

Response to Reviewer 1

April 4, 2025

Major Concern:

“Overall, the article is well written, figures are high quality and the mathematical formulations and the technical information are presented accordingly. However, I have one major concern for the publication of this paper. For me is very difficult to follow the reasoning about the EKF implementation/design, specially the sensors used and the observation model of both the V3 and V9 kites flight tests.

In my opinion, the paper should be optimized for increased clarity and conciseness. The authors should make an effort to facilitate the reader the matching between caps 4 and 5.”

Response: We thank the reviewer for highlighting the need for greater clarity in the explanation of the EKF design and its relationship to the sensor configurations used in the V3 and V9 kite flight tests.

To address this concern, we have revised Sections 3 to 5 to explicitly distinguish between required and optional measurements across different EKF configurations. In particular:

- In Section 3 (Sensor Setup), we clarify more concisely the most reliable measurements, which include position and velocity (from GPS), tether force (from a load cell), and reel-out speed (from the tether reel-out encoder), which are sufficient to estimate the kite motion. We also specify that when the KCU is modeled, a measurement of acceleration is additionally required to account for its inertial effects.
- In Section 4 (Filter Design), we state more clearly the required measurements for the EKF, and the need for additional acceleration measurement if the KCU is modeled.
- In Section 5, we improved the explanation of the different EKF setups and explicitly reference Section 3 when introducing the baseline configuration. This reinforces the logic behind the sensor combinations used in the evaluation of V3 and V9 datasets.

Together, these changes clarify the reasoning behind the EKF design and improve the consistency of terminology across sections. We hope these improvements resolve the reviewer’s concern and make the EKF framework easier to follow.

Minor Comment 1:

“Line 115-120, further discussion about direct measurement of in-situ aerodynamic angles of attack and sideslip is welcomed (Oehler and Schmehl, 2019). Using booms for isolating aerodynamic sensors from aircraft’s perturbations is a well-known practice in the aerospace industry during development phases”

Response: We thank the reviewer for this helpful suggestion. We have expanded the corresponding paragraph in the sensor setup section to include the resolution of the sensor. In response to the reviewer’s comment, we now mention the use of boom-mounted sensors on the leading edge of the kite during development phases, which is indeed a common approach in the aerospace industry. While effective for isolating sensors from the perturbations caused by the wing, this solution is generally unsuitable for commercial airborne wind energy systems due to its fragility. The revised paragraph also includes references to Oehler and Schmehl (2019) and Borobia-Moreno et al. (2021) to support these points.

Minor Comment 2:

“Line 143 → Fig2. could be improved by showing a detailed view/scheme of the implementation of the load cell sensing the tension of the tether without interfering with the reel in-out system.”

Response: We appreciate the reviewer’s suggestion. However, we prefer not to include a detailed schematic of the load cell implementation due to its proprietary nature. A schematic of a similar system can be found in Hummel (2018), which illustrates the principle used. We trust the updated description in the manuscript clarifies the sensing approach while respecting confidentiality constraints.

Minor Comment 3:

"Further detail about how airborne data is logged/transmitted to the ground and synchronized with the ground-measured data is also welcomed."

Response: We appreciate the reviewer's interest in the data acquisition and synchronization procedures. However, the airborne and ground-based sensor data used in this study were pre-processed and provided by Kitepower, and the specifics of the logging, transmission, and synchronization infrastructure were not available to the authors. As such, we are unable to provide further technical detail on this aspect. We would also like to note that the focus of this work is on the development and evaluation of the EKF estimation framework, which operates on already time-aligned datasets. As a result, the underlying transmission architecture does not impact the methodology or the conclusions of this study.

Minor Comment 4:

"Line 396, 405-410 → In my opinion, the output of the Px4 position and velocity estimations should not be used as measurements for the EKF as errors are not guaranteed to be zero mean and gaussian. Instead, raw GPS position and velocity from PixHawk Gps should be used, plus a measurement error model to guarantee that the measurement noise described in eq.24a and 24b is Gaussian white noise. (R.Borobia et al. 2018). This change will eliminate the dynamics of the PixHawk onboard estimator increasing the stability of the filter."

Response: We fully agree with the reviewer that using raw GPS measurements would be preferable to ensure that the assumptions on the measurement noise in the observation model (Eq. 24a and 24b) hold. Unfortunately, in the dataset analysed, only the output of the Pixhawk's internal EKF (GPS+IMU fused) was logged, and the raw GPS data were not recorded.

We attempted to reflect this limitation in the manuscript (lines 396–397), but we recognise that the implication for the filter's noise characteristics and stability may not have been sufficiently emphasised. To address this, we have clarified the text accordingly to highlight the impact of using pre-filtered measurements.

Minor Comment 5:

"Line 411 → In Fig9. The measured Euler angles are the estimated ones by Px4?"

Response: Yes, the Euler angles shown in Fig. 9 are the estimates provided by the PX4 onboard EKF, based on the Pixhawk's IMU data. A clarification is added to the text to make this point explicit and avoid future readers to question the same.

Minor Comment 6:

"Line 419 → Calculation of Yaw angle assuming alignment of the kite body axis with aerodynamic velocity vector assumes no side-slip during the flight. However, direct measurement of side-slip angle showed non zero values for a inflatable kite (R.Borobia et al. 2021)"

Response: We agree with the reviewer that the assumption of zero side-slip does not strictly hold, particularly during manoeuvres. Our intention was not to neglect sideslip effects, but rather to illustrate the general tendency of the kite to align with the local inflow. To clarify this point, we have extended the discussion by including measured sideslip angle statistics from the V9 dataset, which show a standard deviation of approximately 2.5° and peak values up to 5° during turns.

Minor Comment 7:

"520 -530 → The underpredicted side-force could be related to assuming zero-side slip angle? "

Response:

We thank the reviewer for the observation. To clarify, the side-force is estimated by the EKF, but it is not modelled as a function of the side-slip angle (see section 4). The dynamic model employed is a 3-DOF point-mass formulation, where yaw dynamics are not considered. The kite orientation (pitch and roll) is inferred from the bridle segment orientation in the quasi-static tether model, rather than modelled as a full 6-DOF body. The assumption of alignment with the apparent wind is used only in post-processing to estimate the yaw angle for qualitative analysis and is not part of the EKF or the dynamic model. Therefore, the underprediction of the side-force is not attributable to a zero side-slip assumption.

Response to Reviewer 2

April 4, 2025

Major Comments:

“This paper addresses some very interesting questions on kite dynamics using fusion techniques for the analysis of experiments. It draws on the substantial experience of the Delft team, which is undoubtedly the world’s leading centre for kite studies. The paper is composed of 41 pages including 4 pages only for the introduction. Section 2, 3 and 4 present the material, i.e. system, sensors and fusion technics used for analysis. Section 5 presents many results in 4 subsections (kite kinematics, system dynamics (aerodynamic identification and turning dynamics), wind estimation and turbulence measurements). It ends with a broad conclusion.

The article could probably have been split into 2 separate articles. That would have made the point clearer. The language is highly technical, which often makes it difficult to read. It is often difficult to find the definition of one of the many variables. In such cases, an appropriate nomenclature is essential. Given the complexity of the problem being addressed and the large number of variables involved, the use of full variable names in the text should be preferred most of the time for easier reading.

One of the main gap in the document is a clear definition of the reference frames used in this study. With all the information available, the reader probably has all the information needed to find the definition of each variable. But this definition is uncertain, and the reader may make a mistake. An appendix at the end of the document gives the values of the experimental parameters and the model used during the tests. This should ensure reproducibility of the results. The codes are also provided.”

Response:

We are grateful to the reviewer for the thoughtful and encouraging comments on our manuscript. We appreciate the acknowledgement of the Delft team’s longstanding contributions to the field and the recognition of the paper’s ambition in consolidating these insights.

We acknowledge that the manuscript is lengthy; however, we consider the topic to be a closed and coherent body of work. The aim was to integrate a broad range of experimental and modelling expertise into a single, comprehensive study. Given the depth of analysis and the novel fusion framework presented, we believe this integrated presentation will serve the airborne wind energy community more effectively than a fragmented approach across multiple papers.

In response to the specific points raised:

- A **nomenclature section** has been added to the manuscript, listing all relevant variables along with their definitions and units, to facilitate readability.
- The manuscript has been revised to **consistently use full variable names** throughout, particularly in technically dense passages, to improve clarity.
- The **main reference frame** used throughout the study is now explicitly defined in Section 4 as the East-North-Up (ENU) frame, in which all vector quantities (e.g., position, velocity, wind velocity) are expressed. The only exception is the definition of the Euler angles, which follows the North-East-Down (NED) convention to avoid discontinuities in angle representation. Furthermore, Figure 4 has been updated to reflect this clarification, with axis labels revised for improved consistency and readability.
- We have carefully revised the text following the reviewer’s 121 in-line comments, aiming to improve clarity and accessibility throughout the manuscript. The response to these comments can be found in the appended pdf.

Minor Comment 1:

"Line 80, The authors claim that their model improves on the existing one by considering the sag of the lines and the dynamics of the KCU. We expect them to present comparisons of measurement results with and without taking these quantities into account. This would make it possible to visualize concretely the impact of taking these factors into account."

Response:

We thank the reviewer for this valuable suggestion. In response, we have revised the text to clarify that the contribution of this work lies in the introduction of a more detailed and physically representative model—rather than claiming direct superiority in estimation performance over previous, simpler models. The proposed model incorporates tether sag and the dynamics of the kite control unit (KCU), which are not commonly accounted for in existing approaches.

While a direct side-by-side quantitative comparison with models omitting these features is beyond the scope of the present study, the advantages of the enhanced model fidelity are illustrated through several key results. In particular, the incorporation of KCU dynamics enables partial estimation of the wing orientation and structural deformation, providing valuable insight into aeroelastic behaviour during flight. These estimations are obtained without substantial increases in computational cost.

To support this point, we have included a new appendix (Appendix C) presenting relevant filter performance metrics and convergence behaviour, which demonstrate the robustness of the implementation.

Minor Comment 2:

"Line 112-114: the KCU appears to be a reference for the orientation of the kite, which does not"

Response:

We appreciate the reviewer's observation. The original formulation may have implied that the KCU serves as a stable reference frame for the orientation of the kite, which is not the case. We have revised the text to clarify that pitch and roll angles are defined with respect to the orientation of the last tether segment, rather than to the KCU. The KCU frame is not used as a reference, as it is not rigidly fixed or well-defined due to its suspended configuration and motion. This correction ensures consistency with the later sections of the manuscript, where kite orientation is explicitly referenced relative to the tether.

Minor Comment 3:

"Line 113-114 The depower angle deserves a more rigorous definition."

Response:

We thank the reviewer for this comment. The text has been revised to provide a clearer and more rigorous definition of the depower angle. We now reference Figure 1 upon first mention and clarify that the depower angle is determined experimentally for each system. Additionally, we have introduced the definition of the tether angle of attack and the parameter λ_0 to better explain the relationship between the relevant aerodynamic angles.

Minor Comment 4:

"Line 119 Fig.3.a does not exist. Replace by Fig.3"

Response:

We thank the reviewer for noticing the typo, which is now corrected.

Minor Comment 5:

"Line 160 Figure 3 shows 4 boxes on 4 battens. We need to specify which one is the IMU and which other sensors are in the others."

Response:

We thank the reviewer for this observation. We have clarified in the caption that all four battens shown in the image are equipped with GPS+IMU units. Additionally, the specific sensor configurations used in the analysed flights—namely, the number and placement of the units—are now detailed in the results section. Please note that the kite depicted in the figure differs from the one used in the presented datasets.



Kite as a Sensor: Wind and State Estimation in Tethered Flying Systems

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Abstract. Airborne wind energy systems (AWESs) leverage the generally less variable and higher wind speeds at increased altitudes by utilizing kites, with significantly reduced material costs compared to conventional wind turbines. Energy is commonly harnessed by flying crosswind trajectories, which allow the kite to achieve speeds significantly higher than the ambient wind speed. However, the airborne nature of these systems demands active control and makes them highly sensitive to changes in wind conditions, making accurate wind measurements essential for steering the kite along its optimal trajectory. This paper presents an advanced sensor fusion technique based on an iterated extended Kalman filter (EKF) for state and wind estimation for AWESs. By integrating position, velocity, tether force, and reeling speed, this method provides accurate estimations of system dynamics, including kite orientation and tether shape. The estimates of the wind speed and direction are compared to lidar measurements, showing a strong agreement across various atmospheric conditions. The results demonstrate that this approach can effectively capture the transient dynamics of atmospheric wind using sensors typically already present in AWESs, making it suitable for supervisory control strategies and ultimately enhancing energy efficiency and system reliability across diverse atmospheric conditions.

1 Introduction

Airborne wind energy systems (AWESs) harness wind energy with tethered aerial devices, substantially reducing material usage compared to conventional wind turbines by employing one or more tethers and a flying apparatus instead of towers and blades. This reduction has the potential to lower the costs associated with wind energy production but also allows for the exploitation of higher-altitude winds, which are generally less variable and of a higher average speed than those at ground level.

Despite these advantages, AWESs face significant challenges, particularly regarding system robustness against the complexities of atmospheric wind dynamics. The motion of the kite during crosswind flight is strongly influenced by the wind, which largely dictates the flight speed and the tether force. This dependency makes the system highly susceptible to changes in wind speed and direction. For soft kites, the low mass of the tensile structure allows for rapid adaptation to changes in wind speed, making this type of kite particularly sensitive to turbulence and gusts. Therefore, a detailed understanding of wind dynamics at the operational altitudes is crucial.



25 Above the well-studied surface layer, logarithmic wind profiles may not accurately represent the variation of wind speed
with height, and phenomena such as wind veer and low-level jets become increasingly significant. As a result, it is crucial to
adapt the kite's trajectory to these specific higher-altitude wind conditions, which necessitates reliable wind measurements.
This need for accurate wind data can be met through remote sensing devices such as lidar (Sommerfeld et al., 2019), or by
using the kite itself as a sensor.

30 Using the aerial device as a sensor eliminates the need for additional equipment beyond what is already used for kite control
and allows wind velocity information to be integrated into a supervisory control strategy for the AWES. This integration
enables the system to adjust the flight trajectory in response to changing wind conditions, optimizing performance and aiding
in high-level decisions, whether to take-off or to land.

A common method for determining ambient wind conditions at the kite involves mounting flow sensors on the kite to
35 measure the apparent wind speed and direction. Pitot tubes are frequently used, in varying configurations. Five-hole probes
and single-hole probes combined with two flow vanes can measure the three-dimensional velocity vector of the apparent wind
(Elfert et al., 2024; Borobia-Moreno et al., 2021; Oehler and Schmehl, 2019), allowing for the determination of ambient wind
speed, provided the kite's velocity is known. Simpler setups with single-hole probes alone (Vlugt et al., 2013; Borobia et al.,
2018) or with one vane (Schelbergen, 2024) are also used but do not capture the full three-dimensional velocity, limiting their
40 capability.

However, this approach comes with significant challenges. The accuracy of the measurements depends heavily on the sen-
sor's position, mounting method, and regular maintenance and recalibration. For soft kites, which undergo substantial defor-
mation during flight along with vibrating bridle lines and fluttering membrane, the collected data can become excessively noisy
and unreliable (Dunker, 2018; Leuthold, 2015). These challenges, particularly for tensile, lightweight kite systems, highlight
45 the need for more advanced approaches.

One effective solution is sensor fusion, which combines data from multiple sensors integrated into the AWES to provide a
more robust and consistent representation of the kite state and wind characteristics. Sensor fusion relies on a time-dependent
model that represents the system's dynamics. By integrating sensor data within this model, the method enhances the reliability
of the measured states and can also serve to estimate quantities such as wind speed and direction. Depending on the model's
50 complexity, the estimated state may encompass not only the kite's position and velocity but also its aerodynamic characteristics
and the tether sag, resulting in a more comprehensive understanding of the system's dynamics.

Numerous studies have investigated sensor fusion techniques for AWE state and wind estimation (Table 1). For instance,
Fagiano et al. (2013, 2014) proposed an extended Kalman filter (EKF) to estimate the kinematics of a tethered aircraft, using
a purely kinematic model and evaluating various sensor configurations, including satellite-based global positioning system
55 (GPS) and tether angle measurements. Similarly, Polzin et al. (2017); Wood et al. (2018) explored configurations incorporating
inertial measurement units (IMUs), tether angles, and camera tracking, introducing a novel kinematic model that accounts for
tether dynamics and sag through time delays and ground velocity differences. This study also addressed kite steering delays by
modelling the yawing motion with a linear turn rate law. To further address tether sag, Freter et al. (2020) proposed an adaptive
Kalman filter with variable weights based on tether force, combining data from load cells, tether angles, IMUs, and camera



Table 1. Summary of studies on sensor fusion for AWESs.

Study	Filter Type	Minimum Required Measurements	Kite Model	Tether Model
Fagiano et al. (2013, 2014)	EKF	Position, acceleration, orientation, orientation rates	Kinematic	Straight & Inelastic
Polzin et al. (2017); Wood et al. (2018)	EKF	Position, orientation, orientation rates	Kinematic	Straight & Inelastic
Freter et al. (2020)	Adaptive EKF	Position, acceleration, tether force	Kinematic	Straight & Inelastic
Williams et al. (2008)	Square-root UKF	Position, tether force and direction, tether length and reeling speed	Point Mass	Straight & Inelastic
Ranneberg (2013)	Square-root UKF	Position, tether force, tether length, steering input	Point Mass	Straight & Inelastic
Schmidt et al. (2017, 2020)	EKF	Position, velocity, wind speed and direction (reference height), tether force, tether length and reeling speed, steering input	Point Mass	Straight & Inelastic
Borobia et al. (2018); Borobia-Moreno et al. (2021)	EKF	Position, velocity, angular velocities, magnetic field, airspeed magnitude, tension at the bridles, kite center of mass	Rigid Body	Straight & Inelastic
Current Study	Iterated EKF	Position, velocity, tether force, tether reeling speed	Point Mass	Curved & Elastic (Quasi-Static)

60 tracking, which effectively reduced estimation errors under sagged conditions. However, these approaches do not estimate the wind velocity, which requires the inclusion of forces in the modelling to capture the wind impact on system behaviour.

In Williams et al. (2008), an unscented Kalman filter (UKF) was proposed as a state estimator for both the kite's state and wind conditions within a non-linear tracking control framework. The simulation results demonstrated that the UKF performed well when assuming a straight tether and was robust against noise. However, the wind velocity estimates were found to be the
 65 most sensitive to noise.

Ranneberg (2013) utilized a UKF with a Lagrangian dynamic model that incorporates the forces on the kite, assuming constant aerodynamic coefficients, as well as rotational inertia of the drum. The results were validated against simulation data and experimental measurements, including pulsed lidar measurements at various heights, demonstrating that measuring the kite's position and the tether force is sufficient for estimating wind speed, although the vertical component of the wind velocity
 70 was assumed to be zero. Schmidt et al. (2017, 2020) proposed a similar approach using an EKF with a Lagrangian dynamic model but without including drum inertia. Their model adds measured wind speed and direction at a reference altitude, which



works well for their case study of a kite flying at low altitudes but can introduce errors when the kite flies at higher altitudes. Nevertheless, the model is validated against experimental and simulation data, showing the potential of the approach.

In Borobia et al. (2018); Borobia-Moreno et al. (2021), a more complex model is employed to estimate the full state of the kite, including the ambient wind conditions and aerodynamic forces and moments. However, this increased complexity necessitates a significantly larger number of measurements. These measurements include data from GPS and IMU sensors, Pitot tube, including a five-hole Pitot tube, wind sensors on the ground and several load cells installed in the bridle line system of the kite.

A common limitation of existing methods is the assumption of a straight and inelastic tether, which can introduce errors when the tether force is low and the real tether sags. Additionally, soft kites with a suspended robotic control unit are affected by the inertia of the suspended unit, impacting orientation and dynamics (Roullier, 2020). Our study addresses these limitations by employing a more comprehensive model that accounts for both tether sag and KCU inertia, resulting in more accurate wind velocity estimates without requiring additional measurements. Specifically, we employ an iterated EKF that models the wing as a point mass and incorporates a quasi-static tether model (Williams, 2017). To account for the inertial effects of the KCU, an additional point mass is included between the tether and the wing, resulting in a two-point representation of the kite (Schelbergen and Schmehl, 2024). Validation through experimental data demonstrates the effectiveness of this approach in accurately estimating both wind velocity and kite state under varying atmospheric conditions. Although this study focuses on soft kites, the methodology is equally applicable to fixed-wing devices.

The results are presented for two kite prototypes, the V3 and the V9, both being leading-edge inflatable kites operated by Kitepower B.V., with flattened wing areas of 25 and 60 m², respectively. The V3 kite has been extensively studied in prior research and has served as a reference model (Oehler and Schmehl, 2019; Viré et al., 2022; Cayon et al., 2023; Poland and Schmehl, 2023; Schelbergen and Schmehl, 2024). In contrast, the V9 kite, representing Kitepower's current commercial prototype, is primarily used in the present study to showcase the method's ability to predict wind velocities at the kite. This analysis is based on an unprecedented dataset that combines high-quality AWES operational data with high-resolution wind measurements from profiling lidar. The AWES data include measurements of kite position, velocity, orientation, and accelerations; tether tension, length, and reeling speed; as well as airflow measurements from a Pitot tube and wind vanes, while the lidar data provide vertical wind profiles with good temporal and spatial resolution. Together, these datasets enable a comprehensive analysis of wind-kite interactions across various atmospheric conditions.

The remainder of this paper is organized as follows. Sect. 2 provides an overview of the AWE system, Sect. 3 discusses the experimental sensor setup, Sect. 4 details the filter design and sensor calibration, Sect. 5 presents the results and analysis, and Sect. 6 concludes with implications and future research directions.

2 System Overview

The main components of ground-generation soft kite AWESs are the ground station, tether, and kite, which consists of the wing, bridle system, and suspended kite control unit (KCU). The kite flies in cyclic patterns to generate electricity, alternating



105 between traction and retraction phases. During the traction phase, the kite performs crosswind manoeuvres, reeling out the tether and driving a drum connected to a generator. Once the tether reaches its maximum length, the system reverses, using the generator as a motor to reel in the tether while the kite is flown in a **more aerodynamically efficient** configuration to prepare for the next cycle.

In Fig. 1, the key components of a soft kite for airborne wind energy harvesting are shown alongside commonly used sensors. 110 The kite is controlled by the KCU, which connects the bridle line system and the tether. The front bridle lines transmit most of the aerodynamic force from the wing, while the rear bridle lines are used to actuate the wing through the KCU and the steering and depower tapes. The steering tape deforms the wing asymmetrically by modifying the length of the steering lines to initiate turns, while the depower tape symmetrically adjusts the steering lines to pitch the wing **relative to the KCU**. This pitch is **quantified by the depower angle α_d** . Increasing this depower angle directly influences the kite's aerodynamic performance and is mainly used to reel in the kite efficiently. 115

The aerodynamics of the kite are generally characterized by the angle of attack at the centre section of the wing, α_w . However, directly measuring this angle is challenging because it would require isolating the inflow at the kite from the flow disturbances caused by its aerodynamics, which can be difficult to achieve reliably in practice. Consequently, sensors are more commonly installed on the bridle lines (see Fig. 3a) or on the tether below the KCU.

120 The bridle angle of attack α_b is defined as the angle relative to the plane perpendicular to the **power lines** and is related to the angle at the wing by

$$\alpha_w = \alpha_b - \alpha_d, \quad (1)$$

where the depower angle, α_d , is approximated as a linear function of the depower input, u_p . This relationship includes an initial offset, $\alpha_{d,0}$, corresponding to the powered kite state,

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$$\alpha_d = \alpha_{d,0} + \Delta\alpha_d u_p, \quad (2)$$

where u_p ranges from 0 to 1, and $\Delta\alpha_d$ represents the change in angle of attack from the fully powered to the depowered state. In previous works (Oehler and Schmehl, 2019; Schelbergen, 2024), this angle change was estimated using a simple geometric model that relates the length of the depower tape to the depower angle. However, with the integration of the tether model into the EKF, this angle can now be estimated directly from the measurements, as detailed in Sect. 5. Finally, the bridle angle of 130 attack can be translated to the tether angle of attack, α_t , by

$$\alpha_t = \alpha_b + \lambda_0 + \theta_k, \quad (3)$$

where λ_0 depends on the aerodynamic load distribution between the front and rear bridle lines, and θ_k is the kite pitch with respect to the tether caused by the KCU weight and inertia. λ_0 has been found to be relatively constant for a set depower setting but is highly dependent on changes in the depower tape length (Oehler and Schmehl, 2019).

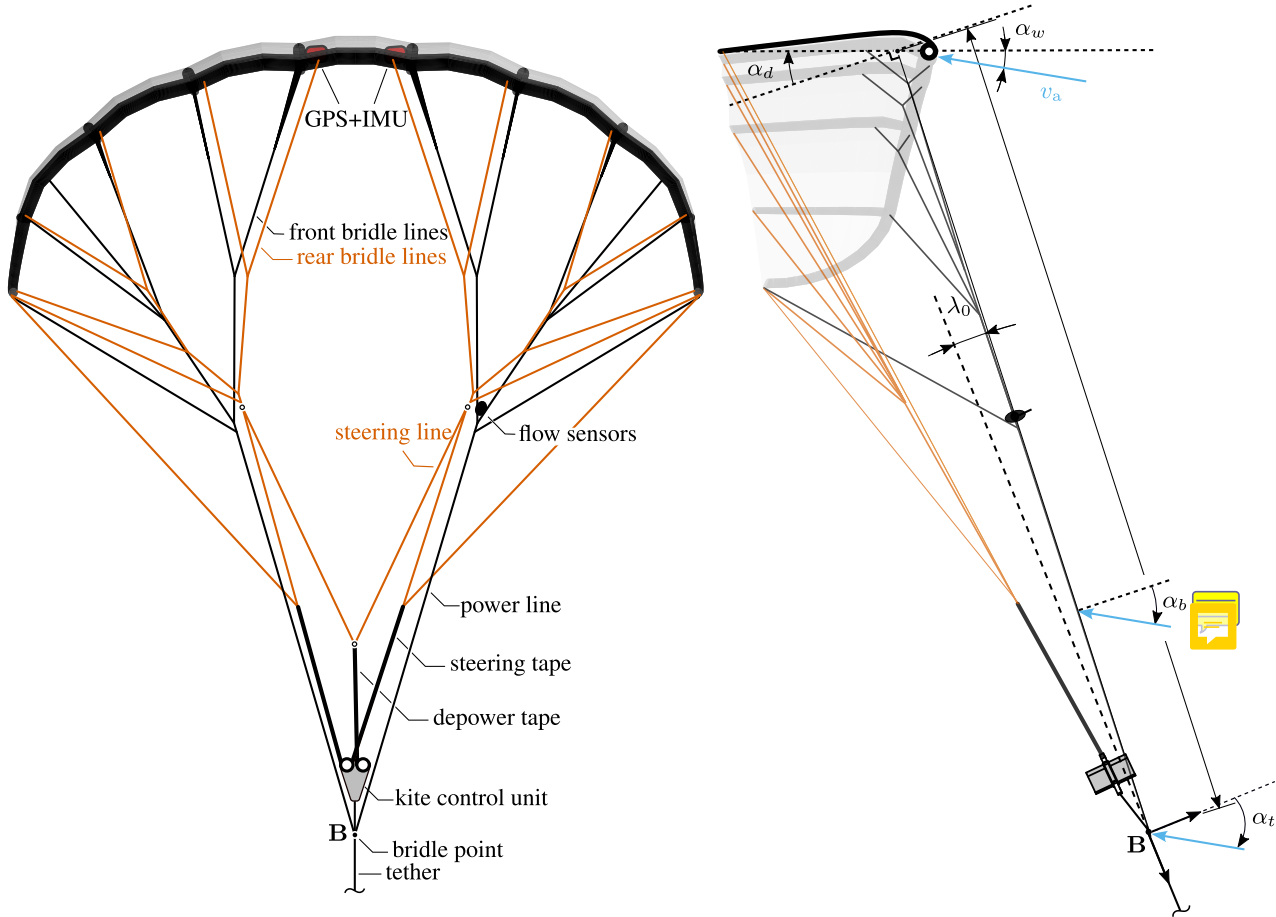


Figure 1. Illustration of system components and sensor setup. Adapted from Oehler and Schmehl (2019). The V3 kite geometry shows the bridle point B below the KCU, unlike the V9 geometry where the KCU is at the bridle point.

135 3 Sensor Setup

Measuring the state of AWESs presents significant challenges, particularly for soft kites, which, by their nature as tensile membrane structures experience substantial deformations during flight, along with vibrating components and high accelerations during turning manoeuvres. Understanding the accuracy and limitations of each sensor within its specific installation context is critical for developing an effective fusion technique. This understanding enables the design of a sensor fusion model relying

140 on the most trustworthy sensors.



The following is a breakdown of the key sensors used in the analysed datasets, along with a qualitative discussion of their advantages, limitations, and considerations for accurate measurements:

- Load Cells: The force exerted by the tether is measured using a load cell located at the tether exit point of the drum (see Fig. 2). This sensor can yield accurate results, provided it is correctly calibrated (Hummel et al., 2018). One could also consider installing load cells in the kite's bridle lines to measure the force distribution (Oehler et al., 2018; Borobia-Moreno et al., 2021). However, this approach significantly increases setup times and also the risks of failures and large inaccuracies in the measurements.



Figure 2. The V9 kite in flight: view from the ground station (left), and close-up showing the suspended control unit (right). Photos courtesy of Kitepower B.V.

- Tether length: The length of the tether is measured through the reeling mechanism of the kite, where an incremental angular encoder on the drum determines the rotational speed. From this, the deployed tether length is calculated (Vlugt et al., 2013). This method allows for accurate measurements, particularly if the initial offset of the tether length is correctly identified and accounted for.
- Tether angles: The elevation and azimuth angles of the tether can be measured at the ground station using magnetic angular encoders. When combined with the tether length, these measurements can be used to estimate the kite position (Dorichel, 2013). The assumption of a straight tether generally holds during reel-out operations when the tether is under high tension, resulting in relatively accurate position estimates (Fagiano et al., 2013). However, the tether generally sags during reel-in due to reduced tension, leading to potential inaccuracies unless the sag is taken into account.
- GPS: The accuracy of GPS data is generally good as it is not affected by the deformation of the soft kite, making it a reliable source for position and velocity information. However, it is important to consider that GPS signals can be subject to problems such as signal loss, particularly during high acceleration manoeuvres (Vlugt et al., 2013).



Figure 3. Fully instrumented V3.25 kite before launch. Photo courtesy of Kitepower B.V.

- 160 – IMU: The placement of an IMU sensor on one of the inflatable tubes (see Fig. 3) of the kite has several implications. The sensor is affected by the in-flight deformations of the wing, which are particularly noticeable when transitioning from powered to depowered states and during turns. These measurements of structural deformation are useful for assessing specific aspects of the wing deformation but can induce errors if used for trajectory estimations. Furthermore, the high accelerations of the kite during turns can lead to increased noise and sensor drift (Hesse et al., 2018).
- 165 – Wind Vanes: In the analysed setups, wind vanes were mounted in the bridle line system, where determining their orientation relative to the wing is challenging due to deformation of both the wing and the bridle lines. Furthermore, vibrations in the bridle lines can introduce noise into the measurements. Alternatively, these sensors could be mounted below the KCU, alleviating most of these issues. Ideally, these sensors would be integrated with an IMU for accurate measurements relative to the ground.
- 170 – Pitot Tube: Although Pitot tubes typically achieve good accuracy, they require regular maintenance and calibration, and external factors like ice, insects, or pollution can cause clogging (Ezzeddine et al., 2019). Furthermore, when used to measure wind speed, small errors propagate into larger errors due to the wind's small contribution to the total apparent



speed. Finally, the mounting position is critical; if the sensor is not mounted at the centre of rotation of the kite, it will measure velocity induced by the kite yaw rate, further amplifying inaccuracies.

Overall, the sensors that are least susceptible to the intrinsic deformations of the soft kite and the high accelerations of the system, and thus more reliable, are the GPS, the load cell (for tether force), and the mechanism measuring the tether length and tether angles. These sensors can maintain their accuracy despite the flexible nature of the kite. Consequently, the proposed sensor fusion model primarily relies on these measurements, resulting in a minimal sensor setup consisting of a GPS (for position and velocity), a load cell, and a tether length measurement. Furthermore, if the KCU inertia is modelled, a measurement of the kite or KCU acceleration should also be included. In this study, due to data availability, this acceleration has been estimated by numerically differentiating the velocity. Additional measurements, such as airflow data or tether angles, are optional but can potentially enhance the accuracy of the estimations.

4 Filter Design

In this section, a filter is designed to estimate the state of a tethered flying system by integrating a dynamic model and an observation model in an EKF. The dynamic model captures the kite translational motion governed by aerodynamic, gravitational, and elastic tether forces. The other dynamics are represented using a quasi-static lumped mass approach proposed by Williams (2017), expanded to include the effects of the KCU inertia and weight (Schelbergen et al., 2024). The observation model requires at least the position and velocity of the kite, as well as the tether force and reel-out speed as inputs. Additionally, to model the KCU inertia, a measurement of either the KCU or the wing acceleration should be included for accurate orientation predictions. Its effect is accounted for by adding an extra tether segment to the model, representing the bridle line system, which connects to a point mass representing the KCU.

4.1 Dynamic Model

The dynamic model represents the kite wing as a point mass (m_k) following Newton's second law. Its acceleration results from the sum of the tether force at the kite $\mathbf{F}_{t,k}$, aerodynamic force $\mathbf{F}_{a,k}$, and weight $\mathbf{F}_{g,k}$. The components of the aerodynamic force are expressed as a function of the kite apparent velocity \mathbf{v}_a and the vector of aerodynamic coefficients $\mathbf{C}_a = (C_L, C_D, C_S)$, which are assumed to be time-invariant,

$$\mathbf{F}_{a,k} = \begin{cases} \mathbf{F}_L = \frac{1}{2} \rho A_k C_L \|\mathbf{v}_a\|^2 \mathbf{e}_L, \\ \mathbf{F}_D = \frac{1}{2} \rho A_k C_D \|\mathbf{v}_a\|^2 \mathbf{e}_D, \\ \mathbf{F}_S = \frac{1}{2} \rho A_k C_S \|\mathbf{v}_a\|^2 \mathbf{e}_S, \end{cases} \quad (4)$$

where ρ is the air density, A_k is the projected area of the wing, C_L , C_D , and C_S are the lift, drag, and side-force coefficients, respectively, and \mathbf{e}_L , \mathbf{e}_D and \mathbf{e}_S are unit vectors in the directions of the lift force, drag force and side-force, respectively. The drag force acts in the direction of \mathbf{v}_a , the lift force acts in the opposite direction of the tether force projected in the perpendicular



plane to \mathbf{v}_a , and the side force acts orthogonally to both. The apparent velocity is a function of the kite velocity \mathbf{v}_k and the wind velocity \mathbf{v}_w , which is also assumed to be time-invariant,

$$\mathbf{v}_a = \mathbf{v}_w - \mathbf{v}_k. \quad (5)$$

The wind velocity can be accounted for using two different approaches: firstly, assuming it is time-invariant and not dependent on height, and secondly, using a logarithmic relation with height for its horizontal component. The latter can be done by means of the friction velocity u_* and wind direction ϕ_w instead of the horizontal wind components such that the height-dependent horizontal wind speed $v_{w,h}$ is given by (Watson, 2023),

$$v_{w,h} = \frac{u_*}{\kappa} \log \frac{z}{z_0}, \quad (6)$$

where z is the height above the ground, $\kappa \approx 0.4$ is the von Karman constant and z_0 is the surface roughness length. Even though this approach generally improves estimations by incorporating physical knowledge of the wind profile, it can lead to poorer estimations compared to modelling it as height-independent if the actual wind profile deviates from the assumed logarithmic model.

The tether force at the kite is determined by assuming a shape derived from a quasi-static force equilibrium, detailed in Williams (2017), with the addition of accounting for the KCU and its localised inertia, representing the kite by two separate point masses (Schelbergen and Schmehl, 2024). The tether model uses a lumped mass approach with point masses connected by spring elements (see Fig. 4). The shape of the tether is calculated based on the tether force at the ground $F_{t,g}$, the position velocity and acceleration \mathbf{a}_k of the kite wing, the wind velocity, the azimuth ϕ_0 and elevation θ_0 of the first tether segment, and the total deployed tether length l , all of which are either incorporated into the dynamic model or directly measured and used as inputs.

The tether force at the wing is calculated using a shooting method, where the direction for each subsequent tether segment is determined by the sum of the elastic, drag, gravitational, and inertial forces given an initial estimate of the tether length and the tether force magnitude and orientation at the ground. Inertial forces for each segment are determined by their centripetal acceleration, with the segment lengths l_i adding up to the total tether length, including the bridle segment.

To compute these inertial forces, the velocities \mathbf{v}_j and accelerations \mathbf{a}_j of the discrete point masses along the tether are estimated under the assumption that they all rotate with a fixed angular velocity $\boldsymbol{\omega}$, behaving like particles of a rigid body (see Fig. 5). The velocity at the tether attachment point \mathbf{B} particle can be represented assuming a purely rotational motion about a point, the instantaneous centre of rotation (Meriam et al., 2018), which is unique for each tether particle.

$$\mathbf{v}_B = \boldsymbol{\omega} \times \mathbf{r}_{c,B}, \quad (7)$$

where $\mathbf{r}_{c,B}$ is the vector from \mathbf{B} to its instantaneous centre of rotation, which is perpendicular to $\boldsymbol{\omega}$. The acceleration can then be estimated by differentiating the velocity,

$$\mathbf{a}_B = \frac{d\mathbf{v}_B}{dt} = \frac{d(\boldsymbol{\omega} \times \mathbf{r}_{c,B})}{dt} = \frac{d\boldsymbol{\omega}}{dt} \times \mathbf{r}_{c,B} + \boldsymbol{\omega} \times \frac{d\mathbf{r}_{c,B}}{dt}, \quad (8)$$

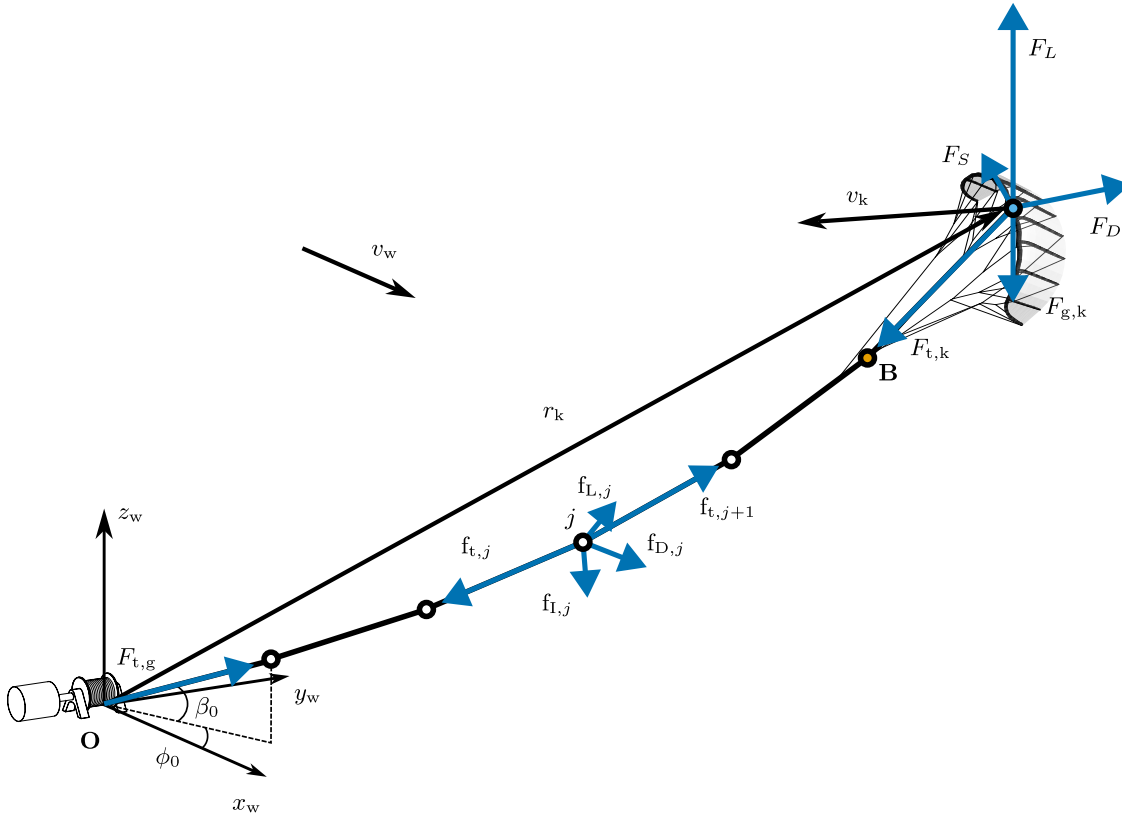


Figure 4. Schematic representation of the tether model and kite forces, as modelled by the dynamic system in the EKF. Adapted from Schelbergen and Schmehl (2024).

which can be expressed as,

$$\mathbf{a}_B = \boldsymbol{\alpha} \times \mathbf{r}_{c,B} + \boldsymbol{\omega} \times \mathbf{v}_B. \quad (9)$$

Here, $\boldsymbol{\alpha} = d\boldsymbol{\omega}/dt$ is the angular acceleration. The two terms of the acceleration represent the tangential acceleration $\mathbf{a}_t = \boldsymbol{\alpha} \times \mathbf{r}_{c,B}$ and the centripetal acceleration $\mathbf{a}_n = \boldsymbol{\omega} \times \mathbf{v}_B$.

If the acceleration and velocity of the tether attachment point **B** at the kite are known, we can compute the angular velocity, instantaneous centre of rotation, and angular acceleration as follows, assuming the tangential acceleration to be in the direction of the kinematic velocity,

$$\boldsymbol{\omega} = \frac{\mathbf{a}_n \times \mathbf{v}_B}{\|\mathbf{v}_B\|^2}, \quad \mathbf{r}_{c,B} = \frac{\mathbf{v}_B \times \boldsymbol{\omega}}{\|\boldsymbol{\omega}\|^2}, \quad \boldsymbol{\alpha} = \frac{\mathbf{a}_t \times \mathbf{r}_{c,B}}{\|\mathbf{r}_{c,B}\|^2}. \quad (10)$$

On the straight flight path segments, the kite moves on a great circle trajectory, and $\boldsymbol{\omega}$ is perpendicular to the tether, resulting in the centre of rotation being located at the ground station along the extension of the tether. (Schelbergen and Schmehl, 2024).

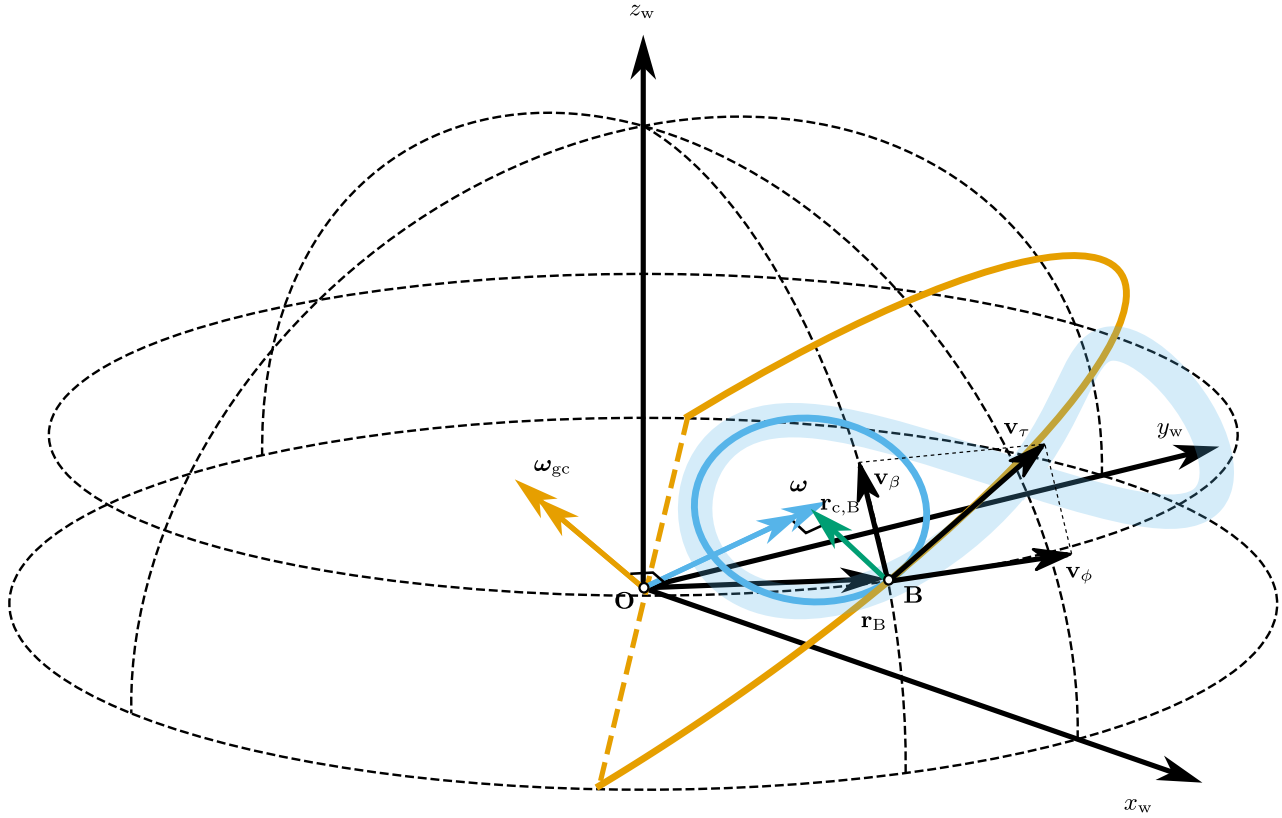


Figure 5. The angular velocity during straight flight, ω_{gc} (orange), and during turns, ω (blue), for a kite linked by a straight and inelastic tether. Adapted from Schelbergen and Schmehl (2024).

However, during turns, the centre of rotation aligns with ω , and at each point along the tether, the centre of rotation will lie in the plane perpendicular to the angular velocity vector (see Fig. 5).

Given the angular velocity ω and acceleration α , the velocity and acceleration at an arbitrary point 2 on the rigid body can be determined relative to a reference point 1 as follows,

$$\mathbf{v}_2 = \mathbf{v}_1 + \omega \times \mathbf{r}_{2-1}, \quad (11)$$

$$\mathbf{a}_2 = \mathbf{a}_1 + \alpha \times \mathbf{r}_{2-1} + \omega \times (\omega \times \mathbf{r}_{2-1}), \quad (12)$$

where \mathbf{r}_{2-1} is the position vector from point 2 to 1. The velocity at the ground tether attachment point is zero by definition of the system, which can also be confirmed as a direct result of these equations when applied to that point. Therefore, the velocities and accelerations along the tether, relative to the ground point, can be written as,

$$\mathbf{v}_j = \omega \times \mathbf{r}_j, \quad (13)$$

$$\mathbf{a}_j = \alpha \times \mathbf{r}_j + \omega \times (\omega \times \mathbf{r}_j). \quad (14)$$



In practice, assuming the kite-tether assembly to be a rigid body can lead to inaccuracies. Firstly, the kite can rotate freely around \mathbf{B}^1 , and secondly, the tether deforms and sags. As a result, the angular velocity vector $\boldsymbol{\omega}$ is no longer aligned with the ideal rotation axis and does not pass through the ground station.

Initial attempts to model the assembly as a single rigid body yielded limited success, leading to the decision to treat the kite and tether as two independent rigid bodies. This approach significantly improved the estimations.

Since the kinematic measurements are obtained at the kite wing, the angular velocity of the kite, $\boldsymbol{\omega}_k$, is calculated using the accelerations and velocities at the wing (Eq. (10)),

$$\boldsymbol{\omega}_k = \frac{\mathbf{a}_{n,k} \times \mathbf{v}_k}{\|\mathbf{v}_k\|^2}, \quad \mathbf{r}_{c,k} = \frac{\mathbf{v}_k \times \boldsymbol{\omega}_k}{\|\boldsymbol{\omega}_k\|^2}, \quad \alpha = \frac{\mathbf{a}_{t,k} \cdot \mathbf{r}_{c,k}}{\|\mathbf{r}_{c,k}\|^2}. \quad (15)$$

Subsequently, the velocities and accelerations are translated to the bridle point \mathbf{B} , representing the KCU, using Eq. (11).

Regarding the tether, since the position, velocity, and accelerations at \mathbf{B} are not measured, it is assumed to perform a great rotation around the ground station, which allows the angular velocity to be calculated using Eq. (13),

$$\boldsymbol{\omega}_t = \frac{\mathbf{r}_k \times \mathbf{v}_k}{\|\mathbf{r}_k\|^2}. \quad (16)$$

This assumption introduces inaccuracies, particularly in the acceleration values. However, since the point masses of the tether are relatively small, this does not significantly impact the overall accuracy of the model, as shown in Williams (2017). Assuming a constant angular velocity ($\alpha \approx 0$), the velocities and accelerations along the tether are calculated as (Eq. (13)) (Williams, 2017),

$$\mathbf{v}_j = \boldsymbol{\omega}_t \times \mathbf{r}_j, \quad (17)$$

$$\mathbf{a}_j = \boldsymbol{\omega}_t \times (\boldsymbol{\omega}_t \times \mathbf{r}_j). \quad (18)$$

The tangential velocity at the bridle point is then given by,

$$\mathbf{v}_\tau = \boldsymbol{\omega}_t \times \mathbf{r}_B. \quad (19)$$

This tangential velocity vector is projected into the horizontal and vertical planes, yielding v_ϕ and v_β , to estimate the rate of change of the tether orientation angles.

The aerodynamic force acting on the tether is estimated based on the cross-flow principle, where the flow components parallel and perpendicular to the body are treated independently (Hoerner, 1965; Bootle, 1971), which was found to have a good relation with test data for sub-critical flows ($Re_{crit} \approx 3.5 \times 10^5$), where the Reynolds number is formed using the tether diameter as the characteristic length. The lift $\mathbf{f}_{L,j}$ and drag $\mathbf{f}_{D,j}$ forces acting on each tether segment can then be estimated as follows (Dunker, 2018),

$$\mathbf{f}_{L,j} = \frac{1}{2} \rho (C_\perp \sin^2 \alpha_j \cos \alpha_j - \pi C_\parallel \cos^2 \alpha_j \sin \alpha_j) l_j d_t v_{a,j}^2 \mathbf{e}_{L,j}, \quad (20)$$

$$\mathbf{f}_{D,j} = \frac{1}{2} \rho (C_\perp \sin^3 \alpha_j + \pi C_\parallel \cos^3 \alpha_j) l_j d_t v_{a,j}^2 \mathbf{e}_{D,j}, \quad (21)$$

¹In this work, we intentionally collocate the bridle point with the KCU for modelling simplicity. However, this was not the case for the V3 kite, as shown in Figs. 1 and 4, where the bridle point is slightly lower than the KCU.



where C_{\perp} is the drag coefficient in the direction perpendicular to the tether, C_{\parallel} is the skin friction drag coefficient (along the tether), α_j is angle of attack of the tether segment (which is 90° when the flow is perpendicular to the tether), l_j is the length of the tether segment, and d_t is the tether diameter. The direction of the drag force aligns with the apparent velocity of the segment, while the lift is directed perpendicular to the drag and lies in the plane defined by the apparent velocity and the tether direction, where $\mathbf{e}_{L,j}$ and $\mathbf{e}_{D,j}$ are unit vectors in the direction of these forces.

Similarly, the aerodynamic forces acting on the KCU are estimated by simplifying its geometry to that of a cylinder and applying the cross-flow principle, using experimentally derived coefficients for cylinders with different aspect ratios in the normal and tangential directions (Blevins, 1984), assuming the KCU is pitched 90° relative to the tether. However, since the KCU operates in a supercritical regime, the cross-flow principle may not provide an accurate approximation. A more suitable model for this regime is beyond the scope of the current project and will be considered in future work. Despite this, the contribution of the KCU drag to the overall system is very small compared to the other forces acting on the KCU and the system, so any inaccuracy here will not have a significant effect. This is further illustrated by the analysis presented in the results section.

The EKF state vector comprises the kite wing position and velocity, aerodynamic coefficients, wind velocity, tether length, and azimuth and elevation of the first tether segment. The tether length is determined by the reel-out speed (v_t), while the orientation of the first tether segment depends on its angular velocity relative to the ground station, which can be approximated with the tangential velocity and radial distance of the tether attachment point. The tether force at the ground $F_{t,g}$ is given as an input. With these considerations, the dynamics of the model can be written as a function of the state vector (\mathbf{x}) and the input vector (\mathbf{u}),

$$\mathbf{x} = (\mathbf{r}_k, \mathbf{v}_k, \mathbf{C}_a, \mathbf{v}_w, l_t, \beta_0, \phi_0), \quad \mathbf{u} = (v_t, F_{t,g}). \quad (22)$$

The full system of ordinary differential equations (ODEs) to be solved is,

$$\mathbf{f}(\mathbf{x}, \mathbf{u}) = \begin{cases} \dot{\mathbf{r}}_k = \mathbf{v}_k & (23a) \\ \dot{\mathbf{v}}_k = \frac{\mathbf{F}_{t,k}(\mathbf{r}_k, \mathbf{v}_k, \mathbf{v}_w, l_t, \beta_0, \phi_0, F_{t,g}) + \mathbf{F}_{a,k}(\mathbf{C}_a, \mathbf{v}_w, \mathbf{v}_k) + \mathbf{F}_{g,k}}{m_k} & (23b) \\ \dot{\mathbf{C}}_a = 0 & (23c) \\ (\mathbf{v}_w = 0) \text{ or } (\dot{u}_* = 0, \quad \dot{\phi}_w = 0, \quad \dot{v}_{w,z} = 0) & (23d) \\ \dot{l} = v_t & (23e) \\ \dot{\beta}_0 = \frac{v_\beta}{\|\mathbf{r}_k\|} & (23f) \\ \dot{\phi}_0 = \frac{v_\phi}{\|\mathbf{r}_k\|}, & (23g) \end{cases}$$

Additionally, it is possible to estimate the offset in the measurements that are directly modelled, such as the tether length and angles, by adding them as a time-invariant parameter ($\dot{\delta} = 0$).

This model forms the basis for the EKF design, capturing the essential dynamics of the kite and tether system. The model can be expanded to fly-gen systems by accounting for an additional thrust force acting on the kite, which can be modelled as



a function of the control inputs and the kite velocity. When added to Eq. (23b), the thrust can be an input or a state variable, depending on the EKF design.

310 4.2 Observation model

The required minimum measurements are the position and velocity of the kite wing. An additional observation is required to ensure that the position of the wing calculated with the tether model, $\mathbf{r}_{k,t}$, matches the estimated position of the kite wing, \mathbf{r}_k . This ensures agreement between the position of the kite (Equation 23a) and the shape of the tether (defined by the tether length and the orientation of the first tether segment). Therefore, the observation model vector is given by,

$$\begin{aligned}
 \mathbf{r}_{k,m} &= \mathbf{r}_k + \eta_{\mathbf{r}_k} & (24a) \\
 \mathbf{v}_{k,m} &= \mathbf{v}_k + \eta_{\mathbf{v}_k} & (24b) \\
 \mathbf{0} &= (\mathbf{r}_k - \mathbf{r}_{k,t}) & (24c) \\
 &\text{—optional—} \\
 \mathbf{h}(\mathbf{x}, \mathbf{u}) &= \begin{cases} v_{a,m} = \|\mathbf{v}_w - \mathbf{v}_k\| + \delta_{v_a} + \eta_{v_a} \\ l_m = l + \delta_l + \eta_l \\ \beta_{0,m} = \theta_0 + \delta_{\beta_0} + \eta_{\beta_0} \\ \phi_{0,m} = \phi_0 + \delta_{\phi_0} + \eta_{\phi_0} \\ \alpha_m = \alpha + \delta_{\alpha} + \eta_{\alpha}, \end{cases} & (24d)
 \end{aligned}$$

where the subscript m refers to the measured quantities, η_i represents the Gaussian-distributed measurement noise and δ_i the measurement offset for each variable i .

320 Additionally, several other measurements can be incorporated into the EKF to enhance its accuracy, such as the tether length, the orientation of the tether measured at the ground, the apparent wind speed, and the angle of attack, each potentially subject to an offset. However, it is important to recognize that poorly calibrated or faulty equipment can introduce significant errors in the estimation process.

4.2.1 Sensor Offset Correction

The EKF is designed to correct sensor biases, such as those in the tether length and angle measurements, by incorporating their offset as a state within the filter. This allows the filter to estimate and subtract the offset from sensor readings.

325 However, if the measurement is not directly modelled as a state variable, the filter may fail to estimate its offset accurately, requiring alternative methods. This problem is particularly relevant for airflow sensors like Pitot tubes and wind vanes. In such cases, a correction procedure is advised by initializing the filter without using the biased sensors. The estimated states are then used to calibrate the sensors after the filter has converged, provided the filter has been correctly pre-tuned to the system at hand.



Some measurements, such as the Euler angles from the IMU, are not directly modelled in the filter, and their offsets are corrected using the orientation of the bridle segment, which closely follows the measured orientation of the wing. However, if the IMU is positioned at the wing, the sensor will also measure the deformations due to the actuation. Larger deformations around the central strut of the wing are observed during reel-in and can be estimated based on the linear relationship between the variation in pitch and the de-power setting u_p , which is directly linked to the length of the de-power tape. By comparing EKF-estimated pitch with the measured pitch θ_m , it is possible to infer the pitch sensor offset δ_θ and the de-power angle of attack α_d . This comparison allows the kinematic pitch of the kite θ_k to be isolated from the sensor readings:

$$\theta_k = \theta_m - \delta_\theta - \alpha_d \quad (25)$$

The yaw angle, however, can only be estimated directly by incorporating the yaw rate into the filter model. Nevertheless, the conical shape of the kite naturally aligns it with the apparent wind, enabling an offset correction based on this tendency. The good agreement between estimations and measurements, along with the offsets for the Euler angles mentioned earlier, is presented in Sect. 5.

4.3 Extended Kalman Filter

In this section, the process followed by the iterated EKF to correct the measured states and predict the unknowns is described. This is illustrated in the flowchart in Fig. 6, where the hatted symbols denote the predicted states, and the superscript * represents the nominal state around which the EKF is linearised. The algorithm follows the standard setup of an iterated EKF (Gibbs, 2011) with a slight modification. After the one-step-ahead prediction, where the dynamic model is propagated to the next timestep, the Jacobians of the observation and dynamic model vectors are calculated. In this step, the tether force at the kite, obtained with the tether model, is differentiated only with respect to the tether length and the first tether segment orientation, whilst the rest of the states it depends on are taken from the last predicted state, given as input in the Jacobian calculation. There are several reasons for this choice; first, the tether model (Williams, 2017), in its original formulation, solves an optimisation problem for these three variables, while all the other variables are assumed to be known. Second, and more importantly, the introduction of the wind and kite velocity within the tether model introduces so much non-linearity that the performance of the Kalman filter is degraded. Therefore, the exact dependency of on these states in the tether model is not accounted for when propagating the covariance matrices.

As shown in the remaining steps of the flowchart in Fig. 6, the iterated EKF follows a standard procedure to update its gain and state, as well as the covariance matrix of the state estimation error.

4.3.1 Tuning

One of the most crucial and complex aspects of a well-performing Kalman filter is tuning, which can be done by means of the state and measurement noise covariance matrices Q and R . For simplicity, these are defined as diagonal matrices, with the diagonal elements representing the expected variance of the state and measurement noise, assuming a Gaussian-distributed noise with zero mean. These matrices were found to be system-dependent, meaning their optimal values can vary between

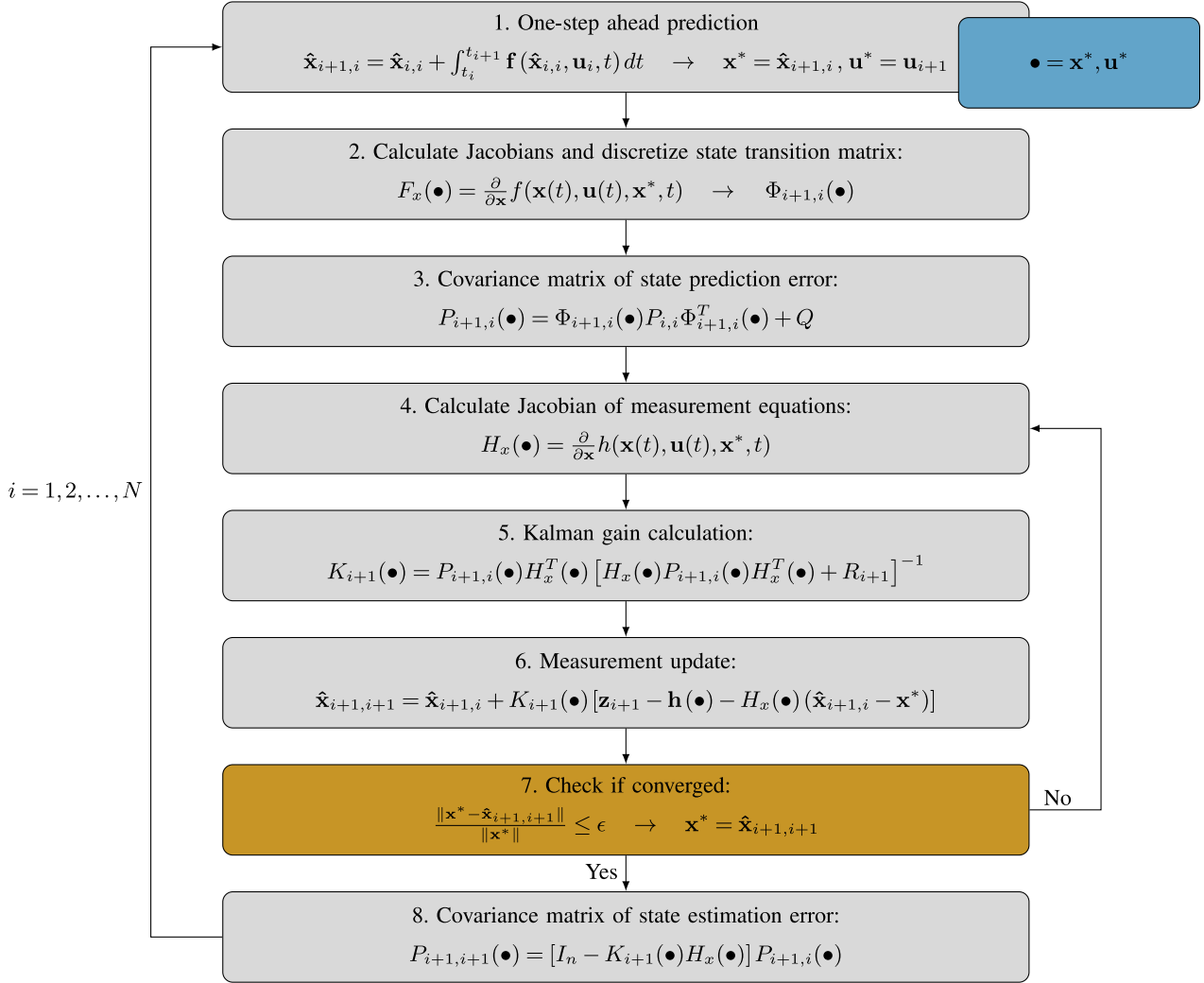


Figure 6. Iterated extended Kalman filter process flowchart.

different systems or kites. However, for the same kite, once calibrated, these coefficients maintain good performance even under varying environmental conditions.

The tuning of the EKF was performed manually, requiring an initial understanding of the magnitude and time dependence of the modelled parameters and a good knowledge of the accuracy of each sensor. There are, however, a few aspects that can be checked to ensure proper calibration. The first is to ensure that the wind speed and direction estimates do not show any pattern-related variations, such as periodic changes due to the figure-of-eight pattern flown by the kite. Moreover, the filter estimates for position and velocity should closely align with the measurements. Finally, the aerodynamic coefficients should remain within the expected values of the flying wing. For a better understanding of the accuracy of the EKF estimates, analysing the time history of the filter performance parameters can be helpful. The normalized innovation squared (NIS) metric is commonly used

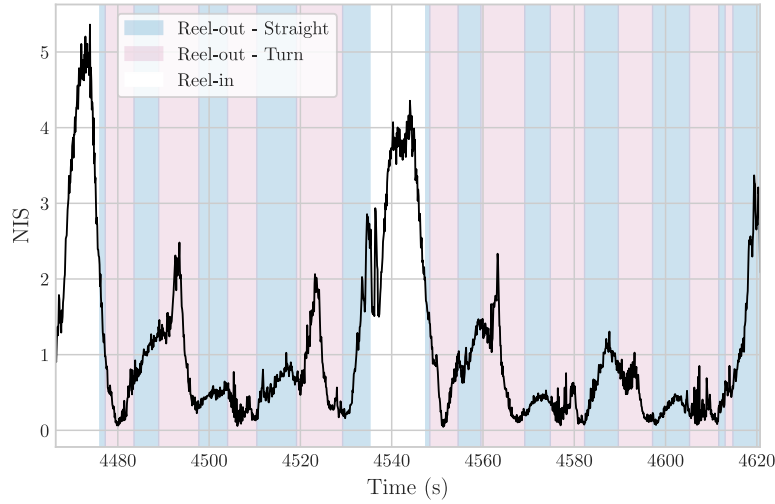


Figure 7. NIS metric for two power generation cycles.

for filter tuning in the absence of ground truth measurements (Bar-Shalom et al., 2002). It quantifies the consistency between the predicted measurements and the actual measurements, relative to the expected uncertainty.

$$\text{NIS} = \nu_i^T \mathbf{S}_i^{-1} \nu_i, \quad (26)$$

where ν_i is the measurement residual and \mathbf{S}_i the associated innovation covariance matrix.

As shown in Fig. 7, the performance decreases during turns and reel-in, which may indicate either that the measurements degrade during these phases or that the dynamic model cannot capture the relevant dynamics in these sections of the flight.

Since position and velocity in the analysed datasets come from GPS+IMU-fused measurements, we believe the former to be the case, particularly during reel-in, as further discussed in the results section. For an optimally tuned filter, this metric should follow a chi-squared distribution; however, achieving this level of tuning is outside the scope of this work. For the leading-edge inflatable V3 kite, the standard deviations of the process and measurement noise terms detailed in Appendix A result in reasonable estimates.

5 Results

The datasets used in this study were acquired during three test flights conducted by Kitepower in the frame of two test campaigns. The first campaign took place in 2019 at the former naval air base Valkenburg, the Netherlands, using the 25 m² V3.25B kite developed by Kitepower on the basis of the TU Delft V3 kite (Poland and Schmehl, 2024). The selected dataset was published in Schelbergen et al. (2024) and analysed in Roullier (2020); Schelbergen and Schmehl (2024). It includes data from two sensor boxes with GPS+IMU mounted on the two central struts of the wing, an airflow sensor comprising a Pitot tube and a single wind vane measuring the angle of attack, a load cell on the ground, and tether length and reeling speed sensors.



Table 2. Overview of EKF models with corresponding sensor setups and wind model types.

Model	Additional Measurements	Wind Model
EKF 0	-	Constant
EKF 1	Tether length	Constant
EKF 2	-	Logarithmic
EKF 3	Apparent wind speed	Constant
EKF 4	Zero vertical wind speed	Constant
EKF 5	Tether length and angles	Constant

The second campaign took place 2023 to 2024 in Bangor Erris, Ireland, using the 60 m² V9 kite developed by Kitepower. This site in Northern Ireland is known for its consistently strong winds, predominantly from the south-west. The two selected flights of that campaign (Cayon et al., 2024a, b) include additional sensors used to study different measurement configurations. Measurement data was complemented with profiling lidar readings recorded using a Windcube v2 (Vaisala), which is used to validate the wind estimations of the EKF.

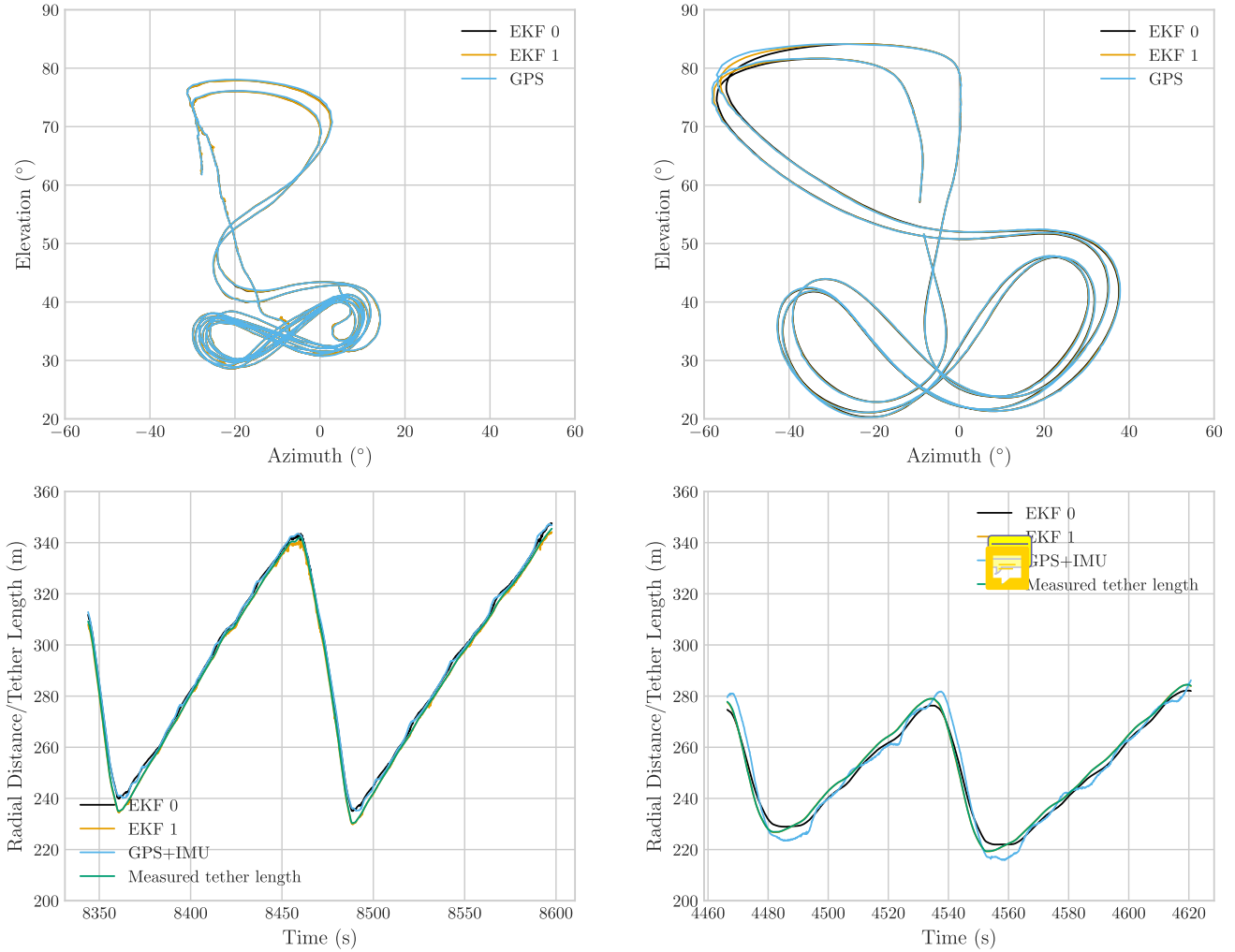
In this section, we explore various sensor setups and model configurations. The different EKF models are detailed in Table 2. The additional measurements listed in the table are used alongside the minimum required sensors for a system with a KCU, which include the position, velocity, acceleration of the kite wing, tether force, and reel-out speed.

The position and velocity data used in this study come from a GPS+IMU fused dataset processed with the embedded EKF of a Pixhawk sensor using PX4 autopilot. However, the fusion of GPS and IMU data can introduce inaccuracies, especially if the sensor fusion technique is not tailored to tethered flight.

5.1 Kite Kinematics

One of the primary functions of the EKF is to enhance the accuracy of existing measurements, such as the kite position and velocity. By integrating additional information, the EKF refines data from standalone kinematic sensors like GPS. In Fig. 8, portions of two flights from the two campaigns are depicted in terms of azimuth, elevation, and radial distance.

Overall, there is good agreement between the EKF estimations and the measurements throughout the flights. However, the highest discrepancies occur during the reel-in phase, when the kite is depowered, and to a lesser extent during turns. A significant factor contributing to these discrepancies is that the proprietary EKF of the Pixhawk relies on a model tailored to drones, which does not account for the constrained tethered flight dynamics of kites. This limitation likely contributes to inconsistencies in sensor readings, such as the mismatch between radial distance and tether length during reel-in, where the radial distance shows unphysical values several meters longer than the actual tether length. On the other hand, when the tether length is incorporated as an additional measurement, our EKF estimation aligns well with the tether length, correcting the position measurements to be consistent with the physical constraints of the system.

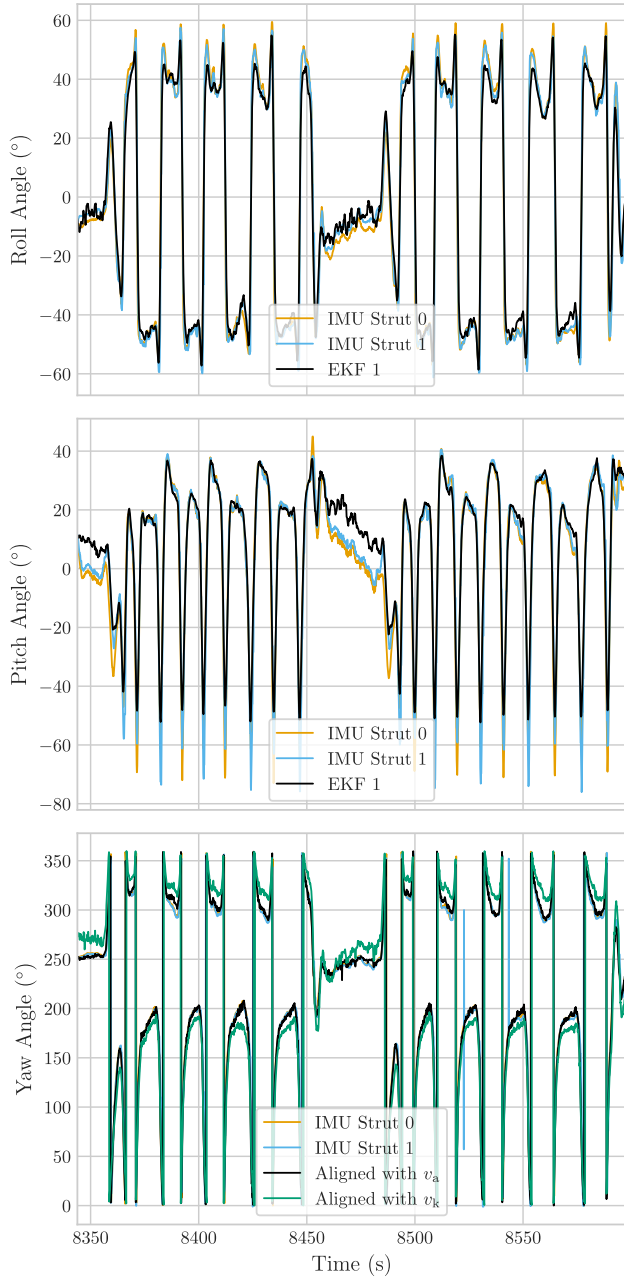


(a) V3 kite, flight 08-10-2019

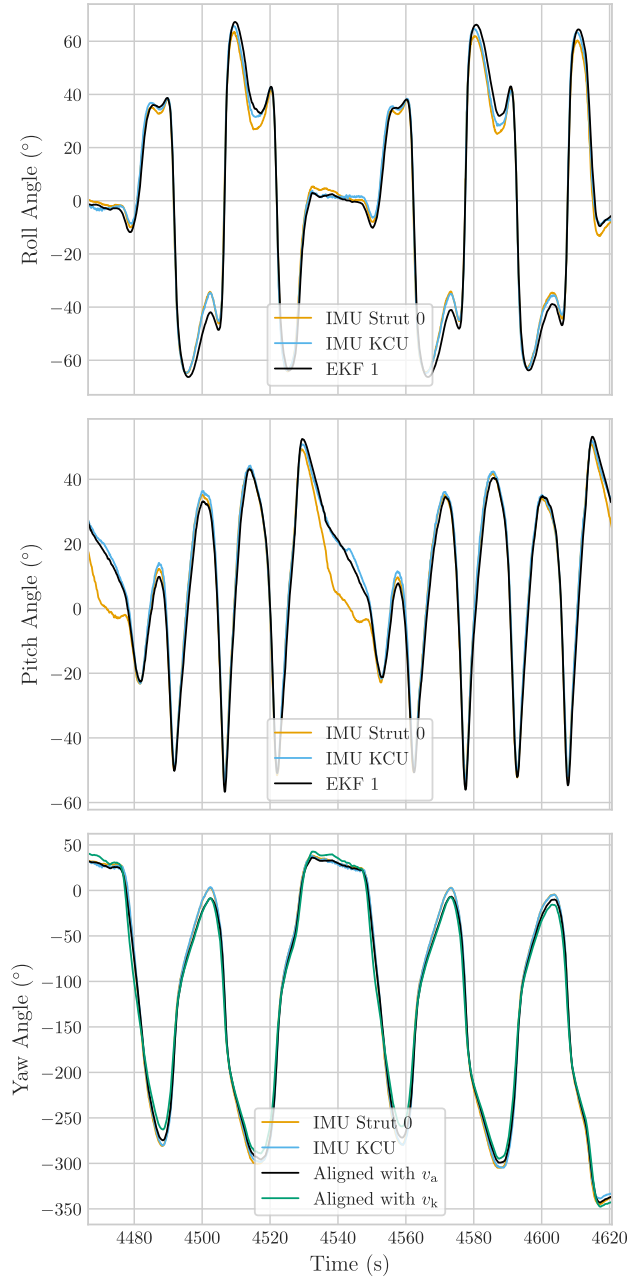
(b) V9 kite, flight 27-11-2023

Figure 8. Comparison of estimated and measured kite trajectory, in terms of the azimuth and elevation angles and radial distance.

In Fig. 9, the Euler angles measured at the two central struts of the wing are compared with the orientation of the bridle segment, defined by a pitch and a roll. The third orientation angle, the yaw, is not modelled by the EKF and has been computed by aligning the kite reference frame either with the apparent wind or the kinematic velocity directions. As summarised in Table 3, the results show a strong agreement between the tether model and the orientation measurements from the IMU. This level of consistency suggests that, for soft kites, a quasi-static two-point mass model—representing both the wing and the suspended KCU—can accurately capture the orientation of the kite.



(a) V3 kite, flight 08-10-2019



(b) V9 kite, flight 27-11-2023

Figure 9. Comparison of estimated and measured Euler angles, with measurement biases removed using EKF estimations.



Furthermore, although yaw is not directly modelled, there is a notable alignment between the estimated and measured angles when the kite is aligned with the apparent wind direction. Conversely, the yaw estimation error increases when aligned with the kite kinematic velocity. This behaviour indicates that the kite's anhedral shape promotes alignment with the local inflow rather than the kinematic velocity of the kite.

By modelling the tether shape, which includes the KCU, the kite deformation at the IMU can be estimated by comparing the predicted orientation of the bridle segment from the EKF with the measured orientations at the wing. This approach allows for an approximate assessment of wing deformation during flight and helps isolate the rigid body orientation.

Additionally, the model captures deformation effects that occur during changes in the depower setting and turning manoeuvres. For instance, the depower-induced deformation is evident in Fig. 9, where a pitch change of approximately 9° is observed for the V3 kite during reel-in. This information can be utilised to translate the measured angle of attack at the bridle to the wing angle of attack (see Eq. 1).

Regarding turning deformation, this effect is most pronounced in the V3 kite (see Fig. 9a), which corresponds to a kite whose structure exhibited greater overall deformation. Such deformation may be undesirable if the goal is to maintain aerodynamic performance. However, this clear identification of turning deformation, which is more pronounced in one strut than the other depending on the turning direction, provides valuable insight into the aero-structural deformations of the wing (Schelbergen and Schmehl, 2024).

Table 3. Root mean squared errors (RMSE) of pitch, roll, and yaw for two kite models

Orientation RMSE	V3 (2019-10-08)	V9 (2023-11-27)
Pitch	3.63 deg	3.07 deg
Roll	3.84 deg	2.91 deg
Yaw (aligned with v_a)	4.15 deg	4.65 deg
Yaw (aligned with v_k)	13.43 deg	11.73 deg

5.2 System dynamics

Modelling the various components of the kite and tether system allows for the isolation of individual force components, enabling an assessment of their relative significance. Fig. 10 illustrates the different forces acting on the V3 kite system.

As expected, the lift force generated by the wing is the dominant contribution, primarily responsible for pulling the tether. It is followed by the wing drag force, which exhibits considerable variability, peaking during turns and decreasing during the reel-in phases. The parasitic drag of the tether and KCU can be seen to account for a relatively small portion of the total drag. The side force, though relatively low, plays a crucial role in balancing the forces during turns by providing the necessary lateral force to counteract the centripetal acceleration of the wing. The primary force component of the KCU is its inertia, which can be interpreted as an external force on the tether. In this particular system configuration, where the KCU was oversized relative



to the wing, its inertia could reach up to 40% of the tether force during turns, exerting a greater influence than its weight due to the high accelerations during turns.

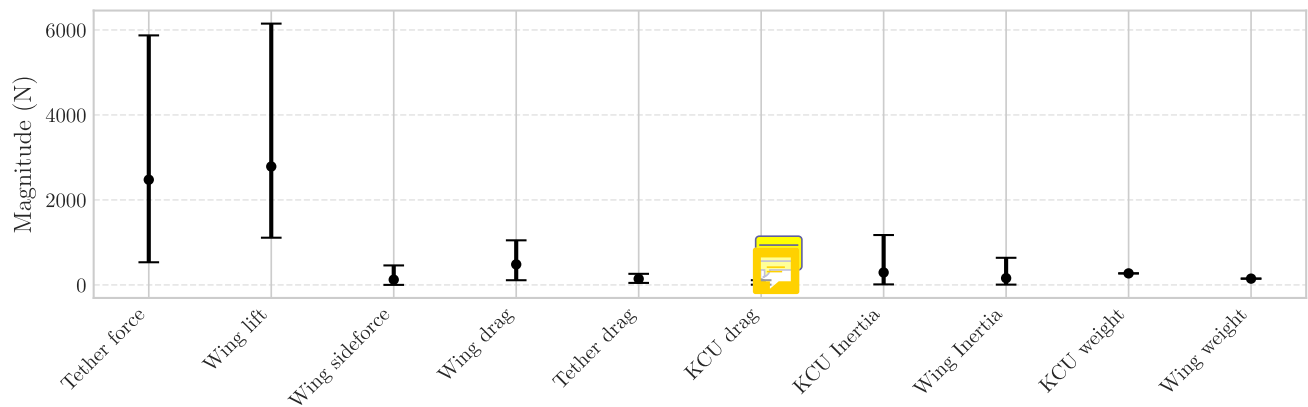


Figure 10. Mean, maximum, and minimum values of the different force contributions acting in the airborne subsystem during the flight on 2019-10-08 using the V3 kite.

Another novelty is that the current EKF can effectively estimate tether sag, understood as the difference between the radial distance and the tether length. Fig. 11 presents the sag and ground tether force for two power generation cycles, revealing a clear relationship between the two. As expected, the tether experiences the most sag during the reel-in phases, when the kite is lowered, and the tether forces are lowest.

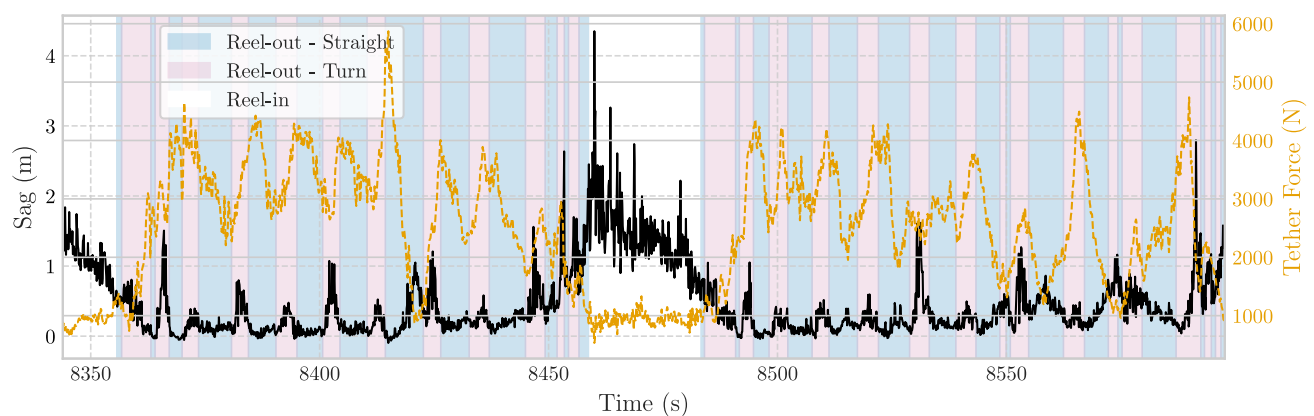


Figure 11. Variation of sag and tether force during two power generation cycles from the flight on 2019-10-08 using the V3 kite. The plot shows the sag in meters (left y-axis) and the tether force in Newtons (right y-axis).



Additionally, a consistent peak in sag is observed during turns, partly due to the reduced speed at the top of the figure-eight pattern (i.e., lower tether force). This effect is further amplified by the inertia of the KCU, which causes the kite to rotate relative to the tether. This misalignment between the aerodynamic forces and the tether force might lead the kite to dive into the sphere, causing the tether to sag.

Aerodynamic identification

To accurately estimate the aerodynamic performance of the kite, it is crucial to precisely estimate both the orientation of the tether and the wind speed and direction. The latter is particularly critical for determining the direction of the drag force and obtaining accurate estimates of the drag coefficient. Linking the instantaneous aerodynamic coefficients to the angle of attack at the wing α_w adds another layer of complexity, as this angle is currently measured at the bridle. This section aims to improve the accuracy of these estimates by integrating deformation estimates from the EKF to calculate the angle of attack at the wing, thereby enhancing the prediction of the wing aerodynamic coefficients as a functions of the angle of attack.

Alternatively, the angle of attack can be calculated using the orientation of the wing measured by the IMU and the estimated apparent wind velocity. However, the accuracy of this method is limited by the time resolution quality of the wind velocity estimates, making the measured angle of attack better at capturing temporal variations. Nevertheless, this angle is used to find α_a , which is subtracted from the measured angle at the bridle (see Eq. (1)),

Fig. 8a, the measured trajectory of two power generation cycles is presented alongside the EKF estimates, with the azimuth angle centered on the mean wind direction. During this flight segment, the trajectory was slightly misaligned with the wind direction by approximately 10° , according to the EKF predictions.

In Fig. 12, the aerodynamic coefficients and angles of attack are plotted for the selected flight segment. The lift and drag coefficients remain relatively constant throughout the reel-out phase, with spikes during turns corresponding to decreased lift increased drag. Additionally, the side of the figure-eight pattern that is more misaligned with the wind direction shows a higher increase in drag coefficient and a smaller decrease in lift, while on the other side, the drag peaks are smaller, and the decrease in lift is higher. The increase in drag coefficient on the misaligned side of the figure of eight pattern could be attributed to a higher sideslip angle, although relating this directly to the lift coefficient is less straightforward. The observed changes in lift might be linked to variations in the kite's trim angle, which could be influenced by shifts in aerodynamic polars with sideslip, although this relationship warrants further investigation.

The parasitic drag of the tether and KCU contributes a significant portion of the total drag, approximately 30% during reel-out and up to 50% during reel-in. As for the angles of attack, the measured angle at the bridle lines remains fairly constant throughout the flight, suggesting that the kite maintains pitch stability around a certain trim angle (Thedens and Schmehl, 2023; Cayon et al., 2023). The angle measured at the bridle lines can be translated to the wing angle of attack using the power-induced deformations identified in Fig. 9a.

The wing polars using this estimated angle are presented in Fig. 13 as mean values, with shaded areas indicating the 99% confidence interval. As inferred from the angle of attack and aerodynamic coefficient estimates shown in Fig. 12, the kite bits relatively constant behaviour for a fixed depower setting, which limits the range of angles of attack explored during

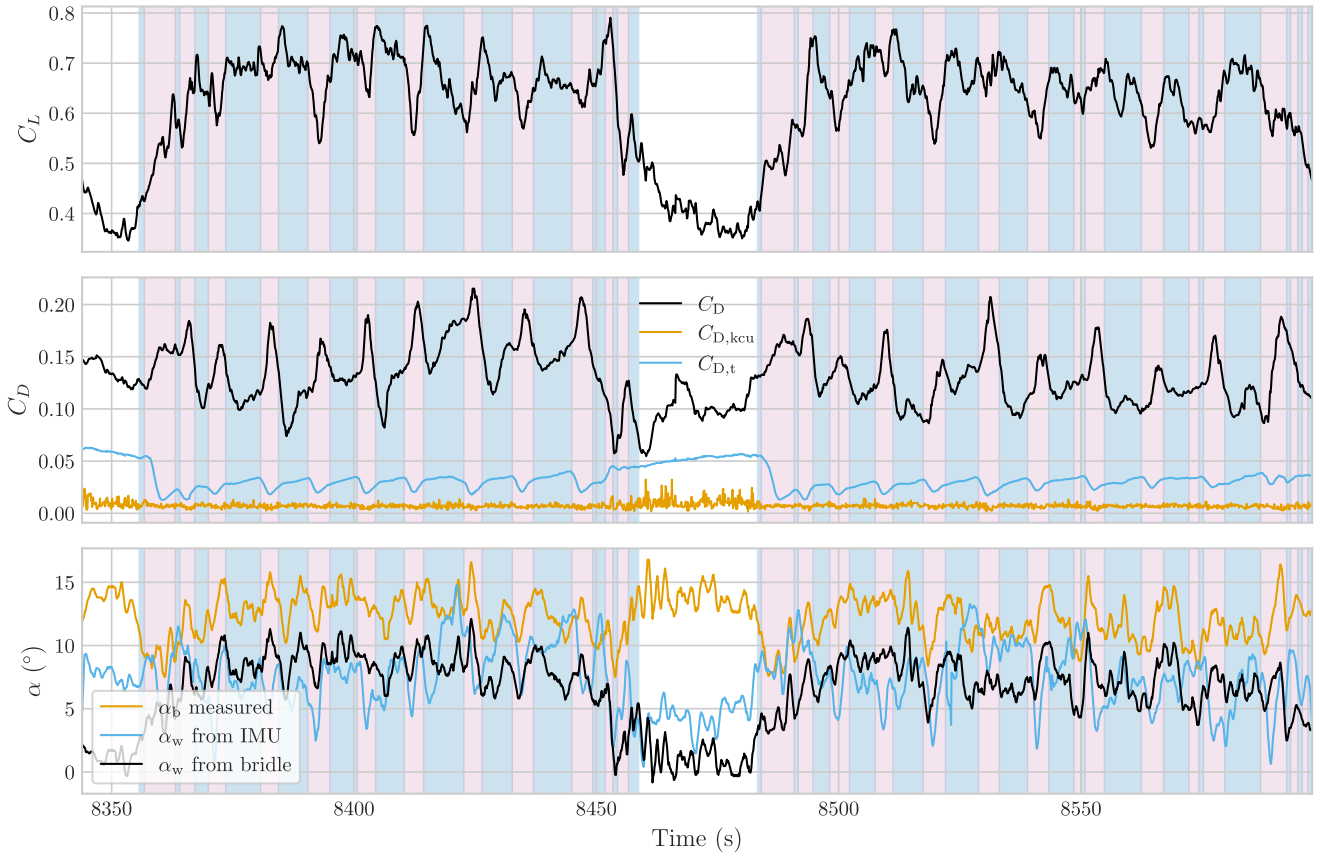


Figure 12. Aerodynamic coefficients and angle of attack of the V3 kite during two power generation cycles. The background colours indicate the flight phase of the kite, legend can be found in Fig. 11.

this flight. Despite this constraint, portions of the polar curves can still be estimated. However, for a complete aerodynamic characterisation of the kite, tailored test flights should be conducted, where the kite is forced to dynamically change the angle of attack to explore the wider range of conditions. The experimentally derived polars are compared with findings from previous studies employing different levels of fidelity. The Reynolds-Averaged Navier-Stokes (RANS) simulations by Viré et al. (2022) were conducted using the CAD model of the V3 kite, whereas the results from the Vortex Step Method (VSM) incorporate an aero-structural solver that accounts for kite deformation caused by actuation inputs (Cayon et al., 2023; Poland and Schmehl, 2023). Additionally, the estimations are compared with an experimental study of the same dataset that used a simpler tether model (Roullier, 2020). In this study, the wind speed at the kite was extrapolated from ground measurements using a logarithmic wind profile, and the angle of attack was estimated based on geometric relations rather than experimentally identified deformations.

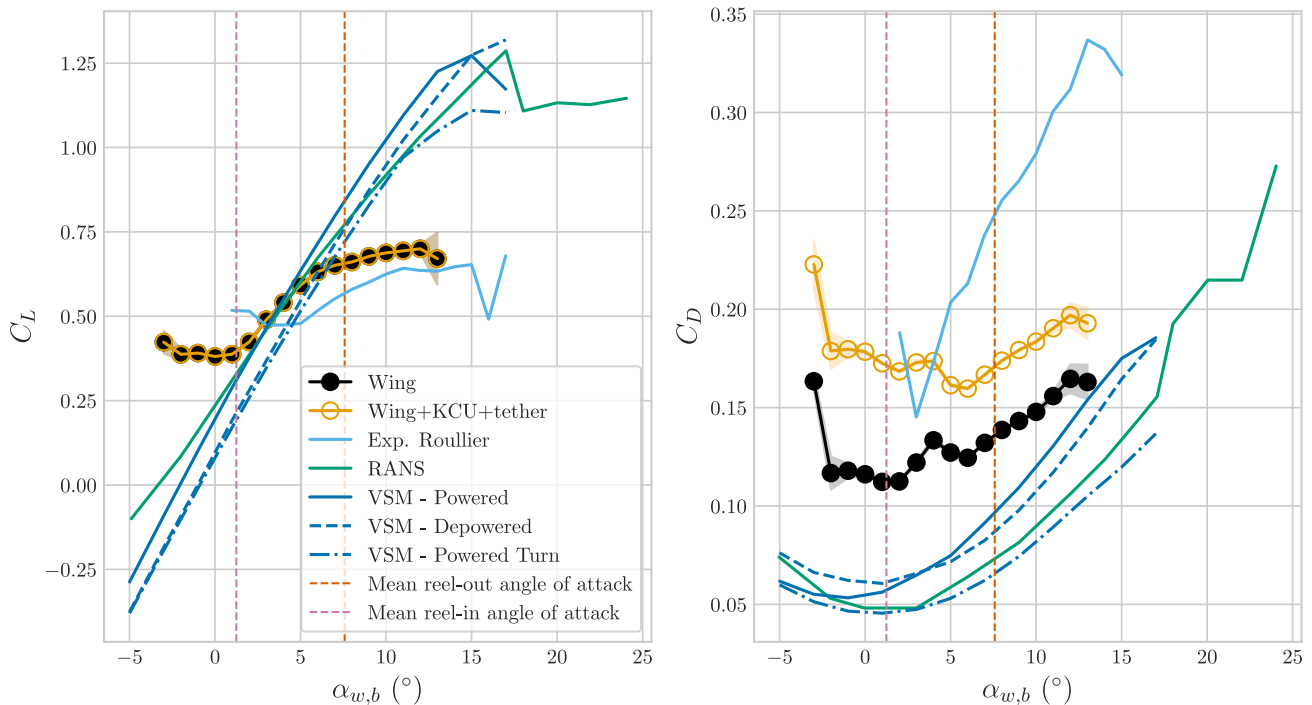


Figure 13. Aerodynamic polars of the V3 kite on the flight of 08-10-2019.

Compared to the RANS simulations of the constant design wing shape, a similar lift slope is observed between the mean angles of attack in powered and depowered states, consistent with the VSM results. However, the behaviour around the mean angle of attack is flatter than in the **previous simulations**. This flattening can be attributed to two main factors. First, the angle of attack measurements have an accuracy of approximately 2° and are subject to vibrations, introducing noise that smooths the curve around the trim angle of the kite during reel-out. Second, the aerodynamic performance of the kite is significantly influenced by steering-induced deformations, which may alter the polars.

When comparing these results to the experimental analysis by Roullier (2020), the derived polars exhibit **a closer resemblance to the simulations**, largely due to **improvements in both angle of attack and wind vector estimations**. Additionally, by **modelling the drag of various parasitic elements in greater detail, a curve with lower drag coefficients and higher lift coefficients is identified**.

Turn dynamics

To steer the kite, a lateral force is generated by asymmetrically deforming the wing, controlled by the steering input u_s via actuation of the steering tape. This deformation creates a lift difference between the two sides of the wing, producing a net



505 lateral force that steers the kite and a moment that induces yaw. Therefore, we can broadly characterise the turning behaviour by the side-force coefficient C_S and the yaw rate $\dot{\psi}$.

For soft kites, where turns are predominantly induced by aerodynamic forces at the wing tips, the yaw rate can be described by a simple relationship dependent on steering input u_s and the apparent wind speed v_a (Fagiano and Novara, 2014; Erhard and Strauch, 2012). This relationship suggests equilibrium of the aerodynamic moment during turns and is expressed as:

510
$$\dot{\psi} = g_k v_a (u_s(t - d(t)) - u_{s,0}), \quad (27)$$

where g_k is the steering gain parameter, $u_{s,0}$ is an offset observed in the side-force coefficient estimates (Fechner, 2016), and $d(t)$ is the time delay between the steering input and the kite response (Elfert et al., 2024).

A time delay of approximately 0.1 seconds is observed when cross-correlating the yaw rate with the steering input, while the delay for the side-force coefficient is around 0.8 seconds relative to u_s . Understanding these delays is crucial for improving the
515 kite responsiveness and steering precision. Further investigation is needed to determine whether these delays originate from the filter dynamics or the physical response of the kite.

In Fig. 14, the kite turn dynamics are depicted in terms of yaw rate and side force coefficient. The identified yaw rate closely matches the measured values, particularly when the offset in the steering input is accounted for. The largest discrepancies occur during straight flight sections and reel-in phases, where the kite is minimally steered. Nevertheless, as shown in Fig. 15, the
520 yaw rate of the kite is well represented across all flight conditions by a simple turn rate law.

For the side-force coefficient, a linear relationship is fitted between the steering input and side force, providing accurate estimates during turns. However, during straight paths, a notable mismatch arises, where the side force appears to be consistently underpredicted, indicating that the same linear fit might not be suitable for all flight regimes.

This is further illustrated in Fig. 16, which shows the side force as a function of u_s . The data highlight distinct behaviours
525 during turns and straight flight, with changes in side force due to the steering being more pronounced during straight flight. This phenomenon can be attributed to aerodynamic damping caused by the wing's yaw motion, which results in the outer side of the kite moving at a higher velocity relative to the inner side. Consequently, the force generated by the turn opposes the manoeuvre, altering the rate of change of C_S with respect to u_s .

Beyond the direct effects of steering input on turn dynamics, it is also essential to consider how other components, such as
530 the KCU, influence the overall system behaviour. By modelling the kite and KCU separately, it is possible to assess the effects of KCU inertia on the manoeuvres and performance of the kite system. In Fig. 17, the estimated angles between the tether and kite, defined by the orientation of the bridle segment, are shown for two power generation cycles. It is important to note that in the flight shown, the KCU was significantly oversized compared to the kite, with its weight reaching twice that of the wing itself. As a result, the behavior observed is exaggerated compared to what would be expected in an optimised system.
535 Nevertheless, this exaggerated scenario provides clearer insights into the effects of the KCU on the system.

During reel-out, the pitch angle remains relatively low, while the roll angle oscillates between positive and negative values, depending on the direction of the kite. During turns, where the accelerations are highest, a peak is observed in both the roll and pitch angles caused by the centrifugal force acting on the KCU. On the straight path segments of the figure eight manoeuvres,

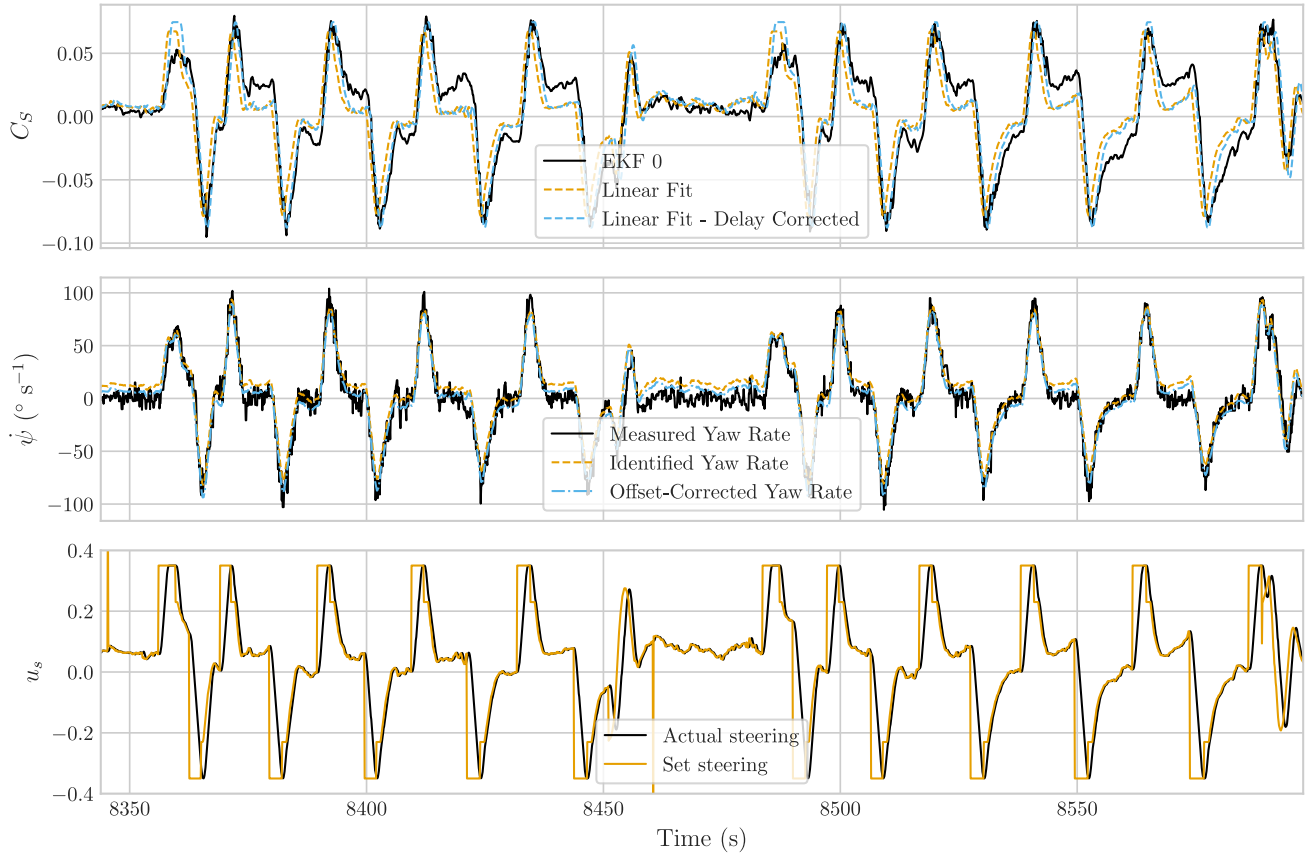


Figure 14. Side force coefficient, yaw rate, and steering input for two power generation cycles.

the roll angle has a lower value, primarily compensating for the weight of the KCU. However, when the kite is reeled in, due to the orientation change toward the ground station, the weight of the KCU is compensated mainly by the pitch angle.

This misalignment of the kite with respect to the tether means that a portion of the aerodynamic force generated by the kite is not transmitted as tether tension but is instead used to compensate for the inertial forces at the KCU. In this exaggerated scenario, these losses can reach up to 6% during turns, highlighting the significant impact of the KCU mass on the system performance Roullier (2020).

5.3 Wind Estimations

In this section, we present results from two selected flights of the more recent flight campaign in Ireland. The 2023-flight exhibits a typical logarithmic wind profile, while the 2024-flight displays a transient phenomenon characterised by a sudden wind gust and a rapid change in wind direction. Estimates relying on a logarithmic law were obtained assuming a surface

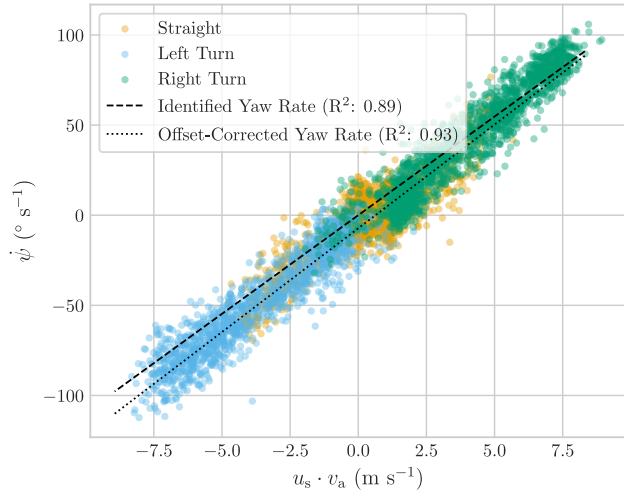


Figure 15. Measured yaw rate and identified turn rates with and without offset correction.

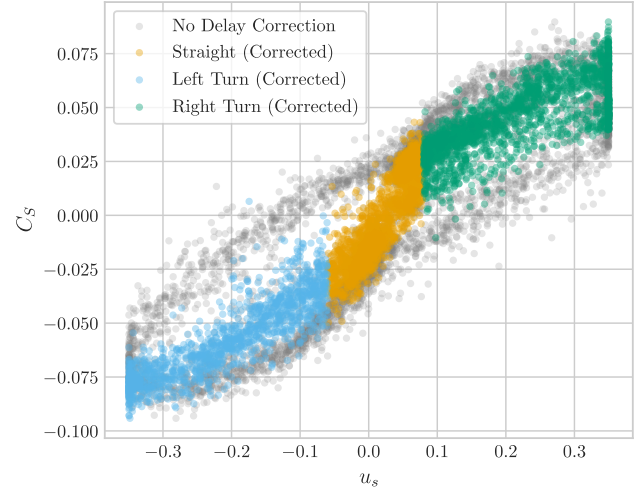


Figure 16. Sideforce coefficient as estimated by the EKF with and without correcting the time delay.

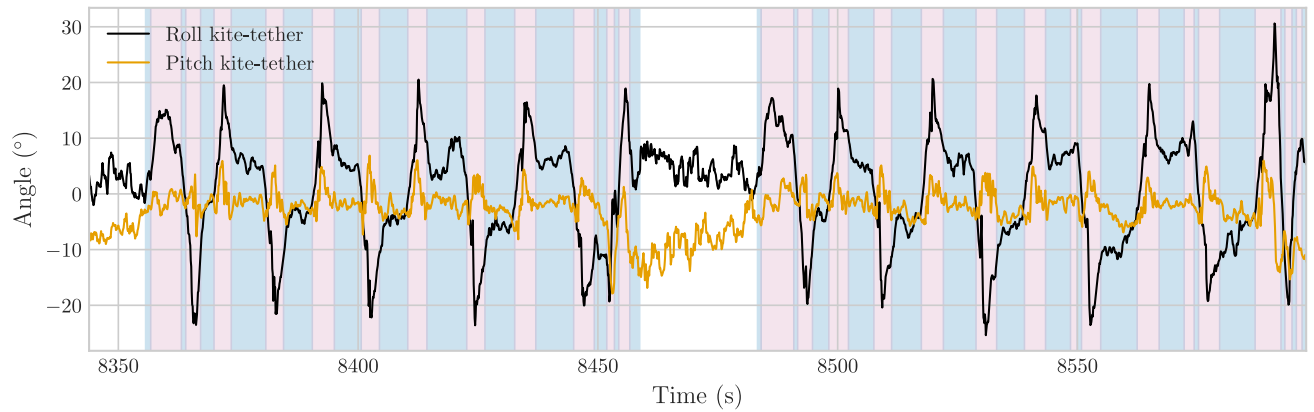


Figure 17. Estimated angle between tether and kite for the V3 kite during two power generation cycles. The background colors indicate the flight phase of the kite, legend can be found in Fig. 11.

roughness length z_0 of 0.1 m. Below, we introduce these two flights and provide a detailed commentary on the wind speed and direction estimates.

For the 2023-flight, Fig. 18 shows a comparison between the wind speed and direction profiles and the results of several EKF model configurations with different sensor measurements as inputs. Ground wind measurements from a cup anemometer and wind vanes were also available for that flight, with the wind speed extrapolated to the kite height using a logarithmic wind profile (see Equation 6). Likewise, lidar data collected at different fixed heights was interpolated to the kite altitude, with



555 shaded areas indicating the range between minimum and maximum values. The lidar data consist of one-minute averages, with the minimum and maximum values showing variability within each averaging period.

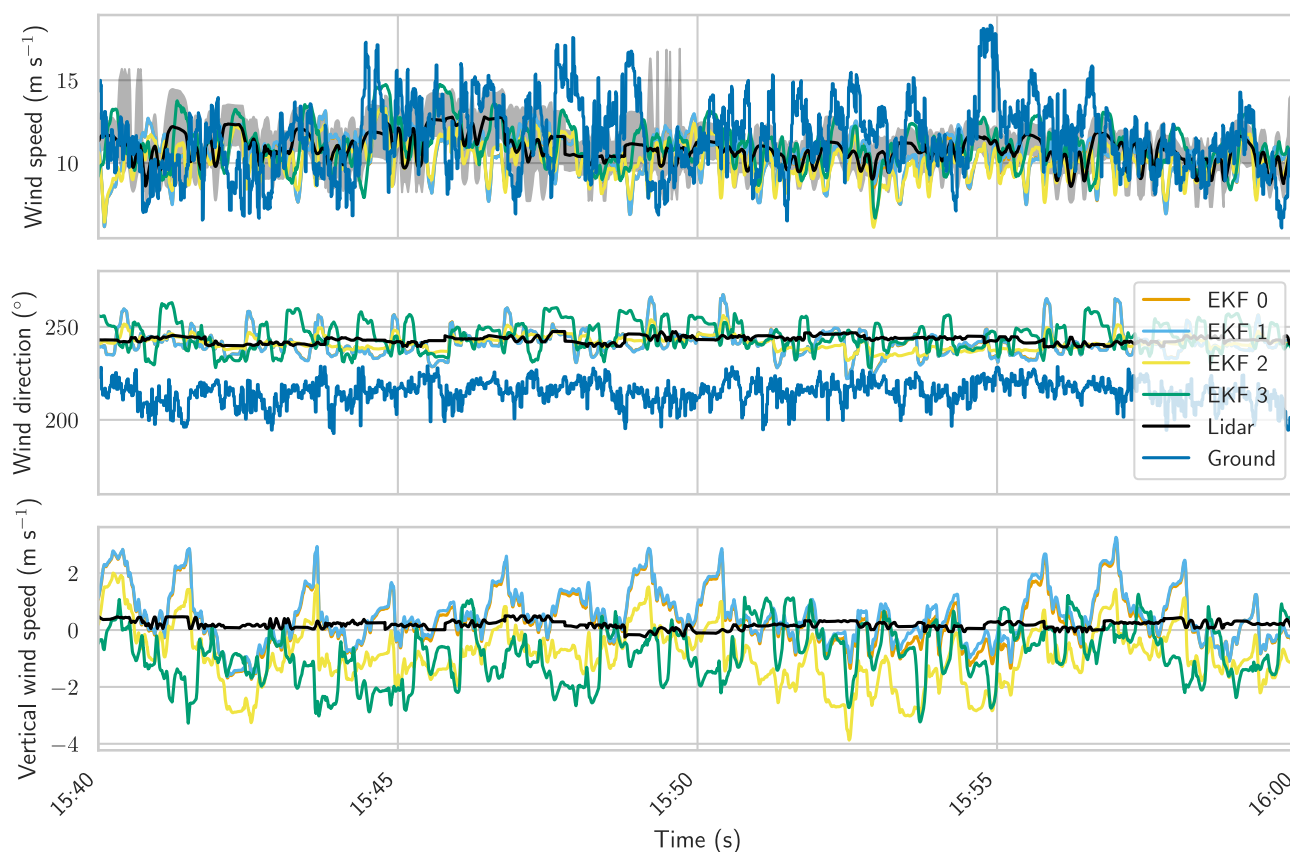


Figure 18. Test flight from 27-11-2023. Time series comparison of different EKF model results and lidar observations and ground measurements.

The results show strong agreement across all configurations for both wind speed and direction. For this flight, incorporating the sensor length as a measurement (EKF 1) does not lead to significant changes in the wind estimates. By modelling wind speed as logarithmically dependent on height (EKF 2), it is possible to tune wind speed and direction separately, allowing for independent control over their fluctuations. This approach reduces variability in wind direction while maintaining a clear dependence of wind speed on height.

The highest fluctuations in wind direction are observed when the apparent wind speed is included as a measurement (EKF 3). However, it is challenging to determine whether these fluctuations are physical or the result of errors in the Pitot tube readings, especially when compared against the lidar's 1-minute average data. A poorly calibrated tube or its position away from the



centre of rotation of the kite might cause these fluctuations. For this flight, the Pitot tube readings were corrected using the methodology described in Sect. 4.2, resulting in an estimated bias of approximately 2 ms^{-1} .

Regarding vertical wind speed, lidar measurements indicate an average speed close to zero, which aligns with the EKF estimates. Among the configurations, EKF 3 shows a slightly lower average vertical wind speed.

Finally, a comparison with ground-level wind measurements reveals a substantial wind veer, which the EKF effectively captures. Although the extrapolation of wind speed to the kite height provides velocities of a similar magnitude, these ground measurements cannot accurately capture wind speed variations at altitude.

Fig. 19 presents the 10-minute averaged wind speed and direction profiles for the same flight. The results show that incorporating the apparent wind speed yields the most accurate estimates of the wind speed profile. At the same time, all models provide similarly accurate estimates of wind direction, closely following the lidar measurements. The largest deviations from the lidar data occur at altitudes above 200 m, corresponding to the reel-in phase. These discrepancies may be due to the degradation in the quality of position and velocity measurements, as discussed earlier.

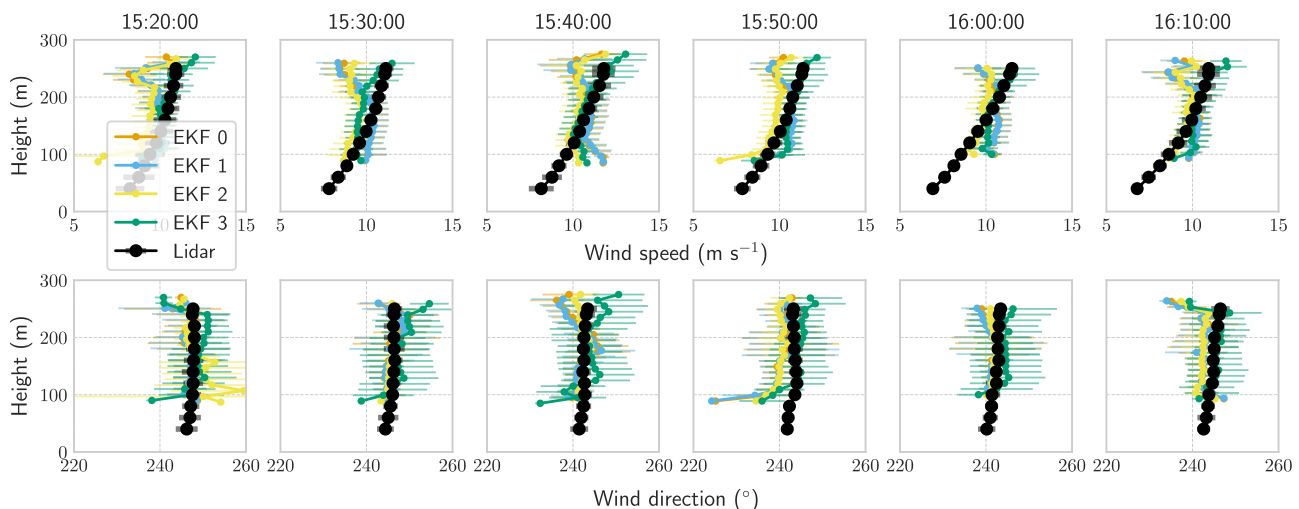


Figure 19. Test flight from 27-11-2023. Wind profile comparison between EKF model wind speed and direction estimates with a minimum sensor input setup, three variants with additional inputs, and lidar observations.

In contrast to the typical wind profile of the 2023-flight, the 2024-flight, shown in Fig. 20, featured a wind gust starting around 13:40, accompanied by a shift in wind direction that remained fairly constant until the gust subsided. During this flight, lidar data was available at a higher resolution of 1 second, with measurements presented at three different heights. Additionally, measurements of the tether angles at the winch outlet were included in the model EKF 5. It is important to note that the IMU readings from the Pixhawk during this flight struggled to keep up with the high accelerations experienced during turns, resulting in clamped acceleration values and deteriorated measurements of the kite kinematics. This issue affected the performance of the EKF and led to non-physical peaks in the wind velocity estimates. Although adding additional measurements helped mitigate

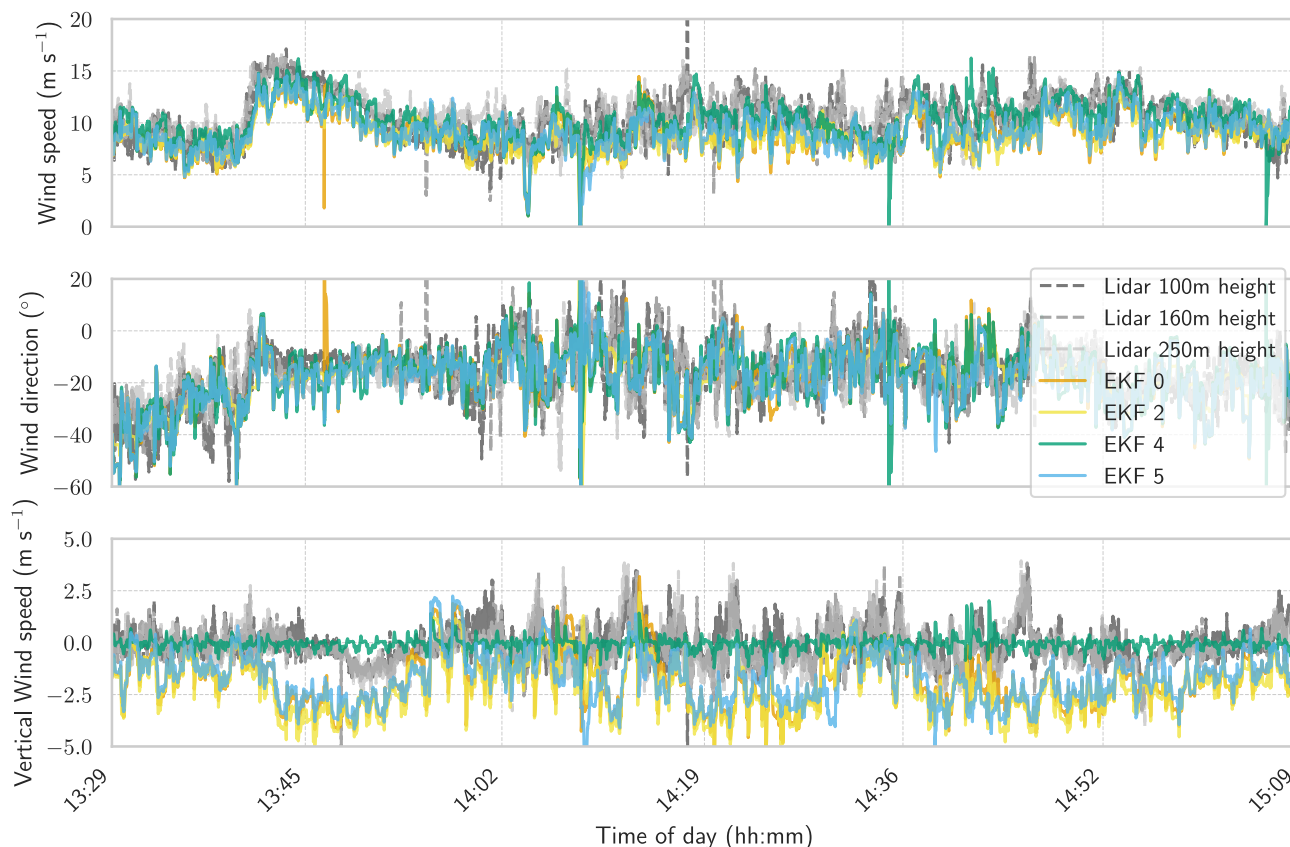


Figure 20. Test flight from 05-06-2024. Wind profile comparison between EKF results with a minimum sensor setup and lidar observations.

some of these peaks, such as the one observed at 13:47, it did not lead to significant improvements throughout the rest of the
 585 flight.

A more detailed analysis of the shape of the wind profile during the wind gust event is shown in Fig. 21. By incorporating a zero vertical wind speed measurement (EKF 4), the time response of the wind model improves. In contrast, other models show a slower time response for horizontal wind speed and instead exhibit a decrease in vertical wind speed to match the same apparent wind speed. Furthermore, around 13:55, there is a localised increase in wind speed at higher altitudes that none of the
 590 models can effectively capture. Apparent wind speed measurements might have been more effective at capturing these transient phenomena, but unfortunately, they were unavailable for this flight.

Regarding the wind direction, the time response appears to be better across all models, which similarly track the changes throughout the flight. The higher resolution of the lidar data also enables verification that the fluctuations in wind velocity align with the observations.

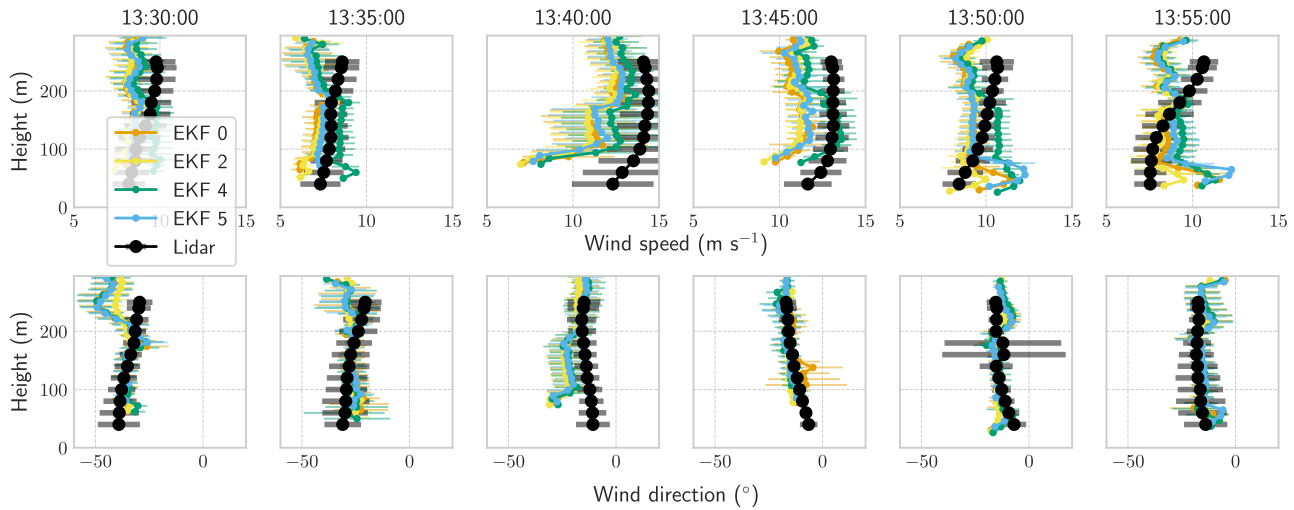


Figure 21. Test flight from 05-06-2024. Wind profile comparison between EKF results with a minimum sensor setup and lidar observations.

595 5.4 Turbulence measurements

Since the EKF estimates wind characteristics based on measurements that are not directly related to the inflow, accurate estimates of the variability in wind speed are highly dependent on the correct tuning of the filter. To verify that the rapid changes estimated are physical, one can examine the turbulence estimates, which quantify these variations.

A key aspect to investigate is the power density spectrum of the wind speed, as shown in Fig. 22. The sampling frequency
 600 of the measurements was 0.1s, corresponding to frequencies resolved of up to 5Hz. It is observed that the energy cascade follows the Kolmogorov slope within the range of ~ 0.01 Hz – 0.3 Hz, with higher frequencies damped, likely due to the time response of the EKF. Additionally, a peak is observed below 0.01Hz, corresponding to the cycle timescale for the analysed flight. This peak coincides with a rapid change in wind speed, attributed to the significant variation in kite height experienced during reel-in.

605 Another parameter assessed in the study is the turbulence intensity, defined as the standard deviation of the wind speed divided by its mean value. This parameter is commonly used in conventional wind energy assessments, particularly when assessing turbine fatigue loads. Turbulence intensity is also measured by the profiling lidar, providing an additional validation of the EKF. However, it is important to note that the quantities measured by the lidar and the EKF are not directly equivalent.

The lidar measures turbulence intensity over an averaged volume at a fixed height, with the area determined by the laser
 610 cone angle. In contrast, the turbulence intensity derived from the EKF is calculated over a range of heights within ± 10 m of the lidar measurement to obtain comparable values. It is calculated as the 1-minute standard deviation divided by the mean.

With these considerations in mind, we can compare the turbulence intensity estimates from both the EKF and lidar, as shown in Fig. 23 for the two analysed flights. The comparison reveals good agreement in magnitude, and the temporal behaviour of

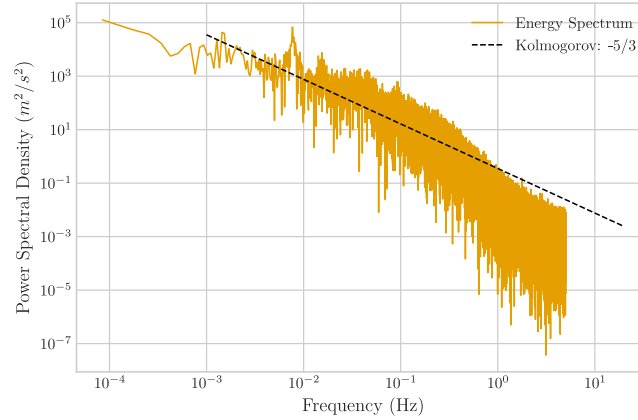
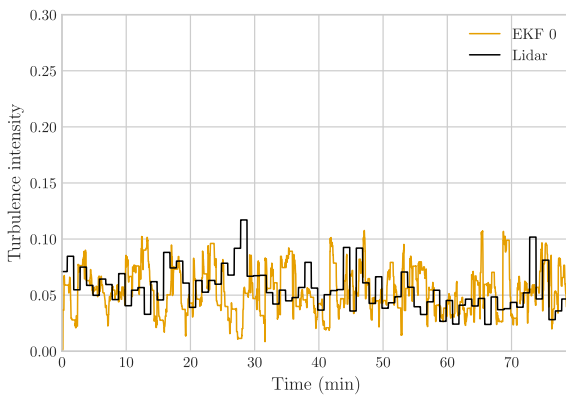
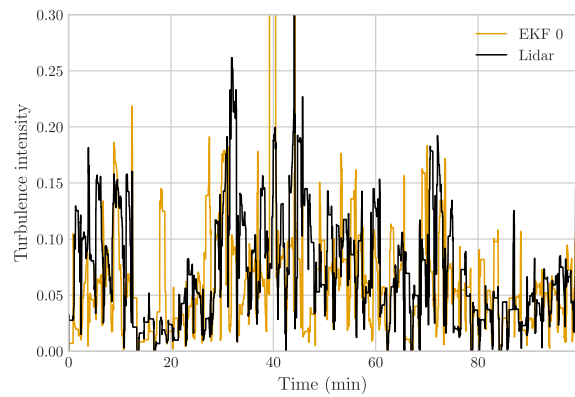


Figure 22. Test flight from 10-08-2019. Power spectral density of the wind speed.

the EKF closely matches that of the lidar, as illustrated in Fig. 23b. While these initial comparisons are promising, a more
 615 detailed analysis is needed to fully assess the accuracy of these measurements.



(a) V9 kite, flight 27-11-2023



(b) V9 kite, flight 12-03-2024

Figure 23. Turbulence intensity at a height of 140m

6 Conclusions



This study presents a sensor fusion technique for tethered flying systems to estimate the state of the system and the wind conditions at the kite. The system state includes the kite's position, velocity, aerodynamic performance, and tether shape. The sensor fusion technique consists of an iterated extended Kalman filter (EKF), modelling the kite as a point mass and the tether



620 as a system of point masses linked by spring damper elements. The tether shape is assumed to be quasi-static and includes the robotic control unit as a point mass, linked to the kite by an additional spring damper element representing the bridle line system. By integrating data from multiple sensors, such as position, velocity, tether force, and reeling speed, the EKF model can accurately estimate system dynamics and wind conditions, provided the filter is appropriately tuned to the specific system configuration.

625 The proposed EKF effectively estimates average wind profiles, particularly those that follow a conventional logarithmic slope. However, its performance is less accurate in scenarios with significant deviations, such as sudden wind gusts, where the filter requires a few minutes to adapt to rapid changes in wind speed. Notably, the filter adapts faster to changes in wind direction, indicating greater sensitivity to directional variations. To improve the time resolution in wind estimations, direct airflow measurements should be included, such as a well-calibrated and maintained Pitot tube.

630 The accuracy of the estimations is highly dependent on the quality and reliability of the input measurements. While the EKF compensates for minor inaccuracies and correct for biases in some measurements, substantial issues such as improperly calibrated sensors or malfunctioning equipment can significantly degrade the accuracy of wind speed and direction estimations.

Sensor noise and filter tuning are areas that deserve further attention. While the paper acknowledges the potential inaccuracies stemming from incorrect tuning and noise modelling, it does not discuss strategies to mitigate these problems in-depth. 635 For the proposed EKF to be more robust for a specific system, it can be beneficial to incorporate a more comprehensive noise modelling. Implementing advanced calibration techniques, such as adaptive filtering methods for real-time sensor noise adjustments, could enhance the accuracy and reliability of state estimations.

The proposed approach also demonstrates the ability to estimate tether and kite orientations, which closely align with the measurements at the kite. This capability enables the estimation of the pitch deformations at the central struts of the wing 640 relative to the tether, also referred to as the depower angle. This information can be used to estimate the wing angle of attack based on measurements made on the bridle lines. The kite was aerodynamically characterized for the range of flight conditions available. Using this newly estimated angle, showing an improvement with respect to previous analyses. However, for a complete aerodynamic characterization, tailored test flights must be conducted to capture the aerodynamic behaviour of the kite across different conditions.

645 This study explored several sensor setups, demonstrating that a single airborne sensor measuring the kite position and velocity, combined with ground-based force and tether length sensors, is sufficient to obtain reasonable estimates. While modelling the wind profile as logarithmic does not necessarily improve the estimates, it offers flexibility in independently tuning the process noise of wind speed and direction, which can be useful for supervisory control where high-frequency variations need damping. Adding a zero vertical wind speed measurement could improve the filter time response during transient events 650 by preventing the misinterpretation of horizontal wind speed changes as vertical wind variations. Installing well-calibrated flow sensors on the kite is essential for high-resolution wind velocity estimates. Furthermore, a high-resolution angle-of-attack sensor is strongly recommended to accurately capture the wing angle of attack changes and enable accurate aerodynamic characterization of the kite.



Overall, the EKF has proven to be a robust method for wind and state estimation for AWESs, demonstrating sufficient accuracy for mean wind speed and direction estimation for power generation cycles. However, its responsiveness to rapid changes in wind conditions is limited by the quality and availability of sensor data. Future work should focus on optimising sensor setups and conducting targeted system identification test flights to capture dynamic states beyond normal operational limits, ensuring the kite can be characterized fully. Ultimately, this study highlights that the kite can be effectively used as a sensor, providing valuable insights into system dynamics and wind conditions.

Code and data availability. The code can be found in the attached Github repository. It is currently private, but will be made public when the paper is published. <https://github.com/ocayon/EKF-AWE>.
The datasets can be found on different data repositories: 1. Flight data 08-10-2019, Schelbergen et al. (2024). 2. Flight data 27-11-2023, Cayon et al. (2024a). 3. Flight data 05-06-2024, Cayon et al. (2024b). The flights from 2023 and 2024 are under one year embargo and will be public in November 2025.

Appendix A: System Specifications and Tuning Parameters

This appendix provides detailed information about the components of the Airborne Wind Energy System (AWES) and the specific tuning parameters used for the Extended Kalman Filter (EKF) implementation.

A1 System Description

Kite Parameters

Table A1. Kite specifications

Parameter	Value	Unit
Model Name	V3	–
Mass	15	kg
Area	19.75	m ²
Span	10	m

Bridle and KCU Parameters

Tether Parameters

A2 Tuning Parameters for EKF

Measurement Standard Deviations



Table A2. Kite Control Unit (KCU) specifications


Parameter	Value	Unit
KCU Length	1	m
KCU Diameter	0.48	m
$C_{\perp, \text{kcu}}$	0.69	–
$C_{\parallel, \text{kcu}}$	0.83	–
Mass	27.6	kg
Distance KCU to Kite	11.5	m
 Length of Bridle Lines	96	m
Diameter of Bridle Lines	0.0025	m

Table A3. Tether specifications

Parameter	Value	Unit
Material	Dyneema-SK78	–
Density (ρ_t)	970	kg m ^{−3}
Young’s Modulus (E)	132	GPa
Diameter	0.01	m
C_{\perp}	1.1	–
C_{\parallel}	0.01	–
Number of Elements	10	–

Model Standard Deviations



Author contributions. Conceptualisation, O.C. and R.S.; methodology, O.C.; software, O.C.; investigation, O.C.; writing—original draft preparation, O.C.; writing—review and editing, R.S.; supervision, R.S.; funding acquisition, R.S. All authors have read and agreed to the published version of the manuscript.

Competing interests. At least one of the (co-)authors is a member of the editorial board of Wind Energy Science. R.S. is a co-founder of and advisor for the start-up company Kitepower B.V., which is commercially developing a 100 kW kite power system and provided their test facilities and staff for performing the in situ measurements described in this article. Both authors were financially supported by the European Union’s Meridional project, which also provided funding for Kitepower B.V.

Table A4. Measurement standard deviations used in the EKF

Parameter	Value	Unit
Position (\mathbf{r}_k)	5	m
Velocity (\mathbf{v}_k)	2	m s ⁻¹
Tether Length (l)	0.5	m
Tether Elevation (β_0)	3	°
Tether Azimuth (ϕ_0)	3	°
Position tether model	1×10^{-5}	m
Zero Vertical Wind Speed ($v_w^z = 0$)	2	m s ⁻¹
Apparent Airspeed (v_a)	1	m s ⁻¹
Bridle Angle of Attack (α_b)	4	°

Table A5. Model standard deviations used in the EKF

Parameter	Value	Unit
Position (\mathbf{r}_k)	2.5	m
Velocity (\mathbf{v}_k)	1	m s ⁻¹
Wind Velocity (\mathbf{v}_w)	0.1	m s ⁻¹
Wind Friction Velocity (u_*)	0.002	m s ⁻¹
Wind Direction (ϕ_w)	0.2	°
Vertical Wind Speed (v_w^z)	0.01	m s ⁻¹
Lift Coefficient (C_L)	0.01	—
Drag Coefficient (C_D)	0.003	—
Side Force Coefficient (C_S)	0.01	—
Tether Elevation (β_0)	5	°
Tether Azimuth (ϕ_0)	5	°
Tether Length (l)	0.1	m

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