



# A digital-twin solution for floating offshore wind turbines validated using a full-scale prototype

Emmanuel Branlard<sup>1</sup>, Jason Jonkman<sup>1</sup>, Cameron Brown<sup>2</sup>, and Jiatian Zang <sup>2</sup>

**Correspondence:** E. Branlard (emmanuel.branlard@nrel.gov)

Abstract. In this work, we implement, verify, and validate a physics-based digital twin solution applied to a floating offshore wind turbine. The digital twin is validated using measurement data from the full-scale TetraSpar prototype. We focus on the 3 estimation of the aerodynamic loads, wind speed, and section loads along the tower, with the aim at estimating the fatigue life-time of the tower. Our digital twin solution integrates: 1) a Kalman filter to estimate the structural states based on a linear model of the structure and measurements from the turbine, 2) an aerodynamic estimator, and 3) a physics-based virtual sensing procedure to obtain the loads along the tower. The digital twin relies on a set of measurements that are expected to be available 6 7 on any existing wind turbine (power, pitch, rotor speed, and tower acceleration), and motion sensors that are likely to be 8 standard measurements for a floating platform (inclinometers and GPS sensors). We explore two different pathways to obtain physics-based models: a suite of dedicated Python tools implemented as part of this work, or the OpenFAST linearization feature. In our final version of the digital twin, we use components from both approaches. We perform different numerical 10 experiments to verify the individual models of the digital twin. In this simulation realm, we obtain estimated damage equivalent 11

loads with an accuracy of the order of 5% to 10%. When comparing the digital twin estimations with the measurements from

the TetraSpar prototype, the errors increased to 10%-15% on average. Overall, the accuracy of the results appears promising 13 14

and demonstrates the possibility to use digital twin solutions to estimate fatigue loads on floating offshore wind turbines. A

natural continuation of this work would be to implement the monitoring and diagnostics aspect of the digital twin, to inform 15

operation and maintenance decisions. The digital twin solution is provided with examples as part of an open-source repository. 16

#### Introduction 17

18 The offshore floating wind turbine market is expected to grow in the next decades as the technology is gaining in maturity,

with several floating wind turbine prototypes already tested and commissioned, such as the TetraSpar, developed by Sties-19

20 dal Offshore(Stiesdal Offshore, 2022). Operation & maintenance (O&M) costs can account for approximately one-third of

offshore wind farm life-cycle expenditures for a fixed-bottom project and are expected to be higher for remote (floating)

projects (Castella, 2020). Reducing the O&M costs is therefore an impactful and effective means to lower the costs of floating 22

offshore projects. Digital twin solutions are increasingly being considered to follow products during their life cycle to assess 23

component conditions, guide predictive maintenance, and thereby reduce O&M costs. A review of digital twins for power sys-

<sup>&</sup>lt;sup>1</sup>National Renewable Energy Laboratory, Golden, CO 80401, USA

<sup>&</sup>lt;sup>2</sup>Stiesdal Offshore A/S, Denmark

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tems is found in Song et al. (2023). Digital twins often include a virtual sensing component, whose role consists in providing information that are not measured by the physical system, and a structural health monitoring component to assess the condition of the system. Virtual sensing technology is usually achieved using physics-based or data-driven approaches; both approaches relying on measurements from the physical system to infer and extrapolate information about its current state. Physics-based approaches use a numerical model of the system, whereas data-driven approaches either use ad-hoc algorithms or machine-learning techniques. This work presents the development, verification and validation of a physics-based digital twin for floating wind turbines, as a proof of concept for future maturation of the technology.

Digital twins for wind turbine applications have recently become a topic of research interest. The current authors explored the topic of physics-based digital twins in previous work, where a method to estimate tower loads on land-based turbines was developed (Branlard et al., 2020a, b). The approach relied on a Kalman filter model (Kalman, 1960; Zarchan and Musoff, 2015), which combines a linear physics-based model of the structure with measurements from the turbine to perform a virtual sensing of the tower section loads and estimate the fatigue of this component. The measurement data was taken from the supervisory control and data acquisition (SCADA) system using sensors readily available on most turbines. The approach used a mix between an augmented Kalman filter approach (Lourens et al., 2012), where the loads are estimated with the states of the system, and a physics-based aerodynamic estimator for aerodynamic thrust. Bilbao et al. (2022) used a Gaussian process latent force model instead to estimate the forcing of the system, and thereby obtain the section loads along the tower. Drivetrains are another component that has recently been an application of digital twin, with physics-based approaches presented for instance in (Mehlan et al., 2022, 2023), and data-driven models in Kamel et al. (2023).

In spite of the term "digital twin" becoming recently popular, it is heavily based on the fields of structural-health monitoring and load estimations (or more generally, virtual sensing), which have long been topics of research. For instance, Iliopoulos et al. (2016) used physics-based modal decomposition to estimate the dynamic response on the substructure of a fixed-bottom wind turbine. Neural networks have been used to establish transfer functions or surrogate models based on SCADA data to obtain wind turbine loads with the aim of performing conditional monitoring (see, e.g. Cosack (2010); Schröder et al. (2018)). Kalman filters were introduced in fields other than wind energy to perform load estimation, for instance in the following references: Auger et al. (2013); Ma and Ho (2004); Eftekhar Azam et al. (2015); Lourens et al. (2012). Kalman filtering has been extensively used in wind energy to estimate rotor loads and improve wind turbine control, see, e.g. Boukhezzar and Siguerdidjane (2011); Selvam et al. (2009); Bottasso and Croce (2009); Bossanyi (2003). Load estimations were also achieved using hybrid-techniques combining physics based on SCADA data by Noppe et al. (2016). Other load estimation techniques may be used, such as lookup tables (Mendez Reyes et al., 2019), modal expansion (Iliopoulos et al., 2016), machine learning (Evans et al., 2018), neural networks (Schröder et al., 2018), polynomial chaos expansion (Dimitrov et al., 2018), deconvolution (Jacquelin et al., 2003), or load extrapolation (Ziegler et al., 2017).

In this work, we build on our previous work and present a digital twin solution for floating wind turbines that relies on physics-based models and a Kalman filter. We apply the digital twin to the TetraSpar structure and use measurements from the full-scale prototype. In section 2, we provide an overview of our digital concept, the vision for future application, and the TetraSpar prototype on which the digital twin is applied. In section 3, we present the individual components of the digital twin,



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- and run some isolated verification studies on them. In section 4, we present results from the digital twin application first using
- 61 numerical experiments, and then using measurements from the TetraSpar prototype, before concluding. To avoid lengthening
- 62 the main text, we provide derivations (some being important contributions of this work) and additional results in appendices.

# 2 Overview of the digital twin concept

64 In this section, we provide an overview of our digital twin concept and how it is applied in this study.

# 2.1 Long-term vision of the digital twin concept

- Many definitions and applications of digital twins are possible. The vision for the concept discussed in the work is to follow the life-cycle of a wind turbine in real-time and ultimately provide tangible signals to inform O&M decisions. Our goal is to
- 68 achieve this by relying only on measurements expected to be available on most wind turbines, thereby avoiding the extra cost of adding sensors. We illustrate our approach and vision in Figure 1. The digital twin is intended to run in real-time on a cloud

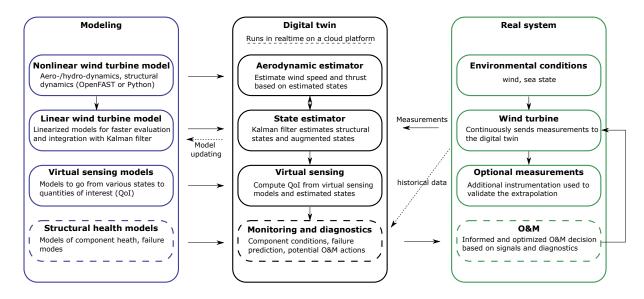


Figure 1. Overview of the digital twin concept. Dashes lines indicate features that are outside the current scope.

platform. It combines a set of models (on the left of the figure) with data from the real system (on the right) to perform the estimation of various states and eventually produce diagnostics that can be use to inform the O&M. The data from the real system are taken from high-frequency measurements from the SCADA system (e.g., power, pitch, rotor speed, etc.). The states estimated by the digital twin include aerodynamic states (wind speed, thrust) and motions of the structure (e.g., surge, pitch, tower deflection). The core algorithm in the estimation is a Kalman filter that uses a linear wind turbine model. The estimated states are used in an "virtual sensing" step, to produce quantities of interests (QoI), such as the loads at key locations of the



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structure. The QoI are then intended to be postprocessed by a monitoring and diagnostic tool to generate the data needed to

77 perform condition-based O&M.

# 2.2 Narrowed scope

- The boxes in Figure 1 that are surrounded with dashes are not addressed in the current work, namely: the structural health 79
- modeling, monitoring and diagnostics, and O&M decisions. These are essential steps necessary to achieve our final vision, 80
- but they are postponed to future work. Dashed lines indicate possible options that may be exploited in the future but are also 81
- 82 outside of our scope: the use of historical data to assist in the diagnostics, the use of estimates to perform modeling updating,
- 83 and real time implementation.
- This work therefore focuses on the estimation of states and environmental conditions under the assumption that the estimated 84
- quantities can replace costly measurements and eventually be used for O&M decisions. We intend to provide a proof of concept 85
- 86 paving the way for future commercial applications. A detailed description of each of the boxes surrounded with plain lines will
- be provided in section 3. 87

#### 2.3 System studied 88

## 2.3.1 The TetraSpar prototype

- Throughout this article, the system studied is the TetraSpar floating offshore prototype. The system consists of a floating 90
- platform and station keeping system developed by Stiesdal Offshore in collaboration with partners Shell, RWE and TEPCO 91
- Renewable Power, and a 3.6-MW wind turbine with a rotor diameter of 130 m developed by Siemens Gamesa Renewable
- Energy. A sketch of the system is provided in Figure 2. The prototype was installed off the coast of Norway and commissioned 93
- in November 2021. The prototype turbine is equipped with additional sensors (labeled "Optional measurements" in Figure 1), 94
- which we will use to validate the estimated QoI.

#### 2.3.2 Numerical experiments 96

- Prior to using measurement data, we will use simulations (referred to as "numerical experiments") in place of the real system 97
- to feed-in data to the digital twin. The advantage of this approach is that the QoI are directly accessible and can be compared
- to the estimates for verification purposes. 99
- Data for the numerical experiments is obtained using OpenFAST simulations (Jonkman et al., 2023). A model of the 100
- TetraSpar floating platform and the wind turbine was implemented in OpenFAST based on data provided by the manufac-101
- turers. The operating conditions of the turbine were extracted from SCADA data and a controller was tuned to approximate 102
- these conditions. We use the following modules of OpenFAST (see Table 2, and Jonkman et al. (2023)): MAP (mooring lines), 103
- HydroDyn (hydrodynamics), ElastoDyn (tower and blade elasticity; rigid floater), AeroDyn (aerodynamics), InflowWind (wind 104
- inflow), ServoDyn (controller interface). 105







Figure 2. Sketch of the TetraSpar prototype

For the numerical experiments, we use synthetic turbulent wind fields generated using TurbSim (Jonkman and Buhl (2006)).

In particular, we will often use the same wind field, that we will refer to as the "turbulent step", where a deterministic ramp and drop are added to a turbulent field. The advantage of this 10-min wind field is that is covers all the operating regions of the turbine in a challenging way. The wind speed at hub height for the turbulent step can be seen in Figure 6.

# 2.3.3 Main aspects of the structural model

DOFs and its time derivative:  $x = [q, \dot{q}]$ .

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- 111 We model the structure using a set of 8 degrees of freedom (DOFs), as illustrated in Figure 3. The platform is represented as a rigid body and its motion is described using 6 DOFs: surge, sway, heave, roll, pitch, yaw, respectively noted  $x, y, z, \phi_x, \phi_y, \phi_z$ . The tower bending in the fore-aft direction is represented using one generalized DOF,  $q_t$ , associated with a Rayleigh-Ritz shape function, taken as the first fore-aft mode shape of the tower (see, e.g., Branlard (2019)). The shape function along the tower height,  $z_t$ , is written  $\Phi(z_t)$ , with  $\Phi(0) = 0$  at the tower bottom, and  $\Phi(L_T) = 1$  at the tower top, where  $L_T$  is the tower length. The shaft rotation is noted  $\psi$ , so that the rotation speed of the rotor is  $\dot{\psi}$  where the dotted notation indicates differentiation with respect to time. The rotor-nacelle-assembly (RNA) is modeled as a rigid body. The full vector of DOFs is therefore:  $q = [x, y, z, \phi_x, \phi_y, \phi_z, q_t, \psi]$ . The equations of motion will be recast into a first order form by concatenating the vector of
- In this work, we perform a simplifying assumptions, e.g., neglecting the influence of nacelle yaw on the system. The measurement data is conveniently provided in the fore-aft and side-side system of the nacelle. The main assumption is therefore





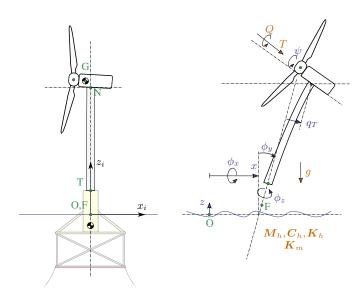


Figure 3. Notations for the structural modeling of the floating wind turbine, assuming no yawing of the nacelle. Left: main points (F,T,N,O,G) and inertial coordinate system (i). Right: degrees of freedom  $(x,y,z,\phi_x,\phi_y,\phi_z,q_t,\psi)$  and main loads: aerodynamics (T,Q), hydrodynamics  $(6\times 6$  mass, damping and stiffness matrices:  $M_h,C_h,K_h$ . Wave excitation force neglected), mooring  $(6\times 6$  stiffness matrix  $K_m$ ) and gravity (g).

- 122 that we assume a rotational symmetry of the platform and mooring system about the yaw axis. We intend to lift this assumption
- 123 in future work

# 124 3 Individual components of the digital twin

- 125 In this section, we describe and verify the individual components of the digital twin presented in Figure 1. In section 4, we will
- 126 present applications of the digital twin where all the individual components are combined together.

# 127 3.1 Wind turbine measurements

- 128 The measurements used as inputs to the digital twin are listed in Table 1. These outputs are stored in a database at a sampling
- 129 rate of 25 Hz. We expect these measurements to be standard sensors for any floating wind turbine. The TetraSpar prototype is
- 130 equipped with additional measurements that will be used to validate the implementation of the digital twin (see section 4).

# 3.2 Nonlinear wind turbine models

- 132 Similar to our previous work (Branlard et al., 2020b), we use two different pathways to obtain nonlinear and linear models of
- 133 floating wind turbines: OpenFAST and WELIB (Wind Energy LIBrary, Branlard (2022)). The different modeling approaches
- are illustrated in Table 2 and further presented below.





**Table 1.** Measurements used as inputs to the digital twin.

Signal	Symbol
Blade pitch angle	$\theta_p$
Rotor speed	$\dot{\psi}$
Generator torque*	$Q_g$
Surge and Sway	x, y
Roll and Pitch	$\phi_x,\phi_y$
Nacelle accelerations	$\boldsymbol{\ddot{r}}_N$

<sup>\*</sup> Obtained from the power measurement using Equation 2.

**Table 2.** Approaches and tools used to obtain nonlinear and linear models.

Approach	Tool	Usage	Formulation & Linearization
1 OpenFAST	OpenFAST (ElastoDyn, HydroDyn, MAP, AeroDyn)	Structural model Hydrodynamics Moorings Aerodynamics Virtual sensing	Numerical and analytical
WELIB (Python tools)	YAMS	Structural model Virtual sensing	Analytical
	pHydroDyn	Hydrodynamics	Numerical
	руМАР	Moorings	Numerical

The OpenFAST approach was described in Section 2.3.2. The WELIB approach consists of a set of dedicated open-source Python tools. We developed this Python code to offer additional modularity and granularity, for instance to allow for: simple linearization of the hydrodynamics (obtention of 6x6 matrices), linearization of hydrodynamics with respect to wave elevation, linearization with respect to parameters (Jonkman et al., 2022), and interactive time-stepping of linear and nonlinear models. One shortcoming is that WELIB does not cover the full range of options available with OpenFAST, which is a continuously evolving, extensively verified and validated tool. For this work, we implemented the following tools in WELIB: 1) YAMS, a symbolic structural dynamics package to obtain the equations of motion of an assembly of rigid and flexible bodies analytically, and allow for their analytical linearization (Branlard and Geisler, 2022); 2) pHydroDyn, a Python version of the module HydroDyn (with a subset of HydroDyn's functionality) to determine the hydrodynamic loads; and 3) pyMAP, a wrapper around the MAP module of OpenFAST, to obtain the mooring quasi-statics. With these three additions, it is possible to perform nonlinear simulations of floating wind turbines using WELIB and perform comparisons with OpenFAST. The benefits of WELIB over OpenFAST is the possibility to obtain analytical linear models and gain physical intuitiveness on the model. Results will be presented in see Section 3.3.







#### 148 3.3 Linear wind turbine models

- 149 As part of our digital twin concept, we have chosen to use linear wind turbine models and a Kalman filter for the core of the
- 150 state estimation (see Section 3.5). Nonlinear models and an extended Kalman filter could be considered in future iterations. In
- 151 this section, we describe how the linear models from OpenFAST and WELIB are obtained.

#### 152 3.3.1 OpenFAST linearization

- 153 OpenFAST can provide full-system linearization of its underlying nonlinear models by using a mix of analytically- and finite-
- difference-derived Jacobians (Jonkman and Jonkman, 2016; Jonkman et al., 2018). The linearization process provides the
- 155 state-space model ( $\delta \dot{x} = A \delta x + B \delta u$ ) and output equation ( $\delta y = C \delta x + D \delta u$ ) for small perturbations (indicated with  $\delta$ ) of
- 156 the internal states (x), inputs (u) and outputs (y) of OpenFAST, around the linearized operating point. OpenFAST provides the
- 157 linear model for the entire set of states, inputs and outputs present in the model (including virtual sensor-type outputs typically
- 158 written to an output file and not used internally). In this work, we extract subsets of the A, B, C, D matrices and combine
- 159 them to form the linear model of the state estimator (see Section 3.5).

#### 160 3.3.2 WELIB linearization

- 161 WELIB performs the linearization of the structure, hydrodynamics and moorings independently, before combining them into
- 162 one model. The aerodynamic loads are not linearized because a dedicated aerodynamic estimator is used in this work (see
- 163 Section 3.4). The steps are as follows:

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- The structural equations are linearized analytically using our symbolic framework (Branlard and Geisler, 2022). We
- introduce a notion of "augmented inputs" to linearize the equations of motion without an explicit knowledge of the
- external forces. The process is described in Appendix A.
- We compute the  $6 \times 6$  linearized rigid-body hydrodynamics matrices (mass matrix  $M_h$ , damping matrix  $C_h$  and stiffness

matrix  $K_b$ ) corresponding to the six rigid-body motions of the platform. We obtain them using numerical differentiation

- in two different ways: 1) using the Python implementation of the HydroDyn module by performing rigid-body perturba-
- tion of the full platform, or, 2) using full-system linearization of the HydroDyn module. The latter provides Jacobians of
- the hydrodynamic loads as function of motions of the individual hydrodynamic analysis nodes (of which models often
- have hundreds to thousands of). To transfer these individual Jacobians to the reference point and obtain the  $6 \times 6$  ma-
- trices, we developed and used the method presented in Appendix B. The consistency between the two approaches was
- verified. The second approach is not straightforward to implement, therefore, we upgraded the OpenFAST HydroDyn
- driver to provide the  $6 \times 6$  hydrodynamic matrices directly without the need to use the full-system linearization.
- The linearized  $6 \times 6$  mooring stiffness matrix,  $K_m$ , is obtained by calling the linearization feature of the MAP module,
- and transferring the Jacobian to the reference point using the method outlined in Appendix B.
- The linearized equations of motion are assembled as:





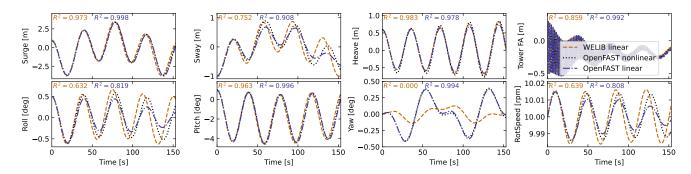
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$$[M_0 + Q_0 M_h] \delta \ddot{q} + [C_0 + Q_0 C_h] \delta \dot{q} + [K_0 + Q_0 (K_h + K_m)] \delta q = \delta f_a + \delta f_h$$
 (1)

where the matrices with subscript 0 originate from the linearization of the structure (see Appendix A). The term  $Q_0$  is used here to map the 6 rigid-body platform degrees of freedom to the full vector of degrees of freedom. The term  $\delta f_a$  is an approximation of the aerodynamic loads, and will be discussed in Section 3.4. The term  $\delta f_a$  is an approximation of the hydrodynamic wave-excitation loads and it will be mapped into the inherent model noise of the Kalman filter in Section 3.5. Equation 1 is recast into a first order system to obtain the state matrix A.

## 3.3.3 Verification of the linear models

In this section, we compare results from the OpenFAST nonlinear model, the OpenFAST linear model and the WELIB linear model, for free-decay simulations of the TetraSpar structure. The OpenFAST linear model is obtained about the operating point defined by  $q_0 = 0$  and  $\dot{\psi}_0 = 10$  rpm. All models (including the OpenFAST nonlinear model) use 8 DOFs. The initial conditions are set to q = [1, -1, 0.6, 0.5, 0.5, 0, -0.2, 0] (in m and deg) and  $\dot{\psi} = 10$  rpm, after which the structure is free to decay,

The time responses from the linear and nonlinear models are in strong agreement when only the structure is considered (see results in Appendix C). Below, we present results for a model that includes hydrodynamics, but without wind or external waves (still water). We set the hydrodynamic drag to zero due to the difficulty in linearizing this term and will let the state



**Figure 4.** Free decay of the structure using non linear and linear models for a case including moorings and hydrodynamics (still water). Time series of the main DOFs.

estimator account for this modeling uncertainty. Results of the free-decay simulation are given in Figure 4, for a time period of 153 s corresponding to the surge frequency. When hydrodynamics is included, the time responses from the linear models are in strong agreement with the nonlinear OpenFAST results for the surge, heave, pitch and tower fore-aft DOFs. The sway, roll, and rotor speed responses tend to drift as the simulation time advances. The WELIB linear model has difficulty capturing the yaw response. We believe that some of the error in the yaw signal is due to differences between the formulations of the three-dimensional rotations in OpenFAST and WELIB, resulting in a difference of coupling between the DOFs. The coefficient of determination  $(R^2)$  is indicated in Figure 4, comparing the linear models to the reference OpenFAST simulations for each response. In all cases, the OpenFAST linear model is closer to the nonlinear OpenFAST model than the WELIB model.





To further quantify the differences between the models, we compare the natural frequencies obtained using the OpenFAST linear and WELIB linear models in Table 3. Overall, the frequencies between the two linear formulations agree very well (less

**Table 3.** Comparison of system frequencies obtained using the WELIB and OpenFAST linear models with and without hydrodynamics (no addded mass, damping, hydrostatics, or wave excitation)

Structure + mooring		Structure + mooring + hydrodynamics				
Mode	OpenFAST [Hz]	WELIB [Hz]	Rel. Err [%]	OpenFAST [Hz]	WELIB [Hz]	Rel. Err [%]
Surge	0.0088	0.0088	-0.2	0.0067	0.0065	-2.4
Sway	0.0088	0.0088	-0.1	0.0067	0.0068	0.7
Yaw	0.0163	0.0162	-1.0	0.0128	0.0128	-0.3
Pitch	0.0879	0.0886	0.7	0.0253	0.0257	1.6
Roll	0.0894	0.0902	0.9	0.0256	0.0266	4.0
Heave	NA	NA	NA	0.0276	0.0276	-0.2
Tower FA	0.5782	0.5789	0.1	0.5129	0.5145	0.3

that 2.5% relative error), except for the roll frequencies (4% error) with hydrodynamics. Given the results of this section, we will continue this study using the OpenFAST linear model. We expect that continuous development of WELIB will further narrow the gap with OpenFAST in the future.

#### 3.4 Aerodynamic estimator

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In Section 3.3, we indicated that the linear models were derived without accounting for aerodynamics. Instead, we choose to include the aerodynamic contribution separately within the digital twin. The reason for this choice is that the determination of the aerodynamic loads is essential to capturing the main loading and deflections of the structure, in particular the tower, and, the aerodynamic loads vary significantly over the range of operating conditions. Therefore, separating this contribution limits the need to obtain different linearized models for different operating conditions. We have successfully applied this approach in the past (Branlard et al., 2020a). In this work, we extend this approach to accommodate the floating wind application. The different elements of the aerodynamic estimator consist of: a torque estimator, aerodynamic maps, and a wind speed estimator.

# 3.4.1 Kalman filter for torque estimation

We assume that the power and rotor speed are reliable measurement signals, and we further assume that the generator torque (relative to the low-speed shaft) can be inferred from the power signal as:

$$218 \quad Q_g = \frac{P}{\dot{\psi}} \frac{1}{n\eta_{\rm DT}(\dot{\psi})} \tag{2}$$





- where  $\eta_{DT}$  is the drivetrain (gearbox and generator) efficiency, and n is the gear ratio. For the TetraSpar, n=1, and we assume
- 220  $\eta_{\rm DT} = 1$ . The dynamics equation of the drivetrain is modeled as:

$$221 \quad J_{\text{DT}}\ddot{\psi} = Q - Q_q \tag{3}$$

- where  $J_{\rm DT}$  is the inertia of the drivetrain about the shaft axis. If we assume that the generator torque is a measurement, then an
- 223 augmented Kalman filter (Lourens et al., 2012) can be used to estimate the aerodynamic torque Q, using the following state
- 224 equation:

$$225 \quad \begin{bmatrix} \dot{\psi} \\ \ddot{\psi} \\ \dot{Q} \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & \frac{1}{J_{\text{DT}}} \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} \psi \\ \dot{\psi} \\ Q \end{bmatrix} + \begin{bmatrix} 0 \\ -\frac{1}{J_{\text{DT}}} \\ 0 \end{bmatrix} Q_g$$
 (4)

- 226 A random walk approach is used for the evolution of the torque, that is,  $\dot{Q} = 0$  and the Kalman filter adds further model noise
- 227 to this equation. The measurement equation of the Kalman filter is:

- 229 In the following, we will write  $\hat{Q}$ , the aerodynamic torque obtained using the method outlined above. We will present verifica-
- 230 tion results in Section 3.4.4.

#### 231 3.4.2 Aerodynamic maps

- 232 It is commonly accepted that the aerodynamic performances of a wind turbine mostly depends on the tip-speed ratio and the
- 233 pitch angle of the blade. With compliant structures, the bending of the blade, the bending of the tower, and the motions of the
- 234 floating platform (in particular the platform pitch) will also affect the aerodynamic performances. These motions are to a large
- 235 extent a function of the mean wind speed. Therefore, we suggest to tabulate the aerodynamic performances as function of wind
- speed (U), rotor speed  $(\dot{\psi})$ , blade pitch  $(\theta_p)$ , and platform pitch  $\phi_y$  (assumed to be in the fore-aft direction). The power and
- 237 thrust coefficients, respectively noted  $C_P$  and  $C_T$ , are precomputed using aeroelastic simulations in OpenFAST for a discrete
- 238 set of values of the 4 input parameters. In the simulations, the blade and tower elasticity are accounted for. To limit the number
- 239 of simulations, only the points that are within reasonable proximity of the regular operating conditions of the wind turbine are
- 240 computed. The 4D aerodynamic maps are precomputed as follows:

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$$C_P(U,\dot{\psi},\theta_p,\phi_u), \quad C_T(U,\dot{\psi},\theta_p,\phi_u)$$
 (6)

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$$U \in \{2, 3, \dots, 25\} \text{ m.s}^{-1}, \quad \dot{\psi} \in \{5, 5.5, \dots, 18\} \text{ rpm},$$
 (7)

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$$\theta_p \in \{-1, 0, \dots, 30\} \text{ deg}, \quad \phi_q \in \{-10, 0, 15\} \text{ deg}$$
 (8)

244 The precomputed values are stored in a database.





# 245 3.4.3 Wind speed estimation

- 246 The digital twin uses the aerodynamic map database to estimate the wind speed and aerodynamic thrust. For a given air density
- 247  $(\rho)$ , rotor radius (R), and given measurements  $\dot{\psi}, \tilde{\theta}_p, \tilde{\phi}_y$ , the aerodynamic torque and thrust are readily obtained as function of
- 248 wind speed from the database:

$$Q(U) = \frac{1}{2} \rho \frac{U^3}{\tilde{\psi}} \pi R^2 C_P(U, \tilde{\psi}, \tilde{\theta}_p, \tilde{\phi}_y), \qquad T(U) = \frac{1}{2} \rho U^2 \pi R^2 C_T(U, \tilde{\psi}, \tilde{\theta}_p, \tilde{\phi}_y)$$
 (9)

250 where S.I. units are assumed for all variables. For a given estimated torque  $(\hat{Q})$ , the estimated wind speed  $(\hat{U})$  is found such

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$$Q(\hat{U}) - \hat{Q} = 0$$
 (10)

As illustrated in Figure 5, multiple values of  $\hat{U}$  can potentially satisfy Equation 10 because the aerodynamic torque is a nonlinear function of the wind speed. In such case, we use the steady state operating condition curve of the turbine to chose

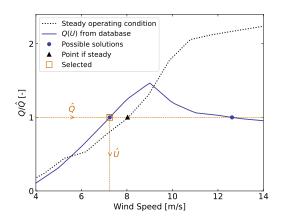


Figure 5. Illustration of wind speed estimation in the case where multiple wind speed values match the target torque value  $\hat{Q}$ 

between the multiple solutions (typically two), by selecting the point that is closest to this curve (see Figure 5). A relaxation scheme is also used, based on the previous estimate, to alleviate sudden jumps of the estimated wind speed.

## 3.4.4 Verification of the aerodynamic estimator

To verify the aerodynamic estimator, we ran an OpenFAST simulation of the TetraSpar with the "turbulent step" wind field mentioned in Section 2.3.2 and irregular waves computed with a significant wave height of  $H_s = 6$  m and a peak spectral period of  $T_p = 14$ , which represent a fairly extreme sea state for the site of the TetraSpar prototype. The simulated values of  $\dot{\psi}$ ,  $\theta_p$ ,  $\phi_y$ ,  $Q_g$  are used as direct input to the aerodynamic estimator. Comparisons of the estimates with the OpenFAST outputs are shown in Figure 6. The shaded area on the figure represent the area where the generator torque is zero (turbine spinning up), and therefore, the wind speed estimator is not expected to work in that region. The top of the plots indicate the ratio of



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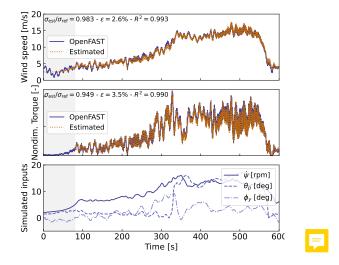
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**Figure 6.** Example of aerodynamic estimation using "simulated measurements" from OpenFAST. Top: wind speed. Middle: Dimensionless torque. Bottom: structural inputs from the OpenFAST simulation provided to the estimator.

standard deviations, the mean relative error  $(\epsilon)$  and the coefficient of determination  $(R^2)$ . Throughout this article, we define the mean relative error of a quantity x as:

266 
$$\epsilon(x) = \operatorname{mean}_{i} \left[ \frac{|x_{\text{est}}[i] - x_{\text{ref}}[i]|}{\operatorname{mean}(|x_{\text{ref}}|)} \right]$$
 (11)

where  $x_{\rm est}$  is the estimated signal,  $x_{\rm ref}$  the reference signal, and x[i] is the value of a signal at the time step i. Using the mean of  $|x_{\rm ref}|$  in the denominator avoids issue related to signals crossing 0. It results in lower mean relative error than if the instantaneous value was used, but the metric is still indicative of how far the two signals are on average.

To quantify the performance of the estimator, we reproduced the simulation above, but adding different noise levels to the measurements to account for measurement errors by the sensors. A Gaussian noise signal of zero mean and standard deviation  $r\sigma$  is added to each input, where r is the noise level and  $\sigma$  is the standard deviation of the clean input. The results are shown in Table 4. As expected, the error in the estimation increases with increasing noise levels. This numerical experiment provides a

**Table 4.** Mean relative error  $(\epsilon)$  of the wind speed, torque and thrust estimates, for increasing noise levels.

Noise level	0%	1%	5%	10%	20%
Wind Speed	2.6%	2.6%	3.1%	4.1%	6.7%
Torque	3.5%	3.8%	5.0%	6.8%	11.1%
Thrust	4.1%	5.1%	5.6%	7.3%	11.6%

274 rough quantification of the errors that can be expected from the aerodynamic estimator.





#### 275 3.5 State estimator

- 276 In this work, we follow a similar approach to our previous work (e.g. Branlard et al. (2020a)), where an augmented Kalman
- 277 filter is used to estimate states and loads. The Kalman filter used in the aerodynamic estimator (Section 3.4) is augmented
- 278 with additional states and outputs. The Kalman filter uses two linear models: a state-equation, describing the time evolution of
- 279 the states, and an output equation, describing how the measurements are related to the states and inputs. The state and output
- 280 equations are written:

281 
$$\delta \dot{\boldsymbol{x}}_{\text{KF}} = \boldsymbol{X}_x \delta \boldsymbol{x}_{\text{KF}} + \boldsymbol{X}_u \delta \boldsymbol{u}_{\text{KF}} + \boldsymbol{w}_x$$
 (12)

282 
$$\delta y_{KF} = Y_x \delta x_{KF} + Y_u \delta u_{KF} + w_y$$
 (13)

- 283 where  $\delta x_{KF}$ ,  $\delta u_{KF}$ , and  $\delta y_{KF}$  are the state, input, and output<sup>1</sup>, respectively,  $X_x$ ,  $X_u$ ,  $Y_x$ , and  $Y_u$  are the system matrices that
- 284 relate the different system vectors, and,  $w_x$  and  $w_y$  are Gaussian processes represented modeling noise.  $\div$ The output vector,
- 285  $\delta y_{KF}$ , is also referred to as the "measurement" vector, because it corresponds to the measured signals. At a given time step,
- 286 the Kalman filter algorithm uses the system matrices, a set of measurements, and an a-priori knowledge of the model and
- 287 measurement uncertainties to estimate the state vector (Kalman, 1960; Zarchan and Musoff, 2015).
- In this work, we design the state estimator such that the state vector contains the structural degrees of freedom ( $\delta q$  and  $\delta \dot{q}$ )
- and the aerodynamic torque (Q), and the input vector consists of the thrust (obtained with the aerodynamic estimator), and
- 290 the generator torque (obtained from the power). These design choices were guided by our previous work on the topic. For
- 291 this choice of state and input variables, we build linear models for the state and output equations. We use the linear models
- 292 described in Section 3.3 (the A, B, C, D matrices), to populate the system matrices of the Kalman filter. We provide additional
- details on how the relevant Jacobians are extracted in Section 3.6.1. Given our choice of system vectors, the state equation is:

$$294 \quad \begin{bmatrix} \delta \dot{\mathbf{q}} \\ \delta \ddot{\mathbf{q}} \\ \dot{Q} \end{bmatrix} = \begin{bmatrix} \mathbf{0} & \mathbf{I} & \mathbf{0} \\ \mathbf{A}_{12} & \mathbf{A}_{22} & \frac{\partial \ddot{\mathbf{q}}}{\partial Q} \\ \mathbf{0} & \mathbf{0} & \mathbf{0} \end{bmatrix} \begin{bmatrix} \delta \mathbf{q} \\ \delta \dot{\mathbf{q}} \\ Q \end{bmatrix} + \begin{bmatrix} \mathbf{0} & \mathbf{0} \\ \frac{\partial \ddot{\mathbf{q}}}{\partial Q_g} & \frac{\partial \ddot{\mathbf{q}}}{\partial T} \\ 0 & 0 \end{bmatrix} \begin{bmatrix} Q_g \\ T \end{bmatrix} + \mathbf{w}_x$$

$$(14)$$

- where,  $A_{12}$  and  $A_{22}$  are the two lower blocks of the A matrix, and I is the identity matrix. The Jacobians with respect to the
- loads are extracted from the B and D matrices. A random walk approach is used for the evolution of the torque Q (that is, we
- 297 set  $\dot{Q} = 0$ ). The output equation, which effectively relates the measurements to the system states and inputs, is set as:

$$\begin{vmatrix}
\delta \tilde{\mathbf{q}} \\
\dot{\psi} \\
\ddot{\mathbf{r}}_{N} \\
Q_{g}
\end{vmatrix} = \begin{vmatrix}
\frac{\partial \tilde{\mathbf{q}}}{\partial \mathbf{q}} & \frac{\partial \tilde{\mathbf{q}}}{\partial \dot{\mathbf{q}}} & \frac{\partial \tilde{\mathbf{q}}}{\partial \dot{\mathbf{q}}} & \frac{\partial \tilde{\mathbf{q}}}{\partial Q} \\
\mathbf{0} & \tilde{\mathbf{I}} & 0 \\
\frac{\partial \tilde{\mathbf{r}}_{N}}{\partial q} & \frac{\partial \tilde{\mathbf{r}}_{N}}{\partial \dot{\mathbf{q}}} & \frac{\partial \tilde{\mathbf{r}}_{N}}{\partial Q} \\
\mathbf{0} & \mathbf{0} & 0
\end{vmatrix} \begin{bmatrix}
\delta \mathbf{q} \\
\delta \dot{\mathbf{q}} \\
Q
\end{bmatrix} + \begin{pmatrix}
\mathbf{0} & \mathbf{0} \\
0 & 0 \\
\frac{\partial \tilde{\mathbf{r}}_{N}}{\partial Q_{g}} & \frac{\partial \tilde{\mathbf{r}}_{N}}{\partial T} \\
1 & 0
\end{vmatrix} \begin{bmatrix}
Q_{g} \\
T
\end{bmatrix} + \mathbf{w}_{y}$$
(15)

where  $\ddot{r}_N$  is the vector of nacelle accelerations, and  $\tilde{q} = \{\delta x, \delta y, \delta \phi_x, \delta \phi_y\}$  is the measurements of surge, sway, roll and pitch as given in Table 1.

 $<sup>^{1}</sup>$ In general, the Kalman filter system vectors are different from the ones used for the linearization presented in Section 3.3, therefore the subscript KF (for Kalman Filter) is added to these vectors.

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The state and output equations are used as part of a Kalman filter algorithm implemented in WELIB, which continuously takes as input the measurements from the wind turbine (corresponding to the left hand side of Equation 15). The process and covariance matrices used within the Kalman filter algorithm (determining the values of  $w_x$  and  $w_y$ ) are populated based on the estimated standard deviations of the different states and outputs. At each time step, the thrust is estimated using the aerodynamic torque of the previous time step and used as input. The result of the Kalman filter consists of the estimated states and outputs at each time step. Sample simulation results will be provided in section 4.

#### 3.6 Virtual sensing

- 308 Once the states are estimated by the Kalman filter, the virtual sensing step is used to derive quantities of interest (see Figure 1).
- 309 In this work, we focus on the estimation of the sectional loads along the tower using a physics-based model. We investigate
- 310 two methods to obtain these loads.

## 311 3.6.1 OpenFAST linearization outputs

- 312 The first method consists in using the linearization outputs of OpenFAST, namely using a subset of the equation  $\delta y = C\delta x + C\delta x$
- 313  $D\delta u$  (see Section 3.3.1). In general, if a QoI is present in the output vector of OpenFAST, it can be retrieved as follows. If the
- 314 variable is located at the row index k in the vector y, then this variable can be obtained from the states and inputs as:

315 
$$[y]_k = [\delta y]_k + [y_0]_k = [C]_k \delta x + [D]_k \delta u + [y_0]_k$$
 (16)

- where  $[\cdot]_k$  indicates that the row k of the matrix or column vector is used. In our case,  $[y]_k$  in Equation 16 would for instance
- 317 be the sectional fore-aft bending moment at the height  $z_i$  along the tower, noted  $\mathcal{M}_y(z_i)$ . The advantages of using this method
- are multiple: 1) the method is directly applicable to any other outputs computed by OpenFAST, 2) the calculation procedure
- 319 is linear and therefore computationally efficient, 3) if strain measurements are available at given heights, the rows  $[C]_k$  and
- 320  $[D]_k$  could be included in the output equation of the Kalman filter (Equation 15) to provide information about the model's
- 321 expectation of these measurements, 4) the underlying linear model is consistent with the nonlinear model of OpenFAST. The
- 322 downside of the method is its linearity, in the sense that it is only valid close to the operating point and could lack important
- 323 nonlinear effects. The values of  $[C]_k$ ,  $[D]_k$  and  $[y_0]_k$  would potentially need to be reevaluated if the system operates away
- 324 from the linearized operating point. One possible solution would be to introduce gain-scheduling to modify the linear system
- 325 based on the estimated wind speed.

# 3.6.2 Non-linear calculation (WELIB)

- 327 An alternative method consists in computing the section loads based on first principles using the formulation presented in
- 328 Branlard (2019). The calculation requires a knowledge of the tower-top loads and the full kinematics of the tower and nacelle
- 329 (position, velocity and acceleration). At a given time step, the kinematics are computed based on q,  $\dot{q}$  and  $\ddot{q}$ . The tower-top
- 330 loads are estimated based on the aerodynamic loads and the inertial loads of the rotor-nacelle assembly. We describe the method
- 331 in more details in Appendix D. The advantages are that nonlinearities are accounted for and the model is valid irrespectively of



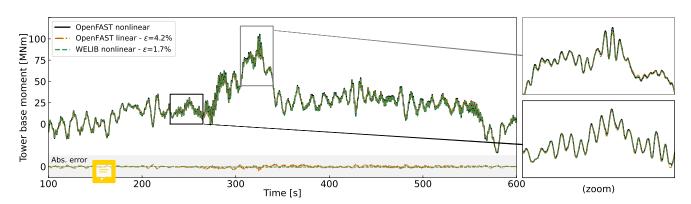


the operating condition. The downside is that this method does not provide any of the four advantages offered by the OpenFAST linearization method.

#### 3.6.3 Verification of the section loads calculation

To verify the calculation of the section loads, we use the same "turbulent step" wind field and irregular sea state that was used in Section 3.4.4. We assume that the time series of q,  $\dot{q}$  and  $\ddot{q}$  are entirely known, extracted from the OpenFAST simulation. These time series are provided to the two section loads algorithms: the WELIB nonlinear algorithm, and the OpenFAST linear algorithm.

We run two sets of virtual sensing. In the "ideal" set, the loads at the tower top are extracted from OpenFAST results and provided to the two virtual sensing algorithms. In this ideal case, the linearized operating points of the OpenFAST linear model is set as the mean of each of the OpenFAST time series values. Results for the ideal case are provided in Figure 7. The two algorithms are able to reproduce the section loads of OpenFAST with relatively high accuracy, which verifies our two



**Figure 7.** Tower fore-aft bending moment for the "turbulent step" and an irregular sea state as calculated by OpenFAST and compared to the WELIB nonlinear and OpenFAST linear method. The motion of the structure is determined by OpenFAST and provided to the two algorithms. The tower-top loads are also provided to the algorithms ("ideal" case, as opposed to Figure 8).

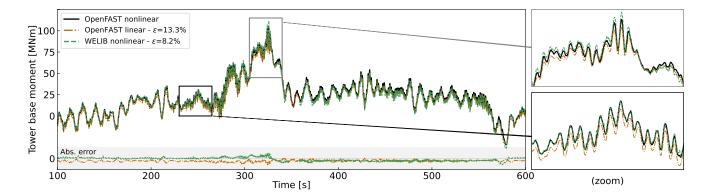
calculation procedures.

In the second set, labeled "unknown thrust", the tower top loads are not provided to the algorithms, but instead, the aerodynamic estimator mentioned in Section 3.4.4 is used to estimate the aerodynamic loads. This time, we do not set the linearized operating point of the OpenFAST linear model to the mean value of the time series, but set it to the static equilibrium (without loading). The results are provided in Figure 8. The accuracy of the section loads calculation is seen to deteriorate when the aerodynamic loads are estimated with the aerodynamic estimator, which is expected. The damage equivalent load computed with a Wöhler slope of m=5 is found to be 3.7% lower with the OpenFAST linear method and 1.2% lower with the YAMS nonlinear method compared to the value for reference signal.

The performances of both algorithms remain satisfactory because we observe that the extrapolated signals follow the reference OpenFAST nonlinear simulation. The relative error obtained with the OpenFAST linear algorithm is higher (13.3%) than







**Figure 8.** Tower fore-aft bending moment for the "turbulent step" and an irregular sea state as calculated by OpenFAST and compared to the WELIB nonlinear and the OpenFAST linear method. The motion of the structure is determined by OpenFAST and provided to the two other algorithms. The tower-top loads are estimated using the aerodynamic estimator ("unknown thrust" case, as opposed to the ideal case presented in Figure 7)

the one obtained using the WELIB nonlinear method (8.2%). The main source of error in the linear model is associated with the fact that the linearization point was not tuned for this specific simulation. It is our simplifying design choice to use only one linearization operating point throughout. Because of the loss of accuracy associated with this design choice, we will use the WELIB nonlinear algorithm in the digital twin for the calculation of section loads.

We note that the variable that affects the most the fore-aft section loads is the platform pitch ( $\phi_y$ ), the tower fore-aft bending degree of freedom ( $q_t$ ), and then, the aerodynamic thrust. In this section, we assumed that all the states where known (including  $\phi_y$  and  $q_t$ ), leading to great accuracy in the estimation of the section loads. The final verification step consists of providing estimated states to the algorithm, which is the topic of the next section.

# 4 Applications of the digital twin

In section 3, the different components of the digital twin were introduced and tested using increasing level of complexity. In this section, we combine the different components to form the digital twin. We begin using numerical experiments from OpenFAST (see Section 2.3.2), similar to what was done in the previous section, before using measurements from the TetraSpar prototype.

#### 4.1 Numerical experiment

First, we use the same "turbulent step" wind field and sea state that was used throughout section 3. The augmented states of the system are determined at each time step using the state estimator described in Section 3.5. The measurements (see Table 1) are taken from the nonlinear OpenFAST simulation. The wind speed and aerodynamic loads are estimated using the aerodynamic estimator described in Section 3.4. The linear model is derived from linearized OpenFAST while the section loads in the tower are obtained using the WELIB virtual sensing algorithm described in Section 3.6. The estimates from the digital twin are





compared with the reference nonlinear OpenFAST simulation results in Figure 9. A visual inspection of the time series reveals

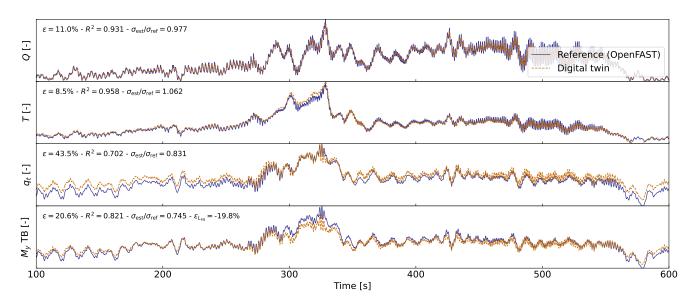


Figure 9. Estimated signals from the digital twin compared to results from an nonlinear OpenFAST simulation using the turbulent-step numerical experiment. From top to bottom: aerodynamic torque (Q), aerodynamic thrust (T), tower-top position  $(q_t)$ , tower-bottom fore-aft bending moment  $(M_y, TB)$ . Results are made dimensionless for confidentiality reasons.

that the digital twin is able to capture the main trends and fluctuations of the different signals. The match can be considered remarkable given that only the sensors provided in Table 1 are used by the digital twin. Metrics such as mean relative error  $(\epsilon)$ , and coefficient of determination  $(R^2)$  are indicated on the figure. Despite the visually appealing match, the metrics indicate that the tower-bottom moment has a mean error of  $\epsilon = 21\%$ . The damage equivalent load of the tower-bottom moment is underestimated by  $\tilde{\epsilon}_{L_{eq}} = -21\%$ , where we define:

377 
$$\tilde{\epsilon}(L_{eq}) = \frac{L_{eq,\text{ref}} - L_{eq,\text{ref}}}{L_{eq,\text{ref}}}$$
(17)

Differences in damage equivalent loads typically indicate differences in the frequency content of the signals. We compare the frequency content of the estimated signals with the reference signals in Figure 10. The low-frequency content (below 1 Hz) is reasonably well captured, in line with the visual inspection of Figure 9. Unfortunately, no clear trend is found for the high frequency content: the power spectra of the aerodynamic loads indicate an underestimation whereas the spectra of the tower-top position and tower-bottom bending moment tend to have higher energy content. As shown in previous studies (Branlard et al., 2020a), adequate filtering of the input measurements can be used to tune the energy content at high frequencies.

To quantify the errors in the estimation under a wider set of operating conditions, we ran 10-min simulations for a set of wind speeds under normal turbulent conditions and sea states. We selected wind speeds from 5 to 20 m/s using 10 different seeds per bin of wind speed. The seeds are used to randomise the turbulent field and sea states. The wind speed range is selected such as to avoid cut-in and cut-out events where the aerodynamic estimator is not expected to perform well. The turbulence

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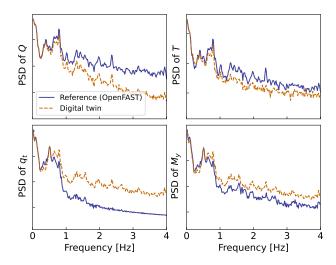


Figure 10. Power spectral density of the time series presented in Figure 9. A logarithmic scale is used on the y axis.

intensity is selected based on the normal turbulence model for a turbine of class "A". The wave height and wave period are set as function of the wind speed as:  $H_s(U) = 0.16U + 1$  and  $T_p = 0.09U + 5.57$ , based on the sea state measurements at the test site. OpenFAST simulations were run for each case, and then the digital twin was run using these numerical measurements. A summary of the mean relative error on some key estimated quantities is given in Figure 11. We observe that the mean relative

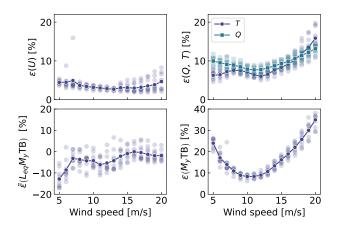


Figure 11. Mean relative error of estimated signals for various wind speed and seeds. Clockwise: wind speed (U), aerodynamic loads, tower-bottom moment  $(M_y \text{ TB})$ , and damage equivalent load of the tower-bottom moment  $(L_{eq,M_y} \text{ TB})$ . The individual simulations are indicated by transparent markers. The average over each seed is indicated using plain lines.

error of the wind speed and aerodynamic loads are between 5% and 15% with a tendency for larger errors on the aerodynamic loads at low and high wind speeds. The error further propagates within the system and the tower-bottom moment is estimated with a relative error between 10% and 40%. The error levels indicate that the aerodynamic estimator, which is based on quasi-

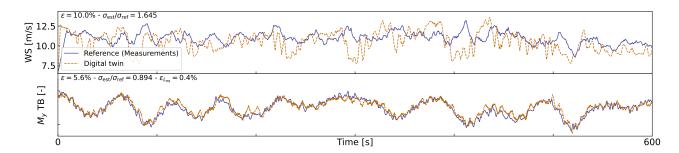




steady rotor-averaged aerodynamics, cannot fully capture the dynamic aerodynamic state of the rotor in floating conditions. In general, the digital twin lacks sufficient information to fully capture the tower-top loads and the frequency content of the system. It is expected that placing additional sensors, such as accelerometers or load cells along the tower, can significantly improve the estimation of the tower loads (in that case, we would either use OpenFAST linearization outputs, or, an extended Kalman filter and a non-linear model for the outputs). As seen in Figure 11, the relative error levels on the damage equivalent loads are between -10% and 5%, with the loads being either overestimated or underestimated depending on the wind speed. The structural health monitoring system could potentially use the estimated error levels indicated in Figure 11 to provide a confidence interval on the fatigue life time of the tower. We note that these error levels represent a best case scenario, because we assumed that no noise or biases were present in the measurements. We expect the error levels to increase with additional measurement noise.

### 4.2 Estimations using measurements from the full-scale prototype

In this section, we use measurements from the full-scale TetraSpar prototype installed off the Norwegian coast. Four days of data were selected based on data availability; a wide range of wind speeds are present in the time series. Two days were selected in summer and two in winter to account for potential seasonality. Apart from these criteria, the selection of time series can be considered random. The measurement data is stored as 10-min time series sampled at 25 Hz. The total number of 10-min samples used over the four days is 576. The measurement data is provided to the digital twin to perform the state estimation and virtual sensing. The state estimation is currently 10 times faster than realtime. The virtual sensing step is half realtime but computational improvements are possible, in particular, by using a compiled language instead of Python. The prototype is equipped with load cells at the tower top, middle and bottom, and nacelle wind speed measurements. We use these measurements to compare with the digital twin estimates. A sample of results is provided in Figure 12. The figure illustrates a selected case where the estimation of the tower load is reasonably accurate, with an error on the damage equivalent load of only 0.4%. We note that the wind speed from the measurement is a point measurement, and it is therefore not expected to be



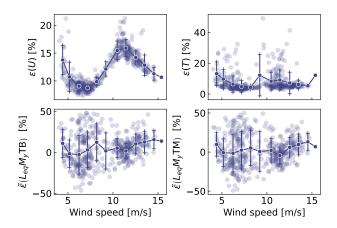
**Figure 12.** Comparison of digital twin outputs with wind speed and tower-bottom moment measurements from the TetraSpar prototype. The measured wind speed comes from a nacelle anenometer and therefore is expected to differ from the rotor-averaged value estimated by the digital twin.

in strong agreement with the digital twin estimate which is representative of a rotor-averaged wind speed.





An aggregate of results from all the 10-min digital twin runs is illustrated in Figure 13. The figure shows relative errors in



**Figure 13.** Similar to Figure 11 but using measurements from the Tetra Spar prototype. Each marker indicate a 10 min simulation result. The bottom plots are for the tower bottom (TB) and tower middle (TM) bending moments.

wind speed, thrust, and damage equivalent loads at the tower bottom and tower middle. As indicated previously, the wind speed from the digital twin and the measurements are different quantities, but the level of error obtained indicates that the digital twin is able to capture the main level of wind speed. The aerodynamic thrust from the aerodynamic estimator is compared with the load cell at the tower top in the fore-aft direction. This is a crude first-order approximation, but the overall estimated levels appears to be on average around 10% from the measured ones. The tower damage equivalent loads are on average within  $\pm 10\%$  of the values obtained from the measurements, but some cases show errors ranging between  $\pm 50\%$ . To give perspective on the large values taken by the metrics, we illustrate two cases with large errors in Figure 14 and Figure 15. In both cases, we

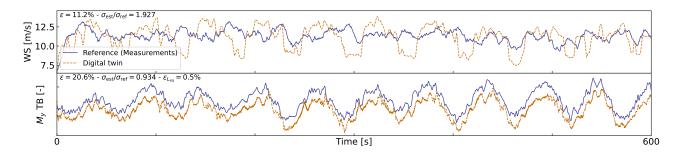


Figure 14. Similar to Figure 12, but for a case where a clear offset is present in the tower loads.

observe that the estimator is capturing the trends and low frequencies with accuracies that, from a pure qualitative perspective, would appear satisfactory. As seen in Figure 14, an offset is present in the signal, which indicates that some physics might be missing from the load virtual sensing, or that the state estimator is failing. In Figure 14, the overall load level is well captured, but the error in the damage equivalent load is  $\epsilon_{L_{eq}}$  is 33%. As illustrated in Figure 10, our current method fails at capturing the





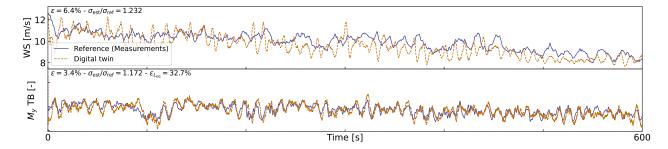


Figure 15. Similar to Figure 12, but for a case where a large error in damage equivalent load is observed.

high-frequency content of the signals, which can have a significant impact on the accuracy of the damage equivalent loads. In spite of these challenges, the average accuracy of 10% is promising and indicates that the current methodology can be used to reconstruct some structural and environmental signals from a limited number of readily-available sensors.

#### 5 Conclusions

 In this work, we implemented, verified, and validated a physics-based digital twin solution applied to a floating offshore wind turbine. The work focused on the estimation of the aerodynamic loads and the section loads along the tower, using a set of measurements that we expect to be available on any existing wind turbine (power, pitch, rotor speed, and tower acceleration), and motion sensors that are likely to be standard measurements for a floating platform (inclination and GPS sensors). The key concept behind our approach consists in using: 1) a Kalman filter to estimate the structural states based on a linear model of the structure and measurements from the turbine, 2) an aerodynamic estimator, and 3) a physics-based virtual sensing procedure to obtain the loads along the tower. An important part of the work consisted in developing the methodology and implementing the tools and models necessary for the aerodynamic estimation, state estimation, and load virtual sensing. We explored two different pathways to obtain models: a suite of Python tools, or OpenFAST linearization. We used components from both approaches for the digital twin.

Using numerical experiments, we found that the accuracy of the individual models were typically in the order of 5%. When comparing the digital twin estimations with the measurements from the TetraSpar prototype, the errors increased to 10%-15% on average for the quantities of interest. Overall, the accuracy of the results appeared promising given the scope of our work, which aimed at illustrating a proof of concept for a floating wind turbine digital twin. We observed non-negligible scatter of results for the estimation of the tower damage equivalent loads that we attributed to the difficulty of capturing high-frequency content. Future work, should therefore explore possible improvements of the method to address this issue. Additional improvements could include: gain-scheduling of the linear models, using nonlinear models and extended Kalman filtering techniques, introducing additional degrees of freedom and a full account of the yawing of the nacelle, adding a model to account for wave excitation forces, introducing additional measurements, improving the robustness of the aerodynamic

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- estimator (in particular beyond the cut-in and cut-out wind speed), and expanding the virtual sensing steps to estimate additional
- 454 signals.
- 455 Author contributions. EB implemented the digital twin and wrote the main corpus of this paper. JJ, CB and JZ provided continuous feedback
- 456 on the project and reviewed the article.
- 457 *Competing interests.* No competing interests are present.
- 458 Code availability. The revised version of this paper will contain a Zenodo link for the repository https://github.com/NREL/wtdigitwin. The
- 459 source code of the digital twin and examples using a generic spar turbine are provided in the github repository.
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- 467 Technologies Office.

#### 468 Appendix A: Linearization of the equations of motion with augmented inputs

- 469 In this section, we describe the procedure used to linearize the structural equations of motion without a knowledge of the external loads,
- 470 which is used to obtain Equation 1. We write the implicit form of the equations of motion as

$$471 \quad \mathbf{e}(\mathbf{q}, \dot{\mathbf{q}}, \ddot{\mathbf{q}}, \tilde{\mathbf{u}}, t) = \mathbf{0} \tag{A1}$$

- 472 where q,  $\dot{q}$ ,  $\ddot{q}$  and  $\tilde{u}$  are the degrees of freedom, velocities, accelerations and "augmented inputs" of the model, respectively. The term
- 473 augmented input is used because the external loads are included in this vector. The external loads are (in general) a function of the degrees
- 474 of freedom. Therefore, we write the augmented input vector as:

475 
$$\tilde{\boldsymbol{u}} = \tilde{\boldsymbol{u}}(\boldsymbol{q}, \dot{\boldsymbol{q}}, \ddot{\boldsymbol{q}}, \boldsymbol{u})$$
 (A2)





- 476 where u is the vector of inputs in the classical sense, that is, consisting of system inputs that do not depend on the degrees of freedom (for
- 477 instance, the wave elevation). The operating point is written using the subscript "0", and defined as:

478 
$$\mathbf{e}(q_0, \dot{q}_0, \ddot{q}_0, \tilde{u}_0, t) = \mathbf{0}$$
 (A3)

- 479 We perturb each variable, as  $\mathbf{q} = \mathbf{q}_0 + \delta \mathbf{q}$ ,  $\dot{\mathbf{q}} = \dot{\mathbf{q}}_0 + \delta \dot{\mathbf{q}}$ , etc., where  $\delta$  indicates a small perturbation of the quantities. The perturbation of the
- 480 augmented input is then:

481 
$$\tilde{\boldsymbol{u}} = \tilde{\boldsymbol{u}}(\boldsymbol{q}_0, \dot{\boldsymbol{q}}_0, \boldsymbol{q}_0, \boldsymbol{u}_0) + \frac{\partial \tilde{\boldsymbol{u}}}{\partial \boldsymbol{q}} \Big|_{0} \delta \boldsymbol{q} + \frac{\partial \tilde{\boldsymbol{u}}}{\partial \dot{\boldsymbol{q}}} \Big|_{0} \delta \dot{\boldsymbol{q}} + \frac{\partial \tilde{\boldsymbol{u}}}{\partial \dot{\boldsymbol{u}}} \Big|_{0} \delta \dot{\boldsymbol{q}} + \frac{\partial \tilde{\boldsymbol{u}}}{\partial \boldsymbol{u}} \Big|_{0} \delta \boldsymbol{u}$$
 (A4)

- 482 where | 0 indicates that the expressions are evaluated at the operating point. The linearized equations are obtained using a Taylor-Series
- 483 expansion:

484 
$$\left[ \boldsymbol{M}_{0} - \boldsymbol{Q}_{0} \left. \frac{\partial \tilde{\boldsymbol{u}}}{\partial \ddot{\boldsymbol{q}}} \right|_{0} \right] \delta \ddot{\boldsymbol{q}} + \left[ \boldsymbol{C}_{0} - \boldsymbol{Q}_{0} \left. \frac{\partial \tilde{\boldsymbol{u}}}{\partial \dot{\boldsymbol{q}}} \right|_{0} \right] \delta \dot{\boldsymbol{q}} + \left[ \boldsymbol{K}_{0} - \boldsymbol{Q}_{0} \left. \frac{\partial \tilde{\boldsymbol{u}}}{\partial \boldsymbol{q}} \right|_{0} \right] \delta \boldsymbol{q} = \boldsymbol{Q}_{0} \left. \frac{\partial \tilde{\boldsymbol{u}}}{\partial \boldsymbol{u}} \right|_{0} \delta \boldsymbol{u}$$
(A5)

485 with

494

486 
$$M_0 = -\frac{\partial \mathbf{e}}{\partial \ddot{\mathbf{q}}}\Big|_0$$
,  $C_0 = -\frac{\partial \mathbf{e}}{\partial \dot{\mathbf{q}}}\Big|_0$ ,  $K_0 = -\frac{\partial \mathbf{e}}{\partial \mathbf{q}}\Big|_0$ ,  $Q_0 = \frac{\partial \mathbf{e}}{\partial u}\Big|_0$  (A6)

and where  $M_0$ ,  $C_0$ ,  $K_0$  are the linear mass, damping, and stiffness matrices,  $Q_0$  is the linear forcing vector, also called input matrix.

#### 488 Appendix B: Transfer of a Jacobian from one destination point to another

- 489 The Jacobians provided by OpenFAST and MAP are provided at given nodes of the structure (e.g. the hydrodynamic nodes, or the fairleads).
- 490 In this section, we highlight the procedure to transfer these Jacobians to another node (the platform reference point) assuming a rigid-body
- 491 relationship between the nodes. The procedure is used in this work to compute the linear  $6 \times 6$  matrix for the hydrodynamics and mooring
- 492 dynamics in Section 3.3.2. We obtain different relationships depending if the destination point is assumed to be displaced or not.

#### 493 B1 Transfer of Jacobians between two points

We consider a point source (noted S) and a destination point (noted D). The notations are illustrated in Figure B1. We assume a rigid body

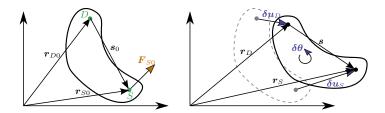


Figure B1. Rigid-body kinematics with the loads from one source point (S) transferred to ta destination point (D), assuming small motion of the points.

495 relationship between the two points. The forces and moments at the destination and source are related as follows:

496 
$$F_D = F_S$$
 (B1)

497 
$$M_D = M_S + \tilde{s}F_S$$
 (B2)





- 498 where  $s = r_S r_D$  is the vector from destination point to the source point,  $F_S$  and  $M_S$  are the force and moments, respectively, at point
- 499 S, and the tilde notation refers to the skew symmetric matrix which is a matrix representation of the cross product. We seek to linearize
- 500 Equation B1 and Equation B2 for small displacements and rotations of the destination and source nodes. In particular, we seek to express
- 501 the Jacobians at the destination node as function of the source node, assuming a rigid-body relationship between the two. The rigid-body
- 502 relationship linking the small displacements ( $\delta u$ ) and small rotations ( $\delta \theta$ ) of the source and destination points is:

503 
$$\delta \boldsymbol{u}_D = \delta \boldsymbol{u}_S + \tilde{\boldsymbol{s}}_0 \delta \boldsymbol{\theta}_S$$

$$\delta \theta_D = \delta \theta_S \tag{B3}$$

- 505 where  $s_0$  is the vector between the source and destination points at the operating point (prior to the perturbation). The Jacobians of the
- transformations given in Equation B3 (and its inverse) are:

$$\begin{bmatrix}
\frac{\partial \mathbf{u}_{D}}{\partial \mathbf{u}_{S}} & \frac{\partial \mathbf{u}_{D}}{\partial \boldsymbol{\theta}_{S}} \\
\frac{\partial \boldsymbol{\theta}_{D}}{\partial \mathbf{u}_{S}} & \frac{\partial \boldsymbol{\theta}_{D}}{\partial \boldsymbol{\theta}_{S}}
\end{bmatrix} = \begin{bmatrix}
\mathbf{I} & \tilde{\mathbf{s}}_{\mathbf{0}} \\
\mathbf{0} & \mathbf{I}
\end{bmatrix}, \qquad \begin{bmatrix}
\frac{\partial \mathbf{u}_{S}}{\partial \mathbf{u}_{D}} & \frac{\partial \mathbf{u}_{S}}{\partial \boldsymbol{\theta}_{D}} \\
\frac{\partial \boldsymbol{\theta}_{S}}{\partial \mathbf{u}_{D}} & \frac{\partial \boldsymbol{\theta}_{S}}{\partial \boldsymbol{\theta}_{D}}
\end{bmatrix} = \begin{bmatrix}
\mathbf{I} & -\tilde{\mathbf{s}}_{\mathbf{0}} \\
\mathbf{0} & \mathbf{I}
\end{bmatrix}$$
(B4)

508 To linearize Equation B1 and Equation B2, we introduce the following perturbations:

509 
$$F_D = F_{D0} + \delta F_D, \quad F_S = F_{S0} + \delta F_S$$
 (B5)

510 
$$M_D = M_{D0} + \delta M_D$$
,  $M_S = M_{S0} + \delta M_S$ , (B6)

511 where the subscript 0 indicates values at the operating point. At the operating point, Equation B1 and Equation B2 are satisfied, that is:

512 
$$F_{D0} = F_{S0}$$
 (B7)

513 
$$M_{D0} = M_{S0} + \tilde{\mathbf{s}}_0 F_{S0}$$
 (B8)

#### 514 Transfer of forces

515 Inserting Equation B5 into Equation B1 leads to:

516 
$$\mathbf{F}_{D0} + \delta \mathbf{F}_D = \mathbf{F}_{S0} + \delta \mathbf{F}_S$$
 (B9)

517 Which, using Equation B7, leads to:

518 
$$\delta \boldsymbol{F}_D = \delta \boldsymbol{F}_S$$
 (B10)

- The Jacobians of the loads at node D with respect to the displacements at node D are then obtained by applying the chain rule to Equation B10
- 520 and making use of the Jacobian of the displacements given in the right of Equation B4. For instance, for the force:

521 
$$\frac{\partial \mathbf{F}_{D}}{\partial \mathbf{u}_{D}} = \frac{\partial \mathbf{F}_{S}}{\partial \mathbf{u}_{S}} \frac{\partial \mathbf{u}_{S}}{\partial \mathbf{u}_{D}} + \frac{\partial \mathbf{F}_{S}}{\partial \mathbf{\theta}_{S}} \frac{\partial \mathbf{\theta}_{S}}{\partial \mathbf{u}_{D}} = \frac{\partial \mathbf{F}_{S}}{\partial \mathbf{u}_{S}}$$
522 
$$\frac{\partial \mathbf{F}_{D}}{\partial \mathbf{\theta}_{D}} = \frac{\partial \mathbf{F}_{S}}{\partial \mathbf{u}_{S}} \frac{\partial \mathbf{u}_{S}}{\partial \mathbf{\theta}_{D}} + \frac{\partial \mathbf{F}_{S}}{\partial \mathbf{\theta}_{S}} \frac{\partial \mathbf{\theta}_{S}}{\partial \mathbf{\theta}_{D}} = \frac{\partial \mathbf{F}_{S}}{\partial \mathbf{\theta}_{S}} - \frac{\partial \mathbf{F}_{S}}{\partial \mathbf{u}_{S}} \tilde{\mathbf{s}}_{0}$$
(B11)

- 523 For the transfer of the moments, the relationship will be different whether the moments are transferred at the undisplaced destination point,
- 524 or the displaced destination point.





# 525 Moments at the undisplaced destination point

- 526 In this section, the moments are transferred to the undisplaced destination point. The vector from undisplaced destination point to the
- 527 displaced source is:

$$528 \quad r = s_0 + \delta u_S \tag{B12}$$

529 Introducing Equation B6 and Equation B12 into Equation B2, and temporarily using the "x" notation instead of the tilde notation:

530 
$$M_{D0} + \delta M_D = M_{S0} + \delta M_S + s_0 \times F_{S0} + s_0 \times \delta F_S + \delta u_S \times F_{S0} + \delta u_S \times \delta F_S$$
 (B13)

531 Making use of Equation B8, neglecting the non-linear term ( $\delta u_S \times \delta F_S$ ) and reintroducing the tilde notation, leads to:

532 
$$\delta M_D = \delta M_S + \tilde{\mathbf{s}}_0 \delta F_S - \tilde{F}_{S0} \delta \mathbf{u}_S$$
 (B14)

- 533 The Jacobians of the moments at the undisplaced node D with respect to the displacements at node D are then obtained by applying the
- 534 chain rule to Equation B14:

535 
$$\frac{\partial M_D}{\partial u_D} = \frac{\partial M_S}{\partial u_S} \frac{\partial u_S}{\partial u_D} + \frac{\partial M_S}{\partial \theta_S} \frac{\partial \theta_S}{\partial u_D} + \tilde{s}_0 \left[ \frac{\partial F_S}{\partial u_S} \frac{\partial u_S}{\partial u_D} + \frac{\partial F_S}{\partial \theta_S} \frac{\partial \theta_S}{\partial u_D} \right] - \tilde{F}_{S0} \frac{\partial u_S}{\partial u_D}$$
536 
$$= \frac{\partial M_S}{\partial u_S} + \tilde{s}_0 \frac{\partial F_S}{\partial u_S} - \tilde{F}_{S0}$$
(B15)

537 and

538 
$$\frac{\partial M_{D}}{\partial \theta_{D}} = \frac{\partial M_{S}}{\partial \theta_{S}} \frac{\partial \theta_{S}}{\partial \theta_{D}} + \frac{\partial M_{S}}{\partial u_{S}} \frac{\partial u_{S}}{\partial \theta_{D}} + \tilde{s}_{0} \left[ \frac{\partial F_{S}}{\partial \theta_{S}} \frac{\partial \theta_{S}}{\partial \theta_{D}} + \frac{\partial F_{S}}{\partial u_{S}} \frac{\partial u_{S}}{\partial \theta_{D}} \right] - \tilde{F}_{S0} \frac{\partial u_{S}}{\partial \theta_{D}}$$
539 
$$= \frac{\partial M_{S}}{\partial \theta_{S}} - \frac{\partial M_{S}}{\partial u_{S}} \tilde{s}_{0} + \tilde{s}_{0} \frac{\partial F_{S}}{\partial \theta_{S}} - \tilde{s}_{0} \frac{\partial F_{S}}{\partial u_{S}} \tilde{s}_{0} + \tilde{F}_{S0} \tilde{s}_{0}$$
(B16)

# 540 Jacobian relationships at the undisplaced destination point

- 541 Equation B11, Equation B16 and Equation B15 can be gathered in matricial form to relate the different Jacobians between the source point
- 542 and the undisplaced destination point:

$$\begin{bmatrix}
\frac{\partial F_D}{\partial u_D} & \frac{\partial F_D}{\partial \theta_D} \\
\frac{\partial M_D}{\partial u_D} & \frac{\partial M_D}{\partial \theta_D}
\end{bmatrix}_{\text{undisplaced}} = \begin{bmatrix}
\mathbf{I} & \mathbf{0} \\
\tilde{\mathbf{s}}_0 & \mathbf{I}
\end{bmatrix} \begin{bmatrix}
\frac{\partial F_S}{\partial u_S} & \frac{\partial F_S}{\partial \theta_S} \\
\frac{\partial M_S}{\partial u_S} & \frac{\partial M_S}{\partial \theta_S}
\end{bmatrix} \begin{bmatrix}
\mathbf{I} & -\tilde{\mathbf{s}}_0 \\
\mathbf{0} & \mathbf{I}
\end{bmatrix} + \begin{bmatrix}
\mathbf{0} & \mathbf{0} \\
-\tilde{\mathbf{F}}_{S0} & \tilde{\mathbf{F}}_{S0}\tilde{\mathbf{s}}_0
\end{bmatrix}$$
(B17)

#### 544 Moments at the displaced destination point

- 545 In this section, the moments are transferred to the displaced destination point. The vector from the displaced destination point to the displaced
- 546 source is:

$$547 \quad r = s_0 + \delta u_S - \delta u_D = s_0 - \tilde{s}_0 \delta \theta_S \tag{B18}$$

548 Introducing Equation B6 and Equation B18 into Equation B2, and temporarily using the "x" notation instead of the tilde notation:

549 
$$M_{D0} + \delta M_D = M_{S0} + \delta M_S + s_0 \times F_{S0} + s_0 \times \delta F_S - (s_0 \times \delta \theta_S) \times F_{S0} - (s_0 \times \delta \theta_S) \times \delta F_S$$
 (B19)





550 Making use of Equation B8, neglecting the non-linear term  $((s_0 \times \delta \theta_S) \times \delta F_S)$  and reintroducing the tilde notation, leads to:

551 
$$\delta \mathbf{M}_D = \delta \mathbf{M}_S + \tilde{\mathbf{s}}_0 \delta \mathbf{F}_S + \tilde{\mathbf{F}}_{S0} \tilde{\mathbf{s}}_0 \delta \boldsymbol{\theta}_S$$
 (B20)

The Jacobians of the loads at the displaced node D with respect to the displacements at node D are then obtained by applying the chain rule

553 to Equation B20 and making use of the Jacobian of the displacements given in the right of Equation B4.

554 
$$\frac{\partial M_D}{\partial u_D} = \frac{\partial M_S}{\partial u_S} \frac{\partial u_S}{\partial u_D} + \frac{\partial M_S}{\partial \theta_S} \frac{\partial \theta_S}{\partial u_D} + \tilde{s}_0 \frac{\partial F_S}{\partial u_S}$$
555 
$$= \frac{\partial M_S}{\partial u_S} + \tilde{s}_0 \frac{\partial F_S}{\partial u_S}$$
(B21)

556 and

565

557 
$$\frac{\partial M_{D}}{\partial \theta_{D}} = \frac{\partial M_{S}}{\partial u_{S}} \frac{\partial u_{S}}{\partial \theta_{D}} + \frac{\partial M_{S}}{\partial \theta_{S}} \frac{\partial \theta_{S}}{\partial \theta_{D}} + \tilde{\mathbf{s}}_{0} \frac{\partial \mathbf{F}_{S}}{\partial \theta_{D}} + \tilde{\mathbf{F}}_{S0} \tilde{\mathbf{s}}_{0}$$
558 
$$= \frac{\partial M_{S}}{\partial \theta_{S}} - \frac{\partial M_{S}}{\partial u_{S}} \tilde{\mathbf{s}}_{0} + \tilde{\mathbf{s}}_{0} \frac{\partial \mathbf{F}_{S}}{\partial \theta_{D}} + \tilde{\mathbf{F}}_{S0} \tilde{\mathbf{s}}_{0}$$
559 
$$= \frac{\partial M_{S}}{\partial \theta_{S}} - \frac{\partial M_{S}}{\partial u_{S}} \tilde{\mathbf{s}}_{0} + \tilde{\mathbf{s}}_{0} \frac{\partial \mathbf{F}_{S}}{\partial \theta_{S}} - \tilde{\mathbf{s}}_{0} \frac{\partial \mathbf{F}_{S}}{\partial u_{S}} \tilde{\mathbf{s}}_{0} + \tilde{\mathbf{F}}_{S0} \tilde{\mathbf{s}}_{0}$$
(B22)

# 560 Jacobian relationships at the displaced destination point

561 Equation B11, Equation B22 and Equation B21 can be gathered in matricial form to relate the different Jacobians:

$$562 \quad \begin{bmatrix} \frac{\partial F_D}{\partial u_D} & \frac{\partial F_D}{\partial \theta_D} \\ \frac{\partial M_D}{\partial u_D} & \frac{\partial M_D}{\partial \theta_D} \end{bmatrix}_{\text{displaced}} = \begin{bmatrix} I & \mathbf{0} \\ \tilde{\mathbf{s}}_0 & I \end{bmatrix} \begin{bmatrix} \frac{\partial F_S}{\partial u_S} & \frac{\partial F_S}{\partial \theta_S} \\ \frac{\partial M_S}{\partial u_S} & \frac{\partial M_S}{\partial \theta_S} \end{bmatrix} \begin{bmatrix} I & -\tilde{\mathbf{s}}_0 \\ \mathbf{0} & I \end{bmatrix} + \begin{bmatrix} \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \tilde{F}_{S0}\tilde{\mathbf{s}}_0 \end{bmatrix}$$
(B23)

# 563 B2 Relationships at the displaced destination point for multiple source points

We now consider the case where multiple point sources are present. The derivation can be seen as a generalization of the previous case between two points, but special care is needed. The notations are illustrated in Figure B2. The loads at the destination points are obtained as:

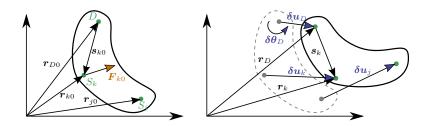


Figure B2. Rigid-body kinematics with the loads from multiple source points  $(S_i)$ , transferred to a destination point (D)

 $\mathbf{F}_D = \sum_k \mathbf{F}_k \tag{B24}$ 

567 
$$M_D = \sum_k M_k + \tilde{s}_k F_k$$
 (B25)





- where k is an index looping over all points of the rigid structure. To shorten notations, we define the vector between the destination point and 568
- 569 a given point as:

$$570 s_k = r_k - r_D (B26)$$

$$571 \quad s_{k0} = r_{k0} - r_{D0} \tag{B27}$$

- where  $s_k$  is the vector between the displaced points and  $s_{k0}$  is the vector prior to the displacement (at the operating condition). Due to the 572
- rigid-body assumption, the elementary displacements of the points are related as follows: 573

574 
$$\delta \boldsymbol{u}_D = \delta \boldsymbol{u}_j + \tilde{\boldsymbol{s}}_{j0} \delta \boldsymbol{\theta}_j$$

$$\delta \theta_D = \delta \theta_j \tag{B28}$$

576 from which one obtains the following useful relationships:

577 
$$\frac{\partial u_j}{\partial u_D} = I$$
,  $\frac{\partial \theta_j}{\partial u_D} = O$ ,  $\frac{\partial u_j}{\partial \theta_D} = -\tilde{s}_{j0}$ ,  $\frac{\partial \theta_j}{\partial \theta_D} = I$ ,  $\frac{\partial \theta_j}{\partial \theta_k} = I\delta_{jk}$ ,  $\frac{\partial \theta_j}{\partial u_k} = O$  (B29)

Using a similar Taylor expansion as for the case with two nodes, the perturbation loads are obtained as:

$$\delta \boldsymbol{F}_D = \sum_k \delta \boldsymbol{F}_k \tag{B30}$$

580 
$$\delta \boldsymbol{M}_D = \sum_{k} \delta \boldsymbol{M}_k + \tilde{\boldsymbol{s}}_{k0} \delta \boldsymbol{F}_k + \tilde{\boldsymbol{F}}_{k0} (\tilde{\boldsymbol{s}}_{k0} \delta \boldsymbol{\theta}_k)$$
 (B31)

The chain rule for a given quantity of interest (Q) is obtained by summing over all the elementary variables: 581

582 
$$dQ = \sum_{j} \frac{\partial Q}{\partial \mathbf{u}_{j}} d\mathbf{u}_{j} + \frac{\partial Q}{\partial \boldsymbol{\theta}_{j}} d\boldsymbol{\theta}_{j}$$
 (B32)

583 For instance, the application of the chain rule to  $F_D$  and using Equation B30 leads to:

584 
$$\frac{\partial \mathbf{F}_{D}}{\partial \mathbf{u}_{D}} = \sum_{j} \frac{\partial \mathbf{F}_{D}}{\partial \mathbf{u}_{j}} \frac{\partial \mathbf{u}_{j}}{\partial \mathbf{u}_{D}} + \frac{\partial \mathbf{F}_{D}}{\partial \boldsymbol{\theta}_{j}} \frac{\partial \boldsymbol{\theta}_{j}}{\partial \mathbf{u}_{D}} = \sum_{j} \sum_{k} \frac{\partial \mathbf{F}_{k}}{\partial \mathbf{u}_{j}} \frac{\partial \mathbf{u}_{j}}{\partial \mathbf{u}_{D}} + \frac{\partial \mathbf{F}_{k}}{\partial \boldsymbol{\theta}_{j}} \frac{\partial \boldsymbol{\theta}_{j}}{\partial \mathbf{u}_{D}} = \sum_{j} \sum_{k} \frac{\partial \mathbf{F}_{k}}{\partial \mathbf{u}_{j}}$$
(B33)

585 Eventually, the Jacobians at the displaced destination node are obtained as:

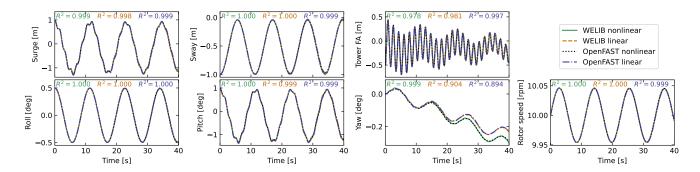
$$\begin{bmatrix}
\frac{\partial F_{D}}{\partial u_{D}} & \frac{\partial F_{D}}{\partial \theta_{D}} \\
\frac{\partial M_{D}}{\partial u_{D}} & \frac{\partial M_{D}}{\partial \theta_{D}}
\end{bmatrix}_{\text{displaced}} = \sum_{j} \left\{ \sum_{k} \begin{pmatrix} \begin{bmatrix} I & \mathbf{0} \\ \tilde{\mathbf{s}}_{k0} & I \end{bmatrix} \begin{bmatrix} \frac{\partial F_{k}}{\partial u_{j}} & \frac{\partial F_{k}}{\partial \theta_{j}} \\ \frac{\partial M_{k}}{\partial u_{j}} & \frac{\partial M_{k}}{\partial \theta_{j}} \end{bmatrix} \begin{bmatrix} I & -\tilde{\mathbf{s}}_{j0} \\ \mathbf{0} & I \end{bmatrix} \right\} + \begin{bmatrix} \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \tilde{F}_{j0}\tilde{\mathbf{s}}_{j0} \end{bmatrix} \right\}$$
(B34)

#### **Appendix C: Verification of the linear models** 587

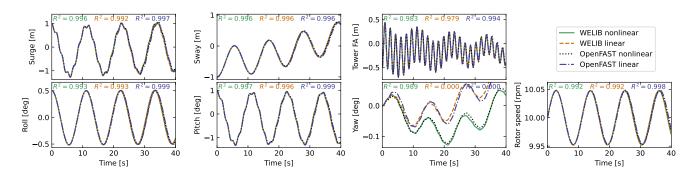
- In this section, we supplement the results given in Section 3.3.3, by showing free-decay results without hydrodynamics (no added mass, 588
- damping, hydrostatics). We show results with the structure only in Figure C1, and results with the structure and moorings in Figure C2. 589
- These results also include the nonlinear WELIB formulation. A strong agreement is found between the nonlinear OpenFAST and WELIB 590
- 591 models, and between the linear OpenFAST and WELIB models. The yaw degree of freedom appears to be more challenging to capture for
- 592 the linear models.







**Figure C1.** Free decay of the structure using non linear and linear models for a case including only the structure (no moorings, no hydrodynamics). Time series of the main DOFs.



**Figure C2.** Free decay of the structure using non linear and linear models for a case including moorings (no hydrodynamics). Time series of the main DOFs.

#### 593 Appendix D: Computation of section loads

594 595

596

597

In this section, we describe the nonlinear calculation procedure used in Section 3.6.2 to assess the section loads along the tower based on estimates of the structure kinematics and the loads at the tower top. For conciseness, in this appendix, we use x and z for the coordinates along the tower fore-aft and tower height, respectively, instead of  $x_T$  and  $z_T$ .

# D1 Tower fore-aft bending moment and shear force

The fore-aft and side-side loads are computed the same way, therefore this section focuses on the fore-aft direction. The sectional fore-aft bending moment at a given tower height *z* is determined as:

600 
$$\mathcal{M}_y(z) = \mathcal{M}_{y,\text{top}} - \int_{z}^{L_T} S_x(z')dz'$$
 (D1)

where  $\mathcal{M}_{y,\text{top}}$  is the fore-aft bending moment at the tower top and  $S_x$  is the shear force in the x direction, obtained as:

602 
$$S_x(z) = \int_{-\infty}^{L_T} p_{x,\text{all}}(z') dz'$$
 (D2)





- 603 where  $p_{x,\text{all}}$  is the force per length acting on the tower section in the fore-aft direction, including contributions from the external loads
- 604 (aerodynamic loads on the structure), inertial loads due to the acceleration of the structure (including gravity), and nonlinear correction terms
- from the loads in the z direction ( $p \Delta$  effect, including self-weight effects). The different contributions are written as follows:

606 
$$p_{x,\text{all}} = p_{x,\text{ext}} + p_{x,\text{corr}} - p_{x,\text{acc}}$$
 (D3)

- 607 In this work, we neglect the external loads on the tower,  $p_{x,\text{ext}} = 0$  (aerodynamic loads on the tower are typically small relative to rotor-thrust
- loads for an operating wind turbine). The acceleration contribution is  $p_{x,acc} = -m(z)(a_{x,struct}(z) a_{x,grav})$ , where m is the mass per length
- along the beam, and  $a_{x,\text{struct}}(z)$  is the acceleration of the section, determined based on the rigid-body acceleration of the floater and the elastic
- 610 motion of the tower  $(\dot{q}_T \text{ and } \ddot{q}_T)$ , and  $a_{x,\text{grav}}$  is the acceleration of gravity in the x direction. The  $p-\Delta$  correction term due to the vertical
- 611 loading is computed as (see Branlard (2019)):

612 
$$p_{x,\text{corr}} = \frac{d^2 \Phi}{d^2 z} \left[ \int_z^L p_z \, dx' + \sum_{z_k \ge z} \mathcal{F}_{z,k} \right] - \frac{d\Phi}{dz} \left[ p_z + \sum_k \mathcal{F}_{z,k} \delta(z - z_k) \right]$$
 (D4)

- 613 where  $p_z$  is the vertical load per length (mostly consisting of the self-weight),  $\mathcal{F}_{z,k}$  is the k-th vertical force acting at point  $z_k$ , and  $\delta$  is the
- Dirac function, and  $\Phi$  is the shape function used to describe the tower displacement field (see Section 2.3.3). In our case, only the vertical
- force acting on top of the tower is present,  $z_1 = L_T$  and  $\mathcal{F}_{z,1} = \mathcal{F}_{z,\text{top}}$ . The procedure is similar to compute the section loads in the y direction
- 616 (using the  $p \Delta$  correction as well).

## 617 D2 Tower and RNA kinematics

- 618 The determination of the tower section loads require a knowledge of the tower kinematics, to compute a<sub>struct</sub>, and the RNA kinematics, to
- 619 compute the inertial contribution to the tower top loads (see Section D3). The position, linear velocity, linear acceleration, rotational speed,
- and rotational acceleration of the floater (point F, body f) are given respectively by:

621 
$$r_F = \{x, y, z\}_i, v_F = \{\dot{x}, \dot{y}, \dot{z}\}_i, a_F = \{\ddot{x}, \ddot{y}, \ddot{z}\}_i,$$
 (D5)

622 
$$\boldsymbol{\omega}_f = \{\dot{\phi}_z, \dot{\phi}_y, \dot{\phi}_z\}_i, \, \dot{\boldsymbol{\omega}}_f = \{\ddot{\phi}_z, \ddot{\phi}_y, \ddot{\phi}_z\}_i$$
 (D6)

- 623 where the notation i indicates that the coordinates of the vector are expressed in the inertial coordinate system. The transformation matrix
- from the floater to the inertial frame is obtained as:  $\mathbf{R}_{f2i} = \mathbf{R}(\phi_x, \phi_y, \phi_z)$ , where  $\mathbf{R}$  is a function computing the rotation matrix. The tower
- base (point T, body t) kinematics are obtained from the floater using rigid body kinematics:

626 
$$r_T = r_F + r_{FT}$$
, (D7)

627 
$$v_T = v_F + \omega_f \times r_{FT}$$
, (D8)

628 
$$a_T = a_F + \omega_f \times (\omega_f \times r_{FT}) + \dot{\omega}_f \times r_{FT},$$
 (D9)

629 
$$\omega_t = \omega_f$$
,  $\dot{\omega}_t = \dot{\omega}_f$ ,  $R_{t2i} = R_{f2i}$  (D10)





630 where  $r_{FT}$  is the vector from the floater point to the tower base. The kinematics of a given tower section (point S, at height z) are given by:

631 
$$r_S = r_T + r_{TS} = r_T + r_{TS_0} + u_S$$
, (D11)

632 
$$v_S = v_T + \omega_t \times r_{TS} + \dot{\boldsymbol{u}}_S,$$
 (D12)

633 
$$a_S = a_T + \omega_t \times (\omega_t \times r_{TS}) + \dot{\omega}_t \times r_{TS} + 2\omega_t \times \dot{u}_S + \ddot{u}_S,$$
 (D13)

$$634 \quad \omega_s = \omega_t + \omega_{ts}, \tag{D14}$$

$$\dot{\boldsymbol{\omega}}_{s} = \dot{\boldsymbol{\omega}}_{t} + \dot{\boldsymbol{\omega}}_{ts} + \boldsymbol{\omega}_{t} \times \boldsymbol{\omega}_{ts}, \tag{D15}$$

- where  $r_{TS_0} = z\hat{z}_t$  is the vector from the tower base to the undeflected section,  $u_S$ ,  $\dot{u}_S$ ,  $\ddot{u}_S$  are the elastic motions of the section computed
- based on the shape function and the generalized coordinates, e.g.  $u_S(z) = \sum_j q_{t,j} \Phi_j = q_t \Phi(z) \hat{x}_t$  (see e.g. Branlard and Geisler (2022)).
- We note that OpenFAST also includes a vertical motion (referred to as a "geometric nonlinearity") associated with the deflection, which we
- are currently neglecting in this work. The transformation matrix from the section to the tower is  $\mathbf{R}_{s2t} = \mathbf{R}(-u_{S,y}', u_{S,x}', 0)$ , where  $u_{S,y}$  and
- 640  $u_{S,x}$  are the components of  $u_S$  in the tower coordinate system, and the prime notation indicates the differentiation with respect to z. The
- of the tower section with respect to the tower base are:

642 
$$\boldsymbol{\omega}_{ts} = \left\{ \dot{u}'_{S,y}, \dot{u}'_{S,x}, 0 \right\}_{t}, \quad \dot{\boldsymbol{\omega}}_{ts} = \left\{ \ddot{u}'_{S,y}, \ddot{u}'_{S,x}, 0 \right\}_{t}$$
 (D16)

- The kinematics of the tower-top point and nacelle (point N, body n) are taken from the last section node (point S with  $z = L_T$ ). Yawing,
- 644 tilting, and rolling of the tower top would change the orientation matrix, rotational velocity and rotational acceleration of the nacelle. These
- 645 kinematics are omitted here for conciseness. The kinematics of the center of mass of the RNA (point G) are obtained using rigid-body
- kinematics (identical to what was used between point F and T).

#### 647 D3 Tower-top loads

648 The tower-top loads are computed as follows:

649 
$$\mathcal{F}_{\text{top}} = \mathcal{F}_{\text{aero}} - \mathcal{F}_{\text{inertia}}$$
 (D17)

650 
$$\mathcal{M}_{top} = \mathcal{M}_{aero} - \mathcal{M}_{inertia}$$
 (D18)

where the aerodynamic loads are transferred to the tower top and where the inertial loads from the rigid-body RNA are:

652 
$$\mathcal{F}_{inertia} = M_{RNA}(a_G - q)$$
 (D19)

653 
$$\mathcal{M}_{\text{inertia}} = r_{NG} \times \mathcal{F}_{\text{inertia}} + J_G \cdot \dot{\omega}_n + \omega_n \times (J_G \cdot \omega_n)$$
 (D20)

- where:  $r_{NG}$  is the vector from the tower top to the center of mass of the RNA,  $M_{RNA}$  is the mass of the RNA,  $J_G$  is the inertia tensor of the
- RNA at it's center of mass,  $a_G$  is the linear acceleration of the center of mass of the RNA,  $\omega_n$  is the rotational acceleration of the RNA,  $\dot{\omega}_n$
- 656 is the rotational acceleration of the nacelle. The load calculation is first done in the coordinate system of the nacelle, and then transferred to
- 657 the coordinate system of the tower where Equation D1 is defined.





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