



Analysis and multi-objective optimisation of model-based wind turbine controllers

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Abstract. The combined wind speed estimator and tip-speed ratio (WSE-TSR) tracking wind turbine control scheme has seen recent and increased traction from the wind industry. The modern control scheme provides a flexible trade-off between power and load objectives. On the other hand, the $K\omega^2$ controller is often used based on its simplicity and steady-state optimality and is taken as a baseline here. This paper investigates the potential benefits of the WSE-TSR tracking controller compared to the baseline by analysis through a frequency-domain framework and by optimal calibration through a systematic procedure. A multi-objective optimisation problem is formulated for calibration with the conflicting objectives of power maximisation and torque fluctuations minimisation. The optimisation problem is solved by approximating the Pareto front based on the set of optimal solutions found by an explorative search. The Pareto fronts obtained for calibration of the baseline and for increasing fidelities of the WSE-TSR tracking controller show that no optimal solution exists, translating into increased power capture with respect to the baseline $K\omega^2$ controller. The frequency-domain analysis, however, shows increased control bandwidth for tip-speed ratio reference tracking for the solution leading to power maximisation. If the objective is to reduce the torque variance, the controller bandwidth decreases with a mild penalty on the energy yield. High-fidelity simulations on the NREL 5 MW reference turbine confirm this trend, proving that, if properly calibrated, the WSE-TSR tracking controller obtains approximately the same generated power of the baseline while reducing torque actuation effort.

1 Introduction

Of all the available renewable energy sources, wind energy is increasingly considered one of the most cost-effective and sustainable with regard to the global demand for clean energy (Watson et al., 2019). The total present wind power capacity installed worldwide is now 837 GW, with year-on-year growth of 12% (Lee and Zhao, 2022). However, this growth rate must quadruple by the end of the decade to meet the net-zero emissions targets set after the Glasgow climate summit (United Nations, 2021; Komusanac et al., 2022). To achieve these ambitious climate goals in an efficient manner, the industry is developing larger turbines with a more flexible rotor assembly and support structure to exploit higher wind speeds (Veers et al., 2019). Increasingly advanced and optimised control technologies are needed to facilitate and enable the increased sizes of wind turbines (Pao and Johnson, 2011).



Variable-speed turbines usually employ a generator torque control strategy to maximise the energy capture in partial load conditions (Bossanyi, 2000; Burton et al., 2011). Maximum power is extracted by operating the turbine at the maximum power coefficient, corresponding to a specific tip-speed ratio and pitch angle (Bottasso et al., 2012). The optimal tip-speed ratio is tracked by varying the generator torque resulting from a closed-loop controller, while the pitch angle is generally kept constant in the partial load region (Pao and Johnson, 2011).

Nowadays, the $K\omega^2$ controller is still the most common partial load region wind turbine torque control used due to its satisfactory performance, ease of derivation, and simple implementation by only requiring a measurement of the rotor or generator speed (Johnson et al., 2006; Ozdemir et al., 2013). Nevertheless, the $K\omega^2$ controller has shortcomings that can result in sub-optimal power tracking performance (Johnson et al., 2004). First, the torque gain K is calculated from modelled wind turbine properties, often subject to assumptions and estimation errors (Abbas et al., 2022). Even if the gain K is initially accurate, the turbine properties can change over time due to, e.g. blade erosion and ice/dirt/bug buildup (Mulders et al., 2023), thereby causing this initial value to be suboptimal (Johnson et al., 2004, 2006). For instance, according to Fingersh and Carlin (1999), a 5% error in the optimal tip-speed ratio can lead to inaccurate K and, consequently, to a cumulative captured energy loss of 1% - 3%. Second, suppose the wind turbine operates in turbulent wind conditions and that K is accurately determined. In that case, the large rotor inertia prevents fast acceleration and thus hinders the tracking of rapid changes in wind speed, leading to a lower operating power coefficient. The torque gain will be suboptimal, consequently impacting the turbine performance. This problem is emphasised for heavy rotors and sharp power coefficient curves (Bossanyi, 2000).

The torque gain K can be calibrated through an Extremum Seeking Control (ESC) acting on the rotor power to overcome the effect of time-varying wind turbine properties (Creaby et al., 2009). While providing an energy capture improvement of 8% - 12% when applied on the Controls Advanced Research Turbine (CART), this control scheme results in being sensitive to wind speed variations (Xiao et al., 2016). Therefore, Rotea (2017) proposes a log-of-power feedback in the ESC algorithm (LP-ESC). Using high-fidelity large eddy simulations, Ciri et al. (2018) demonstrate that this modification renders the controller independent from changes in the mean wind speed.

One way to increase the energy capture for higher turbulence intensity is by reducing the gain K below the nominal value. This choice allows the generator torque to decrease and the rotor to accelerate more quickly in response to a gust. For instance, Johnson et al. (2004) reduced the gain K for the controller of the CART by 10% and observed an increase of 0.5% in captured power. Reducing K improves energy capture and can be easily implemented on any existing wind turbine that uses the $K\omega^2$ controller. However, since the gain reduction factor depends on the turbulence in the wind and no linear correlation can be found between this factor and site condition, choosing a constant value is unrealistic (Johnson et al., 2004).

As a way of providing better rotor acceleration and deceleration, Fingersh and Carlin (1999) proposed the optimally tracking rotor (OTR) controller. This scheme augments the $K\omega^2$ controller with a second term. The additional term is a gain multiplied by the net torque, being the difference between the (estimated) aerodynamic torque and the generator torque contribution resulting from the $K\omega^2$ control law. Subtracting the new term from the original formulation will aid rotor acceleration or deceleration if the wind speed increases or decreases. With this approach applied to the CART, the controller bandwidth for tracking the actual optimal operating point is increased, thereby improving the energy capture by about 1.2% (Fingersh and Carlin, 1999).



60 However, the OTR control scheme relies heavily on correct knowledge of the aerodynamic rotor properties. Incorrect information will inevitably lead to suboptimal operation in transient and steady-state conditions. Another more advanced turbine controller was developed by van der Hooft et al. (2003) and includes pseudo-feedforward control based on an estimation of the rotor-effective wind speed (REWS) to realise an additional pitch control action in partial load. With this strategy, an energy yield increase of 0.9 % was achieved at the expense of larger speed and load variations.

65 To cope with the described disadvantages of the $K\omega^2$ control scheme, combined wind speed estimator and tip-speed ratio (WSE-TSR) tracking control schemes have been recently considered (Abbas et al., 2022). The idea behind this scheme is to use the estimated REWS (Østergaard et al., 2007; Soltani et al., 2013) to calculate an estimate of the desired rotor speed, which in turn is employed as a feedback signal to close the loop by a PI controller. According to Bossanyi (2000), this controller allows tracking the optimal tip-speed ratio even in turbulent wind, with a 1 % power increase compared to the baseline $K\omega^2$, but at the expense of significant power variations.

70 In the work of Boukhezzar and Siguerdidjane (2005), a Kalman filter estimator combined with a rotor speed reference tracking improves by 10 % the power capture when compared with the $K\omega^2$ controller, but no analytical demonstration of its dynamic behaviour was provided. A similar study by Abbas et al. (2022) focused only on a time-domain analysis when comparing the combined estimator-feedback controller with the $K\omega^2$ control law. Earlier work by the current authors (Brandetti et al., 2022) proved that an analytical frequency-domain framework could be a valuable tool for analysing the dynamics of the
75 WSE-TSR tracking controller. However, neither the performance benefits of using such a control scheme over the baseline $K\omega^2$ controller nor the optimal calibration are discussed in (Brandetti et al., 2022).

Therefore, this paper presents the steady-state equivalence and dynamic differences between these $K\omega^2$ and WSE-TSR tracking controllers and proposes a systematic procedure for optimal calibration. Calibration of the parameters in the WSE-TSR tracking control scheme is fundamental to optimising controller performance in terms of power maximisation, load minimisation and stability (Bossanyi, 2000).
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However, the use of classical analysis techniques to calibrate the proposed scheme is complex due to the trade-off between conflicting control requirements, e.g. maximising power production and minimising the loads. Recent studies (Odgaard et al., 2016; Lara et al., 2023) have demonstrated the effectiveness of multi-objective optimisation techniques based on Pareto fronts for tuning wind turbine controllers. For this reason, the calibration of the WSE-TSR tracking controller is formulated as a
85 multi-objective optimisation problem. First, the parameter space of the considered control scheme is explored by a guided search procedure. Subsequently, the set of optimal solutions is found to construct the Pareto front in a trade-off between power maximisation and load minimisation. The solutions found are then assessed using the extended version of the frequency-domain framework, based on (Brandetti et al., 2022), for comparison with the baseline controller. As also shown by Leith and Leithead (1997), analysing a controller in the frequency domain allows for gathering relevant insights into its performance.

90 In this context, the present research aims to illustrate the additional benefits of using the WSE-TSR tracking controller compared to the baseline $K\omega^2$ for partial load control when applied to realistic wind turbine sizes, in terms of two performance metrics widely discussed in the literature: power maximisation and load minimisation (Leith and Leithead, 1997; Leithead and Connor, 2000). Thereby, the following contributions are presented:



- Demonstrating the steady-state similarities and dynamic differences between the WSE-TSR tracking control scheme and the baseline $K\omega^2$ controller in the frequency domain by a universal linear analysis framework.
- Mapping the performance of the fixed-structure WSE-TSR tracking controller for sets of calibration parameters of increasing dimensionality by a guided exploratory search in their constrained parameter spaces.
- Formulating the optimal calibration as a multi-objective problem using Pareto front approximation techniques.
- Exploiting the frequency-domain framework in conjunction with high-fidelity simulations under realistic environmental conditions to showcase and discover the characteristics of an *optimally* calibrated WSE-TSR tracking control scheme to the baseline strategy.

The paper is structured as follows: Section 2 gives a mathematical overview of the WSE-TSR tracking control scheme and baseline $K\omega^2$ controller, together with the assumptions made for their implementation. Based on the nonlinear implementation, Section 3 provides a linear frequency-domain framework analysing the two controllers. Section 4 illustrates the exploration and multi-objective Pareto optimisation strategy for calibrating the WSE-TSR tracking control scheme. Section 5 evaluates the performance of the calibrated WSE-TSR tracking scheme compared to the baseline controller by leveraging the results from the frequency-domain analysis framework and the ones derived from realistic high-fidelity time-domain simulations. Finally, Section 6 summarises the main findings and recommendations for future work.

Prerequisites

This section provides the prerequisites needed for the analysis of the controllers. Estimated quantities and time derivatives are indicated by $\hat{(\cdot)}$ and $\dot{(\cdot)}$, respectively. Values corresponding to a specific operating point are denoted by $(\bar{\cdot})$, whereas values indicating the intended optimal parameters are presented with $(\cdot)_*$. The symbols ω_r , T_g , V and λ , represent the rotational speed, the generator torque, the wind speed and the tip-speed ratio signals in the time domain, while Ω_r , \mathcal{T}_g , \mathcal{V} and Λ represent the corresponding signals in the frequency domain.

In addition, this work relies on a set of assumptions, which are formulated as follows:

Assumption 1.1. *The considered control schemes are analysed in the partial load region with a constant (fine-)pitch angle. For this reason, the power coefficient mapping is only taken as a function of the tip-speed ratio.*

Assumption 1.2. *The generator torque control input and the rotational speed of the turbine are measured signals. The rotor-effective wind speed is considered an unknown and positive disturbance input to the plant.*

Assumption 1.3. *The turbine model information included in the estimator and control framework represents the actual turbine characteristics. This assumption highlights the best-case performance benefits achievable with the WSE-TSR tracking control scheme over the baseline $K\omega^2$ control strategy without capturing the inherent uncertainties of real-world turbine dynamics. The assessment of the effects of model uncertainty on performance levels and control robustness is devoted to future work.*



2 Theory of partial-load control schemes

125 The baseline $K\omega^2$ controller is a well-known, effective and commonly used torque control strategy for maximising energy capture in the partial load operating region (Bossanyi, 2000). Whereas the $K\omega^2$ strategy provides satisfactory performance, it is inflexible in providing a granular trade-off between power and load objectives for present-day wind turbines. Therefore, modern large-scale wind turbines are controlled by either model predictive control (MPC) (Rawlings and Mayne, 2009) or more advanced WSE-TSR tracking schemes to provide such flexibility in the control system. This work focuses on comparing
 130 the baseline strategy with the latter being the WSE-TSR tracking control scheme, which is also often referred to as a power coefficient C_p -tracking scheme in other works (Bossanyi, 2000). In this section, first, the $K\omega^2$ and the WSE-TSR tracking control schemes are derived in their full and nonlinear representations. To this end, the wind turbine system is considered, and the individual required component building blocks are obtained for completing the two schemes.

2.1 Wind turbine

135 The wind turbine system is represented by the first-order model

$$J\dot{\omega}_r = T_r - T_g N, \quad (1)$$

where ω_r represents the rotor speed, and J is the total drivetrain inertia at the low-speed shaft (LSS) side, obtained from the relation $J = J_g N^2 + J_r$, with J_g and J_r , respectively, representing the generator and rotor inertias. The gearbox ratio is defined as the transmission ratio $N = \omega_g / \omega_r$, with ω_g representing the generator speed. The turbine is considered to be subject to a
 140 torque control input $T_g \in \mathbb{R}$, and, according to Assumption 1.1, the aerodynamic rotor torque is given by

$$T_r = \frac{1}{2} \rho A_{\text{rot}} \frac{V^3}{\omega_r} C_p(\lambda), \quad (2)$$

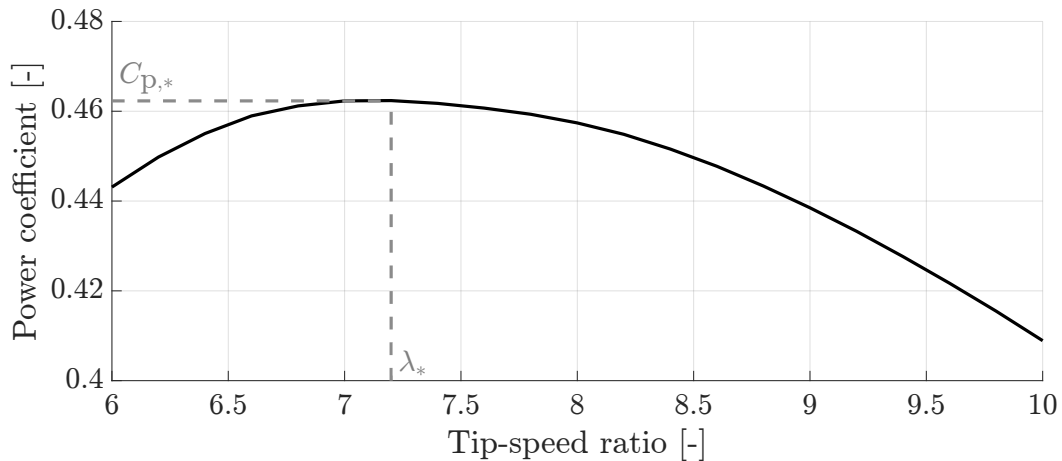


Figure 1. Power coefficient for the NREL 5 MW wind turbine model (Jonkman et al., 2009) under a uniform wind speed of 9 m/s. The maximum power extraction efficiency and the corresponding optimal tip-speed ratio are indicated as $C_{p,*}$ and λ_* , respectively.

where ρ represents the air density, A_{rot} is the rotor-swept area, $V \in \mathbb{R}$ is the rotor-effective wind speed (REWS) and $C_p(\cdot)$ is the power coefficient, being a function of the tip-speed ratio

$$\lambda = \frac{\omega_r R}{V}, \quad (3)$$

145 with R being the rotor radius. The shape of the $C_p(\cdot)$ curve depends on the design of the turbine and can be computed either from numerical simulations or experimental data. For this study, the National Renewable Energy Laboratory (NREL) 5 MW wind turbine model (Jonkman et al., 2009) is used, for which the $C_p(\cdot)$ curve covering the operating region of interest is illustrated in Figure 1. The presented curve is obtained from steady-state wind turbine simulations for a wind profile with a uniform velocity of 9 m/s. It can be observed that a constant λ_* exists, which corresponds to the rotor operating point
 150 for maximum power extraction efficiency $C_{p,*}(\lambda_*)$. In the remainder of this paper, a distinction is made between the torque controller input variable for the two schemes, namely, $T_{g,K}$ and $T_{g,\text{TSR}}$, for the baseline $K\omega^2$ or WSE-TSR tracking controller, respectively.

2.2 Baseline $K\omega^2$ controller

The derivation of the baseline $K\omega^2$ control law is presented in this section. Figure 2 illustrates a block diagram of the controller, and as shown, the framework only consists of the wind turbine and the controller. The controller is a static (nonlinear) function
 155 without dynamics, providing the generator torque control signal based on the rotor speed:

$$T_{g,K} = K \frac{\omega_r^2}{N}, \quad (4)$$

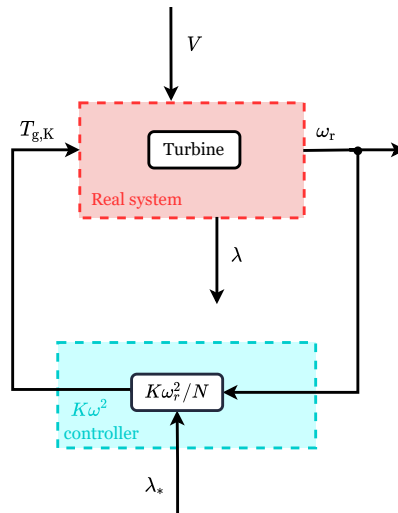


Figure 2. Block diagram of the $K\omega^2$ control framework. The red box highlights the wind turbine system with two inputs (the generator torque $T_{g,K}$, and the wind speed V), and with two outputs (the rotational speed, ω_r , and the TSR, λ). The measured ω_r and the optimal TSR, λ_* , are used as inputs of the controller (cyan box) to compute $T_{g,K}$.

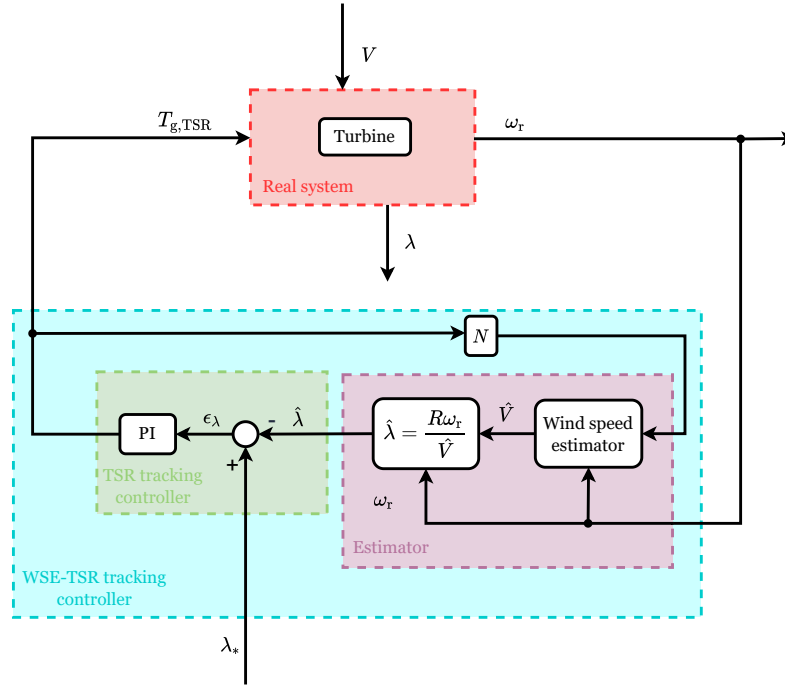


Figure 3. Block diagram of the WSE-TSR tracking control framework. The red box highlights the wind turbine system with two inputs (the generator torque $T_{g,TSR}$, and the wind speed V), and with two outputs (the rotational speed, ω_r , and the TSR, λ). The cyan box highlights the WSE-TSR tracking controller, which includes the estimator (purple box) and the TSR tracker controller (green box). The measured $T_{g,TSR}$ and ω_r are used to estimate the rotor-effective wind speed \hat{V} and to calculate an estimate of TSR, $\hat{\lambda}$, in the estimator block. The controller acts on the difference between $\hat{\lambda}$ and the optimal TSR, λ_* , to calculate the torque control signal $T_{g,TSR}$.

in which the torque gain K (Bossanyi, 2000) is defined at the LSS side of the drivetrain as

$$K = \frac{\rho A_{rot} R^3 C_{p,*}(\lambda_*)}{2\lambda_*^3}, \quad (5)$$

160 under Assumption 1.1.

2.3 WSE-TSR tracking controller

The WSE-TSR tracking framework, outlined in Figure 3, combines an estimator and a tip-speed ratio tracking controller. The estimator provides the tip-speed ratio estimate $\hat{\lambda}$, which is used by the controller that acts on the difference between the estimate and the tip-speed ratio reference. This reference is usually taken as λ_* , corresponding to the rotor operating point for maximum power extraction efficiency C_p^* . The controller provides the torque control signal $T_{g,TSR}$ and forces the turbine to track the reference. The following section provides derivations of commonly used implementations for both elements in the WSE-TSR tracking framework.

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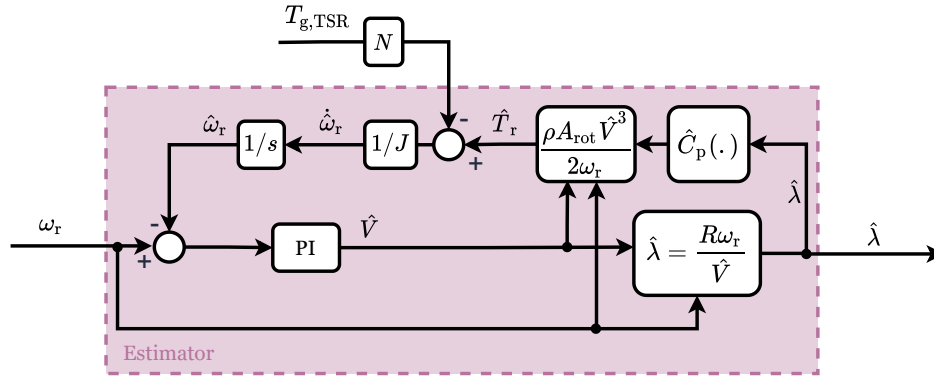


Figure 4. Block diagram of the estimator (Liu et al., 2022; Ortega et al., 2013). The measured generator torque, $T_{g,TSR}$, and rotational speed, ω_r , are used to estimate the REWS, \hat{V} , and to calculate an estimate of the TSR, $\hat{\lambda}$.

2.3.1 Wind speed estimator

The REWS is estimated based on the Immersion and Invariance (I&I) estimator (Ortega et al., 2013) with an augmented integral correction term (Liu et al., 2022). The estimator is illustrated in Figure 4 and uses the control signal, the measured system plant output and a nonlinear plant model to estimate the REWS. Given Assumptions 1.2 and 1.3, the estimator is formulated as follows

$$\begin{cases} J\dot{\hat{\omega}}_r = \hat{T}_r - T_{g,TSR}N \\ \epsilon_{\omega_r} = \omega_r - \hat{\omega}_r \\ \dot{\hat{V}} = K_{p,w}\epsilon_{\omega_r} + K_{i,w}\int_0^t \epsilon_{\omega_r}(\tau)d\tau \end{cases}, \quad (6)$$

with \hat{V} indicating the estimated REWS, $K_{p,w}$ the proportional estimator gain, and $K_{i,w}$ the integral estimator gain. Furthermore, t indicates the present time, and τ is the variable of integration. By adding integral action to the estimator, the error ϵ_{ω_r} is forced to converge to zero, providing consistent estimates of the rotor speed state $\hat{\omega}_r$. Under Assumption 1.1, the estimated aerodynamic torque is defined as

$$\hat{T}_r = \frac{1}{2}\rho A_{rot} \frac{\hat{V}^3}{\omega_r} \hat{C}_p(\hat{\lambda}), \quad (7)$$

where $\hat{C}_p(\cdot)$ is the estimated power coefficient, being a nonlinear function of the estimated tip-speed ratio $\hat{\lambda} = \omega_r R / \hat{V}$.

180 2.3.2 Tip-speed ratio tracking controller

The proportional and integral (PI) controller in the WSE-TSR tracking scheme acts on the tip-speed ratio error, which is defined as

$$\epsilon_\lambda = \lambda_* - \hat{\lambda}, \quad (8)$$

being the difference between reference and estimated tip-speed ratio. This error is used to compute the generator torque demand

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$$T_{g,TSR} = K_{p,c}\epsilon_\lambda + K_{i,c} \int_0^t \epsilon_\lambda(\tau) d\tau, \quad (9)$$

where $K_{p,c}$ and $K_{i,c}$ are the respective proportional and integral controller gains.

3 Frequency-domain framework

This section provides the linear frequency-domain framework for analysing the baseline $K\omega^2$ and the WSE-TSR tracking
 190 controllers, where the dynamics of the nonlinear system are linearised around a specific operating point. The subscripts $(\cdot)_K$
 and $(\cdot)_{TSR}$ are employed to distinguish the transfer functions for the two schemes. Following the structure of Section 2 and
 in the subsequent subsections, the relevant transfer functions are first derived and provided for the wind turbine dynamics,
 followed by the individual and combined subsystems for the considered control schemes. The presented framework has been
 verified through linearisation of the fully-coupled and nonlinear system using a numerical control system linearisation tool (The
 195 MathWorks Inc., 2021). Its correctness is further validated by comparison to the linearisation results for the same coupled
 system in related published work (Mulders et al., 2023). The verification process is not included in this paper for conciseness.

3.1 Wind turbine dynamics

This section considers the linearisation of the wind turbine dynamics. The differential equation in Equation (1) is first combined
 with the nonlinear expression for the aerodynamic rotor torque defined in Equation (2). Subsequently, the resulting expression
 200 is linearised with respect to the rotor speed state, generator torque control input, and wind speed disturbance input, resulting in

$$\dot{\omega}_r = G(V)\omega_r + ET_g + H(V)V. \quad (10)$$

For reasons of conciseness, the values perturbed around their operating points are defined using the same original variables.
 The introduced variables representing partial derivatives are defined as

$$205 \quad G(V) = \frac{1}{J} \frac{\partial T_r}{\partial \omega_r} \Big|_{(\bar{\omega}_r, \bar{V})} = \frac{1}{2J} \rho A_{rot} \left(-\frac{V^3}{\omega_r^2} C_p(\omega_r, V) + \frac{V^2 R}{\omega_r} \frac{\partial C_p(\omega_r, V)}{\partial \lambda} \right) \Big|_{(\bar{\omega}_r, \bar{V})}, \quad E = -\frac{N}{J}, \quad (11)$$

$$H(V) = \frac{1}{J} \frac{\partial T_r}{\partial V} \Big|_{(\bar{\omega}_r, \bar{V})} = \frac{1}{2J} \rho A_{rot} \left(\frac{3V^2}{\omega_r} C_p(\omega_r, V) - VR \frac{\partial C_p(\omega_r, V)}{\partial \lambda} \right) \Big|_{(\bar{\omega}_r, \bar{V})}. \quad (12)$$

The argument V is included here to allow for the convenient definition of estimator-based expressions for G and H in a later
 section; however, the argument is omitted in expressions from this point onwards. Finally, the linearised expression is Laplace
 transformed to obtain the following

$$210 \quad (s - G)\Omega_r(s) = ET_g(s) + H\mathcal{V}(s),$$

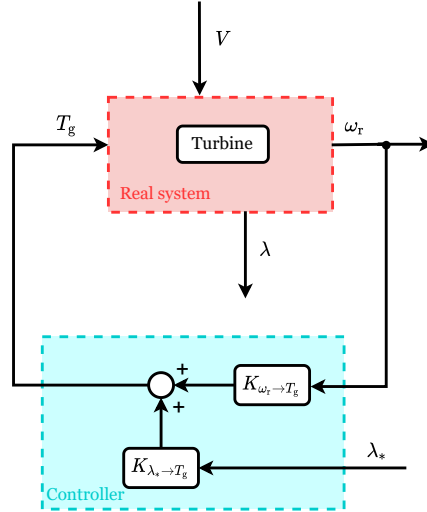


Figure 5. Block diagram of the universal framework used for the controller analysis. The red box highlights the wind turbine system with two inputs (the generator torque T_g , and the wind speed V), and two outputs (the rotational speed, ω_r , and the TSR, λ). The cyan box represents the controller with two inputs (ω_r and the TSR set point, λ_*), one output (T_g) and two terms used for the linear analysis framework (the feedback term, $K_{\omega_r \rightarrow T_g}$, and the reference shaping term $K_{\lambda_* \rightarrow T_g}$).

where s represents the Laplace operator. The resulting equation is defined to give the rotor speed

$$\Omega_r(s) = \frac{E}{s - G} \mathcal{T}_g(s) + \frac{H}{s - G} \mathcal{V}(s), \quad (13)$$

which depends on the transfer functions from the generator torque control and wind speed disturbance, respectively.

3.2 Analysis framework

215 To compare the characteristics of the baseline $K\omega^2$ and WSE-TSR tracking control strategies, a universal analysis framework is defined in this section and is illustrated in Figure 5. Here, the controllers are generalised as a single block with two inputs and one output, being the reference tip-speed ratio, rotor speed and generator torque control signals, respectively. In the linear and frequency-domain formulation, the control scheme is formalised as

$$\mathcal{T}_g(s) = K_{\Omega_r \rightarrow \mathcal{T}_g}(s) \Omega_r(s) + K_{\Lambda_* \rightarrow \mathcal{T}_g}(s) \Lambda_*(s). \quad (14)$$

220 In the remainder of this section, the expressions $K_{\Omega_r \rightarrow \mathcal{T}_g}$ and $K_{\Lambda_* \rightarrow \mathcal{T}_g}$ are derived and analysed for the different controllers, representing the feedback and the reference shaping terms, respectively. In particular, it will be shown that for the $K\omega^2$ controller, these elements are equivalent to a state feedback controller with reference shaping gain. Since both the WSE-TSR tracking controller and a state feedback controller aim to regulate the output of the wind turbine, ω_r , so that it tracks the reference input, λ_* , this equivalence represents the first step to comparing the baseline with the proposed controller.



225 By substituting Equation (14) into Equation (13), the following expression is obtained

$$\Omega_r(s) = \frac{EK_{\Omega_r \rightarrow \mathcal{T}_g}(s)}{s-G} \Omega_r(s) + \frac{EK_{\Lambda_* \rightarrow \mathcal{T}_g}(s)}{s-G} \Lambda_*(s) + \frac{H}{s-G} \mathcal{V}(s), \quad (15)$$

and by further manipulation

$$\Omega_r(s) = \frac{EK_{\Lambda_* \rightarrow \mathcal{T}_g}(s)}{s-G-EK_{\Omega_r \rightarrow \mathcal{T}_g}(s)} \Lambda_*(s) + \frac{H}{s-G-EK_{\Omega_r \rightarrow \mathcal{T}_g}(s)} \mathcal{V}(s). \quad (16)$$

230 In Equation (16), the closed-loop transfer functions are defined with the rotor speed as the output variable. As the scheme intends to regulate the tip-speed ratio to the TSR reference, this output should be converted to the actual tip-speed ratio λ of the turbine rotor. Therefore, the TSR expression defined in Equation (3) is linearised with respect to the rotor speed and wind speed, and the following expression is obtained

$$\Lambda(s) = \frac{R}{\bar{V}} \Omega_r(s) - \frac{R\bar{\omega}_r}{\bar{V}^2} \mathcal{V}(s). \quad (17)$$

By combining Equation (17) with Equation (16)

$$235 \Lambda(s) = \underbrace{\frac{REK_{\Lambda_* \rightarrow \mathcal{T}_g}(s)}{\bar{V}(s-G-EK_{\Omega_r \rightarrow \mathcal{T}_g}(s))}}_{T_{\Lambda_* \rightarrow \Lambda}(s)} \Lambda_*(s) + \underbrace{\frac{R(H - (\bar{\omega}_r/\bar{V})(s-G-EK_{\Omega_r \rightarrow \mathcal{T}_g}(s)))}{\bar{V}(s-G-EK_{\Omega_r \rightarrow \mathcal{T}_g}(s))}}_{T_{\mathcal{V} \rightarrow \Lambda}(s)} \mathcal{V}(s). \quad (18)$$

The two transfer function terms on the right-hand side of Equation (18) represent the closed-loop system reference tracking and disturbance attenuation capabilities, respectively. In particular, the term $T_{\Lambda_* \rightarrow \Lambda}(s)$ indicates if the controller is tracking the optimal condition (i.e. $\lambda = \lambda_*$), while $T_{\mathcal{V} \rightarrow \Lambda}(s)$ shows the controller's performance in reacting to external wind speed disturbances. Later in this paper, these closed-loop transfer functions will be evaluated in terms of optimal controller calibration
 240 to further investigate the controller in the frequency domain.

3.3 Baseline $K\omega^2$ control dynamics

With the open-loop linearised wind turbine plant dynamics and analysis framework defined, this section derives the respective quantities in the universal controller framework for the baseline controller. The nonlinear representation of the $K\omega^2$ controller given by Equation (4) is linearised to obtain the quantities

$$245 K_{(\Omega_r \rightarrow \mathcal{T}_g),K} = \left. \frac{\partial T_{g,K}}{\partial \omega_r} \right|_{(\bar{\omega}_r, \lambda_*)} = \frac{2K\bar{\omega}_r}{N} = \frac{\rho R^3 A_{\text{rot}} C_{p,*}(\lambda_*)}{N \lambda_*^3} \bar{\omega}_r, \quad (19)$$

$$K_{(\Lambda_* \rightarrow \mathcal{T}_g),K} = \left. \frac{\partial T_{g,K}}{\partial \lambda_*} \right|_{(\bar{\omega}_r, \lambda_*)} = \frac{\rho R^3 A_{\text{rot}}}{2N} \left(-\frac{3}{\lambda_*^4} C_{p,*}(\lambda_*) + \frac{1}{\lambda_*^3} \frac{\partial C_{p,*}(\lambda_*)}{\partial \lambda_*} \right) \bar{\omega}_r^2. \quad (20)$$

These are equivalent to the state-feedback and reference shaping gain, respectively, as defined in state-feedback control theory. The interested reader is referred to Appendix A for the full derivation of this similarity.



3.4 WSE-TSR tracking control dynamics

250 This section provides a derivation of the frequency-domain control dynamics of the WSE-TSR tracking controller. As shown in Figure 3, the control scheme consists of a combined estimator and tracking controller. For this reason, to obtain the dynamics of the full scheme, the linear frequency-domain representations of the individual estimator and controller are derived first. Then, the framework dynamics are achieved by coupling the estimator and the controller.

3.4.1 Estimator dynamics

255 As illustrated in Figure 4, the estimator has the generator torque and the rotor speed as inputs and the estimated tip-speed ratio as output. Therefore, several steps must be taken to derive a frequency-domain representation for the estimator, which are briefly summarised here. First, the equations for the estimated rotor speed and REWS (Equation (6)) are combined and applied at the linearisation point in terms of the Laplace variable. As a result, the estimated REWS is defined as a function of the rotor speed and the generator torque. Then, by substituting this expression into the nonlinear function of the estimated tip-speed ratio, the following is obtained

260

$$\hat{\Lambda}(s) = X(s)\mathcal{T}_{g,TSR}(s) + Y(s)\Omega_r(s), \quad (21)$$

where

$$X(s) = \frac{\hat{\Lambda}_{\mathcal{T}_{g,TSR}}(s)}{\mathcal{T}_{g,TSR}(s)} = \frac{R\bar{\omega}_r E(K_{p,w}s + K_{i,w})}{\bar{V}^2 (s^2 + \hat{H}K_{p,w}s + \hat{H}K_{i,w})}, \quad (22)$$

and

$$265 \quad Y(s) = \frac{\hat{\Lambda}_{\Omega_r}(s)}{\Omega_r(s)} = \frac{R \left[(1 - (\bar{\omega}_r/\bar{V})K_{p,w})s^2 + (\hat{H}K_{p,w} - (\bar{\omega}_r/\bar{V})(K_{i,w} - \hat{G}K_{p,w}))s + (\hat{H} + (\bar{\omega}_r/\bar{V})\hat{G})K_{i,w} \right]}{\bar{V} (s^2 + \hat{H}K_{p,w}s + \hat{H}K_{i,w})}, \quad (23)$$

represent the transfer functions from the generator torque and rotational speed, respectively, to the estimated tip-speed ratio. According to Assumption 1.3, the variables $\hat{G} := G(\hat{V})$ and $\hat{H} := H(\hat{V})$ indicate the estimated partial derivatives defined in Equations (11) and (12).

3.4.2 Tip-speed ratio tracking control dynamics

270 According to Figure 3, the TSR tracking controller has two inputs, the tip-speed ratio estimate and set point, and one output, the generator torque. The TSR tracking control dynamics is derived in the frequency domain by combining Equation (9) with the tracking error definition (Equation (8)) at the linearisation point in terms of the Laplace variable. Follows,

$$\mathcal{T}_{g,TSR}(s) = Z(s)\Lambda_*(s) + Q(s)\hat{\Lambda}(s), \quad (24)$$

with

$$275 \quad Z(s) = \frac{\mathcal{T}_{g,TSR}\Lambda_*(s)}{\Lambda_*(s)} = \frac{K_{p,c}s + K_{i,c}}{s}, \quad (25)$$



and

$$Q(s) = \frac{\mathcal{T}_{g, \text{TSR}} \hat{\Lambda}(s)}{\hat{\Lambda}(s)} = -\frac{K_{p,c}s + K_{i,c}}{s}, \quad (26)$$

being the transfer functions from the reference and estimated tip-speed ratio, respectively, to the generator torque.

3.4.3 Combined scheme

280 The combined control scheme can now be formed using the individually derived elements. To this end, the linearised estimator and controller expressions Equations (21) and (24) are combined to comply with the desired form of Equation (14), resulting in the following expression:

$$\mathcal{T}_{g, \text{TSR}}(s) = Q(s)X(s)\mathcal{T}_{g, \text{TSR}}(s) + Q(s)Y(s)\Omega_r(s) + Z(s)\Lambda_*(s). \quad (27)$$

Following further manipulation

$$285 \quad \mathcal{T}_{g, \text{TSR}}(s) = \underbrace{\frac{Q(s)Y(s)}{(1-Q(s)X(s))}}_{K_{(\Omega_r \rightarrow \mathcal{T}_g), \text{TSR}}(s)} \Omega_r(s) + \underbrace{\frac{Z(s)}{(1-Q(s)X(s))}}_{K_{(\Lambda_* \rightarrow \mathcal{T}_g), \text{TSR}}(s)} \Lambda_*(s), \quad (28)$$

with

$$K_{(\Omega_r \rightarrow \mathcal{T}_g), \text{TSR}}(s) = \frac{\mathcal{T}_{g, \text{TSR}} \Omega_r(s)}{\Omega_r(s)} = \frac{R(K_{p,c}s + K_{i,c}) \left((\bar{\omega}_r K_{p,w} - \bar{V})s^2 + F_4 s - (\bar{V}\hat{H} + \bar{\omega}_r \hat{G})K_{i,w} \right)}{(\bar{V}^2 s^3 + F_1 s^2 + F_2 s + F_3)}, \quad (29)$$

and

$$K_{(\Lambda_* \rightarrow \mathcal{T}_g), \text{TSR}}(s) = \frac{\mathcal{T}_{g, \text{TSR}} \Lambda_*(s)}{\Lambda_*(s)} = \frac{\bar{V}^2 (K_{p,c}s + K_{i,c}) (s^2 + \hat{H} K_{p,w} s + \hat{H} K_{i,w})}{(\bar{V}^2 s^3 + F_1 s^2 + F_2 s + F_3)}, \quad (30)$$

290 representing the controller transfer functions from the rotational speed and tip-speed ratio reference, respectively, to the generator torque output. The unknown quantities in the above expressions are defined as

$$F_1 = \bar{V}^2 \hat{H} K_{p,w} + R\bar{\omega}_r E K_{p,c} K_{p,w},$$

$$F_2 = \bar{V}^2 \hat{H} K_{i,w} + R\bar{\omega}_r E K_{p,c} K_{i,w} + R\bar{\omega}_r E K_{i,c} K_{p,w},$$

$$F_3 = R\bar{\omega}_r E K_{i,c} K_{i,w},$$

$$295 \quad F_4 = \bar{\omega}_r K_{i,w} - (\bar{V}\hat{H} + \bar{\omega}_r \hat{G})K_{p,w},$$

in order to simplify Equations (29) and (30).

3.5 Comparison between controllers

In the previous section, the controllers are expressed in a universal analysis framework to allow for comparison. Using the controller expression given by Equation (14), this section analyses the controller transfer functions $K_{\Omega_r \rightarrow \mathcal{T}_g}(s)$ and $K_{\Lambda_* \rightarrow \mathcal{T}_g}(s)$ of

300 the baseline $K\omega^2$ and WSE-TSR tracking controllers to understand the similarities and differences between the two seemingly dissimilar controllers. Since the closed-loop dynamics is strictly dependent on the calibration chosen for the WSE-TSR tracking control scheme, the analysis of the corresponding transfer functions will be evaluated in a later section using the results from the multi-objective optimisation.

Equations (19) and (20) show that the controller transfer functions are merely frequency independent gains for the baseline 305 controller. That is, the gain is constant over all frequencies. In contrast, the WSE-TSR tracking controller transfer functions possess dynamics (Equations (29) and (30)). For this reason, it is assumed that for the low-frequency region, the (DC-)gain of the latter controller equals the gain of the baseline controller, whereas, for higher frequencies, the frequency responses vary.

To examine the controller transfer functions, Equations (29) and (30) are symbolically evaluated $s = j\omega = 0$, with j being the imaginary unit number. By doing so, the steady-state responses of the WSE-TSR tracking controller transfer functions are 310 computed, and after substitutions and simplifications, the following expressions are derived

$$K_{(\Omega_r \rightarrow \mathcal{T}_g), \text{TSR}}(s=0) = -\frac{(\bar{V}\hat{H} + \bar{\omega}_r\hat{G})}{\bar{\omega}_r E} = \frac{\bar{V}}{\bar{\omega}_r N} \left(\frac{\partial \hat{T}_r}{\partial \bar{V}} \right) + \frac{1}{N} \left(\frac{\partial \hat{T}_r}{\partial \omega_r} \right) = \frac{\rho R^3 A_{\text{rot}} C_{p,*}(\lambda_*)}{N \lambda_*^3} \bar{\omega}_r, \quad (31)$$

$$K_{(\Lambda_* \rightarrow \mathcal{T}_g), \text{TSR}}(s=0) = \frac{\bar{V}^2 \hat{H}}{R \bar{\omega}_r E} = -\frac{\bar{V}^2}{R \bar{\omega}_r N} \left(\frac{\partial \hat{T}_r}{\partial \bar{V}} \right) = \frac{\rho R^3 A_{\text{rot}}}{2N} \left(-\frac{3}{\lambda_*^4} C_{p,*}(\lambda_*) + \frac{1}{\lambda_*^3} \frac{\partial C_{p,*}(\lambda_*)}{\partial \lambda_*} \right) \bar{\omega}_r^2. \quad (32)$$

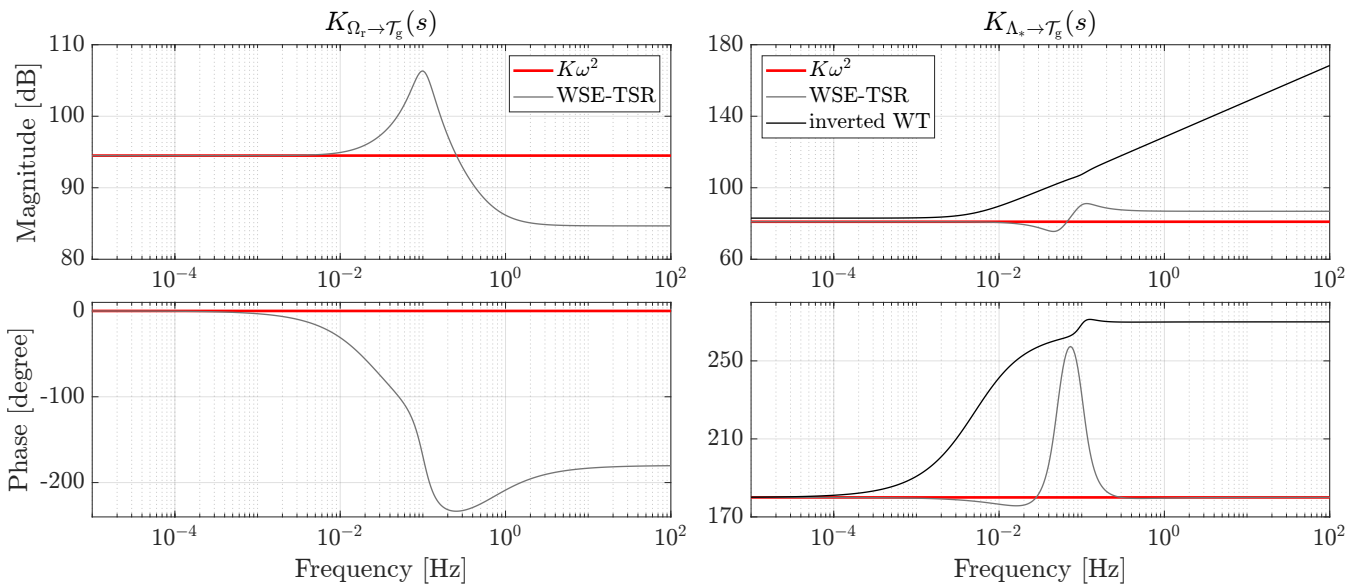


Figure 6. Bode plots of the controller transfer functions $K_{\Omega_r \rightarrow \mathcal{T}_g}(s)$ and $K_{\Lambda_* \rightarrow \mathcal{T}_g}(s)$ for the $K\omega^2$ controller (red line) and the WSE-TSR tracking controller (grey line) without optimal calibration. For the baseline, both transfer functions are frequency independent. For the combined scheme, in the low-frequency region, $K_{\Omega_r \rightarrow \mathcal{T}_g}(s)$ and $K_{\Lambda_* \rightarrow \mathcal{T}_g}(s)$ have gains equal to the baseline. In particular, for the right-hand plot, the controller gains match the inverted model of the wind turbine (black line), exhibiting a second-order lead-lag behaviour. By contrast, for higher frequencies, the response varies for both transfer functions for the combined scheme.



It is immediately evident that $K_{\text{TSR}}(s=0) = K_K$ as defined earlier in Equations (19) and (20). This proves that the WSE-TSR tracking controller is equivalent to the $K\omega^2$ controller in steady-state. Thus, the two controllers will have the same behaviour
315 under the given inputs (Aström and Murray, 2010), operating at the same point of power extraction efficiency, $C_{p,*}(\lambda_*)$.

Similarities and differences between the two controllers are further illustrated in Figure 6 with Bode plots of the analysed controller transfer functions. The frequency responses are obtained using the NREL 5 MW reference turbine parameters (Jonkman et al., 2009) and a controller calibration that performs satisfactorily but is non-optimised. In the figure illustrating the Bode plot for $K_{\Omega_r \rightarrow \mathcal{T}_g}(s)$ of both controllers, it can be observed that the two controllers show the same characteristics
320 for the low-frequency region (between 1×10^{-5} Hz and 1×10^{-2} Hz). However, for higher frequencies, the WSE-TSR tracking controller presents additional dynamics in the form of a resonance resulting from a complex left half-plane pole-pair and a double right half-plane zero. The explanation for these additional dynamics is the controller attaining a higher open-loop unity cross-over, resulting in an increased closed-loop control bandwidth. The right plot presents the frequency response for
325 $K_{\Lambda_* \rightarrow \mathcal{T}_g}(s)$ and for the inverted transfer function of the wind turbine defined in Equation (13). It is clear that both controllers exhibit a second-order lead-lag behaviour related to the model inversion required for the reference shaping action (Leith and Leithead, 1997).

4 Calibration of the WSE-TSR tracking control scheme

From the frequency-domain framework derived in the previous section, it is recognised that the WSE-TSR tracking controller presents a higher dimensional design space than the baseline $K\omega^2$. In particular, while the $K\omega^2$ controller has only the torque
330 gain K to calibrate, the combined scheme has a total of five variables: $K_{p,w}$, $K_{i,w}$, $K_{p,c}$, $K_{i,c}$ and λ_* . This tight integration between a disturbance estimator and a tracking controller makes the mutual calibration of the design variables in the WSE-TSR tracking controller a complex and non-trivial task. Therefore, this section addresses the calibration of the controller by formulating a multi-objective optimisation problem. The approach to *solving* this multi-objective problem is by reconstructing (an approximation of) the true Pareto front, composed of a set of Pareto optimal solutions. To this end, first, the multi-objective
335 optimisation problem is formalised in Section 4.1 and implemented in Section 4.2. An exploratory and guided search over the controller calibration variables examines the performance space formed by all objectives. The outcomes of this search are presented in Section 4.3 to construct approximations of the true Pareto front, which are related to the controller calibrations.

4.1 Multi-objective optimisation

A multi-objective optimisation problem is considered over a set of continuous input variables $\mathcal{X} \subset \mathbb{R}^d$ called the design
340 space (Lukovic et al., 2020). The optimisation goal is to minimise the vector of the objective functions defined as $\mathbf{f}(\mathbf{x}) = (f_1(\mathbf{x}), \dots, f_m(\mathbf{x}))$ with $m \geq 2$, $\mathbf{x} \in \mathcal{X}$ the vector of input variables and $\mathbf{f}(\mathcal{X}) \subset \mathbb{R}^m$ the m -dimensional image representing the performance space. The resulting minimisation of the cost function is defined as:

$$\min_{\mathbf{x}}(\mathbf{f}(\mathbf{x})), \tag{33}$$



and is subjected to the operational conditions under which the multi-objective optimisation is performed.

345 The conflicting nature of the objective functions does not always allow the finding of a single best solution to the minimisation problem but rather a set of optimal solutions, referred to as Pareto set $\mathcal{P}_s \subseteq \mathcal{X}$ in the design space and as Pareto front $\mathcal{P}_f = \mathbf{f}(\mathcal{P}_s) \subset \mathbb{R}^m$ in the performance space (Lukovic et al., 2020). In the following, the Pareto front is approximated by considering as Pareto optimal the point $\mathbf{x}_* \in \mathcal{P}_s$ for which there is no other point $\mathbf{x} \in \mathcal{X}$ such that $f_j(\mathbf{x}_*) \geq f_j(\mathbf{x})$ for all j and $f_j(\mathbf{x}_*) > f_j(\mathbf{x})$ for at least one j , with $j = \{1, \dots, m\}$ (Miettinen, 1999).

350 4.2 Implementation of the optimisation framework

The methodology for calibrating the design variables of the WSE-TSR tracking control scheme is addressed as the multi-objective optimisation problem previously described. A two-dimensional vector of the objective functions is considered. The first objective is the variance of the torque control signal, representing the responsiveness of the controller (i.e. a measure of its response speed). This objective can also act as a measure of loads on the structural components of the turbine. The second
 355 objective is the mean generated power of the wind turbine. These two objectives are conflicting as a more responsive controller is expected to result in higher power production levels with increased loads and fast response time and vice-versa for milder controller calibration. Thereby, the objective function vector is given by:

$$\mathbf{f}(\mathbf{\Gamma}_d) = [f_1(\mathbf{\Gamma}_d), f_2(\mathbf{\Gamma}_d)], \quad (34)$$

with the torque variance being defined as

$$360 f_1(\mathbf{\Gamma}_d) = \frac{\sum_{i=1}^n (T_{g,i}(\mathbf{\Gamma}_d) - T_{g,\text{mean}}(\mathbf{\Gamma}_d))^2}{n},$$

and the mean power as

$$f_2(\mathbf{\Gamma}_d) = -\frac{\sum_{i=1}^n P_{g,i}(\mathbf{\Gamma}_d)}{n}.$$

In the above equations, n is the number of data points, $T_{g,\text{mean}}$ is the mean value of the generator torque, and $T_{g,i}$ and $P_{g,i}$ represent each value of generator torque and power in the dataset, respectively. As shown, the resulting signals T_g and P_g are a
 365 function of $\mathbf{\Gamma}_d \in \mathcal{X}_d \subset \mathbb{R}^d$, which is the d -dimensional vector of input variables. In this study, the dimensionality of the input vectors is investigated to assess the performance of the controller for different levels of complexity as

$$\mathbf{\Gamma}_5 = [K_{p,c}, K_{i,c}, K_{p,w}, K_{i,w}, \lambda_*] \in \mathcal{X}_5,$$

$$\mathbf{\Gamma}_4 = [K_{p,c}, K_{i,c}, K_{p,w}, \lambda_*] \in \mathcal{X}_4,$$

$$\mathbf{\Gamma}_3 = [K_{i,c}, K_{p,w}, \lambda_*] \in \mathcal{X}_3,$$

$$370 \mathbf{\Gamma}_2 = [K_{i,c}, K_{p,w}] \in \mathcal{X}_2,$$

$$\mathbf{\Gamma}_1 = [\lambda_*] \in \mathcal{X}_1,$$

where the subscript $(\cdot)_d$ represents the dimension of each design space and is used in the remainder of this paper to differentiate between the input vectors. Note that $d = 5$ refers to the original formulation of the WSE-TSR tracking controller, whereas the



input vectors $\Gamma_d \subset \Gamma_5$ for $d = \{2, 3, 4\}$. In contrast, Γ_1 represents the one-dimensional design space of the $K\omega^2$ controller, in
 375 which the variation in λ_* leads to variation in the gain K according to Equation (5).

High-fidelity simulations are performed with the NREL's high-fidelity wind turbine simulation software OpenFAST (NREL,
 2021). The NREL 5 MW reference wind turbine (Jonkman et al., 2009) is subject to a realistic turbulent wind profile with a
 mean wind speed of $\bar{V} = 9$ m/s at hub height and a turbulence intensity of $TI = 15\%$. For each simulation, the input vector
 is constrained for a guided search to find a set of optimal solutions $\mathcal{P}_s^d \subset \mathbb{R}^d$ to approximate the Pareto front $\mathcal{P}_f^d = \mathbf{f}(\mathcal{P}_s^d)$.
 380 Simulations are run in parallel by randomly varying the input vector inside the constrained design space. Each simulation has
 a length of 3600 s, of which the first 100 s are discarded to exclude the transient start-up effects from the results. The acquired
 time series is used to calculate the considered objectives $f_1(\Gamma_d)$ and $f_2(\Gamma_d)$.

4.3 Optimisation results

This section presents the results obtained with the described optimisation framework. The performance space is explored
 385 using the guided search for the five sets of calibration input variables. Subsequently, the results are used to approximate the
 corresponding Pareto fronts. Finally, the influence of the gains is assessed by analysing the different regions of the constrained
 design space.

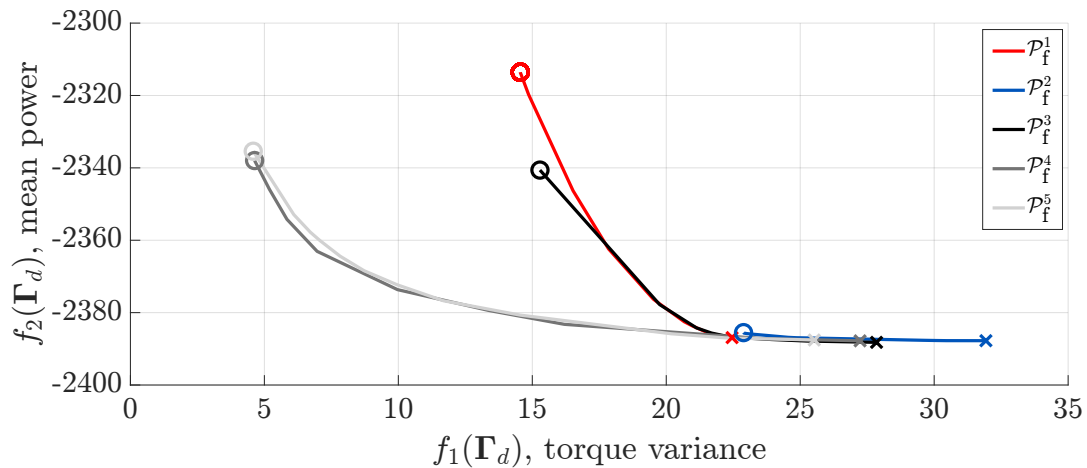


Figure 7. Pareto fronts obtained for the WSE-TSR tracking control scheme under realistic turbulent wind conditions for different sets of estimator-controller design variables: $\Gamma_1, \Gamma_2, \Gamma_3, \Gamma_4$ and Γ_5 . The objective functions $f_1(\Gamma_d)$, i.e. torque fluctuations minimisation, and $f_2(\Gamma_d)$, i.e. power maximisation, define the performance space for the controller. The optimal solutions for $f_1(\Gamma_d)$ and $f_2(\Gamma_d)$ are indicated using circles (o) and crosses (x), respectively. Compared to the baseline controller represented by the Pareto front \mathcal{P}_f^1 , the WSE-TSR tracking controller does not attain an enhancement in power maximisation but allows the minimisation of torque fluctuations with a small penalty in power extraction.



4.3.1 Exploratory search and Pareto front

Before constructing the Pareto front, the performance space is explored by means of a guided search of the input variables Γ_d . With an increasing dimension d of the design space, more data is collected to capture the performance space of interest effectively. The conventional $K\omega^2$ controller is used as a baseline comparison case.

With the exploration data at hand, the Pareto front is approximated by minimising a weighted linear combination of $f_1(\Gamma_d)$ and $f_2(\Gamma_d)$ on the complete data set and for a range of weights. As shown in Figure 7, Pareto fronts are approximated for different dimensionalities of the input vector Γ_d to compare the baseline to the performance of the WSE-TSR tracking controller. The optimal solutions based on each objective function $f_1(\Gamma_d)$ and $f_2(\Gamma_d)$ are indicated using circles (\circ) and crosses (\times), respectively.

From the figure, it is immediately apparent that the fronts of the higher-dimensional controllers $d = \{4, 5\}$ cover the widest area of the performance space; the remaining fronts are subsets of the original WSE-TSR tracking control scheme. Since the Pareto fronts for $d = \{4, 5\}$ overlap, it is concluded that adding an integral term to the estimator (i.e. $K_{i,w}$) leads to no (or marginal) benefits on the performance of the WSE-TSR tracking scheme. It follows that only with a proportional gain (i.e. $K_{p,c}$) in the control scheme does it lead to more flexibility in reaching desired (Pareto) optimal solutions minimising torque fluctuations and corresponding (structural) loads, with a minimal impact on the power extraction performance. This shows the benefits of the more flexible structure of the WSE-TSR tracking scheme.

Another observation is that the baseline controller already attains a Pareto optimal solution minimising $f_2(\Gamma_d)$, i.e. maximising power production. It is clear that increasing the controller bandwidth and allowing for higher torque fluctuations $f_1(\Gamma_d)$ does not result in the enhancement of energy capture $f_2(\Gamma_d)$ compared to the baseline control strategy. A plausible explanation is that the higher inertia of large-scale wind turbines inherently provides resilience against deviations from the optimal operating point. Therefore, increasing the controller bandwidth resulting in tighter tracking to the desired tip-speed ratio reference, might not directly result in additional benefits in terms of energy capture.

4.3.2 Influence of the controller calibration variables

This section qualitatively assesses the influence and correlation of the gains to the performance of the WSE-TSR tracking controller. The analysis is presented in Figure 8, where two areas of interest are selected: the lowest value of $f_2(\Gamma_5)$ (power maximisation) and $f_1(\Gamma_5)$ (torque fluctuation minimisation). The analysis only draws conclusions relating the calibration of the scheme to the considered objectives; a more formal frequency- and time-domain analysis is described in the next section. Furthermore, only the five-dimensional input vector Γ_5 will be evaluated from this point onwards, as the current study focuses on providing calibration guidelines for the complete WSE-TSR tracking control scheme rather than for its subsets.

For the power maximisation case, λ_* should be taken between 7.1 and 7.3, which corresponds to the region of maximum power extraction for the NREL 5 MW (Figure 1). For the torque minimisation case, λ_* should be chosen higher than the power coefficient-maximising value, resulting in a power reduction and rotational speed variance increase. Furthermore, as observed

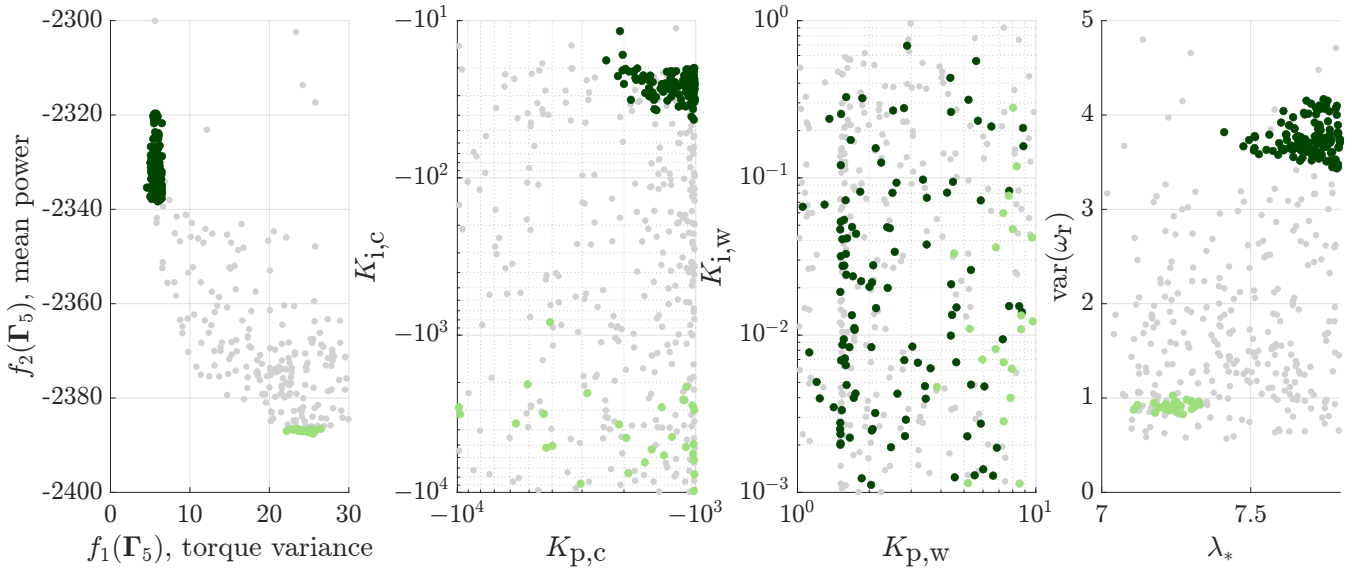


Figure 8. Results for the WSE-TSR tracking control scheme obtained with an exploratory search of its design variables (i.e. Γ_5). Different shades of green are used to highlight two areas of interest: the lowest values of $f_1(\Gamma_5)$ (torque fluctuation minimisation) and $f_2(\Gamma_5)$ (power maximisation). The two objectives and the rotor speed variance ($\text{var}(\omega_r)$) are plotted together with the controller gains ($K_{p,c}$ and $K_{i,c}$), the estimator gains ($K_{p,w}$ and $K_{i,w}$) and the reference tip-speed ratio (λ_*) to show how these calibration variables influence the scheme’s performance. Clearly, neither $K_{i,w}$ nor $K_{p,c}$ correlates to the performance of the WSE-TSR tracking controller. While λ_* and $K_{p,w}$ follow an increasing trend proportional to the increase in torque variance, $K_{i,c}$ exhibits opposite behaviour.

420 from both cases, $K_{p,w}$ follows an increasing trend proportional to the increase in torque variance, while $K_{i,w}$ does not show a clear correlation to the controller performance.

Considering the controller gains, it is clear that the controller heavily relies on integral action to track the desired tip-speed ratio reference and therefore achieve power maximisation. The gain for the proportional action $K_{p,c}$ lies in the same area for the two regions of interest without directly influencing the performance.

425 5 Analysis of *optimally* calibrated WSE-TSR tracking controllers

Pareto fronts have been approximated in the previous section representing a set of optimal solutions among the conflicting objectives. An analysis has been presented by directly relating the objectives to the input vectors of various dimensionalities. This section compares the characteristics of full-dimensional and *optimally* calibrated WSE-TSR tracking controllers to the baseline $K\omega^2$ strategy. The analysis is performed with the frequency domain framework, described in Section 3, and high-

430 fidelity time-domain simulations for realistic turbulent wind conditions.

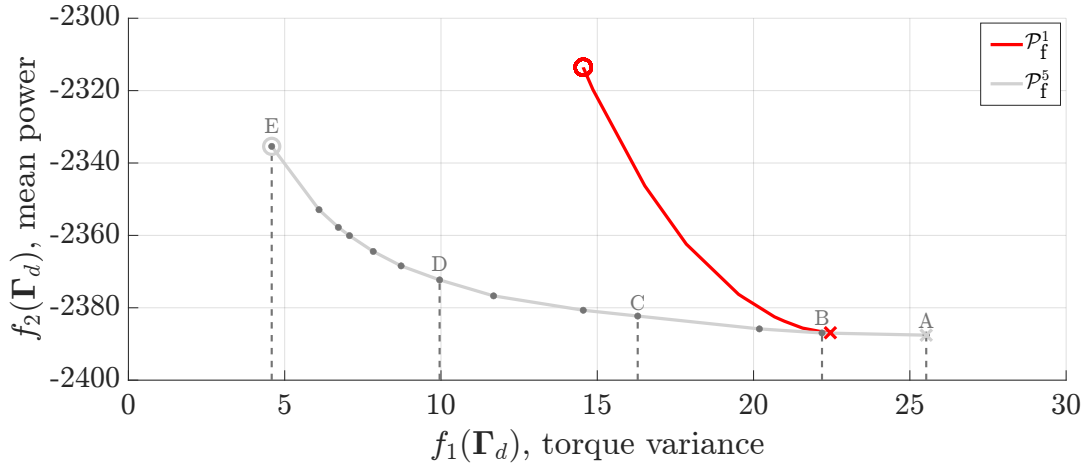


Figure 9. Pareto fronts \mathcal{P}_f^1 and \mathcal{P}_f^5 obtained for the baseline and WSE-TSR tracking control schemes and related to the Γ_1 and Γ_5 design variables. The case studies for the WSE-TSR tracking controller are marked on the \mathcal{P}_f^5 front with letters ranging from A to E, respectively, corresponding to maximum power extraction and minimum generator torque fluctuations. Point B is closest to the optimal baseline controller calibration in terms of power extraction.

5.1 Case studies definition

The case studies analysed in this section are presented in Figure 9. The figure shows the approximated Pareto fronts \mathcal{P}_f^5 and \mathcal{P}_f^1 , representing the WSE-TSR tracking and the baseline controllers, respectively. Along the \mathcal{P}_f^5 front, five distinct optimal solutions are chosen, and the corresponding calibrations Γ_5 are considered for analysis in the following subsections. The selection considers the evaluation of different trade-off levels between the considered objectives from the point of maximum power extraction (A) to the point of minimum torque variance (E). Point B is closest to the maximum power extraction of the $K\omega^2$ controller and is selected to show similarities between these two schemes.

5.2 Frequency-domain results

This section compares the frequency domain characteristics for the defined cases using the linear analysis framework described in Section 3. First, the frequency responses for the controller transfer functions $K_{\Omega_r \rightarrow \mathcal{T}_g}(s)$ and $K_{\Lambda_* \rightarrow \mathcal{T}_g}(s)$ are discussed, followed by the closed-loop transfer functions $T_{\Lambda_* \rightarrow \Lambda}(s)$ and $T_{\mathcal{V} \rightarrow \Lambda}(s)$.

5.2.1 Controller transfer functions

The analysis strategy defined in Section 3.2 is employed to evaluate the characteristics of the controllers. The frequency responses of the transfer functions $K_{\Omega_r \rightarrow \mathcal{T}_g}(s)$ and $K_{\Lambda_* \rightarrow \mathcal{T}_g}(s)$ for the defined cases are presented in Figure 10. The results for the $K\omega^2$ controller are included as a baseline, being frequency independent with a constant gain over all frequencies.

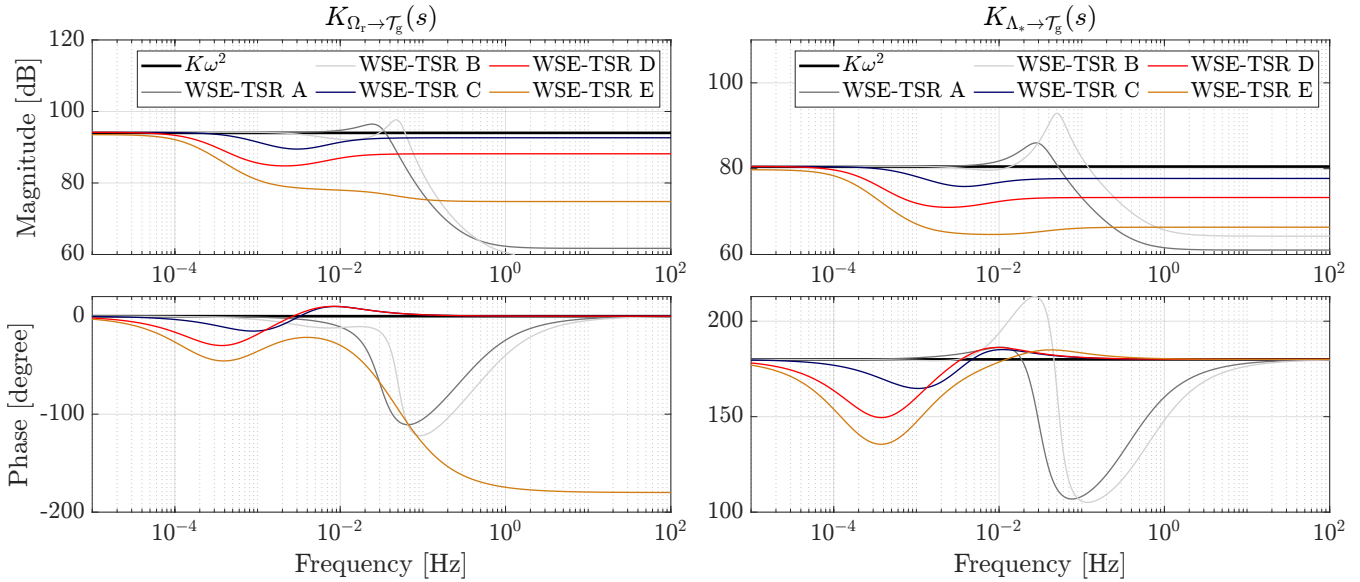


Figure 10. Bode plots of the controller transfer functions $K_{\Omega_r \rightarrow T_g}(s)$ and $K_{\Lambda_* \rightarrow T_g}(s)$ for the baseline $K\omega^2$ and the WSE-TSR tracking controller cases. While, for the baseline, $K_{(\Omega_r \rightarrow T_g),K}$ and $K_{(\Lambda_* \rightarrow T_g),K}$ show a constant gain over all frequencies, for the WSE-TSR tracking controllers, $K_{(\Omega_r \rightarrow T_g),TSR}(s)$ and $K_{(\Lambda_* \rightarrow T_g),TSR}(s)$ exhibit additional dynamics with an increasing cut-off frequency for increasing cases towards B. In particular, cases A and B present resonance peaks in their response to further improve the controller cut-off frequency.

For case E, the steady-state gain deviates from the baseline gain because the reference tip-speed ratio is calibrated at a higher and non-optimal set point of $\lambda_*^E = 7.71$. Furthermore, for the same case, it is seen that the controller cut-off frequencies are at the lowest frequency compared to the other cases, resulting in reduced torque variance responses. For increasing points towards case A, the controller cut-off frequency for both reference shaping and feedback-related transfer functions increases to
 450 higher frequencies, except for B. As shown in Figure 9, case B shows the closest resemblance in performance attained with the optimal baseline controller. A possible explanation is that the controller adheres to the $K\omega^2$ -trajectory for the most extended frequency range. A notable observation is the resonance peaks for cases A and B, which enables a higher cut-off frequency of the loop gain, resulting in an increased closed-loop bandwidth to track the desired tip-speed ratio. A further observation from the phase plots is the opposite sign of the controller transfer functions, which is understandable from a physical perspective. The
 455 generator torque increases for higher rotational speeds ($K_{\Omega_r \rightarrow T_g}(s)$), whereas an inverse proportional relation exists between the desired tip-speed ratio and generator torque ($K_{\Lambda_* \rightarrow T_g}(s)$).

5.2.2 Closed-loop transfer functions

This section presents an analysis of the closed-loop controller characteristics. For the different cases, Figure 11 illustrates the frequency responses of the transfer functions $T_{\Lambda_* \rightarrow \Lambda}(s)$ and $T_{\gamma \rightarrow \Lambda}(s)$, representing the closed-loop system performance
 460 in terms of reference tracking and disturbance rejection, respectively. The results for these transfer functions confirm the

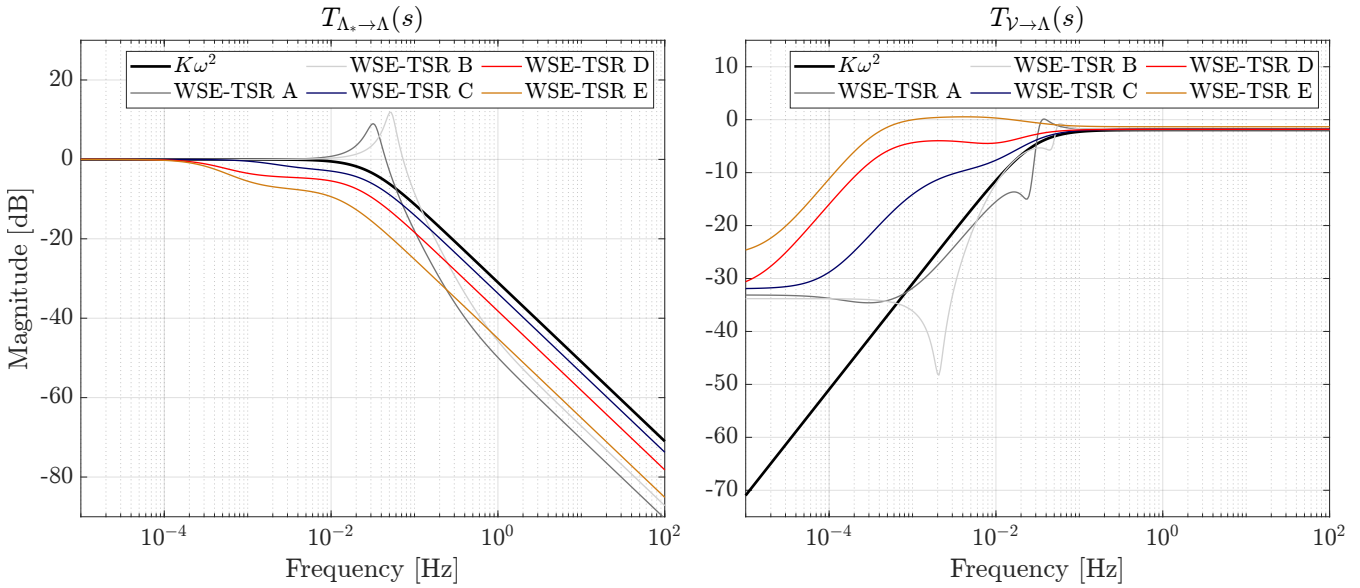


Figure 11. Bode plots of the closed-loop transfer functions $T_{\Lambda^* \rightarrow \Lambda}(s)$ and $T_{\gamma \rightarrow \Lambda}(s)$ for the baseline $K\omega^2$ and the WSE-TSR tracking controller cases. Regarding $T_{\Lambda^* \rightarrow \Lambda}(s)$, an increase in controller bandwidth with respect to the baseline can be observed when the calibration selected aims to maximise the power performance (i.e. A and B). On the other hand, for $T_{\gamma \rightarrow \Lambda}(s)$, this improvement is translated into a high-frequency sensitivity deterioration.

observations in the open-loop analysis: increasing points toward point A exhibit an increased bandwidth and reference tracking performance. Furthermore, only points A and B show a resonance peak resulting in a higher closed-loop cut-off frequency. For the transfer function $T_{\gamma \rightarrow \Lambda}(s)$, it is concluded that cases C, D, and E are subpar in disturbance rejection performance compared to the baseline case. In addition, the effect of the Bode sensitivity integral is represented by the two remaining cases. That is, cases A and B show increased disturbance rejection performance for frequencies below the controller bandwidth, whereas after this value, the characteristics worsen with respect to the baseline controller.

5.3 Time-domain results

To further support the observations from the frequency-domain analysis, this section presents realistic time-domain simulation results. For clarity reasons, only two input vectors Γ_5 corresponding to cases B and C are chosen. This selection aims to illustrate the characteristics of the WSE-TSR tracking controller for the optimal solution $f_2(\Gamma_d)$ and the trade-off between $f_1(\Gamma_d)$ and $f_2(\Gamma_d)$ compared to the baseline controller.

The high-fidelity simulation is performed with OpenFAST using the NREL 5-MW reference turbine for a realistic turbulent wind profile, with a mean wind speed of $\bar{V} = 9 \text{ m/s}$ at hub height, a turbulence intensity of $\text{TI} = 15 \%$, and a total simulation time of 3600 s. Figure 12 shows the wind speed and the simulation results for the tip-speed ratio, tip-speed ratio tracking error,

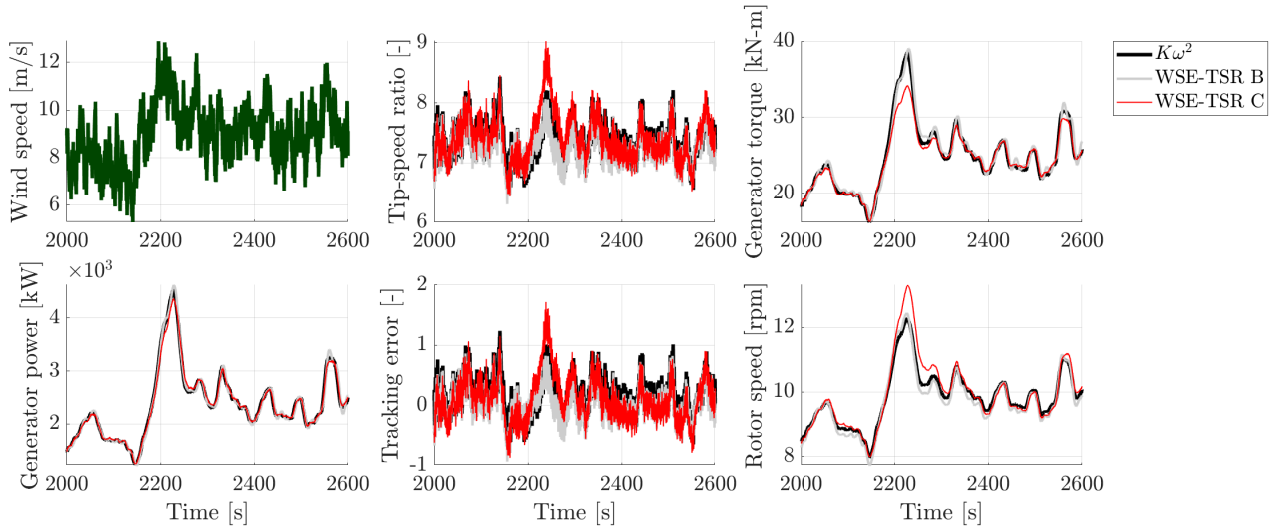


Figure 12. Simulation results for the $K\omega^2$ and the WSE-TSR tracking controllers subject to a realistic turbulent wind speed with a mean of 9 m/s and a turbulence intensity of 15 %. Only results for cases B and C are presented. As expected from the location on the corresponding Pareto front \mathcal{P}_f^5 , case B shows a similar performance to the baseline control strategy. On the other hand, case C represents a trade-off between the two objectives, minimising torque fluctuations with a minor impact on power production.

475 generator torque, rotor speed, and generator power. A smaller portion of the simulation is presented to emphasise the features in the time-domain results.

The WSE-TSR tracking controller, calibrated for case B, demonstrates performance comparable to the baseline controller without exhibiting superior power production. These observations align with the trends of the Pareto front illustrated in Figure 9. Simulation results obtained for case C show reduced torque fluctuations at the expense of increased oscillations in the
 480 rotor speed. This particular calibration results in a slower response of the WSE-TSR tracking controller, rendering the wind turbine more susceptible to variations in wind speed and, consequently, leading to higher fluctuations in rotor speed.

Upon closer examination, a notable instance occurs around 2200 s, wherein a change in wind speed from 8 m/s to 12 m/s prompts a corresponding change in rotor speed from 8 rpm to 13 rpm and an alteration in the tip-speed ratio from 7 to 9. During this transition period, the tip-speed ratio deviates from the reference λ_* , slightly increasing the tip-speed ratio tracking error (i.e. $\lambda - \lambda_*$). However, a minimal impact can be observed in power extraction from the wind, confirming that tuning C
 485 provides a good trade-off between power maximisation and load minimisation for the considered turbine.



6 Conclusions

This study presents a detailed analysis of the conventional $K\omega^2$ and the more advanced WSE-TSR tracking scheme, being a combined estimator-based tracking controller. A linear frequency-domain framework has been derived to evaluate the characteristics of both control schemes. A unified analysis strategy is proposed for a fair comparison of the controllers.

To explore the performance potential of both control schemes and, more specifically, to discover whether the advanced controller provides benefits over the conventional one, a multi-objective optimisation problem is defined. The conflicting objectives are power maximisation and control signal variance minimisation. The approach to solving this optimisation problem is to explore the performance space using a constrained guided search for different dimensionalities of the design space. In other words, the controller calibration parameters have been categorised in input vectors of different dimensions, each subject to the multi-objective optimisation problem. The resulting Pareto front approximations represent the optimal solutions and controller calibrations, providing a trade-off between the defined objectives. A set of Pareto optimal solutions has been evaluated in the frequency and time domains.

Numerical simulations on the NREL 5 MW reference turbine show that an *optimally* calibrated WSE-TSR tracking control scheme can increase the controller bandwidth resulting in larger torque fluctuations. However, as opposed to claims about improved power capture in the literature, no power gains are attainable for present-day relevant turbine sizes compared to baseline control. On the other hand, the proposed calibration framework makes it possible to find a set of design variables for the WSE-TSR tracking control scheme that reduces torque fluctuations with a minor impact on the captured power.

Overall, the WSE-TSR tracking controller exhibits a more flexible control structure compared to the baseline $K\omega^2$ controller, providing a trade-off between power and load objectives that can facilitate the operation of large-scale modern wind turbines. Future work will focus on performing a similar analysis on smaller-scale wind turbines to confirm these benefits even for other commercial turbines.

Appendix A: Similarity to state feedback controller design

This section proves that by following the state feedback control design theory, it is possible to end up with equal results to the analysis strategy proposed for the $K\omega^2$ controller, as illustrated in Figure A1. First, the wind turbine to be controlled is assumed to be described by a linear state model with single input $T_{g,K}$, a single output ω_r and a single state ω_r (Aström and Murray, 2010):

$$\dot{\omega}_r = A\omega_r + BT_{g,K}, \quad \omega_r = C\omega_r + DT_{g,K}, \quad (\text{A1})$$

where $A = G(V)$, $B = E$, $C = 1$ and $D = 0$.

By applying Assumption 1.1, the model general time-invariant control law is a function of the state and the reference input:

$$T_{g,K} = \alpha(\omega_r, \lambda_*).$$

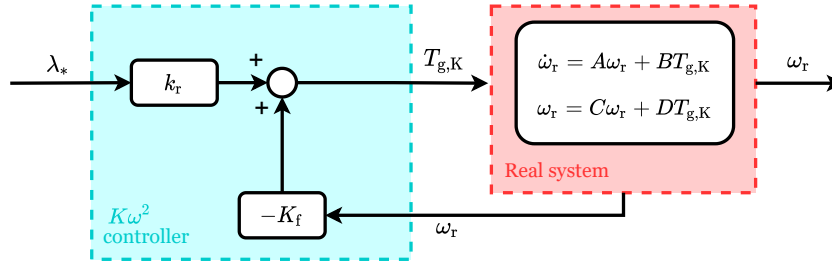


Figure A1. Block diagram of a state feedback controller with a reference shaping block, adapted for the $K\omega^2$ controller (Aström and Murray, 2010). The full system consists of the real system dynamics, here assumed to be linear, and the controller elements K_f and k_r . The controller uses the system state ω_r and the reference input λ_* to command the wind turbine through its input $T_{g,K}$.

If the feedback is restricted to be linear, it can be written as

$$T_{g,K} = -K_f \omega_r + k_r \lambda_*, \quad (\text{A2})$$

in which K_f is the feedback gain, k_r is the reference shaping gain, and λ_* is assumed to be a constant reference signal. This representation illustrates the baseline controller with elements K_f and k_r in a similar form as the analysis strategy presented in Equation (14). Therefore, to prove that the $K\omega^2$ controller is equivalent to a state feedback controller with reference shaping, Equation (14) should match Equation (A2), as

$$K_{1,K} = -K_f, \quad \text{and} \quad K_{2,K} = k_r. \quad (\text{A3})$$

Assuming that this equality is valid, it results in

$$K_f = -K_{(\Omega_r \rightarrow T_g),K} = -\left. \frac{\partial T_{g,K}}{\partial \omega_r} \right|_{(\bar{\omega}_r, \lambda_*)} = -\frac{\rho R^3 A_{\text{rot}} C_{p,*}(\lambda_*)}{N \lambda_*^3} \bar{\omega}_r. \quad (\text{A4})$$

When the feedback (Equation (A2)) is applied to the wind turbine (Equation (A1)), the closed-loop system is given by

$$\dot{\omega}_r = (A - B K_f) \omega_r + B k_r \lambda_*. \quad (\text{A5})$$

Follows the formulation of k_r as the controller aims to drive the output to the given reference

$$k_r = -\frac{1}{\left(C(A - B K_f)^{-1} B \right) \frac{V}{R}}, \quad (\text{A6})$$

in which the term V/R is added to the original formulation (Aström and Murray, 2010) to satisfy the goal of the controller:

$$\omega_r = \lambda_* \frac{V}{R}.$$

Substituting the expressions of A , B , C and D into the formulation of k_r (Equation (A6)) yields

$$k_r = \frac{\rho R^3 A_{\text{rot}} C_{p,*}(\lambda_*)}{2N} \left(-\frac{3}{\lambda_*^4} C_{p,*}(\lambda_*) + \frac{1}{\lambda_*^3} \frac{\partial C_{p,*}(\lambda_*)}{\partial \lambda_*} \right) \bar{\omega}_r^2 = \left. \frac{\partial T_{g,K}}{\partial \lambda_*} \right|_{(\bar{\omega}_r, \lambda_*)} = K_{(\lambda_* \rightarrow T_g),K}. \quad (\text{A7})$$



535 Since $K_{1,K}$ describes the feedback term and $K_{2,K}$ describes the reference shaping term, the equivalence between the $K\omega^2$ controller and state feedback controller with reference shaping is demonstrated.

Author contributions. **Livia Brandetti:** Conceptualisation, Methodology, Software, Validation, Investigation, Visualisation, Writing - original draft. **Sebastian Paul Mulders:** Conceptualisation, Methodology, Supervision, Investigation, Writing - review and editing. **Yichao Liu:** Supervision, Investigation, Writing - review. **Simon Watson:** Resources, Writing - review. **Jan-Willem van Wingerden:** Conceptualisation, Methodology, Supervision, Resources, Writing - review.

540 *Competing interests.* At least one of the (co-)authors is a member of the editorial board of Wind Energy Science.



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