and larger deformations. The ~~The~~ lower side of the visualization is the hub side of the pitch bearing and
235 usually experiences smaller deformations and stresses than the blade side.

Figure 10 shows stresses of two outer-ring bolt holes on the positive and negative y-axis for a full and one-third rotor simulation ~~.~~ over one rotor revolution. The circumferential position of the bolts is on the positive and negative y-axis of the pitch bearing coordinate system as indicated in the right part of the figure. $90°$ is the position on the positive y-axis, and $270°$ the position on the negative y-axis. The results are normalized for the maximum stress at all positions and ~~are~~ given as
240 a function of the rotor position. The axial position in the bolt hole, at which the stress values are obtained, is defined as the position of at which the maximum stress in the respective bolt hole occurs.

From Figure 10, the $90°$-position is identified as the more critical position for fatigue due to its higher stress amplitude. The amplitude of the stress cycle ~~of the~~ in the bolt hole for the one-third rotor model is 9.25% lower than that of the full rotor model. This ~~difference~~ results in a significant difference in outer ring structural fatigue life and ~~supports the initial~~
245 ~~assumption~~ demonstrates the importance of cross-influences ~~between the blade roots. This supports the assumed need for full rotor simulations. This supports the assumed need for full rotor simulations.~~ of the blade loads. The $\Phi_{r,B}$, azimuthal positions of the extreme stresses ~~match~~ are close to those of the extreme $M_{x,B,1}$ during the rotation. ~~The following FE simulations~~
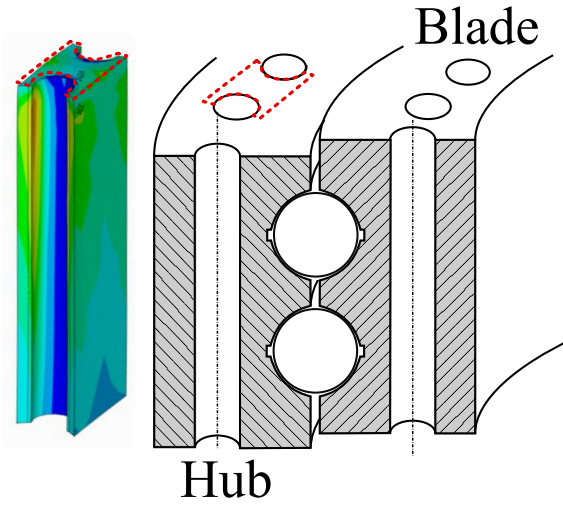
Figure 9. Visualization of tangential stresses in bolt holes of outer ring (left), location in bearing (right)
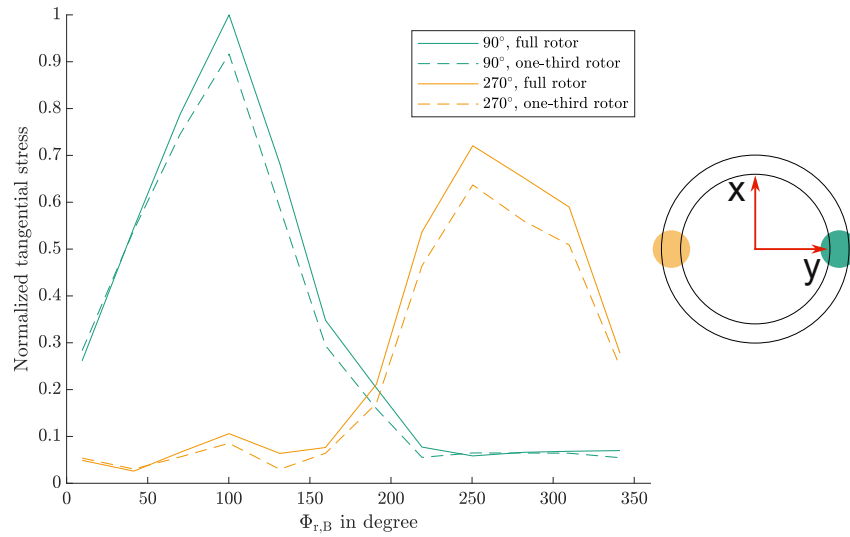
Figure 10. Normalize tangential stresses of bearing outer ring at two positions for full and one-third rotor simulations over one rotor revolution

~~are thus limited to these extreme values~~ Following simulations thus only use the extreme values of $M_{x,B,1}$ to obtain stress amplitudes for comparative analyses.

3.3 Data binning results

This section evaluates possible selections of independent signals which define the load cases for finite elements simulations. For each independent signal, increasing numbers of bins are considered. At this point, the decision criterion for the inclusion of a signal as an independent signal in the load case definition is the standard deviation of assumedly dependent signals, with smaller deviations being better. In the following Section on verification, this standard deviation is exemplarily related to deviations in stress amplitudes. Due to the large number of potential dependent signals a full visualization becomes impractical. Therefore, the tables below present the standard deviations of $M_{x,B,2}$ and $M_{y,B,2}$ as representative signals. These are the edgewise and flapwise bending moments of the second blade. All values are normalized to the maximum value of $M_{y,B,1}$ and also given as percentage of the standard deviation of the signal in the full data set. The edgewise bending moments are primarily influenced by gravitational forces and thus depend on the blade's azimuth angle $\Phi_{r,B}$. The initial data binning thus utilizes this azimuth angle. Other potential independent signals include pitch angle, flapwise and edgewise blade bending moments and rotor moments. For the following analysis, we exclude the rotor moment about the vertical axis, $M_{z,H}$, as it remains approximately constant, see Figure 7.

Tables 3 to 5 contain results of the reference turbine. The first column lists the independent signal or signals. In case of more than one independent signal, the data binning is stacked, i.e. the first signal is sorted into bins and then the second signal is sorted into bins for each bin of the first. The second and fifth column list the number of bin for a convergence of the standard deviation of the exemplary dependent signals, i.e. higher bin numbers do not result in significant further reduction of deviations. The third and sixth column contain the combined, normalized standard deviation of the dependent signals. The normalization is done with reference to a maximum value of $M_{y,B,1}$. Column four and seven finally show the effect of the data binning in comparison to an unprocessed data set.

Table 3 contains results for data binning involving a single independent signal. The first line uses $\Phi_{r,B}$ as independent signal. This is binned into 16 bins, each with a range of 22.5°. The combined standard deviation of $M_{x,B,2}$ over all bins is 2.4% of the maximum $M_{y,B,1}$ in the data set. In comparison to a data set with no binning, this equals a reduction of by 86.4%. However, this binning does not results in a reduction of the standard deviation of $M_{y,B,2}$.

With the exception of $\Phi_{r,B}$ and $M_{x,B,1}$ as independent signals, increasing the number of bins did not lead to a reduction in the standard deviation of the dependent signals. Notably, $\Phi_{r,B}$ significantly outperforms $M_{x,B,1}$ in this regard. It is also worth noting that no discernible relationship could be established between the flapwise bending moments of blade two and any of the signals selected as independent signals. For the following tests with stacked data binning, the number of 16 bins for $\Phi_{r,B}$ is kept constant and $M_{x,B,1}$ is omitted.

Table 4 contains results for stacked data binnings, each employing 16 bins for the blade's azimuth angle $\Phi_{r,B}$ as the first independent signal. The columns with the convergence bins refer to the second independent signal. Interestingly, neither the pitch angle nor the out-of-plane rotor moment improved the results. However, when the flapwise and edgewise bending moments were introduced in addition to the azimuth angle, there was a noticeable reduction in the standard deviations of the selected dependent signals.

Table 3. Data binning results for single independent signals

Independent signal	Convergence bins $M_{x,\mathrm{B},2}$	STD $M_{x,\mathrm{B},2}$ norm.	STD $M_{x,\mathrm{B},2}$ reduction	Convergence bins $M_{y,\mathrm{B},2}$	STD $M_{y,\mathrm{B},2}$ norm.	STD $M_{y,\mathrm{B},2}$ reduction
$\Phi_{\mathrm{r,B}}$	16	0.024	86.4%	1*	0.082	0%
$M_{x,\mathrm{B},1}$	4	0.147	16.9%	1*	0.082	0%
$M_{y,\mathrm{B},1}$	1*	0.177	0%	1*	0.082	0%
θ_1	1*	0.177	0%	1*	0.082	0%
$M_{y,\mathrm{H}}$	1*	0.177	0%	1*	0.082	0%

<p style="text-align:center;">* no significant reduction of standard deviations with more bins</p>

Both moments had positive effects, with more pronounced effects when the dependent bending moments were in the same direction. For instance, binning the flapwise bending moment reduced the deviation of the flapwise moments at blade two more effectively with 32.9% than the binning of edgewise moments, which lead to a reduction by 9.8%. The differences in the reduction of $M_{x,\mathrm{B},2}$ are less pronounced. Thus, the next stack data binning takes the combination of $\Phi_{\mathrm{r,B}}$ and $M_{y,\mathrm{B},1}$ as the first two independent signals.

Table 4. Stacked data binning results with 16 bins for $\Phi_{\mathrm{r,B}}$

Independent signals	Convergence bins $M_{x,\mathrm{B},2}$	STD $M_{x,\mathrm{B},2}$ norm.	STD $M_{x,\mathrm{B},2}$ reduction	Convergence bins $M_{y,\mathrm{B},2}$	STD $M_{y,\mathrm{B},2}$ norm.	STD $M_{y,\mathrm{B},2}$ reduction
$\Phi_{\mathrm{r,B}}$ / $M_{x,\mathrm{B},1}$	16**	0.020	88.7%	16**	0.074	9.8%
$\Phi_{\mathrm{r,B}}$ / $M_{y,\mathrm{B},1}$	16**	0.022	87.6%	16**	0.055	32.9%
$\Phi_{\mathrm{r,B}}$ / θ_1	1*	0.024	86.4%	1*	0.079	3.6%
$\Phi_{\mathrm{r,B}}$ / $M_{y,\mathrm{H}}$	1*	0.024	86.4%	1*	0.079	3.6%

<p style="text-align:center;">* no significant reduction of standard deviations with more bins
** small, but notable improvements with increasing bins</p>

Table 5 shows results for stacked bin counts for three independent signals. As 16 times 16 bins result in 256 bins from the combinations of $\Phi_{\mathrm{r,B}}$ and $M_{y,\mathrm{B},1}$, this evaluation is limited to eight bins as a maximum for the third signal with an eye on the overall number of simulations. The introduction of the pitch angle or the edgewise bending moment did not yield any significant improvements to the deviations. However, the introduction of the rotor moment $M_{y,\mathrm{H}}$ further reduces the standard deviation of $M_{y,\mathrm{B},1}$.

Again with an eye on the overall number of simulations necessary, the following evaluation tries to explore possibilities for bin reductions within the stacked data binnings of two independent signals. The stacked binning using $\Phi_{\mathrm{r,B}}$ and $M_{y,\mathrm{B},1}$ has shown promising results. Given that the selection of 16 bins for $\Phi_{\mathrm{r,B}}$ bases on its individual bin count, it might be possible to reduce any of the number of bins of the combination. Table 6 shows results of such bin variations. In contrast to the previous

Table 5. Combined bin count results with each 16 bins for $\Phi_{r,B}$ and $M_{y,B,1}$

Independent signals	Convergence bins $M_{x,B,2}$	STD $M_{x,B,2}$ norm.	STD $M_{x,B,2}$ reduction	Convergence bins $M_{y,B,2}$	STD $M_{y,B,2}$ norm.	STD $M_{y,B,2}$ reduction
$\Phi_{r,B}$ / $M_{y,B,1}$ / $M_{x,B,1}$	1*	0.020	88.7%	1*	0.055	32.9%
$\Phi_{r,B}$ / $M_{y,B,1}$ / θ_1	1*	0.022	87.6%	1*	0.055	32.9%
$\Phi_{r,B}$ / $M_{y,B,1}$ / $M_{y,H}$	1*	0.021	88.1%	8**	0.046	43.9%

* no significant reduction of standard deviations with more bins
** small, but notable improvements with increasing bins

tables, this table contains results of more dependent signals, again in the form of normalized values. The number of $\Phi_{r,B}$ bins has a larger effect on the deviations of any $M_{x,B}$ than on the $M_{y,B}$ deviations. Conversely, the number of bins for $M_{y,B,1}$ has a more pronounced influence on the deviations of other $M_{y,B}$ signals. Reducing the number of bins within the examined ranges consistently leads to noticeable changes in the deviations. This means the number of bins of any individual signal in the combined data binning cannot be reduced in comparison to binnings with single signals without negative influences on the results.

Table 6. Combined bin count results with varying bins for $\Phi_{r,B}$ and $M_{y,B,1}$

Bins $\Phi_{r,B}$	Bins $M_{y,B,1}$	STD $M_{x,B,1}$	STD $M_{x,B,2}$	STD $M_{x,B,3}$	STD $M_{y,B,2}$	STD $M_{y,B,3}$
16	16	0.020	0.022	0.022	0.055	0.055
16	8	0.021	0.023	0.023	0.060	0.060
8	16	0.037	0.039	0.039	0.055	0.055
8	8	0.038	0.039	0.039	0.060	0.060
4	16	0.076	0.070	0.070	0.057	0.057
4	8	0.076	0.070	0.070	0.061	0.061
4	4	0.077	0.071	0.071	0.068	0.068

To verify the previous results are valid for other turbine designs, especially commercial ones, exemplary data binnings are then repeated for three commercial turbines. Each 16 bins for $\Phi_{r,B}$ and $M_{y,B,1}$ are applied. Table 7 gives the results in relative reduction of standard deviations after the bin counts. The first result line contains the IWT7.5-164 results as a reference.

3.4 Verification by finite element simulations

To relate the results of the data binning to stress amplitude, the following comparisons repeat the simulations with the full rotor model described in Section 3.2. Instead of the time series values for each rotor blade, the values of dependent signals are now varied by the standard deviation. As the extreme stresses in the bolt hole at 90° coincide with the extreme $M_{x,B,1}$, these

Table 7. Bin count results with each 16 bins for $\Phi_{r,B}$ and $M_{y,B,1}$ and commercial turbines

Turbine	STD $M_{x,B,1}$ reduction	STD $M_{x,B,2}$ reduction	STD $M_{x,B,3}$ reduction	STD $M_{y,B,2}$ reduction	STD $M_{y,B,3}$ reduction
IWT	88.7%	87.6%	87.6%	32.9%	32.9%
1	86.9%	86.4%	86.4%	26.8%	26.5%
2	87.6%	87.1%	87.1%	37.7%	37.4%
3	82.5%	82.0%	81.8%	49.8%	49.8%

evaluations omit steps in between. The difference between the stresses obtained at minimum and maximum $M_{x,B,1}$ is the stress amplitude of the rotation. The simulations further use the combination of 16 bins each for $\Phi_{r,B}$ and $M_{y,B,1}$.

Table 8 lists the influence of variations of all $M_{x,B}$ and only secondary $M_{x,B}$ on this stress amplitude at the 90°-position in comparison to a simulation of the full rotor with all loads from the time series. The first two lines show the results of inputs
315 $\Phi_{r,B}$ and $M_{y,B,1}$ from time series and all other signals from bin counts. The first line changes all $M_{x,B}$ by data binning results plus the standard deviation. These variations of all $M_{x,B}$ by the standard deviations lead to significant changes in the stress amplitude. The value deviations are bigger than the deviations between one-third and full rotor and are thus not acceptable. The load case definition cannot rely only on $\Phi_{r,B}$ and $M_{y,B,1}$.

Hence, $M_{x,B,1}$ is introduced as a further independent parameter of the load case definition. Line three and four show results
320 of this addition. It leads to far better results in comparison to the two-dimensional load case definition and surpasses the results of a one-third model as well.

Table 8. Variation with standard deviations

Description of load case variant	Amplitude deviation to full rotor
All $M_{x,B}$ plus standard deviation from bin counting	7.19%
All $M_{x,B}$ minus standard deviation from bin counting	-6.74%
$M_{x,B,2}$ and $M_{x,B,3}$ plus standard deviation from bin counting	-0.57%
$M_{x,B,2}$ and $M_{x,B,3}$ minus standard deviation from bin counting	-0.26%

3.5 ~~Calculation of missing blade azimuth angle~~

~~As the blade's azimuth angle is the single most important signal for the bin counting and might be missing from the input data set, this section covers the use of a calculated $\Phi_{r,B}$ as described in Section A.~~
325 ~~For the entire data set of the IWT7.5-164 reference turbine, $\Phi_{r,B}$ was computed. Figure A1 visualizes exemplary results. The original values are shown as dashed red line and the calculated values as blue line. To provide a reference, the figure also~~

3.5 Selection of load cases

Table 9 lists the selected independent signals and the respective bins, resulting in a total of 16384 load cases. 27 out of the 256 combinations from the stacked data binning involving azimuth angle and flapwise bending moment yielded zero samples. These instances occurred exclusively at the edges of the bin ranges. As such, omitting these cases carries no adverse consequences, effectively reducing the overall required load cases to 14656.

Table 9. Preliminary load case selection for pitch bearing ring and hub fatigue simulations

Signal	Criteria	Bins	Remarks
$\Phi_{\text{r,B}}$	Allows definition of $M_{x,\text{B},2}$, $M_{x,\text{B},3}$ and all $F_{y,\text{B}}$ and $F_{z,\text{B}}$	16	Finer resolution does not improve deviations significantly
$M_{x,\text{B},1}$	Defines stress state for bearing locations close to y-axis	8	Sine characteristics of signal allow lower bin number than for $M_{\text{y,B},1}$
$M_{\text{y,B},1}$	Allows definition of all $M_{y,\text{B}}$ and $F_{x,\text{B}}$	16	Finer resolution does not improve deviations significantly
θ_1	Influences load distribution in the bearing	8	Taken from (Menck et al., 2020)

Further on, the selection of 8 distinct pitch angles is derived from previous work and has not yet been validated for the purpose of the structural fatigue calculations. Based on just one pitch angle for the simulation the load cases reduce to 1832. With the computational resources available for this work, this number is still too high for reasonable calculation times. Further reductions for the calculations of pitch bearing ring fatigue is possible if load cases in between extreme values of $M_{x,\text{B},1}$ and $M_{\text{y,B},1}$ are omitted and the results interpolated between the remaining values. This keeps the important simulation load cases that give stress amplitudes. Table 10 lists the resulting number of cases which result in a total of 384 simulations and are in the range of simulations done in Menck et al. (2020).

Table 10. Final load case selection for pitch bearing ring fatigue simulations

Signal	Criteria	Bins	Remarks
$\Phi_{\mathrm{r,B}}$	Allows definition of $M_{x,\mathrm{B},2}$, $M_{x,\mathrm{B},3}$ and all $F_{y,\mathrm{B}}$ and $F_{z,\mathrm{B}}$	8	Omit four bins at $0°$ and four bins at $180°$
$M_{x,\mathrm{B},1}$	Defines stress state for bearing locations close to y-axis	6	Omit two bins at center of value range
$M_{y,\mathrm{B},1}$	Allows definition of all $M_{y,\mathrm{B}}$ and $F_{x,\mathrm{B}}$	8	Omit eight bins in center of value range
θ_1		1	Do few additional simulation to evaluate worst influence

4 Discussion and conclusions

350 The present work covers the selection of load cases for finite element simulation of wind turbine rotors. Such simulations are used for the design of pitch bearings and hubs. Given the substantial complexity and size of the finite element models, conducting a large number of simulations within a reasonable timeframe becomes challenging. Detailed fatigue calculations, however, necessitate such a large number of simulations to establish the nonlinear relationships between external loads and internal stresses or contact pressures.

355 To address this challenge, the present study aims to uncover relations in between individual loads of the rotor blade roots and loads and rotational position of the hub center. This is accomplished through the use of stacked data binning and an evaluation of standard deviations of other signals within the equidistant bins. In addition to the blade root load signals used in approaches documented in the literature, this study incorporates the blade azimuth angle and the rotor out-of-plane moments for the evaluations. Novel methods for deriving these signals from the blade roots' loads are proposed. The algorithm introduced for 360 calculating the blade azimuth angle has undergone successful testing.

The inclusion of the blade's azimuth angle, denoted as $\Phi_{\mathrm{r,B}}$, renders promising outcomes by narrowing down the range of values of the edgewise bending moments. When combined with $M_{y,\mathrm{B},1}$ and $M_{x,\mathrm{B},1}$ this integration significantly reduces deviations across all load components in comparison to the original data set and was proven to result in similar stress cycle amplitudes as the simulation of a full rotor with load cases based on time series. The maximum deviation of stress amplitudes 365 in the case study was 0.57%. To result in a reasonable number of simulations, however, it was necessary to remove bins which result in stress values at the center of the value range. This made the approach more similar to the rainflow-count based one in Becker and Jorgensen (2023).

Introducing the out-of-plane rotor moment proves to be beneficial when combined with the blade azimuth angle and flapwise bending moment. However, it's important to note that this addition brings an extra dimension to the parameter space of the 370 simulation load cases, resulting in higher computational costs. Based on the findings of the data binning and exemplary finite element simulations, the blade azimuth angle and the bending moments of the primary blade bearing are chosen for the load case definition of full rotor simulations. The present work verified this approach for one exemplary turbine and the use case of pitch bearing ring fatigue.

Future works in this field could explore the use of bins with different lengths and/or mathematical functions to describe the
375 sine-like load components.

Data availability. The time series data from aero-elastic simulation are available from the authors upon request.

Appendix A: Calculation of missing time series signals

Some of the commercial data sets for this work did not have all of the signals described in the Section 2.2 on input data. Re-creating the data sets was not possible with reasonable means. Hence, some of the signals were calculated as functions
380 of other signals. This section covers the calculation methods and verifies the calcualtion of the blade's azimuth angle by the exemplary data set used in the case study.

A1 Calculation approaches

The following calculation approaches were used:

- Pitch angles of secondary blades

385   Although modern turbines can have individual pitch control and differing pitch angles between the blades, it is permissible to assume same pitch angles on all three blade roots. In comparison to the larger angle changes performed by the collective pitch to control the turbine's power, the smaller travels of the individual pitch have a negligible cross-influence between the individual blade roots.

- Out-of-plane rotor moments

390   The out-of-plane rotor moments $M_{y,H}$ and $M_{z,H}$ in a fixed frame of reference can be calculated from the individual flapwise blade root moments. This assumes $\Phi_{r,B}$ as per Figure 4.

$$M_{y,H} = M_{y,B,1} \cdot cos(\Phi_{r,B}) - cos(\Phi_{r,B} + \frac{2}{3}\pi)(M_{y,B,2} + M_{y,B,3}) \tag{A1}$$

$$M_{z,H} = M_{y,B,1} \cdot sin(\Phi_{r,B}) - sin(\Phi_{r,B} + \frac{2}{3}\pi)(M_{y,B,2} + M_{y,B,3}) \tag{A2}$$

- Blade azimuth angle

395   As the edgewise bending moments of the rotor blades are dominated by gravitational forces, the 1p component of $M_{x,B}$ links directly to the blade azimuth angle $\Phi_{r,B}$. An algorithm to obtain $\Phi_{r,B}$ can be outlined as follows for each time series file:

1. Define $0°$ position for $\Phi_{r,B}$, e.g. at local maximum of the first derivative of $M_{x,B}$

2. Apply low pass filter to $M_{x,B}$ to eliminate high frequency components

3. If necessary, calculate derivative of $M_{x,B}$

4. Identify local maxima or minima

5. Check for consistency, i.e. remove extreme values in unrealistic proximity to each other from the analysis

6. For each space between extreme values: calculate linearly increasing vector ranging from $0°$ to $360°$ or 0 to 2π for the time steps from one extreme value to the next

7. Paste the resulting vector at the corresponding positions into a new $\Phi_{r,B,calc}$ signal in the file

8. For a leading or trailing incomplete rotation of the rotor, use portions of the adjacent full vector

This algorithm reproduces speed changes between full rotor revolutions, but not within a revolution. It is essentially equivalent to taking the inverse sine of the 1p-component of the edgewise bending moment observed at one of the blade roots.

A2 Blade azimuth angle verification

For a verification of the $\Phi_{r,B}$ calculation, it was calculated for the entire data set of the IWT7.5-164 reference turbine. This data set contains the original signal, so it can be compared against the calculated. Figure A1 visualizes exemplary results. The original values are shown as dashed red line and the calculated values as blue line. To provide a reference, the figure also includes $M_{x,B,1}$. The zero position for the calculated azimuth angle was aligned to the local maxima of the derivative of the filtered $M_{x,B,1}$. A slight phase shift is observable, attributed to the fact that $M_{x,B,1}$ is not precisely zero at the upper dead point of the blade's circular motion. This load case at mean wind speed of $19\,\mathrm{m/s}$ showed a comparatively pronounced frequency content above 1p in $M_{x,B,1}$ and is displayed to show the robustness of the algorithm.

To assess the validity of the calculated azimuth angle signal $\Phi_{r,B,calc}$ for data binning, Table A1 reproduces some of the bin combinations of Table 6 with the calculated azimuth angle. The results in Table A1 exhibit only very minor differences when compared to those in Table 6.

Table A1. Combined bin count results with varying bins for $\Phi_{r,B,calc}$ and $M_{y,B,1}$

Bins $\Phi_{r,B}$	Bins $M_{y,B,1}$	STD $M_{x,B,1}$	STD $M_{x,B,2}$	STD $M_{x,B,3}$	STD $M_{y,B,2}$	STD $M_{y,B,3}$
16	16	0.021	0.023	0.023	0.054	0.054
16	8	0.021	0.023	0.023	0.060	0.060
16	4	0.022	0.024	0.024	0.067	0.067
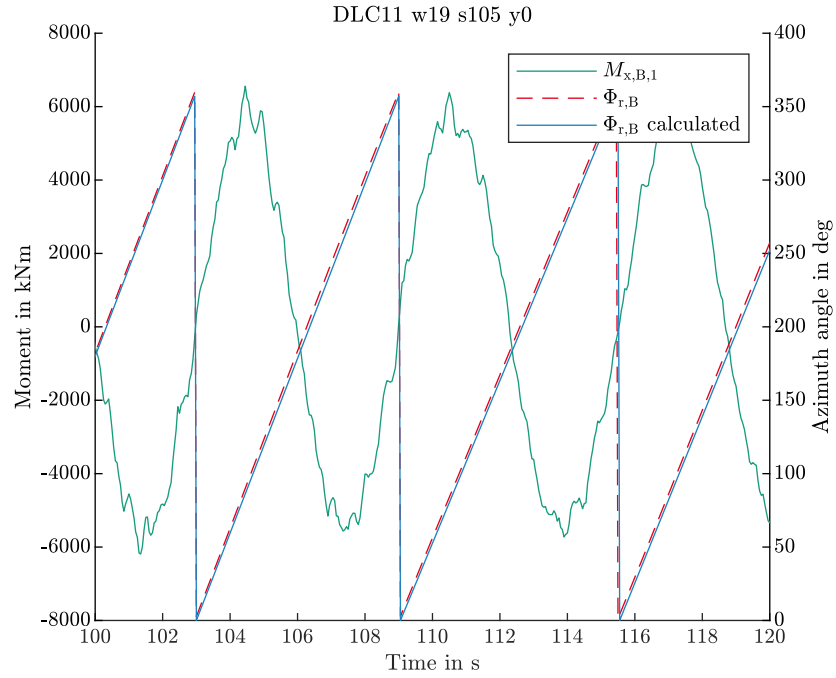
Figure A1. Exemplary comparison of original and calculated $\Phi_{r,B}$

Author contributions. MS: Idea, data analysis, bin counting, writing

    FS: Finite element simulations, writing, review

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