Revealing inflow and wake conditions of a 6MW floating turbine

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Abstract. We investigate the characteristics of the inflow and the wake of a 6MW floating wind turbine from the *Hywind Scotland* offshore wind farm, the world's first floating wind farm. We use two commercial nacelle-mounted lidars to measure the up- and downwind conditions, with a fixed and a scanning measuring geometry, respectively. In the analysis, the effect of the ~~surge and sway motion~~ pitch and roll angles of the nacelle on the lidar measuring location is taken into account. The upwind conditions are parameterized in terms of the mean horizontal wind vector at hub height, the shear and veer of the wind profile along the upper part of the rotor and the induction of the wind turbine rotor. The wake characteristics are studied in two narrow wind speed intervals between $8.5 - 9.5$ ms^{-1} and $12.5 — 13.5$ ms^{-1}, corresponding to below and above rotor rated speeds, respectively, and for turbulence intensity values between $3.3\% - 6.4\%$. The wake flow is measured along a horizontal plane by a wind lidar scanning in a ~~horizontal~~ plan position indicator mode, which reaches ten rotor diameters downwind. This study focuses on the downstream area between 3 and 8 rotor diameters. In this region, our observations show that the transverse profile of the wake can be adequately described by a self-similar wind speed deficit, that follows a Gaussian distribution. We find that even small variations ($\sim 1\% - 2\%$) of the ambient turbulence intensity can result in an up to 10% faster wake recovery. Furthermore, we do not observe any additional spread of the wake due to the motion of the floating wind turbine examined in this study.

1 Introduction

The increase of the global renewable energy capacity is largely based on the continuation of the current expansion rate of the wind energy sector and the reduction of the associated production costs (Wiser et al., 2021). To accomplish this increase, wind turbines and wind farms will continue to increase in size, with a growing focus on offshore wind energy production. Despite the operational challenges that wind turbines encounter in offshore conditions, several factors favor offshore deployment: the size of the available areas, the generally ~~good windresource~~strong wind, and the spatial homogeneity of wind conditions. ~~The latter and in connection with the current foundation and the operation and maintenance costs further justify the increasing size of the wind turbines (Jørgensen et al., 2021), that form offshore wind farms.~~

~~In general,~~ In order to optimize the energy production of both onshore and offshore wind farms and to ensure that they are operational during their expected lifetime, it is necessary to be able to ~~model realistically~~ realistically model intra- and inter-farm flows, e.g., the individual wakes, the blockage in front and speed up around the wind farms, and the wind farm wake.

In the case of intra-farm flows, the wind turbines are typically located in the far wake of adjacent wind turbines, where the characteristics of the flow are mainly related to the ambient wind conditions, which are usually described by the inflow speed, shear and veer profiles, turbulence intensity, atmospheric stability, and surface roughness. A thorough review of the current state-of-the-art physical description of those flows is presented in Porté-Agel et al. (2020), who highlights the importance of a realistic physical parameterization of the flow in the far-wake, to enable accurate prediction of the wind turbine production and the wind-induced loads. The impact of atmospheric conditions on wake properties is investigated in numerical studies (e.g. Wu and Porté-Agel, 2012; Rodrigues et al., 2015) and wind tunnel experiments (e.g. Chamorro and Porté-Agel, 2009, 2010). For example, the results of such studies have formed our current knowledge that an increase of turbulence intensity results in a faster wake recovery, and that stable atmospheric stratification favours the downwind propagation of the wake trace.

Due to the varying sea depth of the exclusive economic zone of coastal countries and the wind farm construction restrictions regarding the minimum distance from land, floating wind turbines will often be an attractive option for the development of offshore wind farms. In the case of floating wind turbines, the motion that results from the interaction of the floating structure with the wind and sea has to be considered, in addition to the atmospheric conditions. The wake characteristics of floating wind turbines have been studied using numerical (Wise and Bachynski, 2020; Kleine et al., 2021; Nanos et al., 2022; Chen et al., 2022; Li et al., 2022) and wind tunnel (Fu et al., 2019; Schliffke et al., 2020) experiments. Those studies focused on the impact of the sway (Fu et al., 2019; Nanos et al., 2022; Li et al., 2022), surge (Fu et al., 2019; Schliffke et al., 2020; Chen et al., 2022) and heave (Kleine et al., 2021) motions on the turbine operation. Yet, the absence of the study of the motion of floating turbine under realistic atmospheric turbulence conditions limits our understanding on how the impact of the motion of the wind turbine on the wake properties can be utilized in control strategies that optimize the operation of wind turbines and subsequently wind farms.

In this context the conduction of field campaigns is necessary for increasing our knowledge about the physics that govern the wake flow. In this respect, the development of remote sensing sensors based on the light detection and ranging (lidar) technique has extended the study of wake flows generated by full-scale wind turbines in the atmospheric boundary layer. This was achieved since their design enables the acquisition of wind observations with high spatial and temporal resolution while operating either ground-based (e.g. Iungo et al., 2013; Iungo and Porté-Agel, 2014; Archer et al., 2019; Menke et al., 2020) or nacelle-mounted (e.g. Bingöl et al., 2008; Aitken et al., 2014; Aitken and Lundquist, 2014; Carbajo Fuertes et al., 2018; Schneemann et al., 2021; Cañadillas et al., 2022; Brugger et al., 2022). Wind lidars are now used to detect the propagation of the wake trace (Archer et al., 2019) and, subsequently, measure both the mean (Iungo et al., 2013; Iungo and Porté-Agel, 2014; Menke et al., 2020) and the dynamic (Carbajo Fuertes et al., 2018) wake characteristics. Thus, they are used to evaluate the accuracy of different wake models (Trujillo et al., 2011; Trabucchi et al., 2017; Brugger et al., 2022). Furthermore, the capability of scanning wind lidars in acquiring long range measurements ($1 - 3$ km) enable the investigation of the far wake region while being installed on the ground and the nacelle of wind turbines (Archer et al., 2019; Carbajo Fuertes et al., 2018; Brugger et al., 2022).

In this study, we use two wind Doppler lidars installed on the nacelle of a floating wind turbine that is part of a small offshore wind farm with five wind turbines. Using two lidars enables the synchronous monitoring of the up- and ~~down-wind~~ downwind conditions. Thus it was feasible ~~first~~ to acquire observations of the characteristics of the wake and ~~subsequently~~ relate those to the inflow wind statistics. Similar studies using nacelle-mounted lidars have been performed on onshore wind turbines focusing on wake model validation (Carbajo Fuertes et al., 2018) or investigating the relationship between the wake meandering and the fluctuations of the transverse wind component (Bingöl et al., 2008; Trujillo et al., 2011; Brugger et al., 2022).

Here we present, to our knowledge, the first combined inflow and wake measurements of a floating offshore wind turbine using two nacelle-mounted wind lidars. In ~~Section~~Sect. 2, we describe the field campaign and the measuring configuration of the two wind lidars and the data post-processing steps. In ~~Section~~Sect. 3, we present the two models used to describe the acquired wind lidar measurements in the up- and down-wind directions based on the characteristics of the free and wake flow. Finally, we present our results in ~~Section~~Sect. 4 where the accuracy of both the up- and down-wind wind lidar is assessed, the properties of the mean free wind field are estimated and the wake flow characteristics are quantified for different inflow wind cases.

2 Field Study
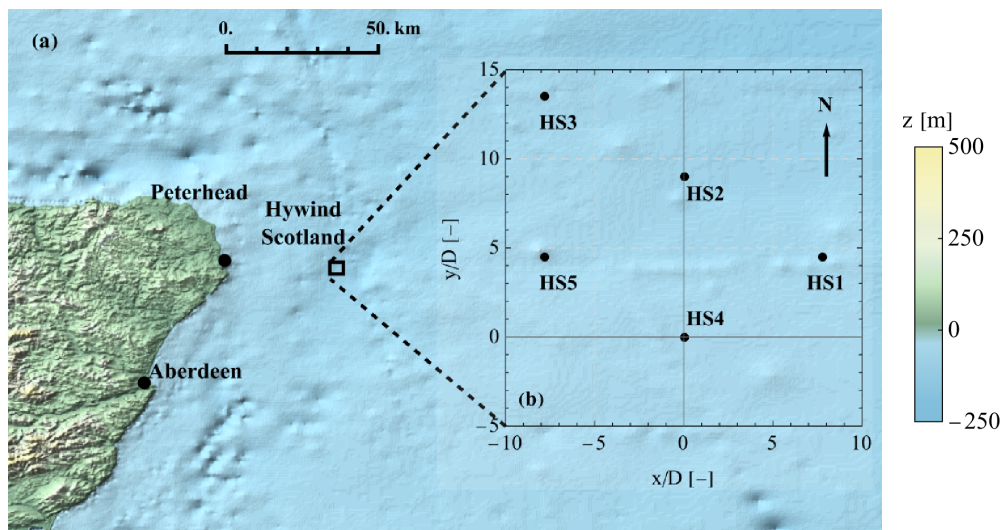
Figure 1. (a) Map of the eastern coast of Scotland where the offshore *Hywind Scotland* wind farm in located (black rectangle). (Inset, b) Drawing of the wind farm layout consisting of five wind turbines (denoted as HS1, HS2, HS3, HS4 and HS5) using a right-handed coordinate system ~~whose~~ where the y-axis is aligned to the North and the origin is placed at the location of the wind turbine (HS4).

Hywind Scotland is the world's first commercial floating offshore wind farm. It is located approximately 26 km from the east coast of Scotland (see Fig. 1(a)). In total, five Siemens Gamesa SWT-6.0-154 turbines with a hub height $H = 98.6$ m, a rotor

diameter D = 154 m and a rotor rated speed of ~10 ms^{-1} mounted on a ballast floating platform (Jacobsen and Godvik, 2021). The blade pitch is controlled as a conventional bottom fixed wind turbine during operation below rated wind speed. However, above the rated wind speed the blade pitch control system interacts with a floater motion control system. The closest distance between neighbouring wind turbines is approximately equal to 1387 m ($9D$). The wind turbines' (denoted as HS1, HS2, HS3, HS4, and HS5) locations form a "W"-shape layout, with a clockwise rotation of $30°$ in relation to the North, as shown in Fig. 1(b). The layout is presented in a right-handed coordinate system whose y-axis is aligned to the North and the origin is the location of the HS4 wind turbine. The HS4 wind turbine was instrumented with two nacelle-mounted wind lidars: a *Wind Iris* lidar by *Vaisala Oyj* (Finland) to measure the inflow and a *G4000 Galion* lidar by *SgurrEnergy* (Scotland) to measure the wake. The two wind lidars operated for a period of 3.5 months between June and September 2020. During this period, an additional *G4000 Galion* wind lidar was installed on the HS2 wind turbine to measure downwind relative of the turbine. Both HS2 and HS4 wind turbines were further instrumented with a motion reference unit (MRU) to monitor the motion of the nacelle. The MRU measured the rotation about the longitudinal and transverse axes in relation to the yaw direction of the turbine. The data acquired from the MRU were logged by the supervisory control and data acquisition (SCADA) system at 1 Hz. Figure 2 presents the pitch ϕ_y and roll ϕ_x angles averaged over a period of approximately 2 minutes as a function of the mean horizontal wind speed U. The 2-minute period was selected to study the response of the wind turbine over a period that was similar to the duration of the wake scan performed by the *G4000 Galion* wind lidar (see more in Sect. 2.1). The mean pitch corresponds to a rotation about the transverse axis relative to the yaw direction and the roll about the longitudinal axis.

We observe that both the pitch and roll angles depend on the wind speed. The pitch angle has an increasing trend with wind speed, reaching approximately $7°$ at 11 ms^{-1} (slightly higher than the rotor rated speed), followed by a decrease down to $3°$. Positive pitch angles indicate a counter-clockwise rotation of the rotor plane. The decrease to $3°$, that is observed when the wind is higher that the rotor rated speed, is attributed to a decrease in the thrust exerted on the wind turbine's rotor, due to the pitch of the wind turbine's blades. The roll angle shows a constant and slightly increasing trend with increasing wind speed, which on average varies between $0°$ and $1°$, balancing the torque of the rotor. Jacobsen and Godvik (2021) studied the dynamic response of the wind turbines at *Hywind Scotland* and found an increase in the standard deviation of both the pitch and roll angles with an increasing wind speed. However, up to mean wind speeds of 20 ms^{-1}, those variations are normally less than $1°$, indicating that the response of the floating platform is very stable.

2.1 Wind lidars

The two nacelle-mounted wind lidars used for this study were the *Wind Iris* and the *G4000 Galion* monitoring the upwind and downwind conditions, respectively, are both pulsed Doppler wind lidars. Doppler wind lidars measure the *radial speed* which corresponds to the projection of the wind vector on the line-of-sight of a laser beam. In the case of the *Wind Iris*, radial wind speed measurements are acquired over four fixed line-of-sights, which form the corners of a rectangle at any measuring distance. In our study, radial wind speeds were measured at a sampling rate of 0.25 Hz in 10 separate range gates corresponding to the upwind distances 50 m ($0.32D$), 80 m
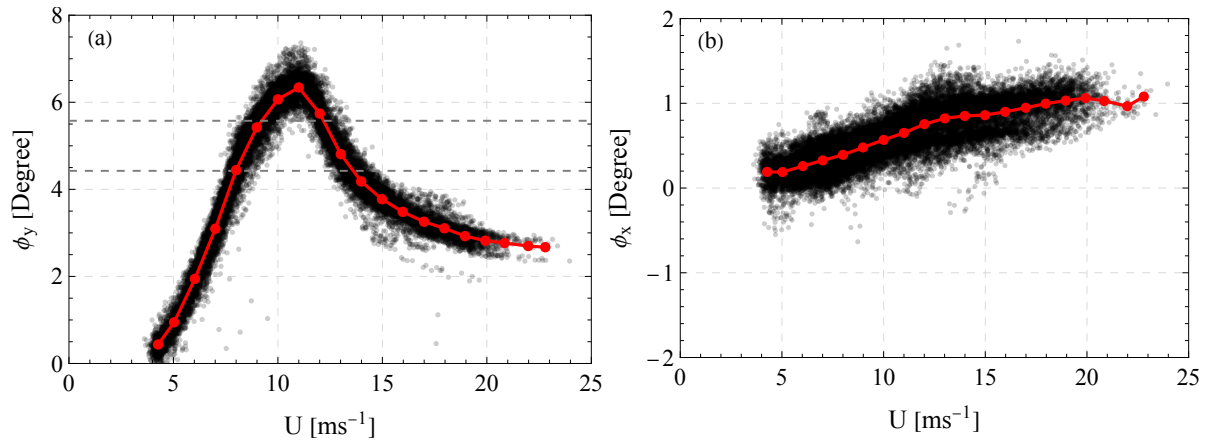
Figure 2. (a) Pitch ϕ_y and (b) roll ϕ_x values of the HS4 wind turbine for different wind inflow speeds U. The data presented in black correspond to the mean measurements of the MRU installed on the nacelle over a 2-minute period. The red line depicts the mean value of the pitch and roll angle per wind speed. The gray dashed lines in the pitch plot highlight the interval used in the analysis of this study (see more in ~~Section~~Sect. 4.3).

110 (0.52D), 120 m (0.78D), 160 m (1.04D), 200 m (1.30D), 240 m (1.56D), 280 m (1.82D), 320 m (2.08D), 360 m (2.34D), and 400 m (2.60D), when the *Wind Iris* was ~~horizontally leveled~~levelled. The first seven range gates were located within the ~~area covered by the rotor~~swept area of the wind turbine, while the last three were located outside the rotor plane with respect to the transverse direction (see Fig. 3, red ~~points~~dots). The four telescopes ~~defining the~~ that define the measuring geometry are enclosed in a single module installed 4.5 m above the rotor center, which is 103.4 m above sea level, and 4 m behind the rotor

115 plane. Furthermore, the telescope of the *Wind Iris* was tilted by 2.5° with respect to the horizontal plane to bring the center of ~~symmetry of~~ the measuring plane to the hub height at a distance of 2.5D, when the wind turbine was not operating.

The *G4000 Galion* mounted on the HS4 wind turbine is ~~also~~ a pulsed Doppler lidar where a scanner controls the direction of the beam. This lidar was configured to do a Position Indicator (PPI) scan. The PPI scan consisted of 41 line-of-sight measurements ~~spanned~~ spanning from −20° to 20° in the azimuthal direction and had a duration of approximately 2 minutes.

120 Each line-of-sight measurement consisted of 50 range gates that extended from 15 m to 1485 m (9.6D), which were sampled at 0.32 Hz. The 0.32 Hz was chosen in order to ensure high data availability along the measuring range. Furthermore, the PPI scan was performed with an elevation angle of 5°. This elevation angle was selected to compensate for the pitch angle of the wind turbine's nacelle so that the scan was horizontal when the mean wind speed was between either ~~8.0~~8.5 – 9.5 ms⁻¹ or ~~12.0~~ 12.5 – 13.5 ms⁻¹, see Fig. 2~~a~~(a). The pulsed scanning Doppler lidars have the advantage that they can acquire instantaneous

125 measurements along a beam with a fixed spatial resolution. However, the required pulse accumulation time for producing reliable estimates of the radial speed limits the scanning speed, especially when measurements at long ranges are required. For these reasons, the *~~G4000 Galion~~ ~~wind lidar completed a PPI scan in approximately~~* PPI scan duration of 2 minutes ~~, following~~ was chosen, following by 26 seconds of resetting the scanner head to its initial position. Thus, approximately 12 scanning

patterns were acquired per 30-minute period~~.~~, which was the time period used in the wake analysis (see more in Sect. 4.3.2).

130 The measurements were grouped in a Cartesian grid whose x-axis was aligned with the downwind direction parallel to the yaw direction of the wind turbine, with an origin at the center of the wind turbine's rotor. The grid consisted of three-dimensional cells with dimensions $D/5 \times D/5 \times D/5$. The size of the cells was determined by the length of the range gates (30 m) and resulted in having at least one measurement per grid cell per scanning pattern (see Fig. 3~~).~~

~~The *Galion* on the HS2 wind turbine scanned in two alternating modes, i.e., a PPI and a Range Height Indicator (RHI)scan.~~
135 ~~The PPI scan had the same characteristics as the one performed by the *Galion* lidar on HS4. The RHI scan consisted of 36~~
~~line-of-sight measurements with elevation angles that extended from $-15°$ to $20°$. In our study, the RHI measurements acquired~~
~~on the HS2 wind turbine were used only to investigate the average vertical motion of the wake (see Appendix A~~(a)).
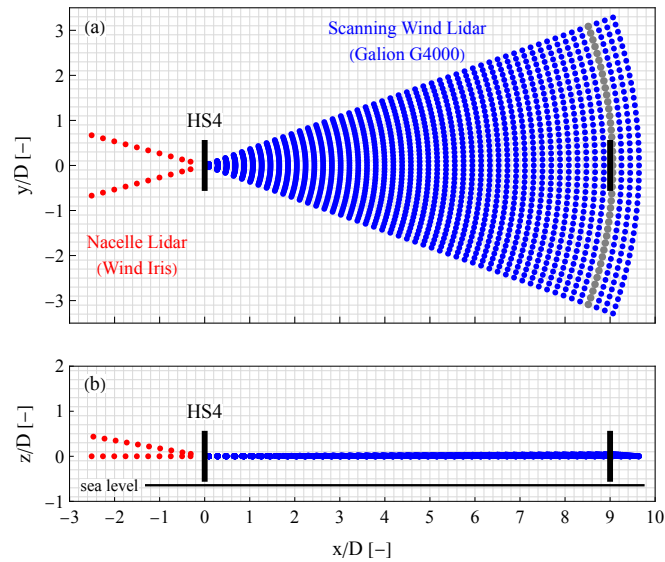
Figure 3. Top (a) and side (b) view of the measuring configuration used to monitor the up- and downwind flow relative to the HS4 wind turbine when the pitch of the rotor is equal to $5°$. The scanning pattern of the *Galion G4000* is presented with blue ~~points~~ dots and the measuring locations of the *Wind Iris* with red ~~points~~dots. The coordinate system is defined such that the x-axis is aligned with the downwind direction relative to the wind turbine, and its origin is located at the wind turbine's rotor. The figure also depicts the expected position of the rotor of the HS1, HS2, and HS5 wind turbines when the yaw of the HS4 was equal to either $120°$, $180°$ or $240°$ (black line at $9D$). The ~~orange~~ gray arc highlights those range gates where the rotor of the HS1, HS2 and HS5 wind turbines ~~are~~ is expected to be when the yaw direction of the HS4 is within the sectors $100° - 140°$, $160° - 200°$ and $220° - 260°$.

2.2 Post-processing of wind lidar data

Prior to the lidar data analysis, a quality check was performed in order to minimize biases that could originate from erro-
neous radial speed measurements. We present the post-processing of the two lidar data sets separately in the following two
subsections.

2.2.1 *Wind Iris* wind lidar

In the analysis of the *Wind Iris* measurements, only the data flagged with a valid radial wind speed estimation was used. This
data was selected based on the *Radial Wind Speed Status index* (*RWS Status index*), a parameter that is provided by the *Wind
Iris*~~for~~, which describes the quality of the radial wind speed estimation of each measurement (for more information we refer to
the *Wind Iris* user manual (Avent Lidar Technology, Version 2.1.1)). However, it was observed that on 84% of the 1-h periods
examined, on average 0.2% erroneous estimations of the radial wind speed still remained after the valid data selection. Due to
this, an additional filtering was applied, in which values outside the lower and upper outer statistical fences of the time series
were treated as outliers for each 1-h period. The fences were defined by the first (lower fence) or third (upper fence) quartiles
minus (lower fence) or plus (upper fence) 1.5 times the interquartile range of the distribution of the radial wind speeds per
period per range gate. The highest signal-to-noise ratio (SNR) values in all four line-of-sights were found approximately at 200
m, corresponding to the range where the *Wind Iris* has the highest sensitivity and thereafter it decreased linearly (in dB) with
distance. The corresponding data availability (defined here as the ratio between the selected and total acquired data) varied
between 90% and 70%, with a decreasing trend for increasing measuring distance. In addition, the two lower beams presented
a slightly lower availability compared to the two upper, which could be attributed to blade blockage.

2.2.2 *G4000 Galion* wind lidar

~~In the case of the *G4000 Galion*, the data~~ As described in Sect. 4.3, the *G400 Galion* wind lidar data was filtered for cases
where the PPI scans were leveled. The data filtering was based on the *intensity* values provided by the *Galion* software (Sgur-
rEnergy Ltd., 2017), according to which the lower threshold value of 1.01 is recommended as the lower acceptable threshold
for a valid measurement. This value corresponds to a SNR of -20 dB. Even though this is a conservative threshold, in re-
lation to the ones typically used in profiling ~~(Gryning and Floors, 2019) and scanning (Menke et al., 2020)~~ (e.g. - 29dB in
Gryning and Floors (2019)) and scanning (e.g. -24 dB in Menke et al. (2020)) wind lidars, an adequate data availability was
observed in the acquired data set. In addition, in order to exclude erroneous wind ~~estimation~~ estimations that were observed
mainly in the closest ~~range gate~~ and furthest range gates, an additional filter was constructed following the same method as the
one applied to the *Wind Iris* data to detect outliers.

3   Methods

The parameterization of the upwind and ~~wake~~ downwind conditions was performed using a right-handed coordinate system whose x-axis was anti-parallel to the axis normal to the rotor plane and thus aligned to the mean downwind direction in cases with no yaw misalignment. Furthermore, we denote the three-dimensional wind vector $\boldsymbol{U} = \{u, v, w\} = \{u_1, u_2, u_3\}$, where u_1 is the component aligned with the x-direction. Using Reynolds decomposition, we express each of the three components as the sum of a mean (denoted with an over-bar symbol) and a fluctuating (denoted with a prime symbol) component: $u_i = \overline{u_i} + u_i'$.

3.1   Upwind radial speed model

The parameterization of the inflow wind conditions was performed by assuming that:

– the two components of the horizontal mean wind speed $\{\overline{u}, \overline{v}\}$, at a given height, are horizontally homogeneous within each measuring distance

– the vertical wind component is negligible ($\overline{w} = 0 \ \mathrm{ms}^{-1}$)

– the wind shear $\dfrac{\partial \overline{u}}{\partial z}$ and veer $\dfrac{\partial \overline{v}}{\partial z}$ within the vertical range of the measuring area of the nacelle lidar are constant with height.

The first two aforementioned are justified by the horizontal homogeneity of the offshore mean wind field. The third assumes that in the vertical range between 68 m – 138 m (where the *Wind Iris* measurements are acquired) non-linearities in the wind profile are weak ~~in~~ at the measurement height (Peña et al., 2009). Based on the above assumptions, the mean wind vector $\boldsymbol{U}$ in any given location with coordinates (x, y, z) can be expressed only as a function of height z as:

$$\boldsymbol{U}(z) = (\overline{u}, \overline{v}, \overline{w}) = \left(\overline{u}_\infty + \frac{\partial \overline{u}}{\partial z} \cdot z, \overline{v}_\infty + \frac{\partial \overline{v}}{\partial z} \cdot z, 0 \right) \tag{1}$$

where $\overline{u}_\infty$ and $\overline{v}_\infty$ are the mean free horizontal velocities at the height of the *Wind Iris* (103.4 m) and $\dfrac{\partial \overline{u}}{\partial z}$ and $\dfrac{\partial \overline{v}}{\partial z}$ are the vertical gradients. ~~Further, the~~ The wind component u is not expected to be homogeneous along the streamwise direction due to the induction by the wind turbine. We express this blockage effect using the induction factor a that characterizes the reduction of the longitudinal wind speed along a line normal to the center of the rotor, based on the vortex sheet theory (Conway, 1995; Medici et al., 2011). This can adequately describe the wind speed evolution as it approaches a wind turbine rotor, as demonstrated in a field test by Simley et al. (2016) in the case of an onshore wind turbine, using the following formula:

$$\frac{\overline{u}}{\overline{u}_\infty} = 1 - a \left(1 + \frac{\zeta}{\sqrt{1 + \zeta^2}} \right), \tag{2}$$

where ~~a is the induction factor which depends on the wind turbine operation and~~ $\zeta = -x/R$ is the distance normalized by the rotor radius $R = 77$ m. Here, it is also assumed that the induction effect does not induce a spatial variability of the transverse

component of the wind and that the induction is independent of y and z for the positions of the range gates. These simplifying approximations are judged reasonable compared to the full expressions of Conway (1995).

Based on the above considerations the wind vector of Eq. 1 can be rewritten as:

$$\boldsymbol{U}(x,z) = \{(\overline{u}_\infty + \frac{\partial \overline{u}}{\partial z} \cdot z)f_{\text{ind}}(x), \overline{v}_\infty + \frac{\partial \overline{v}}{\partial z} \cdot z, 0\}, \tag{3}$$

where

$$f_{\text{ind}}(x) = 1 - a\left(1 + \frac{-(x-x_L)/R}{\sqrt{1 + (-(x-x_L)/R)^2}}\right) \tag{4}$$

describes the expected reduction of the longitudinal speed across the whole rotor area, and x_L is the distance between the rotor plane and the nacelle lidar (i.e. 4 m). Such parameterization formulations of the radial speed of a wind lidar have also been used in other studies of nacelle-mounted wind lidars (e.g. Borraccino et al., 2017).

The *Wind Iris* is acquiring radial wind speed v_r measurements in four different upwind directions, which correspond to the projection of the wind vector $\boldsymbol{U}$ onto the unit vector of each of the line-of-sights of the wind lidar:

$$v_r^{(i)} = -\boldsymbol{n}^{(i)} \cdot \boldsymbol{U}(x,z), \tag{5}$$

where $\boldsymbol{n}^{(i)} = \{n_1^{(i)}, n_2^{(i)}, n_3^{(i)}\}$ is the three-dimensional unit vector and the superscripts i = 1, 2, 3, ~~and~~ 4 denote the index of each beam. The unit vector $\boldsymbol{n}$, which is defined by both the azimuth ϕ and elevation θ angles of the line-of-sight, and by the pitch ϕ_y and roll ϕ_x angles of the wind turbine's nacelle, is equal to:

$$\boldsymbol{n}^{(i)} = R_y(\phi_y)R_x(\phi_x)\boldsymbol{n}'^{(i)}, \tag{6}$$

where $\boldsymbol{n}'^{(i)}$ is equal to:

$$\begin{pmatrix} \boldsymbol{n}'^{(1)} \\ \boldsymbol{n}'^{(2)} \\ \boldsymbol{n}'^{(3)} \\ \boldsymbol{n}'^{(4)} \end{pmatrix} = \frac{1}{1 + \tan^2\phi + \tan^2\theta} \begin{pmatrix} -1 & -\tan(\phi) & \tan(\theta) \\ -1 & \tan(\phi) & \tan(\theta) \\ -1 & -\tan(\phi) & -\tan(\theta) \\ -1 & \tan(\phi) & -\tan(\theta) \end{pmatrix}, \tag{7}$$

where $\phi = \pm 15°$ and $\theta = \pm 5°$ depending on the line-of-sight direction.

Equation 5 can be written as:

$$\begin{pmatrix} v_r^{(1)} \\ v_r^{(2)} \\ v_r^{(3)} \\ v_r^{(4)} \end{pmatrix} = -\boldsymbol{M}\begin{pmatrix} \overline{u}_\infty \\ \frac{\partial \overline{u}}{\partial z} \\ \overline{v}_\infty \\ \frac{\partial \overline{v}}{\partial z} \end{pmatrix} \quad \text{where} \quad \boldsymbol{M} = \begin{pmatrix} & & \vdots & & \\ n_1^{(i)} f_{\text{ind}}(n_1^{(i)}d_f) & n_1^{(i)}n_3^{(i)}d_f f_{\text{ind}}(n_1^{(i)}d_f) & n_2^{(i)} & n_2^{(i)}n_3^{(i)}d_f \\ & & \vdots & & \end{pmatrix} \tag{8}$$

is the matrix of the line-of-sight unit vectors and d_f is the distance from the instrument to the measurement volume. In the *Wind Iris* data, for each beam, an upwind distance x_f is reported, which is the nominal x distance from the instrument. Thus, d_f can be computed by multiplying x_f by the norm of the vector $\{1, \tan\phi, \tan\theta\}$.

The estimation of the upwind parameters $\overline{u}_\infty, \overline{v}_\infty, \frac{\partial \overline{u}}{\partial z}, \frac{\partial \overline{v}}{\partial z}$ and of the induction factor a was performed by solving Eq. 8. The solution was found using a non-linear model solver in *Mathematica* (Wolfram Research), based on the 10-minute mean values

220   of the radial speeds in all available range gates. The solver had as input the initial estimation of the wind conditions using only those radial wind speed measurements acquired in the furthest available range gate per 10-minute period. In this analysis, we have selected only the 10-minute periods with ~~an~~ a radial speed availability larger than 50%. The performance of the model, in estimating the upwind mean wind speed characteristics, is investigated through the calculation of the root-mean-square error (hereafter denoted as ε_u) between the modelled and measured radial wind speeds, for each 10-minute period.

225   ## 3.2   Wake radial speed model

The study of the wake characteristics was performed by expressing the radial wind speed as a function of both the upwind conditions (mean wind speed and direction) and the corresponding wind speed deficit that propagates downwind from the wind turbine, using the following expression:

$$v_r\left(x,y\right) = U\cos\left(\phi - \gamma\right)\left(1 - \frac{\beta\left(x\right)}{\sqrt{2\pi}\sigma\left(x\right)} \cdot \exp\left(-\frac{1}{2}\left(\frac{y - y_o\left(x\right)}{\sigma\left(x\right)}\right)^2\right)\right), \tag{9}$$

230   where v_r is the radial wind speed measurement acquired by the scanning wind lidar in different longitudinal x and transverse y distances in relation to the center of the rotor, $U = \sqrt{\overline{u}_\infty + \overline{v}_\infty}$ the mean free speed of the horizontal wind at the height of the wind lidar, ϕ the azimuth angle of the line-of-sight of the scanning wind lidar equal to $\arctan\frac{y}{x}$, γ the mean wind direction relative to the yaw of the wind turbine equal to $\arctan\frac{\overline{v}_\infty}{\overline{u}_\infty}$, $\sigma\left(x\right)$ a parameter representing the spread of the wake, $y_o\left(x\right)$ the center of the wake, defined by the location of the maximum wind speed deficit in the transverse direction at any downwind

235   distance, y the transverse coordinate relative to the center of the rotor and $\beta\left(x\right)$ a scaling parameter representing the wind speed deficit. ~~Using~~

We assume using Eq. 9 ~~, we assume~~ that the transverse profile of the flow in the wake can be described by a wind speed deficit with a Gaussian distribution. A similar wake model is presented in Aitken et al. (2014) and applied to nacelle-mounted wind lidar data in Aitken and Lundquist (2014). The parameterization of the radial speed measurements in the wake using

240   Eq. 9 does not only enable investigating the propagation of the wake center due to wake meandering, but also the impact of potential wind direction changes in the area scanned by the wind lidar~~,~~. This is possible since each of the two aforementioned parameters induce a different pattern in the distribution of the radial wind speeds along the transverse axis. Similar to the analysis of the upwind conditions, the solution of Eq. 9 was computed using a non-linear model solver in *Mathematica* (Wolfram Research), based on the 30-minute mean values of the radial speeds. The solver was applied in each streamwise distance, and

245   the measurements at $x/D = 6$ were chosen as an input of the initial estimation of the free wind and wake parameters~~, those measurements at $x/D = 6$ were chosen. The reason for selecting that distance is that we had a~~. This choice is supported by the sufficient number of measurements distributed in the transverse direction and a well-defined wake profile (an example is presented in Figure 9(c)).

4 Results

4.1 Free wind
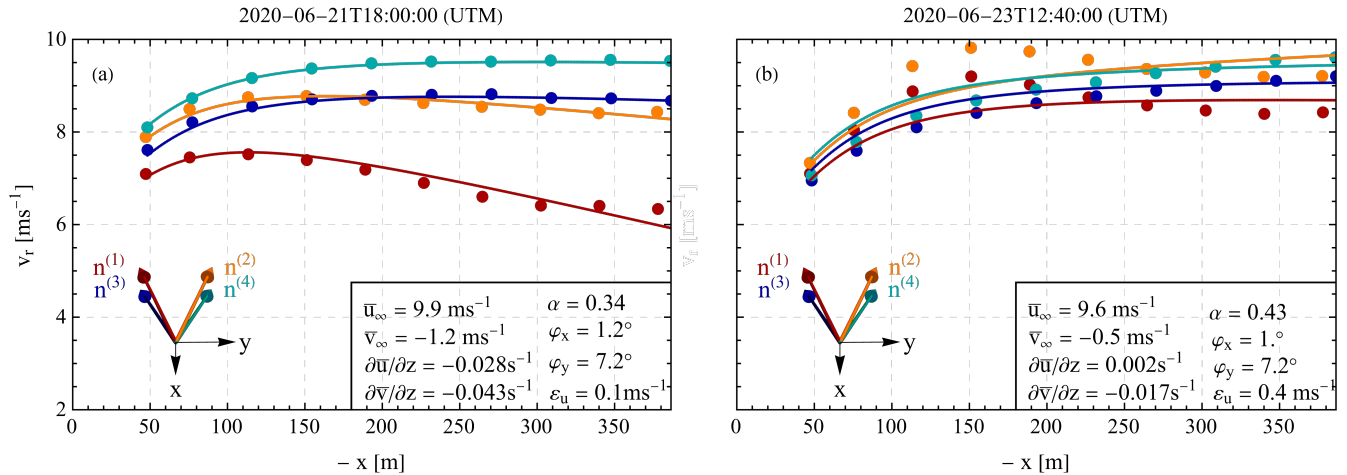
Figure 4. Example of two 10-minute periods where Eq. 5 describes either adequately (a) or poorly (b) the measured radial wind speed per upwind distance. The ~~points~~ dots correspond to the ~~10-minute~~ mean radial wind speed measured by the *Wind Iris*, and the solid lines represent the corresponding simulated radial wind speeds of each of the four line-of-sights for the upwind distances between 50 and 400 m, using the fitted parameters presented in the bottom right part of each plot. The negative x axis denotes upwind distances in accordance with the coordinate system shown in Fig. 3.

During the approximately 3.5 month period when the *Wind Iris* was operating, a total of 10529 10-minute periods of data were acquired~~in total~~, corresponding to a 70% system availability. Equation 8, which describes the ~~impact~~ measured radial wind speeds as a function of the mean upwind conditions~~on the measured radial wind speeds~~, was applied to 4502 10-minute periods~~, which~~. They were selected on the basis that, i. both *Wind Iris* and SCADA data was available (9348), ii. the wind turbine was operating (7900), iii. radial wind speed measurements were available in all ten ranges (7315), and iv. the yaw direction was between either 90° and 270° or 12.5° and 37.5° (4502) to avoid cases where the *Wind Iris* measured partially or fully in the wake of one of the adjacent wind turbines. We selected those wind directions based on both the wind farm layout (see Fig. 1(b)), but also by investigating the standard deviation of the line-of-sight measurements of the two lower beams of the upwind-staring lidar. In ~~that wind direction sector~~those wind direction sectors, we observed consistent values of the standard deviation of the radial speeds. This finding is typical in free wind conditions, as shown by Held and Mann (2019). ~~The model's performance in estimating the free wind mean wind speed is investigated through the calculation of the root-mean-square error (hereafter denoted as ε_u) between the modeled and radial wind speeds during every 10 minutes.~~

Figure 4 presents two samples of 10-minute mean radial wind speed measurements of each of the four line-of-sight beams (denoted in the figure as $n^{(1)}$ and $n^{(2)}$ for the two top beams and $n^{(3)}$, and $n^{(4)}$ for the two bottom beams and shown as arrows),

along with the simulated radial wind speeds using the estimated values of the upwind conditions and Eq. 8. The figure presents two cases where the applied model is found to describe ~~both accurately the wind conditions with relatively low values of ε_u~~ either accurately (Fig. 4(a)) ~~and inaccurately with relatively high values of ε_u~~ or inaccurately the wind conditions (Fig. 4(b)), determined by relatively low or high values of ε_u, respectively. In both plots, we observe that the radial speed values of all beams decrease as wind approaches the wind turbine rotor. This is attributed to the induction of the operating wind turbine. However, in Fig. 4(a), we see that the radial wind speeds of the two top beams are lower than those of the corresponding bottom beams and have a decreasing trend as the upwind distance increases. This pattern corresponds to a negative wind shear as it is predicted by the model in ~~the~~ this case, where $\frac{\partial \overline{u}}{\partial z}$ is found to be equal to -0.028 s^{-1}. The reason why the two right beams ($\boldsymbol{n}^{(2)}$ and $\boldsymbol{n}^{(4)}$) report higher values than the left ones ($\boldsymbol{n}^{(1)}$ and $\boldsymbol{n}^{(3)}$) is attributed to the negative value of the mean transverse component of the free wind $\overline{v}_\infty$. On the other hand, in Fig. 4(b), even though we see a similar trend in the two bottom beams with decreasing speed closer to the rotor, the two top beams present an increase in radial wind speeds with upwind distance up to 180 m, followed by a decrease. The derived wind characteristics in both cases could be attributed to a wind speed profile with an inversion. Such wind profiles are typically observed in either very stable atmospheric stability conditions with a low atmospheric boundary layer height or in the case of low-level jets. Low-level jets are not uncommon over offshore areas in Northern Europe. They are characterized by a non-linear wind shear (Emeis, 2014; Kalverla et al., 2019), ~~resulting in~~ whicn in our case results in a high root-mean-square error ε_u.

To further investigate the relationship between the fitted values of the wind shear and veer and the resulting root-mean-square error, we plot the fitted values of $\frac{\partial \overline{u}}{\partial z}$ and $\frac{\partial \overline{v}}{\partial z}$ as a function of the mean horizontal wind speed ~~and the corresponding value of ε_u~~ in Fig. 5. ~~Negative wind shear cases are usually have~~ Each dot corresponds to a 10-minute period and the color highlights the corresponding value of ε_u ~~higher than 0.2 ms^{-1}. When ε_u is lower than the value above, the~~ . We observe that on average the wind shear is usually within $0-0.02$ s^{-1}, which can be considered as ~~low~~ a low range of values, typical of offshore conditions. However, an increasing trend of the wind shear values is found when the mean free wind speed is higher than ~~15~~ 12 ms^{-1}~~.~~ ~~It is worth mentioning that among the estimated wind shear values with $\varepsilon_u < 0.02$ s^{-1},~~, as seen by the mean shear values (black dots) in Fig 5(a). Furthermore, when ε_u is usually higher than 0.2 ms^{-1} then negative wind shear cases are found. This is observed in the 31% ~~are negative~~ of the 10-minute periods examined. This shows that wind profile inversions are common at those heights (100 m – 150 m) and should be considered when studying the wind turbine operation. In the case of $\frac{\partial \overline{v}}{\partial z}$, we find generally negative values, ~~which~~ that on average range between $0 - -0.2$ s^{-1} Fig 5(b). These values are expected from the Ekman spiral in the Northern hemisphere. Similarly to the wind shear, high ε_u are related to strong negative values of $\frac{\partial \overline{v}}{\partial z}$.

For assessing the accuracy of the model of Eq. 8, we compare the 10-minute mean horizontal wind speed at the hub height with the corresponding values of the nacelle-mounted anemometer~~, recorded in the SCADA system (see Fig.~~. Figure 6~~)~~(a) presents a scatter plot between the estimated free wind at hub height based on the *Wind Iris* and the nacelle anemometer data. For this purpose we use only cases where $\varepsilon_u < 0.2$ ms^{-1}. We find an overall good agreement between the two data sets, with a bias of less than 0.1 ms^{-1} and a high Pearson correlation coefficient r>0.99. When studying the mean differences between the two data sets we find that the higher errors are observed between $7 - 9$ ms^{-1} and between $18 - 22$ ms^{-1}~~.~~, as it is presented in Fig. 6(b). This error could be attributed to a non-optimal transfer function used in the nacelle-mounted anemometer.
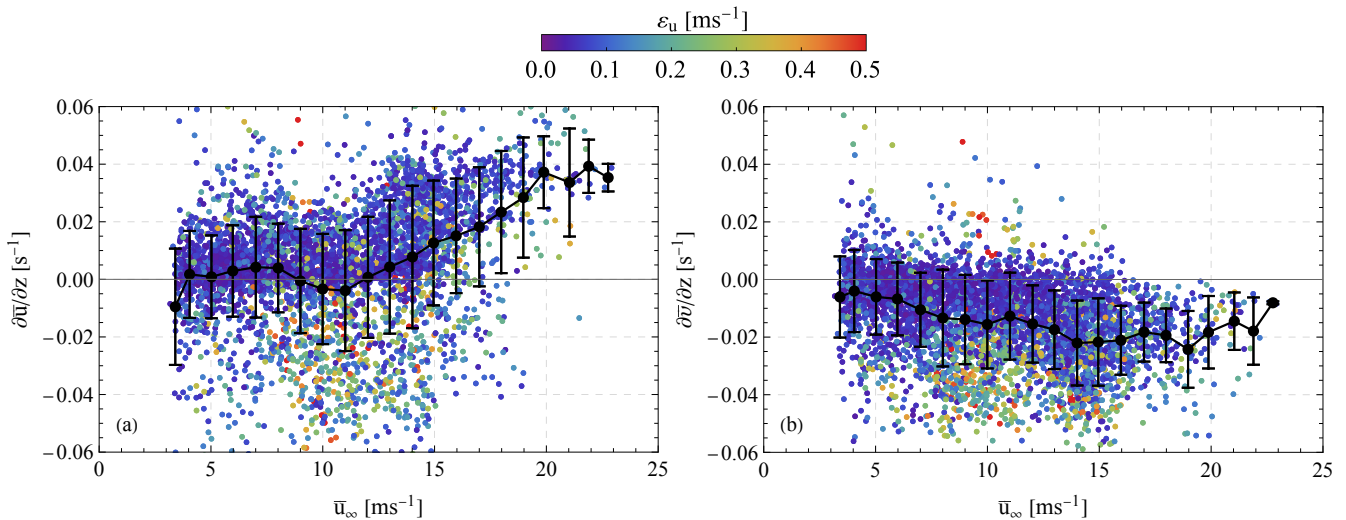
Figure 5. Scatter plot of the 10-minute mean wind sheer (a) and veer (b) versus the longitudinal component of the mean free wind speed. The color scale depicts the magnitude of the root-mean-square-error ε_u of the fit of the 10-minute mean radial wind speed measurements of the *Wind Iris* to Eq.8. The mean and standard deviation sheer and veer in different 1-ms^{-1} bins are presented with blacks dots and error bars, respectively.

300   Furthermore, the *Wind Iris* data was used to estimate the turbulence intensity (TI) of the ambient wind conditions. ~~For this purpose, the~~ The turbulence statistics are not expected to be biased by the wind turbine operation, as it was demonstrated by Mann et al. (2018), where they have showed the induction zone influences mainly the low-frequency fluctuations. Therefore, the measurements acquired closest to the rotor distance (i.e. ~~,~~ 50 m) were used ~~. This selection~~ for the estimation of TI. This choice was based on i. having the smallest spatial separation of the two measuring points that can introduce a bias in the

305   estimated second order statistics (i.e. ~~,~~ standard deviation of u), ii. the vertical displacement between the two line-of-sights due to the roll angle was on average small, since a 1° mean roll angle induced ~~an average~~ a mean vertical displacement of less than half a meter. ~~Moreover, the estimated statistics is not expected to be biased by the wind turbine operation, as it was demonstrated by Mann et al. (2018), where they have showed the induction zone influences mainly the low-frequency fluctuations.~~ Furthermore, at those range gates, we observe the maximum data availability. The estimation was performed by

310   using the 0.25 Hz time series of the radial wind speeds, by solving the equation $v_r^{(i)} = \{n_1^{(i)}, n_2^{(i)}\} \cdot \{u, v\}$. In the calculation of the standard deviation of u we don't take into account the contribution of the nacelle's motion to the radial speed. Thus, the estimated TI values are expected to be slightly biased, as it is presented in the work of Gräfe et al. (2022). However, considering the magnitude of the pitch of the wind turbine's nacelle, this error is expected to be less than 15%.
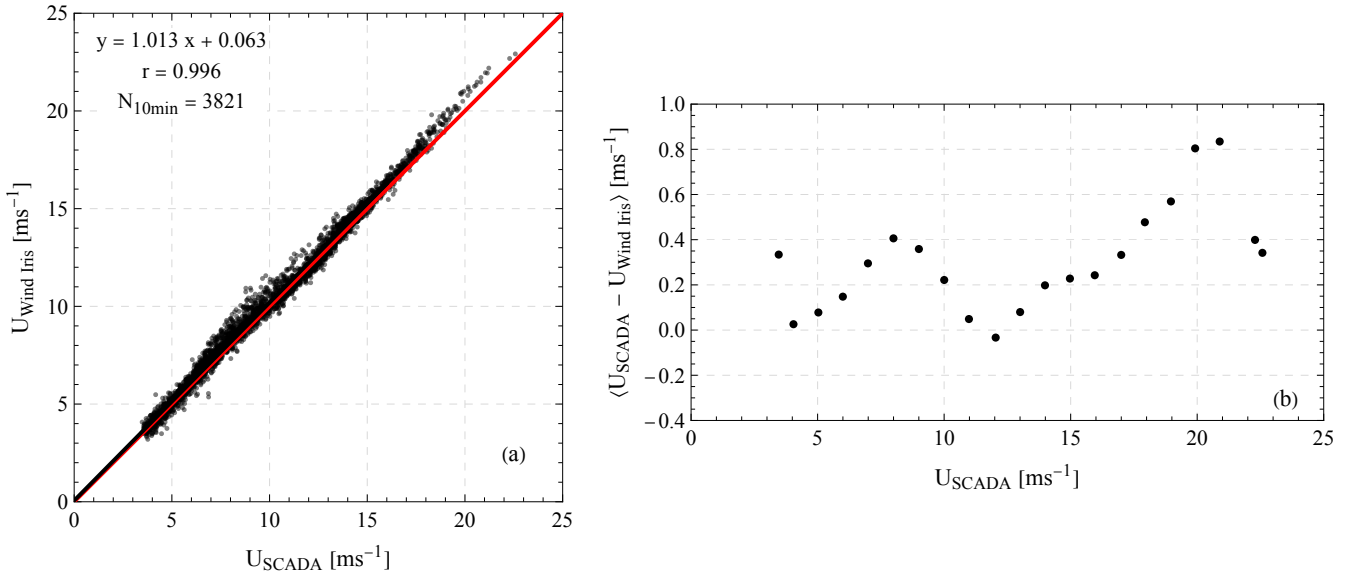
Figure 6. (a) Scatter plots of the estimated free wind speed $U_{\text{Wind Iris}}$ at hub height using the *Wind Iris* measurements and the corresponding 10-minute mean value U_{SCADA} as measured by the nacelle-mounted anemometer. (b) Bin averaged mean difference ~~$U_{\text{SCADA}} - U_{\text{Wind Iris}}$~~ $\langle U_{\text{SCADA}} - U_{\text{Wind Iris}} \rangle$ as a function of U_{SCADA}.

4.2 Induction zone

315   In Fig. 7, the induction factor a is presented as a function of the estimated free horizontal wind at the height of the *Wind Iris*. ~~The~~ Similarly to Fig. 5, the color of each ~~point~~ dots denotes the corresponding rmse ε_u ~~values~~ value of Eq. 8. An increase in the ε_u ~~values~~ results in a spread of the estimated induction factor values per wind speed. In general, we observe that the induction factor is on average equal to 0.37 ± 0.07 in the below rated wind speed range, between $4\ \text{ms}^{-1}$ and $10\ \text{ms}^{-1}$. These values are close to the theoretical Betz limit, assuming that the operation of a wind turbine can be simulated using an actuator disk model

320   (Hansen, 2015, Ch. 4). Above that wind speed range, the induction factor is decreased until it reaches 0.05 ± 0.02 when the wind speed ~~gets larger than~~ exceeds $18\ \text{ms}^{-1}$. Overall, we do not observe any correlation between the induction factor and the estimated wind speed shear or veer ~~, which would indicate that the wind turbine, for a given wind speed, responds differently when the shear or veer changes~~(plots not shown).

4.3 Wake

325   In addition to the selection criteria listed in ~~Section~~Sect. 4.1 for the characterization of the upwind flow, four additional criteria were ~~needed~~ included for the wake study. First, only *G4000 Galion* wind lidar data acquired during periods when the mean tilt angle of the wind turbine was within $4.425°$ and $5.575°$ were selected, to ensure that the ~~measurements of the PPI scan were~~ PPI scan was approximately horizontal. This tilt angle range results in a vertical displacement of the furthest range gate by $\pm D/10$,
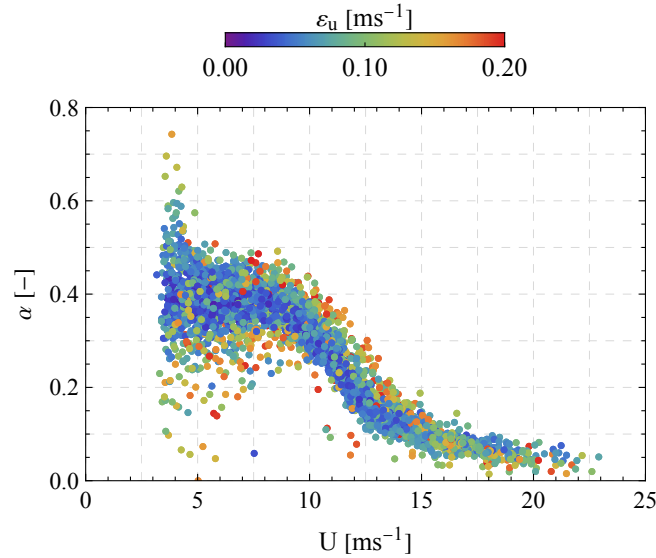
Figure 7. Estimated values of the induction factor a per 10-minute mean horizontal wind speed using Eq. 4. The colors denote the corresponding rmse ε_u values.

equivalent to half the dimension of one grid cell. Further, to avoid systematic biases introduced by spatial variations of the data availability, only those scans with a data availability of 75% or higher were selected. 5907 scanning pattern iterations remained after applying the two criteria above. Subsequently, to study the wake characteristics in relation to the upwind conditions, we first had to identify those 10-minute periods where: i. both SCADA and *Wind Iris* data were available (1719), ii. the wind turbine was operating (1719), iii. the inflow was free from wakes (1121), and iv. the measured radial wind speeds of the *Wind Iris* could be modelled using Eq. 8 with relatively low errors defined by ~~a~~ an empirical threshold of $\varepsilon_u < 0.2$ ms^{-1} (868).

In the wake analysis, and in addition to the parameters of the upwind conditions, we used the variations of the pitch angle to estimate the standard deviation of the velocity of the rotor and the frequency f_x of the periodic side-to-side motion to estimate the Stouhal number St for each of the selected cases as $\dfrac{f_x D}{u_\infty}$. We find that the standard deviation of the longitudinal velocity of the rotor is, on average, six times smaller than the standard deviation of the wind speed. Therefore, we can assume that in this field study, the impact of the longitudinal motion of the wind turbine's rotor on the wake conditions is negligible compared to the effect of the random variations of the longitudinal wind speed. Thus, we investigated the wake characteristics as a function of the mean wind speed and turbulence intensity values.

4.3.1 Single wake scan

Figure 8 presents four examples of ~~wake measurements~~ single wake scans acquired over different 2-minute periods. The examples correspond to cases with below, and above-rated mean wind speeds and two ~~turbulence intensity~~ TI levels equal to 2% and 4%. The different TI levels could be attributed to the atmospheric stability conditions and possibly to the sea state. We observe
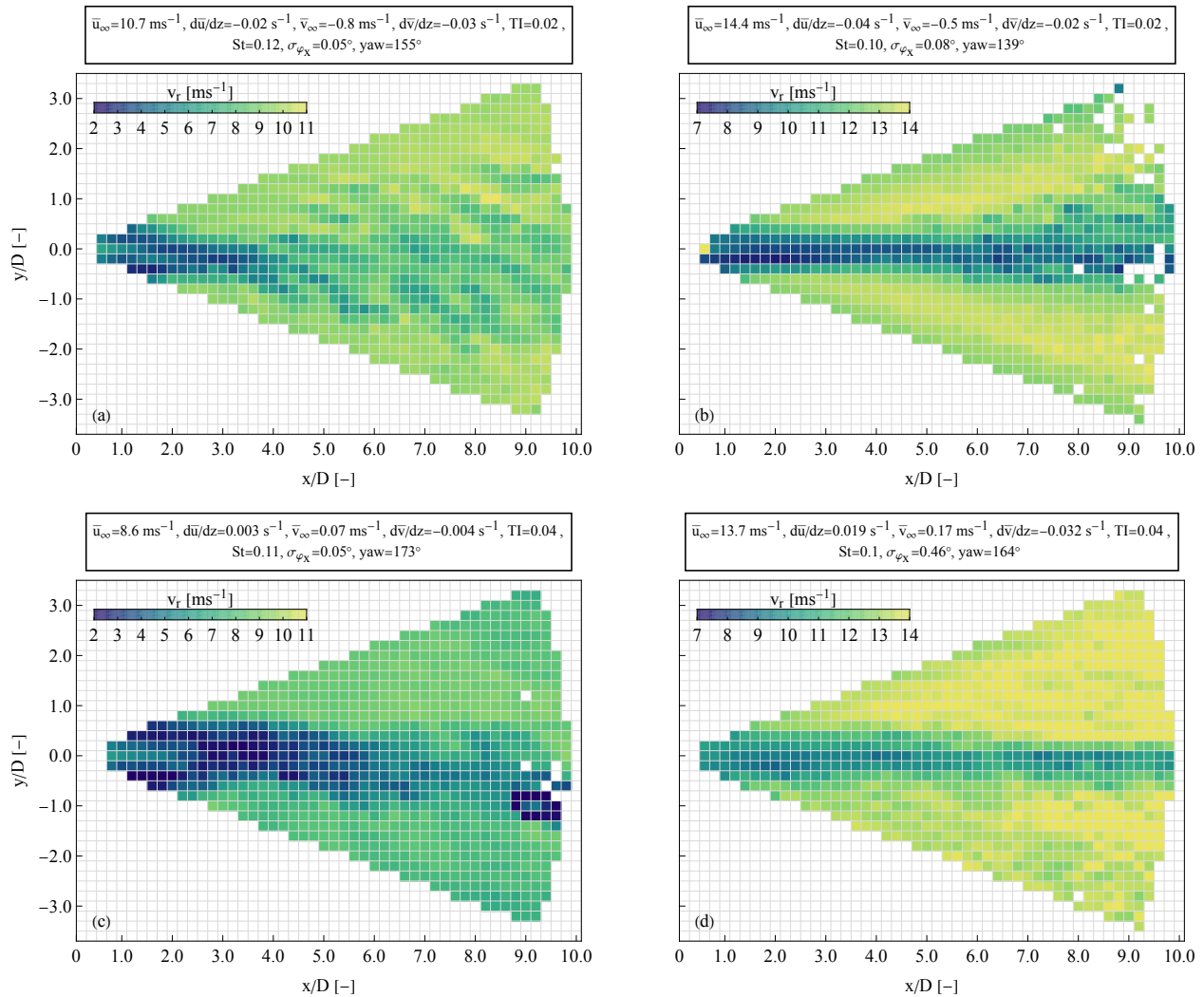
Figure 8. Four examples of radial wind speed measurements in the wake flow acquired during individual PPI scans over a 2-minute period. The examples correspond to cases with two different levels of turbulence intensity of $\sim \%2$ (top row) and $\sim \%4$ (bottom row), for mean wind speeds below (left column) and above (right column) rated speed. The boxes above each plot list the upwind conditions, as well as the Strouhal number (St) of the side-to-side motion, the standard deviation of the roll angle (σ_{ϕ_x}) and the yaw direction of the wind turbine.

that regardless of the turbulence intensity in the above-rated speed (Fig. 8(b) and (d)), the trace of the wake is visible down to 9D, without a clear wake expansion. In the case when TI is equal to 2% (Fig. 8(b)), we observe a very low standard deviation of the roll angle ($\sigma_{\phi_x} < 0.1°$). Jacobsen and Godvik (2021) studied the response of the wind turbines at *Hywind Scotland* and found that very low standard deviations of the roll angle were usually associated with stable atmospheric stratification. In Fig. 8(b), the wind shear appears to be negative, concordant with a very stable atmosphere, which could explain the propagation of the wake down to 9D. However, we observe that the wake deficit is still visible but less strong when both the TI and the wind shear increase, as seen in Fig. 8(d). This indicates that the different sign of the wind shear, doesn't have a significant impact on the wake propagation, at least for the ambient conditions of the cases examined here.

When the wind is below the rotor rated speed, the 2-minute scans showed less systematic characteristics. In the top left plot (Fig. 8(a)), we present a case with a negative shear and low standard deviation of the roll angle, indicating a stable atmospheric stratification. The wake deficit is visible down to 4D, while a reduced wind speed deficit in the range between 1D and 2D downstream of the nacelle is observed. However, after 4D, the wake is less evident. Instead, we observe wavy patterns in the distribution of the radial speeds that are spread in the longitudinal and transverse directions. This feature could be attributed to a combination of the flow characteristics (i.e. atmospheric stability and/or wind direction changes) and the relative slow scanning speed of the wind lidar. The PPI scan starts from the positive y-axis and rotates towards the negative, possibly explaining the direction of the "stripes" in the plot. This feature is not a necessary characteristic of all the below-rated wind speed cases, as shown on the bottom left plot (Fig. 8(c)), where the wake trace reaches 9D and meandering is visible. In Fig. 8(c) we can also see the effect of the induction zone of one of the adjacent wind turbines (i.e. HS2), when $x \sim 9D$ and $y \sim -1D$.

4.3.2 Mean wake scan

In order to perform a systematic study of the wake characteristics, the individual single scans that were acquired during periods that satisfied the criteria stated in Sect. 4.3, were gathered in 30-minute periods and averaged to produce 170 cases of a time-averaged wake in a fixed frame of reference. Furthermore, in the analysis, we chose only periods characterized by a quasi-stationary time series of the longitudinal wind speed, based on the assumption that the time series are quasi-stationary when their dependence on time has a slope of less $0.5 \, \mathrm{ms^{-1}h^{-1}}$. These periods were identified by applying a linear regression on the 0.25 Hz time series of the longitudinal component measurements from the upwind wind lidar, over different 1-h periods. Finally, we selected only those 30-minute periods that had at least 7 PPI scans, which resulted in 89 cases, in which the mean free wind speed was between 8.2 and 14.8 $\mathrm{ms^{-1}}$ and the TI varied between 1.4% and 8.1%. For those cases, we found that the fluctuations of the tilt angle of the wind turbine were either correlated or anti-correlated to the time series of the longitudinal wind speed depending on whether the mean wind speed was below or above rated speed (i.e., 10 $\mathrm{ms^{-1}}$), respectively. The mean peak-to-peak difference of the tilt angle, for the selected cases equals $1.8° \pm 1.1°$.

On the contrary, the roll angle of the nacelle was characterized by a stronger periodic sinusoidal motion with a varying

380 phase and a mean peak-to-peak difference equal to $0.9° \pm 0.6°$ (see also the power spectral densities presented in Fig. B1). This side-to-side motion corresponds to a mean lateral displacement of the rotor equal to approximately $98.5 \text{ m} \times \tan\dfrac{0.9}{2} =$ 0.7 m or less than $1\% D$. The small variations of both the pitch and the roll angle show that the wind turbine is relatively stable regardless of the wind conditions, in accordance with the findings reported by Jacobsen and Godvik (2021), where neither the mean wind speed nor the atmospheric stability had a significant impact on the wind turbine response.

385 ~~In our analysis, we used the variations of the pitch angle to estimate the standard deviation of the velocity of the rotor and the frequency f_x of the periodic side-to-side motion to estimate the Stouhal number St for each of the selected cases as $\dfrac{f_x D}{\overline{u}_\infty}$. We find that the standard deviation of the longitudinal velocity of the rotor is, on average, six times smaller than the standard deviation of the wind speed. Therefore, we can assume that in this field study, the impact of the longitudinal motion of the wind turbine's rotor on the wake conditions is negligible compared to the effect of the random variations of the wind speed.~~

390 ~~Furthermore, given the side-to-side motion's low amplitude, we studied the wake characteristics based on the mean wind speed and turbulence intensity values. In Fig. **??**, we present the number of cases with the same mean wind speed and turbulence intensity, using a 1-ms^{-1} and 2% range resolution, respectively.~~

~~Two dimensional array of the selected 30-minute periods as a function of the mean speed and turbulence intensity of the free wind.~~

395 In Fig. 9, we present the mean and the standard deviation, over a 30-minute period between $12:30 - 13:00$ on 01/09/2020, of the radial wind speeds in the downwind side of the wind turbine. By averaging all scans of the period, we minimize the effect of both random noise and biases due to the natural fluctuations of the wind speed and direction during a single scan (e.g. Fig 8(a)). Furthermore, we should expect that the time-averaged wake has a smaller deficit and wider distribution that an instantaneous snapshot of the wake flow. The measured plane covers the downwind propagation of the wake, where wind speed deficits can

400 be traced down to 1500 m (9.7 D). The wake is concentrated within an area with approximately the same width as the wind turbine rotor. ~~The standard deviation of the radial wind speed reveals two bands of high turbulence at the edges of the wake, which correspond to the areas where the wake mixes with the free flow.~~

An example of the application of the wake model of Eq. 9 is presented in ~~Fig~~ Figs. 9 ~~(e)~~ b) – (d) for three different downwind distances. Applying a Gaussian model to fit the wake deficit is not always suitable for describing the characteristics of the

405 flow. We assess the model's suitability by investigating the root-mean-square error ε_d values between the model described by Eq. 9 and the radial speed profile per downwind distance for each of the 89 cases selected for this study. In Fig. 10, we present the mean values of ε_d per downwind distance, based on all the selected cases. At close distances, ε_d takes values above 0.4 ms^{-1}, but decreases with distance. This trend is attributed to the fact that at short distances, the measurements are distributed over a limited transverse range of the PPI scan, and that the profile of the wake cannot typically be described by

410 a single Gaussian deficit (e.g. Aitken et al., 2014). We empirically define the acceptable threshold of valid application of the model as $\varepsilon_d < 0.25$ ms^{-1}. Using this criterion, we conclude that the adequate model area is within the range $2.7 < x/D < 8.3$. The increase in ε_d, at the range $8.3 < x/D$, is attributed to both the lower SNR of the measurements at those distances, which
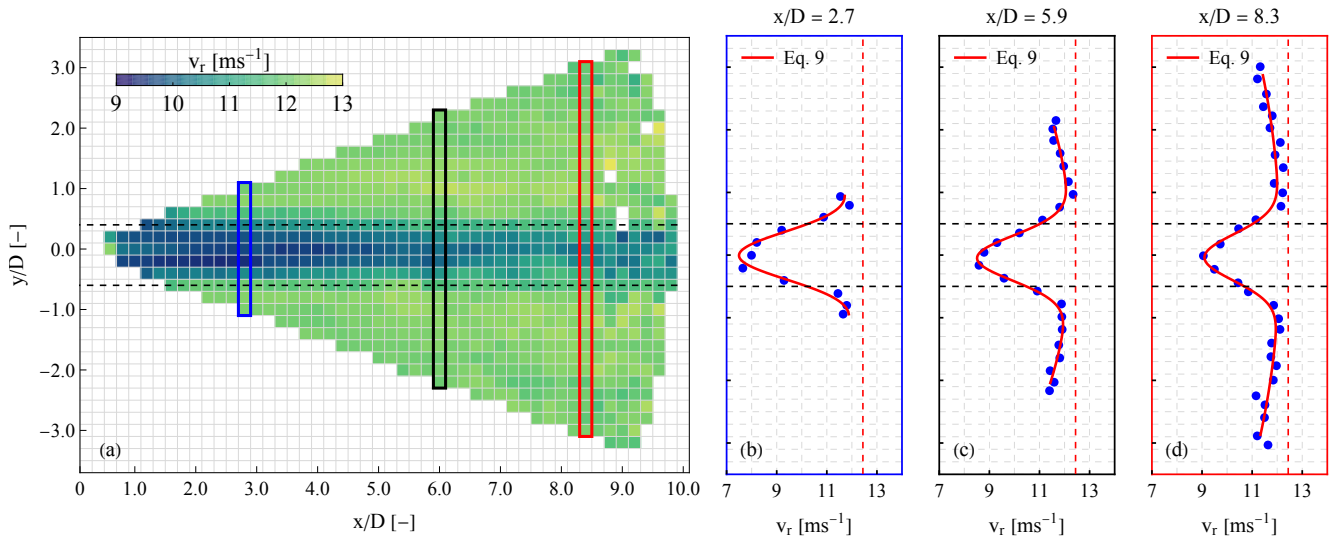
Figure 9. ~~Mean~~ (a) ~~and standard deviation (b) of the~~ Mean radial ~~speed~~ speeds of a 30-minute period over the scanned area ~~. An example and three examples~~ of the transverse profile of the mean ~~the~~ radial speed (~~e~~b) ~~and standard deviation~~ ~~(d) of the radial speed~~ at $x/D =$ ~~6.~~ 2.7, 5.9 and 8.3. The result of the application of Eq. 9 is presented in red in ~~the~~ plot (~~e~~b) ~~–~~ (d).

typically results in higher random errors in the measured radial speeds, and to the fact that occasionally the flow in those ranges was further distorted by the induction zone of the adjacent wind turbines.
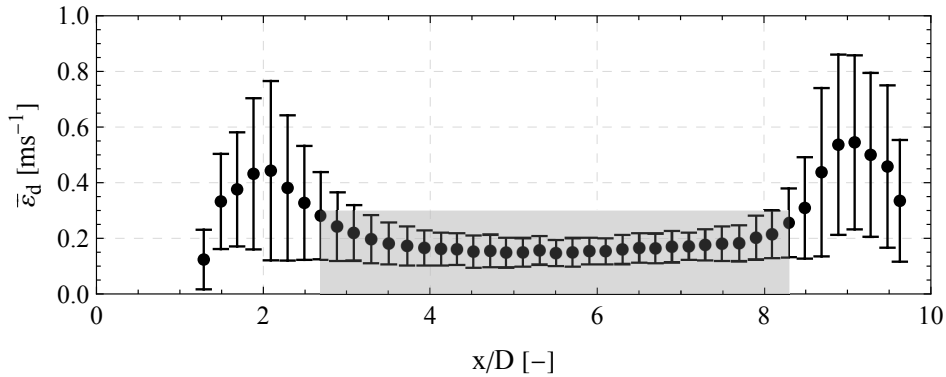
Figure 10. The mean (black dots) and standard deviation (error bars) of the root-mean-square error ε_d between the acquired radial wind speeds and the Gaussian wake deficit of Eq.9 for different downwind distances. The gray opaque rectangular area denotes the limits $2.7 < x/D < 8.3$ over which, on average, we observe acceptable ε_d values and thus denotes the range over which the velocity deficit in the wake ~~characteristics are resolved~~can be reasonably simulated by a Gaussian distribution.

To investigate the accuracy of Eq. 9, we assumed that the free wind speed is constant along the whole measured area where wakes are absent. Then, the ensemble average of the free wind speed $\langle \overline{U} \rangle$ is calculated based on the mean of the free horizontal wind values, U, estimated in each downwind distance between 2.7 and 8.3 rotor diameters. Subsequently, the estimations are compared to the ones derived using the *Wind Iris* data. ~~The regression analysiswas performed using a~~ Using a regression analysis, based on the least squares perpendicular distance method (Deming fit)~~. Except for a few outliers~~, we find that the down- and upstream estimations ~~have a reasonable correlation and a slight~~ of the horizontal wind speed, have a good correlation (i.e. $r=0.99$) and a small bias (~ -0.1 ms^{-1}~~, see Fig. ??(a)).~~). We also find ~~that the~~ a good agreement in the estimated ~~the~~ mean yaw misalignment ~~is equal to $0.1° \pm 1.8°$~~ γ. In specific based on the upwind staring nacelle lidar (i.e. *Wind Iris*) the mean γ over the 89 examined 30-minute periods is equal to $0.1° \pm 1.8°$, while from the downwind scanning lidar it is $-0.2° \pm 2.8°$ ~~(see Fig. ??(b)).~~

~~Scatter plot of the 30-min free wind speed (a) and histogram of the mean yaw misalignment (b) estimations from the Wind Iris (γ_u) and the Galion (γ_d) wind lidars. The black and red lines in (a) represent the results of the regression analysis (black) and the identity (red) line. The regression analysis results and the corresponding correlation coefficients are presented on the bottom right of the plot.~~

4.3.3 Self-Similarity in the far-wake

To investigate the similarity in the far-wake, we calculate the *self-similar velocity defect f* as a function of the *scaled cross-stream variable ξ*, which, according to Pope (2000, Ch. 5), are defined as:

$$f(\xi) = \frac{\overline{u}_\infty - \overline{u}(x,y)}{\overline{u}_\infty - \overline{u}(x,y_0)} \quad \text{and} \quad \xi = \frac{y}{y_{1/2}}, \tag{10}$$

where $y_{1/2} = \sqrt{2\ln 2}\,\sigma$ and σ correspond to the half-width of the half maximum of the wind speed deficit, and the standard deviation of the Gaussian distribution of the wind deficit, $\overline{u}_\infty$ is the mean free wind speed, $\overline{u}(x,y)$ the mean longitudinal wind speed, and y_0 the center of the wake. For estimating the $\overline{u}$ values in the wake, we first assume that the mean vertical speed component is zero. This assumption is based on both the offshore wind conditions~~and on the~~, as well as on that the flow in the *far-wake* region of the wake ~~, being~~ is mainly related to the ambient wind conditions (Vermeer et al., 2003). Thus, one should not expect any rotational motion in the wake flow after $x/D > 3$, as seen in Zhang et al. (2012), that would introduce a vertical component in the wind vector. Therefore a mean radial wind speed $\overline{v_r}$ measurement at a given point $\{x,y\}$ is equal to the projection of the ~~u and v~~ mean $\overline{u}$ and $\overline{v}$ components to the line-of-sight direction:

$$\overline{v_r}(x,y) = \overline{u}(x,y)\cos(\phi - \gamma) + \overline{v}(x,y)\sin(\phi - \gamma), \tag{11}$$

where γ and ϕ, similarly to Eq. 9 denote the yaw misalignment and the azimuth direction of a light-of-sight, respectively.

Since the ϕ angles are small $\{-20°, 20°\}$ and the mean absolute yaw misalignment, derived from the estimated values of $\overline{u}_\infty$ and $\overline{v}_\infty$ ~~,~~ of the 89 selected periods is equal to $\gamma = 1.5° \pm 1.1°$, we can neglect the term $\overline{v}\sin(\phi - \gamma)$ without introducing a bias. Thus, through Eq. 11 we can express the mean ~~u~~ $\overline{u}$ component as:

$$\overline{u}(x,y) = \frac{\overline{v_r}(x,y)}{\cos(\phi - \gamma)}. \tag{12}$$

ThusTherefore, the longitudinal wind speed at the center of the wake y_0, using EqEqs. 9 and 12, is equal to:

$$\overline{u}(x, y_0) = U \left(1 - \frac{\beta(x)}{\sqrt{2\pi}\sigma(x)} \right). \tag{13}$$

~~The results using Eq.12 and Eq.~~
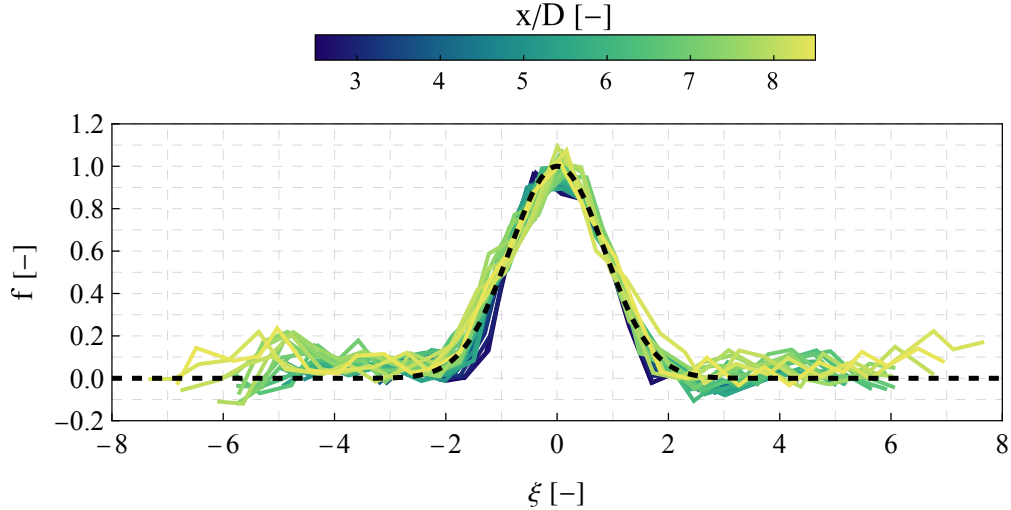
Figure 11. Mean profile over a 30-minute period of the self-similar velocity defect f as a function of the *scaled cross-stream variable ξ* for different downwind distance between ~~2.2 < x/D < 9.6~~ 2.7 < x/D < 8.3. The dashed line corresponds to the theoretical distribution $e^{-\ln 2\xi^2}$ ~~of an axisymmetric wake~~.

450   Subsequently, we apply the same analysis for all 89 30-minute selected periods. Between $3-10$ rotor diameters, we find relatively low rmse ε_f values (<0.25 ms^{-1}) between the estimated and modelled velocity deficit profile. This result supports the hypothesis that the profile of the velocity deficit is generally self-similar and, thus, independent of the downwind distance, regardless of the mean free wind speed and the corresponding turbulence intensity. The results here agree with the findings of Chamorro and Porté-Agel (2009), who, in a wind tunnel study, found that the vertical profile of the wind speed deficit in the

455   wake developed both over ~~a~~ smooth and rough ~~surface~~ surfaces is approximately symmetric.

     ~~Bar charts of the estimated root-mean-square error ε_f of applying a Gaussian function (Eq. 10) to the spanwise radial velocity measurements for different downwind distances between 1 and 10 rotor diameters.~~

4.4   ~~Case studies~~

4.3.1   Case studies

460   Before studying the wake characteristics for different ambient free wind conditions, we investigate the variability in the wake measurements between 30-minute periods with the same mean wind speed and TI values. In Fig. 12, we present 11 profiles of
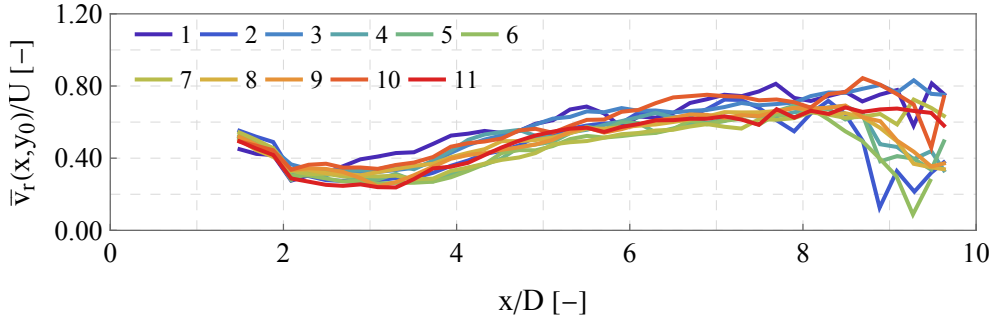
Figure 12. Wind profiles of the velocity in the wake center normalized by the mean wind speed $\overline{u}_{\infty,d}$ for 11 cases when the 30-minute mean wind speed was equal to 9 ms^{-1} and the corresponding TI was equal to 5%.

the mean longitudinal wind speed at the center of the wake when the 30-minute mean wind speed is equal to 9 ms^{-1} and TI equals to 5.0%. The wind speeds were normalized by dividing with the mean horizontal wind speed of each 30-minute period estimated using Eq. 9. The profiles are generally in agreement in the region $x/D < 8$. ~~Case~~ Profile #1, where a faster wake recovery (smaller velocity deficit as the downwind distance increases) is observed, is an exception, with no apparent correlation with the wind shear or veer values. Furthermore, in profiles #2, #5, #9, and #10, we see a decrease in the radial wind speeds when x/D is between 8.5 and 10. This decrease is attributed to the presence of the induction zone of neighbouring wind turbines. Therefore, we apply an additional filter by ~~remove~~ removing measurements beyond 8.3~~rotor diameters~~D, regardless the value of ε_d. Moreover, those 30-minutes periods with negative shear are also excluded from the analysis, in order to avoid cases with inversions in the upwind wind profile.

After applying the two additional filtering criteria, we examine two cases where the mean wind speed is either below (i.e. 9 ms^{-1}) or above (i.e. 13 ms^{-1}) rated speed. In those two mean wind speed values, we have the maximum number of cases ~~based on Fig. ??~~ and (17 and 23, respectively) and thus enables the estimation of the statistical variability of the derived mean parameters. The data from those cases are split and examined based on their TI values. The ~~overall~~ wind conditions of those cases and the corresponding upwind profiles are presented in Table 1 and Fig. 13, respectively. We observe that, on average, the wind shear and veer have similar values for all cases. An exception is case III, where ~~a~~ stronger shear and veer values are found. Overall, as seen in Fig. 13, we observe that the measured longitudinal and transverse wind components increase linearly with height, which supports our hypothesis of constant shear and veer in Eq. 1. In all cases, the absolute yaw misalignment is less than 2° and we find a Stouhal number (St) of the side-to-side motion between 0.1 and 0.2, besides the case V where ~~low~~ even lower values of St are observed. For each of the selected five cases we study the wake characteristics in terms of the downwind propagation of the wake center's position, the wake's spread, and the maximum velocity deficit.

Table 1. The number of 30-minute periods N_{30min} $N_{30\mathrm{min}}$ and the corresponding characteristics of the upwind profile (longitudinal speed $\overline{u}_\infty$, turbulence intensity TI, yaw misalignment γ, shear $\dfrac{\partial \overline{u}}{\partial z}$ and veer $\dfrac{\partial \overline{v}}{\partial z}$, σ_u) at the hub height, the wind turbine's induction zone (a), the standard deviation of the wind rotor speed ($\sigma_{v_\mathrm{rotor}}$) and the Stouhal number of the side-to-side motion (S_t) for each of the five cases examined.

Case	N_{30min} $N_{30\mathrm{min}}$ [#]	$\overline{u}_\infty$ [ms^{-1}]	TI [%]	γ [°]	$\dfrac{\partial \overline{u}}{\partial z}$ [s^{-1}]	$\dfrac{\partial \overline{v}}{\partial z}$ [s^{-1}]	a [-]	$\sigma_{v_\mathrm{rotor}}$ [ms^{-1}]	S_t [-]
I	5	9.0±0.3	3.4±0.5	-1.0±0.6	0.008±0.007	-0.009±0.003	0.38±0.01	0.05±0.01	0.09±0.07
II	12	8.8±0.2	5.0±0.7	-0.0±2.0	0.010±0.007	-0.009±0.008	0.38±0.04	0.07±0.02	0.19±0.17
III	7	13.1±0.2	3.3±0.4	0.8±1.3	0.023±0.010	-0.026±0.006	0.15±0.02	0.09±0.06	0.10±0.15
IV	11	12.9±0.3	4.7±0.5	1.4±0.7	0.013±0.011	-0.010±0.010	0.15±0.01	0.10±0.02	0.10±0.10
V	5	12.7±0.2	6.4±0.6	0.4±0.9	0.011±0.008	-0.011±0.006	0.15±0.02	0.11±0.04	0.02±0.01
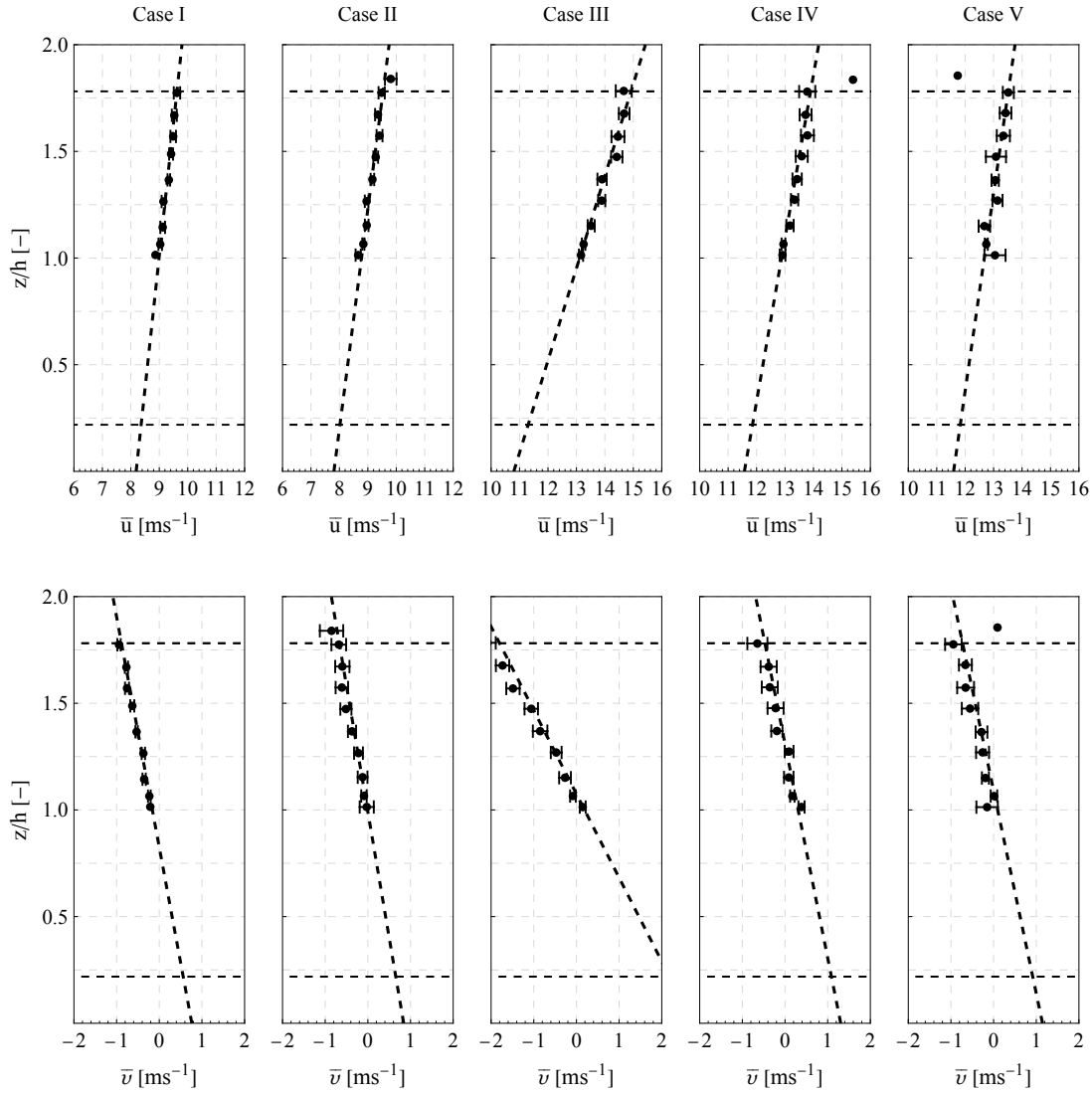
Figure 13. Vertical profiles of the mean longitudinal $\overline{u}$ (top row) and transverse $\overline{v}$ (bottom row) components of the wind vector for each of the five cases I – V examined. The measurement height is normalized by the hub height h, and the two horizontal dashed lines in each plot denote the lower and upper limits of the wind turbine's rotor. The error bars correspond to the standard error of each estimated mean value.

4.4 ~~Wake characteristics~~

~~For each of the selected five cases we study the wake characteristics in terms of the downwind propagation of the wake center's position, the wake's spread, and the maximum velocity deficit.~~

485 **4.3.1 Wake center**

The propagation of the wake center y_0, normalized by the rotor diameter D, for each of the five cases is presented in Fig. 14. The y_0 values are derived from fitting the radial speed model of Eq. 9 to the measurements of the scanning wind lidar in each downwind distance ranging from 2.6 to 8.3D. Subsequently, the mean and the standard error $\sigma_{y_0}/N_{30\mathrm{min}}$ of the y_0 values for each of the cases examined, were calculated. In cases I and II ~~,~~ (Fig. 14(a)), we observe that the wake center is translated

490 towards the negative y-axis with an increasing trend with the downwind distance down to approximately 7D. The observed translation of the wake center could be partially attributed to the estimated yaw misalignment ~~angles~~ angle γ values presented in Table 1. ~~A~~ According to those values the maximum yaw misalignment of ~~2~~ the examined cases was equal to -2°, which could result in a transverse displacement by ~~0.3~~ 0.3D at 8D. On the contrary, in cases III – V, even though the estimated yaw misalignment angles are of the same magnitude, the mean wake center, presented in Fig. 14(b), shows hardly any translation.

495 Specifically, it is within 0.05 D and $-0.10D$ from the center of the rotor within the downwind range $3 - 8D$, with, however, larger standard error ~~$\sigma_{y_0}/N_{30\mathrm{min}}$~~ values (denoted as error bars in ~~the figure~~ Fig. 14). We could not find any correlation between these trends and any other free wind condition characteristics. In all cases, the standard error of the wake center increases with the downwind distance, which could be attributed to the meandering of the wake.

4.3.2 Wake width

500 ### 4.4 ~~Wake width~~

Similarly to Aitken et al. (2014), we define the wake width equal to 4σ, i.e., the spanwise range where the 95% wind speed deficit is concentrated. The values are normalized by the rotor diameter D and presented in Fig. 15. In all cases, we observe an increase in the wake width with downwind distance. Below rated (Cases I & II ~~,~~ in Fig. 15(a)), already at a downwind distance of ~~three rotor diameters~~ 3D, the wake width is approximately equal to 1.5 – 2.0D and increases up to 2 times at ~~eight rotor~~

505 ~~diameters.~~ 8D. This wake expansion is similar to the one reported in the case of field studies of onshore wind turbine wakes by Aitken and Lundquist (2014); Bodini et al. (2017). Furthermore, as the ambient TI increases from 3.4 to 5.0% the wake width also increases. ~~Above rated (Cases III – V)~~ In the above rated cases in Fig. 15(b), we find a slowly growing width as a function of downwind distance, with values ranging between 1.3D and 2.0D. In these cases (III - V) the observed expansion takes place after $5 - 6D$. The relatively constant values indicate a slow wake recovery in the TI range $3.3\% - 6.4\%$.
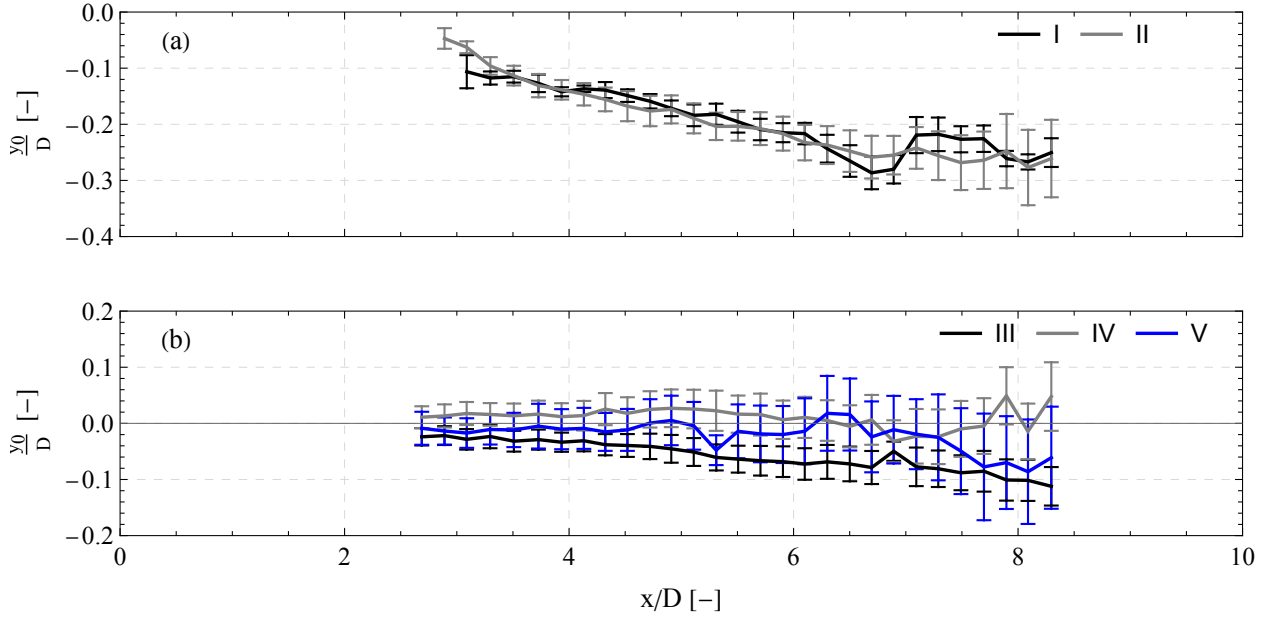
Figure 14. Mean wake center along the downwind distance between 2.7 and 8.3 rotor diameters in a fixed frame of reference, when the mean wind speed is equal to (a) 9 ms^{-1} (below rated speed) and (b) 13 ms^{-1} for different TI levels that range from 3.4 % to 6.3 % (see Table 1). The error bars correspond to the standard error of each mean value.

4.3.1 Velocity deficit

4.4 ~~Velocity deficit~~

The velocity deficit in the center of the wake can be expressed as the relative difference between the mean longitudinal wind component in the center of the wake along the spanwise axis $\overline{u}(x, y_0)$, and the free wind speed $\overline{u}_\infty$. Thus, using Eq. 13 and by assuming that $U \approx \overline{u}_\infty$, the velocity deficit in the wake center is equal to:

$$\frac{\overline{u}_\infty - \overline{u}(x, y_o)}{\overline{u}_\infty} = \frac{\beta(x)}{\sqrt{2\pi}\sigma(x)}, \tag{14}$$

where the $\beta(x)$ and $\sigma(x)$ correspond to the fitted values in Eq. 9. In Fig. 16, we present the percentage of the velocity deficit for different downwind distances extending from 2.7 to 8.3D, when the mean free wind speed is 9 ms^{-1} (Cases I — II) and 13 ms^{-1} (Cases III – V), respectively. Below rated, in Fig. 16(a), we observe a maximum velocity deficit around $69\% - 78\%$ at $3D$ that decreases to $38\% - 41\%$ at $8D$. The estimated percentages of the velocity deficit have relatively low standard errors that depending on the downwind distance range between $0.7 - 3.1$~~. In the below rated wind speed case~~%. Furthermore, we observe that a 1.6% increase in TI results in a velocity deficit decrease of $7.5\% \pm 3.0\%$ in the range between 3 and 8~~rotor diameters~~D, which is independent ~~from~~ of the downwind distance. The observed high velocity deficit values at $x = 3D$ agree with the high induction factors presented in Fig. 7. By taking into account the induction factor value and Eq. 2, we should
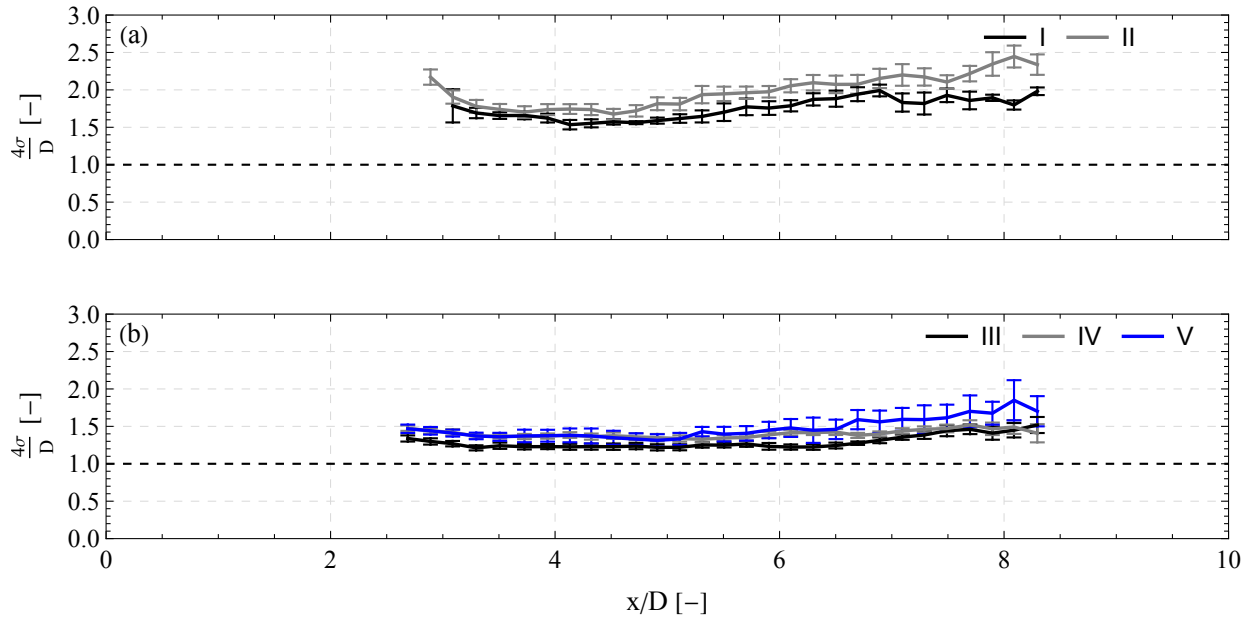
Figure 15. Mean wake width along the downwind distance between 2.7 and 8 rotor diameters in a fixed frame of reference when the mean wind speed is equal to (a) 9 ms^{-1} (below rated speed) and (b) 13 ms^{-1} for different TI levels. The error bars correspond to the standard error of each mean value.

expect a maximum relative velocity deficit~~equal to 2a×100%~~, equal to twice the induction factor $2a \times 100\%$= 76% (which is
presented by a dashed black line in Fig.16(a)). We ~~observe that~~ therefore find, that especially in case I the velocity deficit at $3D$ is approaching the theoretical maximum relative velocity deficit. However, in the case above rated, in Fig. 16(b), we ~~observe~~ find that the velocity deficit spans from around 37% – 38% at 3~~rotor diameters~~ D and decreases with increasing distance down to 27% – 29% at 8.3 rotor diameters. ~~The~~ Thus, the observed velocity deficit at $3D$ is almost ~~10~~8% higher than the theoretical based on the estimated induction factor (a=0.15). Furthermore, an increase of the TI from 3.3% to 4.7% and from 4.7% to 6.4% results ~~to~~ in a decrease of the velocity deficit of $5.7\% \pm 3.4\%$ and $9.9\% \pm 3.8\%$, respectively. This decrease ~~is~~ becomes larger as the downwind distance increases. Overall, the observed decrease in wind speed deficit is a lot slower than the cases I and II. Specifically, we find that wind deficit scales with the downwind distance x on the power of -0.4, -0.5, and -0.6 for cases III – V, respectively. The slow flow recovery in the cases III – V is consistent with the slow expansion of the wake width that is observed in Fig. 12. These values are lower than in cases I and II where we find that the wind deficit scales with the downwind distance on the power of -0.9~~and -0.9 is found~~, which is in close agreement with the findings of Barthelmie et al. (2004). ~~In all cases, III, IV, and V, the wind speed deficit between 2.3D and 3.5D is higher than the expected magnitude based on the corresponding estimated induction factor values.~~
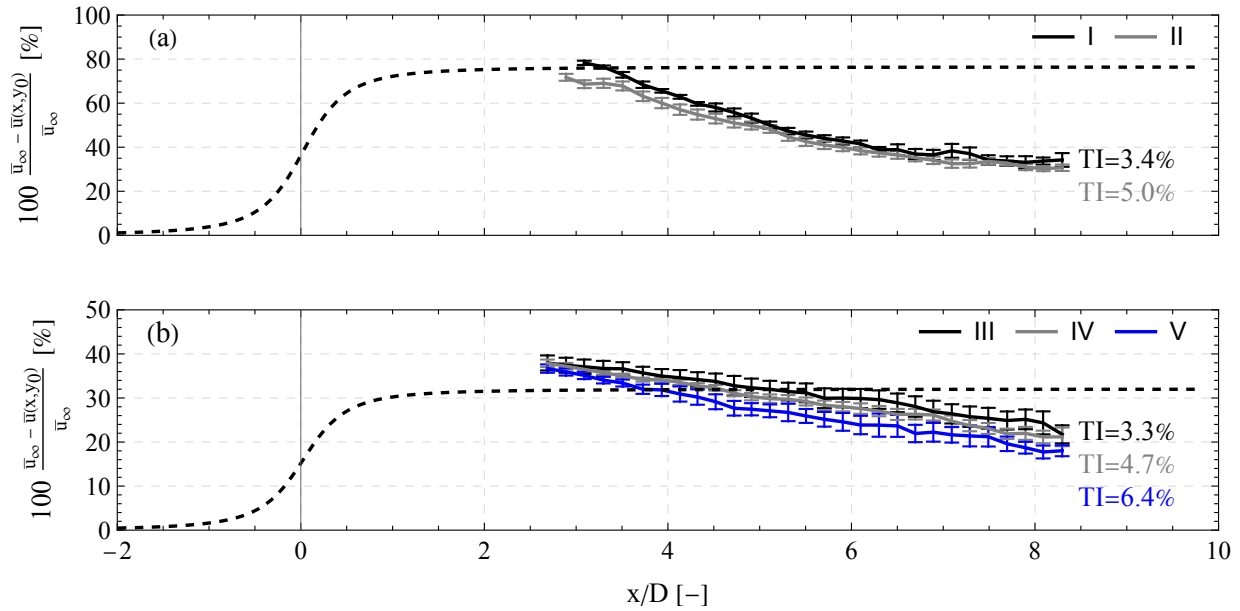
Figure 16. Mean velocity deficit at the wake canter along the downwind distance between 2.7 and ~~8~~ 8.3 rotor diameters, when the mean wind speed is equal either to 9 ms^{-1} (a) or 13 ms^{-1} (b) below rated speed) and for different TI level. The gray dashed line in each plot represents the predicted longitudinal speed using Eq. 2 and the induction factor values of a=0.38 (a) and a=0.15 (b).

5 Discussion

To investigate the impact of the ambient atmospheric wind conditions on the wake flow generated by floating wind turbines,
540 we assumed that: i. the wind shear and veer are constant ~~throughout~~ across the wind turbine rotor area, ii. the wake flow, on overage, propagates horizontally, iii. rather than the atmospheric stability, turbulence plays the dominant role in the wake recovery and iv. estimations of turbulence intensity can be derived by combining radial speed measurements acquired at a 50 m upwind distance and a spanwise separation of 26.8 m (0.17D).

Regarding the first assumption, a constant and height-independent wind sheer and veer was used to parameterize the upwind
545 conditions and simulate the radial wind speed measurements of the *Wind Iris* lidar. In 74% of the cases, we have found a good agreement between the *Wind Iris* measurements and the upwind model of ~~Equation~~ Eq. 3. Cases with a non-constant wind sheer and veer can be attributed to low atmospheric boundary layer height or low-level jets. In either case, measurements at higher and lower heights would provide insight into a more comprehensive description of the vertical profile and are recommended in future studies.

550 Furthermore, since we used only PPI scans in this analysis, it was not possible to study if vertical motions of the wake occurred, which could introduce a bias in the observed velocity deficits. For this reason, we had to hypothesize that the mean wake propagation takes place horizontally. Observations that support this hypothesis have been acquired by the *Galion* wind

lidar on HS2 that was measuring in a RHI scanning mode (see more in Appendix A). The measurements of that lidar could not be analyzed in depth since, due to the layout of the wind farm (see Fig. 1), ~~and~~ since for the wind direction sector examined in this study (southern winds), the inflow of HS2 included wake flows from adjacent wind turbines. However, when we ~~investigate~~ investigated the measurements from that lidar for Northern wind directions and for the same wind speed ranges (see Fig. A1), we observed that on average we could not detect a significant vertical motion of the center of the wake (see Fig. A2). Overall, assessing the wind characteristics with a scanning lidar is challenging, but also offers a lot of possibilities. The acquired data sets point to the direction that wind lidars are technologically mature to be used in ~~commercial applications in offshore conditions~~monitoring the flow around offshore floating wind turbines. As a future best practice, we recommend a combination of PPI and RHI scanning configurations to study the mean characteristics of floating wind turbine wakes. For example this would enable a more thorough study of the features that we observed in the downwind propagation of the wake center (Fig. 14). Furthermore, due to the relative stable response of the floating wind turbine examined in this study, an active motion compensation was not implemented in the scanning wind lidar. However, this could be necessary for the monitoring of the wake flow, especially in the far wake region, in the case of floating wind turbines that are characterized by larger motions.

A limitation of this study was that the lack of information about atmospheric stratification. Unfortunately, during the lidar measuring campaign, there were not available any sea surface temperature measurements, which could enable the characterization of the atmospheric stability. This knowledge would allow a more thorough investigation of the wake properties and their dependence on atmospheric conditions. However, the relatively high speeds, the strong shear values at the examined heights and the low standard deviation of the roll angles (based on the findings of Jacobsen and Godvik (2021)) support the hypothesis that the data set was acquired during either neutral or stable atmospheric stability and thus, the impact of convective effects of the wake ~~is~~ can be considered to be limited.

Finally, regarding the impact of the motion of the floater on the wake characteristics, ~~the~~ and considering the measured pitch and roll variations, the amplitude of the surge and sway motions of the wind turbine used in this study was relatively small compared to the values used in numerical (Nanos et al., 2022; Chen et al., 2022) and wind tunnel (Fu et al., 2019; Schliffke et al., 2020) studies, that focused on the study of the effect of the wind turbine motion on the wake characteristics. Comparing the standard deviation of the surge motion speed with the ~~longitudinal~~ one of the longitudinal wind speed showed that the standard deviation of the wind was one order of magnitude larger. For this reason, we studied the wake characteristics as a function of the mean wind speed and TI values. Similar amplitudes of side-to-side motion with the one observed in our study, with, however, an almost double Strouhal number, have been reported in the work of Li et al. (2022). They state that the side-to-side motion amplifies the wake meandering when the ambient TI is low ($< 3\%$), leading to a faster recovery of the wake deficit. However, in the TI regime studied here 4 % − 8 %, the wake recovery of a floating wind turbine is similar to that of a fixed wind turbine, as reported by ~~(Li et al., 2022)~~Li et al. (2022). This similarity in wake recovery could explain the agreement of the wake characteristics presented in this analysis with results from previous numerical and wind tunnel studies of fixed wind turbine wakes. In this study we have not investigated the impact of the rotational speed of the rotor and the blade pitch angles on up- and downwind conditions, which could be a subject of future work.

6 Conclusions

This study uses two nacelle-mounted wind lidars to investigate the characteristics of the up- and downwind conditions relative to an offshore floating 6MW wind turbine, which was mounted on a ballast platform. The acquired radial wind speeds from the two lidars are parameterized as a function of the upwind and wake characteristics. In the case of the upwind conditions, we find that, in 74% of the cases, modelling the radial speeds as a function of a linear wind shear and veer along the rotor, and of an induction factor due to the wind turbine's operation, performed adequately. Over the examined data set, we found that in 31% of the cases, the wind shear had negative values. These negative values highlight that deviations from a linear increasing profile at a height range between 100 m and 150 m are not negligible in ~~offshore wind profiles~~the wind profile at the offshore area of east of Scotland. The wake study focused on the self-similarity of the wind deficit and the downwind propagation of the wake's center, width and deficit in the far-wake region. The knowledge of these parameters is important since they determine the inflow conditions that the adjacent wind turbines would encounter in a ~~wand~~ wind farm. The wake measurements were grouped based on the mean wind speed at the hub height and the corresponding TI, allowing a statistical ~~wake property analysis~~ analysis of the wake properties. Our findings support the hypothesis that the spanwise velocity ~~profile~~ deficit in the wake can be considered self-similar in the far-wake region (3 − 8 ~~rotor diameters), as well as it can be modelled adequately using a constant eddy viscosity~~ D). Finally, an increase in the ambient TI ~~enhance~~ enhances the recovery of the velocity deficit and the expansion of the wake. These results indicate that the wakes of floating wind turbines, that do not experience high ~~surge and sway motions~~pitch and roll rotations, will have similar characteristics to those of fixed wind turbines. Thus, even though the rotor of floating wind ~~turbines is~~ turbine investigated in this study was subject to motions induced by both wind and sea fluctuations, the primary mechanism for the wake recovery is considered to be the atmospheric turbulence~~intensity~~.

Appendix A: Range height indicator lidar scans

~~This appendix presents the range height indicator~~ The *Galion* on the HS2 wind turbine scanned in two alternating modes, i.e., a PPI and a Range Height Indicator (RHI) ~~scans~~ scan. The PPI scan had the same characteristics as the one performed by the ~~G4000~~ *Galion* ~~wind lidar installed on the~~ lidar on HS4. The RHI scan consisted of 36 line-of-sight measurements with

610 elevation angles that extended from $-15°$ to $20°$. In our study, the RHI measurements acquired on the HS2 wind turbine ~~. The scans were performed along a vertical plane centered in the nacelle.~~ were used only to investigate the average vertical motion of the wake. Figure A1 presents the mean longitudinal speed, estimated by dividing the radial wind speed measurements with the cosine of the elevation angle of the line-of-sight. The estimation of the mean is based on two different data sets based on the wind speed range of $7.4 - 10.5$ ms^{-1} and $10.6 - 13.5$ ms^{-1}. The two sets had 426 and 266 scans for the first and second

615 wind speed ranges, respectively. The data are grouped only based on the mean wind speed.
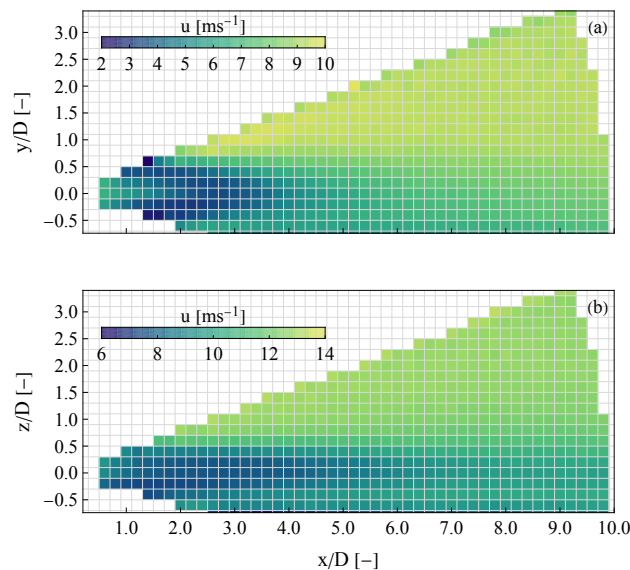
Figure A1. Mean longitudinal wind speed acquired during a range height indicator scan for the two different wind speed ranges of (a) $7.4 - 10.5$ ms^{-1} and (b) $10.6 - 13.5$ ms^{-1}.

Figure A2 presents the vertical profile of the wind speed based on the RHI scans of Fig. A1 for six different downwind distances corresponding to 3, 4, 5, 6, 7, and 8 ~~rotor diameters~~ D. Each profile is normalized by the mean free wind speed at the hub height. The profiles show a visible velocity deficit for all the ranges down to $8D$. Furthermore, the maximum velocity deficit is near the hub height regardless of the downwind distance. On average, the wake center shows no significant vertical

620 motion even though the ~~nacelle tilt~~ pitch angle of the wind turbine's nacelle is $5°$.
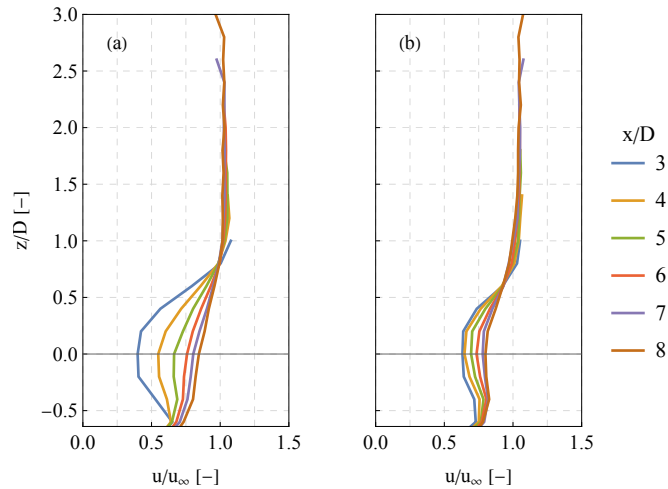
Figure A2. Vertical profiles of the longitudinal wind speed at different downwind distances (3, 4, 5, 6, 7, and 8 *D*) and for two wind speed ranges of (a) 7.4 – 10.5 ms^{-1} and (b) 10.6 – 13.5 ms^{-1}.

Appendix B: Pitch and roll angle of the wind turbine's nacelle

Figure B1 presents the power spectral density of the pitch (a) and roll (b) angles. We observe that in general higher energy levels appear in the spectrum of the pitch angle which corresponds to oscillations longitudinal to the yaw direction. However, in the roll angles we observed a more predominant frequency peak at 0.01 Hz and 0.03 Hz, which correspond to the natural frequency of the sway and roll motions of the wind turbine Jacobsen and Godvik (2021), respectively.

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Author contributions. Hywind Scotland wind farm and CDB planned the campaign and performed the measurements; NA and JM conceptualized the research analysis; NA analyzed the data and prepared the data visualization; NA wrote the original draft of the manuscript; NA, JM and CDB reviewed and edited the manuscript

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Competing interests. At least one of the (co-)authors is a member of the editorial board of Wind Energy Science.

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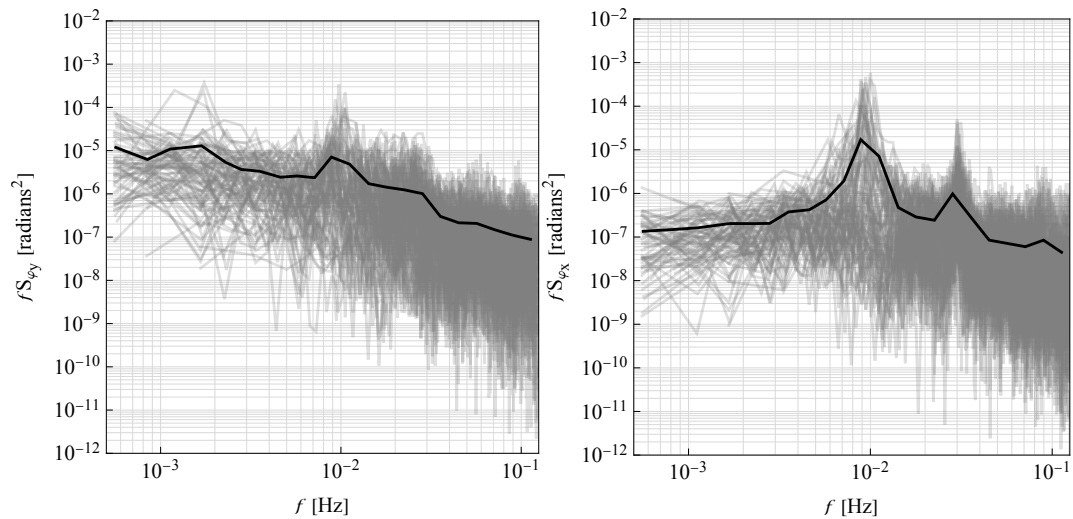
Figure B1. Power spectral densities of the pitch (left) and roll (right) angles of the wind turbine measured by a motion reference unit (MRU) in the nacelle. The gray lines correspond to the individual spectra for each of the 89 cases of Fig. **??**, and the black lines depict the corresponding mean over all cases.

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