



Challenges in Detecting Wind Turbine Power Loss: The Effects of Blade Erosion, Turbulence and Time Averaging

Tahir H. Malik¹ and Christian Bak²

¹Vattenfall, Amerigo-Vespucci-Platz 2, 20457, Hamburg, Germany ²DTU Wind and Energy Systems, Frederiksborgvej 399, 4000 Roskilde, Denmark **Correspondence:** Tahir H. Malik (tahir.malik@vattenfall.de)

Abstract. Blade leading-edge erosion (LEE) and atmospheric turbulence intensity (TI)can significantly impact wind turbine performance and annual energy production (AEP). This study employs aeroelastic simulations to investigate their combined effects. An offshore original equipment manufacturer (OEM) provided aeroelastic model was used to simulate various scenarios. Turbulence intensity was varied for a range of wind speeds and the blade polars were modified to simulate different

- 5 degrees of erosion, represented by varying levels of roughness. Findings reveal that even mild simulated erosion can reduce AEP by 0.82%, while more severe erosion leads to a 2.83% decrease. Increasing TI exacerbates these losses, with a 25% TI causing up to a 3.5% AEP reduction for eroded blades. These effects were most pronounced at lower wind speeds. Furthermore, standard time-averaging practices in power curve analyses can obscure the true magnitude of TI and LEE's impact on short-term power fluctuations. This work emphasises the critical importance of considering both blade condition and TI for
- 10 accurate AEP assessments, optimal maintenance scheduling and improved wind turbine design in the context of site-specific atmospheric conditions.

1 Introduction

The performance of wind turbines is a multifaceted subject of research, being intricately affected by a multitude of environmental Wharton and Lundquist (2012) and operational factors. Among these, turbulence intensity (TI) and leading edge erosion

(LEE) represent two key sources that can negatively impact wind turbine power output and annual energy production (AEP). The detrimental effects of leading edge roughness (LER) or leading edge erosion on aerofoil characteristics have been extensively documented in wind tunnel experiments Hansen (2008), Maniaci et al. (2016), Gaudern (2014), Krog Kruse et al. (2021), Bak et al. (2023). Furthermore, these effects have also been the subject of numerous studies on the impact of erosion and roughness on wind turbine annual energy production Bak et al. (2016), Ehrmann et al. (2017), Kruse (2019) Han et al. (2018). These studies indicate potentially significant energy losses of up to 7%.

20

15

The question this study attempts to answer is: "What makes power losses due to erosion so challenging to detect in operational wind turbines and how can these challenges be more effectively addressed?" Despite extensive theoretical understanding of LEE's impact, a significant challenge remains in the practical identification and validation of these computed energy losses within operational wind turbines using Supervisory Control and Data Acquisition (SCADA) data Ding et al. (2022). This chal-





25 lenge stems from the complex interplay between factors affecting the turbine's performance, making it difficult to isolate the effects of LER from numerous other variables and uncertainties affecting its performance. Consequently, there is an absence of an established correlation between blade erosion and turbine performance and a lack of understanding of why this is the case.

This investigation aims to bridge the gap between empirical data obtained from wind tunnel experiments and theoretical results derived from simulations. This gap in knowledge significantly hampers the wind industry's ability to optimise opera-

- 30 tions and maintenance strategiesBadihi et al. (2022)Gonzalez et al. (2019). In addition, the lack of insight limits the potential benefits of quantifying AEP loss. In practice, such quantification could enable investors to develop more accurate business cases for wind park projects, thereby facilitating better assessment of project viability and maximising returns on investment. Moreover, the industry's ability to effectively plan blade leading-edge repair operations and maintenance, which must balance cost and energy losses, is hindered. Despite significant efforts from blade designers, including the development of leading edge
- 35 protection (LEP) and aerofoils more robust towards the effects of erosion, the industry still faces challenges in mitigating these adverse effects. And in fully leveraging the available knowledge throughout a wind park project's lifecycle.

Furthermore, as wind turbines' rotors increase in length and tip speeds increase Hansen (2008), the potential negative impact of LER on AEP is likely to be exacerbated. To address the challenge of LEE detection and mitigation, this study investigates the problem by shifting the focus of the investigation from the complex environment of SCADA data analysis to a controlled

40 simulation environment. This approach has the potential to isolate and examine the influence of LEE under varying TI, while minimising the impact of the myriad of performance-affecting variables present in real-world operational scenarios Barthelmie and Jensen (2010).

This study will specifically examine the influence of TI relative to LEE, on wind turbine aerodynamic performance using an aeroelastic simulation code. Turbulence is a well-known atmospheric condition that significantly impacts wind turbine perfor-

- 45 mance St. Martin et al. (2016)Saint-Drenan et al. (2020)Kim et al. (2021). This approach enables isolation and quantification of the effects on power output under controlled conditions, excluding the influence of other confounding variables present in real-world operational data. A wind turbine with blade profiles representing blade erosion for various turbulence intensities will be simulated. The turbulence levels typical for an offshore environment will be reproduced and the effect on power output will be analysed. Furthermore, this study has the unique advantage of utilising a proprietary aeroelastic model obtained from
- 50 a leading original equipment manufacturer (OEM). This model accurately represents the complex dynamics of wind turbines operating within an operational wind park.

Finally, this research will investigate the effects of time interval averaging, traditionally performed using 10-minute intervals. Specifically, it will examine the influence of smaller time intervals, aiming to provide a more nuanced understanding of the interplay between erosion, turbulence, time interval averaging and turbine performance.

55 2 Method

This study aims to conduct a fundamental investigation into the impact of turbulence intensity on the aerodynamic performance of wind turbine rotors, focusing on the effects of leading-edge erosion. This is achieved through the use of an aeroelastic code





that incorporates structural dynamics. Also, the effects of wind shear are briefly investigated. Additionally, the study examines
the potential impact of different time-averaging intervals used in operational data analysis on the ability to detect and quantify
the effects of leading-edge erosion.

2.1 Wind turbine and aeroelastic code

The investigation utilises the Blade Element Momentum (BEM) based multi-body aero-servo-elastic tool HAWC2, developed by DTU Wind Denmark. A comprehensive description, usage and implementation of HAWC2 are well-documented in the literature Larsen and Hansen (2007). The HAWC2 model used in this study, provided by an OEM, represents a currently operational offshore wind turbine. It is a three-bladed, multi-megawatt, horizontal axis wind turbine with variable speed, pitch

65 operational offshore wind turbine. It is a three-bladed, multi-megawatt, horizontal axis wind turbine with variabl regulation and yaw control.

Due to intellectual property considerations, specific details about the turbine, such as structural properties and control philosophy, are not disclosed; hence, the power is presented as *normalised power* and is expressed as power relative to the rated power.

70 2.2 Representing leading edge erosion

roughness, compared to a clean aerofoil surface.

Blade leading edge erosion was modelled as a surface roughness, representing a precursor to more significant aerofoil deterioration where voids or cavities may begin to form. The HAWC2 model's blade aerofoil polars for the outer 15% were modified to reflect the effects of erosion. The length and location of this applied degradation correspond to field observations of similar blades after approximately two years of operation.

75 Wind tunnel test data from Krog Kruse et al. (2021), which utilised P400 and P40 sandpaper to simulate different erosion levels on a NACA 63₃-418 aerofoil, served as the empirical basis for these modifications. These textures represent the roughness induced by rain droplets impacting the leading edge at high velocities. While the P40 sandpaper provides a simplified model of severe erosion, it is important to acknowledge that real-world erosion on turbine blades can be influenced by a multitude of factors. Although the tested aerofoil is not identical match to that in HAWC2 model, this approach is deemed a suitable approximation for representing the outboard region of eroded turbine blades.

The wind tunnel tests were conducted at a Reynolds number of 5 x 10^6 . Results for the Clean (no sandpaper), P400 (extra fine, with an average roughness value of 0.035 mm) and P40 (coarse, with an average roughness value of 0.415 mm) sandpapers were used. The P40 sandpaper, which has a larger grain size, was chosen to represent a more severe erosion state. Figures 1 and 2 illustrate that for both P400 and P40 sandpaper roughnesses, the $C_L max$ is reduced by approximately 10% within a specific range of α before deep stall. Similarly, the C_D increases by approximately 50% for P400 roughness and 100% for P40

85

To represent the effects seen in the wind tunnel experiments, derived factors were used to approximate the results. For simplicity, the lift polar representing the clean aerofoil was scaled by a factor of 0.9. Additionally, two artificial drag polars were created by scaling the drag polar representing the clean aerofoil by factors of 1.5 and 2.0, respectively.









Figure 1. Effect of leading-edge erosion on lift coefficient (C_L) as a function of angle of attack (α). Compares Clean, P40, and P400 blade conditions, demonstrating decreased C_L with increased roughness (measurement data from Krog Kruse et al. (2021))

Figure 2. Effect of leading-edge erosion on drag coefficient (C_D) as a function of lift coefficient C_L). Compares Clean, P40 and P400 blade conditions, demonstrating increased C_D with increased roughness (measurement data from Krog Kruse et al. (2021))

90 This approach was deemed acceptable as the HAWC2 simulations were performed over a limited range of angle of attacks, which is relevant for cases of normal turbine operation, detailed in Section 2.5. These factors were applied between the aerofoil's minimum and maximum lift angles of attack. Beyond this range, at high angles of attack (30 degrees), the adjusted characteristics smoothly blend into the original data. The assumption is that at high angles of attack the performance is dominated by flat plate behaviour, thus being independent of the surface characteristics. Due to confidentiality, the final modified 95 aerofoil characteristics cannot be shown.

2.3 Representing Wind Farm turbulence

The simulations reproduce turbulence conditions typical of operational offshore wind farms. Turbulence data was sourced from a meteorological mast located adjacent to an operational offshore wind farm which utilises the same turbine type as the HAWC2 model.

100 The turbulence intensity profile at the site, corrected to the turbine's hub height using WindPro EMD International A/S (2023), is shown in Figure 3. This comprehensive dataset was derived from six years of 10-minute averaged data and includes all wind speeds without directional filtering. It incorporates the effects of wakes from adjacent turbines as well as a wind farm, offering a realistic depiction of the first row in a wind farm environment.

The mean *TI* is 7.3% for the entire period and 6.7% when limited to turbine operational wind speeds - between 4 and 25 m/s. The *TI* distribution is depicted in Figure 4 and together, these figures reveal that although higher turbulence intensities do occur, they are relatively rare and primarily occur at lower wind speeds. For sake of convenience in the simulation environment,





a turbulence intensity of 6% was used to represent mean annual wind farm turbulence with wake free directional filters applied. Specific location details of the wind farm and the met mast are omitted due to confidentiality.



Figure 3. Turbulence intensity at the hub height as a function of wind Figure 4. Probability density distribution of turbulence intensity (TI) speed. Data obtained from the wind farm's meteorological mast for wind speeds between 4-25 m/s (limited at 25%)

2.4 Data Time Averaging

- 110 To better understand the potential impact of different data processing techniques on wind and power measurements, this study investigates the effects of varying time-averaging intervals on the detection and quantification of erosion-related power losses. The analysis of wind and power measurements often involves binning and time-averaging. Binning and time-averaging data are forms of data filtering that can both clarify and potentially complicate the interpretation of results. Careful selection of bin sizes is crucial to avoid information loss and potential misinterpretation.
- 115 Time averaging, traditionally over a 10-minute period, is used to smooth turbine signals such as wind speed, power and behaviours such as pitch or torque. These responses are slightly delayed to wind speed, that can fluctuate rapidly. Time averaging can provide a more representative overview of turbine performance and prevailing wind conditions, allowing identification of trends, patterns in data, supported by findings from Abolude and Zhou (2018)Do and Berthaut-Gerentes (2018)Elliott and Infield that highlight associated benefits and complexities. While longer intervals simplify data processing and reduce data stor-
- 120 age needs, they also risk masking changes in performance and the subtle effects of leading-edge erosion on turbine dynamics Gonzalez et al. (2017) Gonzalez et al. (2019).

Importantly, time averaging potentially introduces bias into data analysis. For example, smoothing out short-term fluctuations in power output can inadvertently alter the perceived shape of the power curve, such as the location of the the knee in the power curve. A crucial aspect to consider is the balance between the need to reduce noise in the data and the risk of masking important

125 turbine responses. An excessively short time interval may lead to noisy data, while an interval that is too long risks filtering the turbine's behaviour too much.





Furthermore, time averaging affects the perceived inertia of the turbine. When power output is averaged over a longer time interval, short-term fluctuations in power output are suppressed, potentially making the turbine appear less responsive to changes in wind speed. If the time interval used for averaging significantly exceeds the characteristic response time of
the turbine, the inertia of the turbine may be underestimated and its ability to respond to changes in wind speed could be overestimated. Conversely, using a time interval that is too short may amplify short-term fluctuations in power output, making data interpretation difficult because the raw data in many cases will be a swarm of data points. It is therefore important that the specific requirements of the analysis should ultimately dictate the selected averaging time interval.

To investigate these effects, this study explores the use of shorter time-averaging intervals to potentially unravel the nuanced
effects of leading-edge erosion on turbine performance, which may be masked in traditional 10-minute averages. The challenge lies in selecting an interval that offers sufficient detail without sacrificing clarity, ensuring that critical information about turbine performance and the impact of blade surface conditions is neither lost nor misrepresented. Data from HAWC2 simulations, with a 0.01 second time step, was collected from all wind speed simulation seeds for a given turbulence intensity and blade profile. Time averaging was then applied to wind speed and turbine sensor variables such as power for time intervals of 0.01, 1, 30, 60, 120, 300 and 600 seconds. Subsequently, the data was averaged into 1 m/s wind speed bins and the turbulence intensity

of the original simulation seed was applied to time intervals sliced from it.

2.5 Simulation settings and test cases

This study employed a range of simulation cases using HAWC2, a Blade Element Momentum (BEM)-based multi-body aero-servo-elastic tool, to explore the impact of turbulence intensity and blade erosion on wind turbine performance. Simulations
145 were executed for a range of turbulence intensities for the clean and and two eroded blade profiles. Individual cases were run in 1 m/s increments ranging from 4 to 25 m/s, representing the turbine's cut-in and cut-out wind speeds. Each configuration of wind speed, *TI* and blade condition was represented by six individual simulation runs, or seeds, to ensure statistical robustness International Standard. Wind energy generation systems - Part 1: Design requirements. IEC 61400-1 International Electrotechnical Commission (IEC) (2019).

The turbulence intensity was varied across a broad spectrum including 0%, 4%, 5.5%, 6.0%, 6.5%, 7%, 10%, 15%, 20%and 25%, with a focus on values around the observed average annual ambient *TI* at an offshore site, along with broader values for comparison. Each simulation was run for 900 seconds, with data from the last 600 seconds used for analysis to ensure steady-state conditions were reached. The time step of the simulations is 0.01 seconds. The wind shear was investigated for a range of conditions, including a zero shear value and a power-law profile with an alpha value of 0.14. The air density was fixed

155 at 1.225 kg/m³, representative of sea-level conditions at 15°C. The Mann turbulence parameter $\alpha \epsilon^{2/3}$ Mann (1994), energy level was set to its default value of 1.0. For a detailed explanation of specific parameters and settings, refer to the HAWC2 manual Larsen and Hansen (2007) or IEC61400-1 ed. 3 International Electrotechnical Commission (IEC) (2019).



170



3 Results and Discussion

The simulations conducted in this study have been analysed from multiple perspectives, with the results presented in four 160 distinct sections:

- Effect of shear and blade erosion on power
- Effect of turbulence intensity and blade erosion on power
- Effect on Annual Energy Production
- Effect of time averaging on power curve

165 3.1 Effect of shear and blade erosion on power

This section investigates the impact of leading edge erosion on wind turbine power curves under different wind shear conditions using HAWC2 simulations. The simulations were executed at a constant turbulence intensity of 0% to isolate the distinct effects of shear and blade condition. Figure 5 presents normalised power curves for clean blades and those exhibiting P400 and P40 roughness levels, under both zero shear and with imposed wind shear conditions. As expected, the leading-edge roughness reduces the power output across the range of wind speeds.



6 Percentage Power Loss [%] 5 3 2 P400 roughness, Shear Loss 0 P40 roughness, Shear Loss Clean, Shear Loss -1 6 7 9 10 11 12 8 Wind Speed [m/s]

Figure 5. Normalised power curves for various roughnesses under no shear and constant shear conditions (Simulations, 0% *TI*).

Figure 6. Percentage power loss due to shear, referenced against the baseline clean blade without shear, for various roughnesses at 0% *TI*).

Comparing the no-shear and shear conditions reveals the turbine's sensitivity to shear-induced variations in the wind profile along the rotor span. Under shear conditions, the power curves for both clean and eroded blades exhibit a shift, up to 5.8% for





the P40 roughness blade with shear, relative to a clean blade at zero shear conditions, as seen in Figure 6. This demonstrates an adjustment in operational behaviour to account for the velocity gradient imposed by the atmospheric shear.

175

Despite these observed shear effects, this analysis will focus on investigating turbulence, as its impact on performance is typically more substantial.

3.2 Effect of turbulence intensity and blade erosion on power

3.2.1 Investigation based on the power curves

180

The normalised, 10-minute averaged power curve of the turbine for various turbulence intensities is shown in Figure 7. Consistent with previous research Saint-Drenan et al. (2020), Wagner et al. (2010), the turbine's power output is significantly influenced by turbulence intensity (TI), particularly pronounced within the partial load region of the power curve, which is the operational range between the wind speed where maximum rotational speed is achieved and the wind speed where rated power is reached. The plot includes higher turbulence intensities, such as 20%, to demonstrate the trend in their effect on the power curve. This variance highlights the the considerable effect of turbulence intensity on turbine performance.



Figure 7. Effect of turbulence intensity on a wind turbine's normalised power curve (clean blades, aeroelastic simulations)

Figure 8. Impact of turbulence intensity and blade erosion on a wind turbine's normalised power curve (aeroelastic simulations)

185

Comparative analysis among "Clean," "P400," and "P40" blade conditions, representing varying degrees of erosion, are presented in Figure 8. For clarity, simulations model erosion on the last 15% of the blade's leading edges. Results are shown for 6% turbulence intensity, representing a typical mean value for offshore sites. The 0% and 20% plots are included for comparison to more outlying conditions, demonstrating a similar trend in power reduction with increasing blade erosion. This affirms the consistent detrimental impact of erosion across various TI conditions.





- 190 The figures facilitate a revealing comparison of effects of turbulence relative to erosion. Analysis of the power curve at a specific point, such as the "knee", reveals that changes in turbulence intensity influence power output are more pronounced than blade erosion. This is evident in Figure 8: for the clean blade at 11 m/s wind speed, power reduces to approximately 97.0% when TI increases from 0% to 6% and further to 88.1% at 20% TI. For eroded blades, these reductions are comparable: 96.2% and 87.2% ("P400") and 95.7% and 86.9% ("P40").
- Considering a wind speed of 11 m/s and 6% TI, erosion causes power losses of approximately 0.9% ("P400") and 1.3% 195 ("P40") relative to the clean blade. Importantly, the power output's standard deviation at this wind speed is approximately 1.03% (6% TI) and 3.23% (20% TI). This underscores a major challenge: particularly at higher TI, the standard deviation exceeds the power loss due to roughness, making it difficult to isolate and detect the effects of erosion on power output based on the power curve alone. However, the comparability of values at lower TI suggests that erosion effects could potentially be detected more readily under less turbulent conditions.
- 200

An interesting observation in Figure 8 is the intersection of power curves around 9.5 m/s. This intersection is caused by a combination of factors. Firstly, the inflection point in the power curve at 9.5 m/s, where the curvature changes, plays a role. Secondly, the averaging effects inherent in calculating power curves from unsteady power output contribute to this phenomenon.

While analysing the changes in power curve shapes provides valuable insights, it offers an incomplete understanding of the true impact of erosion and turbulence. To accurately assess the overall effect, it is crucial to consider the site-specific wind 205 speed distribution and its influence on the turbine's annual energy production. A more comprehensive analysis is presented in Section 3.3.

3.2.2 Investigation relative to a reference power curve

- To further investigate how the power curve is influenced by erosion under varying turbulence intensities, this study conducted 210 a comparative analysis. The change in power relative to a reference Clean profile power curve at 6% TI, focusing on "P40" roughness, was investigated. The results are shown in Figure 9 as a function of wind speed across a range of turbulence intensities. The delta power curve exhibits a 'kink', a point characterised by a sudden change in gradient, at around 9.5 m/s attributed to the previously discussed averaging effect of time averaging. The most substantial reduction of power due to roughness were identified between 9 and 13 m/s. At lower turbulence intensities, i.e. 7% and below, roughness was found
- to have an effect in reducing power. Moreover, for increasing turbulence intensities, the influence of roughness increases 215 dramatically within the same wind speed range.

These findings highlight the non-linear and interdependent relationship between blade roughness and turbulence intensity in their impact on power output. Furthermore, they suggest that both factors must be considered when assessing wind turbine performance, especially within specific wind speed ranges.

3.2.3 Investigation using power coefficients 220

The coefficient of power (C_p) represents a key metric for evaluating the performance of wind turbines. This study analysed how C_p varies with wind speed, turbulence intensity and blade roughness. Figure 10 shows the C_p as a function of wind speed







Figure 9. change in power percentage P40 roughness - Clean (6% TI) Profile for various turbulence intensities

for various turbulence intensities, employing a clean profile blade. The findings indicate that the greatest variation of C_p is observed at wind speeds below approximately 9 m/s. To evaluate the impact of roughened blade leading edges on C_p, Figure 11 shows the variation of C_p for the profiles at 6% turbulence intensity. These results suggest that the impact of both forms of roughness is less pronounced than that of a certain threshold value of turbulence intensity.





Figure 10. Power coefficient as a function of wind speed for a clean profile blade, with various turbulence intensities

Figure 11. Power coefficient as a function of wind speed for various leading edge roughness profiles, with a fixed turbulence intensity of 6%





This investigation analysed HAWC2 simulated data, focusing on the last 10 minutes of each simulation to capture steadystate conditions. Instances where the power coefficient (C_p) exceeds or approaches the Betz limit of 0.593 in high turbulence intensity conditions are carefully examined. The exceeding of the Betz limit may be attributed to several factors, including turbine inertia and control dynamics, where the inherent latency in response mechanisms such as pitch and generator torque control results in a temporal mismatch between the turbine's power response and rapid wind speed fluctuations characteristic of turbulent environments. This mismatch, particularly when results are time-averaged over a 10-minute window, can yield simulated C_p values that momentarily surpass the Betz limit. Thus, it is not believed that CP values exceeding the Betz limit have any physical meaning, but rather that it is an artefact from the averaging of the the wind speed and the rotor performance.

Additionally, the analysis reveals that highly turbulent conditions create localised gusts, temporarily increasing the effective wind speed at segments of the rotor, diverging from steady-state assumptions and causing transient spikes in power output, further exacerbating the mismatch between wind speed and power output. This effect, coupled with the stochastic nature of turbulence that can enhance kinetic energy transfer to the rotor plane and momentarily boost the available wind energy beyond typical averages used in Betz limit calculations. These findings underscore the limitations of steady-state assumptions in accurately capturing the dynamic interactions between wind turbines and complex wind fields. Future efforts should focus on refined simulation models and analysis techniques designed to address these limitations.

Figure 12 provides further insight on the combined effects of roughness and turbulence intensity. It depicts C_p for a limited range of lower turbulence intensities, along with the three blade profiles at 6% *TI* for wind speeds up to 11 m/s. The overlap between the C_p 's for turbulence intensity and roughness suggests that distinguishing between these two effects may

245 be challenging, particularly in high turbulence conditions. This complicates the interpretation of aerodynamic performance degradation.

3.2.4 Summary of the influence of TI and erosion on power

The findings presented herein reinforce the notion that both turbulence and blade erosion exert substantial influences on the wind turbine power output. It has been observed that turbulence profoundly affects the power curve, predominantly in the partial load region. Despite the inherent complexities associated with analysing the performance of the wind turbines under turbulent conditions, this study emphasises the significance of incorporating TI in performance evaluations. This alignment with preceding studies Wagner et al. (2010) and Saint-Drenan et al. (2020) further validates the critical nature of TI in such analyses.

The examination of delta power highlights the detrimental effects blade roughness on wind turbine power output, with the greatest power reduction due to roughness observed at wind speeds between 9 and 13 m/s. This observation is consistent with prior research Bak et al. (2020), emphasising the significance of considering roughness effects when assessing wind turbine performance. The study also showed that the impact of roughness on power output is further exacerbated at higher turbulence intensities, suggesting that both turbulence and erosion should be considered in performance assessment.

While the analysis focused on the impact of blade erosion on power, it is important to recognise that erosion could also influence other aspects such as loads and sensor output. These potential impacts warrant further investigation.







Figure 12. Power coefficient as a function of wind speed for a clean profile blade at various turbulence intensities and various leading edge roughness profiles at 6% turbulence intensity

3.3 Annual Energy Production (AEP) Calculation

This section explores the calculation of annual energy production, investigating the impact of both blade erosion and turbulence on wind turbine performance. Analyses included a real-world operational offshore wind farm and hypothetical scenarios at three fictitious sites.

265 3.3.1 AEP for an existing site

AEP was calculated for a wind turbine situated in an offshore wind farm operating under mean turbulence intensity of 6%, characterized by a Weibull distribution with a scale parameter A = 10.72, a shape parameter of k = 2.17. This corresponds to an average wind speed of 9.49 m/s. The computations expressly exclude the wake effects of upstream wind turbines.

The comparative analysis focused on quantifying the impact of blade erosion and turbulence intensity on AEP by comparing the outcomes for three distinct blade profiles. Table 1 shows the AEP variation for each profile relative to the 6% *TI* power curve of the corresponding profile.

The results revealed an unexpected finding: under certain turbulence conditions, the turbulence intensity reduces AEP less for the rougher P40 blade profile than for the P400 profile. This counterintuitive result warrants further investigation, as it challenges conventional expectations.

275

Similarly, Table 2 shows the AEP variation for each profile relative to the Clean blade profile's 6% *TI* power curve. From the results it is clear that even mild simulated erosion, represented by the P400 blade profile, has a significant impact on the turbine's AEP, with a 0.82% decrease. As erosion progresses, the AEP decreases further to 1.46% for the rougher P40





Table 1. Influence of roughness and TI on AEP relative to a 6% TI power curve of the same profile

Blade profile	TI [%]										
	0	4	5.5	6	6.5	7	10	15	20	25	
Clean delta AEP [%]	0.34	0.11	0.03	0	-0.02	-0.04	-0.23	-0.63	-1.20	-1.89	
P400 delta AEP [%]	0.44	0.11	0.05	0	-0.04	-0.07	-0.29	-0.78	-1.46	-2.32	
P40 delta AEP [%]	0.51	0.12	0.05	0	-0.04	-0.06	-0.26	-0.70	-1.30	-2.07	

Table 2. AEP variation due to Turbulence Intensity relative to a Clean blade with 6% TI power curve

Blade profile	TI [%]										
	0	4	5.5	6	6.5	7	10	15	20	25	
Clean delta AEP [%]	0.34	0.11	0.03	0	-0.02	-0.04	-0.23	-0.63	-1.20	-1.89	
P400 delta AEP [%]	-0.38	-0.71	-0.77	-0.82	-0.86	-0.89	-1.10	-1.59	-2.26	-3.12	
P40 delta AEP [%]	-0.96	-1.33	-1.41	-1.46	-1.49	-1.51	-1.71	-2.14	-2.74	-3.50	

sandpaper, relative to a Clean blade. Moreover, once a blade is rough, its impact on AEP relative to the Clean blade profile is significant.

Table 2 presents turbulence intensities impact on AEP. As turbulence intensity increases, the AEP decreases for all blade profiles. The impact is more significant for the rougher blade profiles, with the P40 sandpaper profile already showing a high decrease in AEP at 2.14% for 15% turbulence intensity.

3.3.2 AEP for Three Fictitious Sites with Varying Wind Speeds

285

The investigation extended AEP calculations to three hypothetical sites, each characterised by average wind speeds of 6, 8 and 10 m/s. The subsequent AEP variations for each blade profile, relative to the Clean blade profile's 6% *TI* power curve, are presented in Table 3 for an average wind speed of 6 m/s, Table 4 for an average wind speed of 8 m/s and Table 5 for an average wind speed of 10 m/s. Three different climates are investigated:

- 6 m/s average wind speed: k=2, A=6.8 m/s (Table 3)
- 8 m/s average wind speed: k=2, A=9 8 m/s (Table 4)
- -10 m/s average wind speed: k=2, A=11.3 m/s (Table 5)

From these results it may be concluded that the impact of turbulence intensity on AEP is more pronounced at lower average wind speeds. This observation is evidenced by the more substantial AEP reductions at lower TI levels for the P400 and P40 blade profiles, as well as the higher AEP decrease at higher TI levels for the Clean blade profile, at lower average wind speeds.





Table 3. AEP variation due to Turbulence Intensity relative to a Clean blade with 6% TI power curve - Vave=6 m/s

Blade profile	TI [%]										
	0	4	5.5	6	6.5	7	10	15	20	25	
Clean delta AEP [%]	0.16	-0.04	-0.20	0	0.02	0.05	0.25	0.86	1.77	3.01	
P400 delta AEP [%]	-1.20	-1.49	-1.65	-1.47	-1.46	-1.44	-1.28	-0.76	0.05	1.08	
P40 delta AEP [%]	-2.51	-2.84	-3.02	-2.83	-2.82	-2.79	-2.60	-2	-1.08	0.07	

Table 4. AEP variation due to Turbulence Intensity relative to a Clean blade with 6% TI power curve - V_{ave} =8 m/s

Blade profile	TI [%]									
	0	4	5.5	6	6.5	7	10	15	20	25
Clean delta AEP [%]	0.32	0.08	-0.02	0	-0.01	-0.03	-0.13	-0.31	-0.52	-0.72
P400 delta AEP [%]	-0.51	-0.85	-0.94	-0.94	-0.97	-1	-1.13	-1.40	-1.72	-2.10
P40 delta AEP [%]	-1.39	-1.78	-1.89	-1.88	-1.91	-1.92	-2.03	-2.24	-2.46	-2.73

Simultaneously it is obvious, that the impact of blade erosion on AEP is more significant for lower average wind speeds. 295 This is evident from the larger AEP decrease due to blade erosion for the P400 and P40 blade profiles, as well as the higher AEP decrease for the Clean blade profile, at higher average wind speeds.

The large loss due to erosion for $v_{ave}=6$ m/s is due to the fact that much of the energy is produced below rated power and that is where erosion has an impact. Erosion has almost no impact at rated power. Smaller losses due to erosion are seen for $v_{ave}=10$ m/s. The higher the TI, the more gain when most of the production is made at low wind speeds because the power increases below 9.5 m/s due to the averaging. The higher the TI, the more loss when most of the production is made at high wind speeds because the power decreases above 9.5 m/s.

Also a trend emerges, suggesting that the comparative effects of blade erosion and turbulence intensity on AEP vary contingent upon the average wind speed and the specific blade profile under consideration. For instance, at an average wind speed of 6 m/s, blade erosion has a larger impact on AEP than turbulence intensity for all blade profiles. At higher wind speeds, turbulence intensity has a more pronounced impact on AEP, particularly evident in the context of the P40 blade profile.

305

300

Table 5. AEP variation due to Turbulence Intensity relative to a Clean blade with 6% TI power curve - V_{ave} =10 m/s

					TI	[0%]				
	11 [%]									
Blade profile	0	4	5.5	6	6.5	7	10	15	20	25
Clean delta AEP [%]	0.30	0.10	0.03	0	-0.02	-0.04	-0.21	-0.61	-1.21	-1.96
P400 delta AEP [%]	-0.67	-0.96	-1.02	-1.06	-1.10	-1.13	-1.32	-1.80	-2.49	-3.40
P40 delta AEP [%]	-0.84	-1.18	-1.25	-1.29	-1.32	-1.34	-1.52	-1.95	-2.58	-3.41





3.3.3 Summary of the effect of TI and erosion on AEP

The investigation into Annual Energy Production encompassed both:

- A specific actual wind climate
- Three artificial wind climates
- 310 For the first AEP calculation the AEP variation for the three blade profiles pertaining to a specific climate with a mean wind speed of 9.49 m/s revealed that even minimal simulated erosion, represented by the P400 blade profile, could precipiate a notable reduction in AEP by 0.82%. As erosion progresses, the AEP decreases further to 1.46% for the coarser P40 sandpaper, relative to a Clean blade. Furthermore, the effect of a blade's roughness on AEP in comparison to the Clean blade profile is substantial.
- The second study additionally examined how three different site specific mean average wind speeds (6, 8 and 10 m/s) affected AEP for the three blade profiles. The findings indicate that at lower wind speeds, the AEP variation caused by turbulence intensity in comparison to a Clean blade profile is more important. This result underlines the importance of considering the level of turbulence intensity there is on AEP in wind farm site selection and design considerations. Notably, the findings from the hypothetical scenario with the highest wind speed at 10 m/s corresponded well to the the first AEP calculation for the
- 320 specific wind climate.

From the study it was observed that alterations in TI invariably influence AEP. Such variability introduces complexities in accurately attributing changes in AEP solely to erosion, as fluctuations in TI could equally account for observed variations.

3.4 Influence of time averaging on power curve

325

This section examines the influence of time averaging on power output. Simulations were conducted employing a clean blade profile across a spectrum of turbulence intensities. Figure 13 delineates the power as a function of wind speed for different time averaging intervals at a fixed turbulence intensity of 15%. Both the low speed region and knee of the power curve are presented in this segmented example.

To further investigate the effect of time averaging on the power curve, the percentage difference in power from the baseline Clean profile power curve 0.01 second time interval was calculated for various time intervals and turbulence intensities. Figure

330

335

influence on power change.

14 shows the results for a fixed wind speed of 7 m/s, situated in the low speed region of the power curve. The data reveal a trend of power reduction with increasing turbulence intensity, with larger time intervals resulting in greater percentage decreases in power. However, the 1 second time interval shows only a marginal effect.

Contrasting, Figure 15 shows the results for a fixed wind speed of 11 m/s, situated at the knee of the power curve. In this case, different time intervals exhibited both increasing and decreasing effects on power output, with lower time intervals of 30 and 60 seconds pulling the power curve upward, 1 second and 120 seconds having a more neutral effect and larger time intervals of 300 and 600 seconds pulling the power curve downward. Increasing turbulence intensity has a somewhat linear

15







Figure 13. Power as a function of wind speed for a Clean blade profile at various time averaging intervals and a turbulence intensity of 15%

In both cases the delta power ratios for longer time intervals are generally higher than those for shorter time intervals. However, the magnitude of the delta power ratios for 7 m/s wind speed appear to be larger than those for 11 m/s wind speed, indicating a potentially larger impact of time intervals on power output for lower wind speeds.



Figure 14. Percentage difference in power from the 0.01 second time Figure 15. Percentage difference in power from the 0.01 second time interval power value as a function of turbulence intensity at a fixed interval power value as a function of turbulence intensity at a fixed wind speed of 7 m/s for the Clean blade profile - low speed region of wind speed of 11 m/s for the Clean blade profile - knee region of power curve power curve





To further investigate the effect of erosion or roughness combined with time averaging, the percentage difference of a clean and then P40 roughness blade profile in power from the base case of a clean profile power curve with 0.01 second time interval and, in this case at 0% turbulence intensity was calculated for different time intervals and turbulence intensities. This is to provide a comparison between the effects of time interval averaging and blade surface roughness.

345

350

Figure 16 and Figure 18 show the results for a fixed wind speed of 7 m/s for the clean and P40 roughness blades, respectively. In contrast, Figure 17 and Figure 19 show the results for a fixed wind speed of 11 m/s for the clean and P40 roughness blades, respectively.

To effectively, correct for the influence of time averaging on power output, it is necessary to consider the time interval employed for data analysis. This requires careful selection of the time interval, since overly short intervals can result in noisy data while overly long intervals can mask important behaviour of the turbine.

Additionally, one may conclude that the effect of time averaging on power output is not uniform and varies depending on the wind speed and turbulence intensity, hence precluding the application of a universal correction to the data. Moreover, it is important to use both a turbine simulation model and meteorological mast data to correct for influence of time interval averaging.

355 3.4.1 Summary of the influence of Time Averaging on Power Curve

In light of the investigation into time averaging effects on power analysis, it becomes evident that the choice of time interval for data analysis can significantly impact the resulting power curve. This accentuates the importance of careful time interval selection for data analysis. The simulation outcomes revealed that larger time intervals, in general, precipitate in a more pronounced decrease in power output with increasing turbulence intensity. The impact of time averaging on power output, however, is not

- 360 always clear-cut and is contingent upon the wind turbine's operational conditions. At lower wind speeds, situated in the low speed region of the power curve, larger time intervals result in a more pronounced decrease in power output. Conversely, at higher wind speeds, situated at the knee of the power curve, lower timer intervals can result in an increase in power output, while larger time intervals can lead to a decrease in power output. Notably, a 1-second time interval maintained a neutral effect on power across all turbulence intensities.
- 365 When comparing the P40 roughness blade to a clean blade at 0% turbulence intensity, the findings demonstrated that the impact of blade surface roughness on power output is less pronounced than the effect of time averaging, with roughness causing a lower reduction in power output. However, the confluence of time averaging and blade roughness can have a significant impact on the power curve. It is vital to consider both factors carefully while analysing power output data.

Time interval averaging impacts the ability to identify or detect changes in wind turbine performance due to subtle modifica-370 tions of aerodynamic efficiency, potentially arising from phenomena such as blade erosion. This is because changes that occur on a shorted time scale can be harder to detect because time interval averaging can smooth out short-term fluctuations in the turbine's response to changes in wind speed and other variables.

To mitigate this issue, consider selecting an averaging time period that is shorter and better suited to capturing transient variations in turbine performance. While shorter time intervals may produce noisier data that is more challenging to analyse, this







Figure 16. Percentage difference in power from the 0.01 second time Figure 17. Percentage difference in power from the 0.01 second time interval power value as a function of turbulence intensity at a fixed interval power value as a function of turbulence intensity at a fixed wind speed of 7 m/s for the Clean blade profile compared to the Clean wind speed of 11 m/s for the Clean blade profile compared to the profile at 0% turbulence intensity Clean profile at 0% turbulence intensity



Figure 18. Percentage difference in power from the 0.01 second time **Figure 19.** Percentage difference in power from the 0.01 second time interval power value as a function of turbulence intensity at a fixed interval power value as a function of turbulence intensity at a fixed wind speed of 7 m/s for the P40 roughness blade profile compared to wind speed of 11 m/s for the P40 roughness blade profile compared to the Clean blade profile at 0% turbulence intensity to the Clean blade profile at 0% turbulence intensity





- 375 trade-off between the degree of analysis detail and data noise is often necessary. The study discerned minimal information loss with 1 second values. In general, shorter time averaging periods led to smaller losses. Since this study is based on simulations there is a good control of the signals. Nonetheless, applying short time averaging periods to measured data presents additional challenges due to the greater uncertainties inherent in real-world measurements.
- It may be argued that the standard deviation of average values can compensate for the effect of time interval averaging. 380 Indeed, the standard deviation can provide a partial offset. By calculating the standard deviation of the averaged data, it is possible to estimate the degree of short-term variability that has been lost due to the averaging process. The impacts of time interval averaging, however, are not entirely offset by the average values' standard deviation. A significant portion of the sensor response may be lost if the time interval used for averaging is much greater than the typical response time of the sensors and this loss cannot be compensated for by calculating the standard deviation of the averaged data.
- 385 Therefore, to ensure accurate and meaningful analysis of wind turbine performance, it is still important to choose an appropriate time interval for averaging sensor data. Even though the standard deviation of the average values can partially compensate for the effect of time interval averaging on the accuracy of the data.

3.5 Influence of other factors

Although the current investigation demonstrates the significant impact of blade surface roughness, turbulence intensity and time interval averaging on wind turbine power output, it is imperative to acknowledge that additional variables also play crucial roles. Among these, atmospheric conditions including shear, that has briefly been demonstrated in this paper to significantly influence the performance, but also temperature, veer, climate change as well as mechanical factors such as, component wear, yaw misalignment, pitch system reliability, ageing, operations and maintenance events and increased friction in the drive train, significantly influence turbine performance. Moreover, reliable measures of wind speed, necessitating regular calibration of wind speed sensor based on turbine output or updates in turbine control software, along with the effects wind speed binning, are pivotal in evaluating turbine performance accurately. Furthermore, the control of the wind turbine such as generator speed

and pitch as a function of wind speed or power, potentially influence the outcomes of such analyses.

However, these aspects were outside the purview of the present study, these factors warrant further exploration to achieve a comprehensively understanding of their individual and combined impacts on turbine power output. Future research should prioritise a holistic approach, systematically investigating the complex interplay between these factors and their implications

for the long-term efficiency and sustainability of wind turbines.

4 Conclusion

400

This study delves into the power and energy losses of multi-megawatt wind turbines caused by erosion-induced degradation of aerofoil characteristics. A key innovation of this work is the use of time-dependent aeroelastic computations to assess the impacts of both erosion and turbulence intensity, providing a more dynamic analysis compared to traditional steady-state approaches.



410

415

425



The investigation reveals that both turbulence intensity and blade roughness have a significant effect on wind turbine performance. Turbulence intensity, in particular, has a significant impact on power output, especially in the partial load region, while the impact of blade erosion was less significant. Blade roughness can significantly affect power production, particularly at wind speeds between 9 and 13 m/s, i.e. in the transition between the partial load region and rated power, as the delta power analysis

demonstrated. The coefficient of power study brought to light the critically of considering both blade roughness and turbulence intensity when assessing wind turbine performance and that lower turbulence intensities are comparable to turbulence intensity.

Additionally, the study's findings on AEP underscore the variable impacts of erosion and turbulence intensity across different wind climates. In climates characterised by lower average wind speeds, the effects of erosion and turbulence intensity on AEP are accentuated compared to those in wind climates with a higher average wind speed.

Moreover, the exploration of time averaging's influence on power output through simulations across different turbulence intensities and time intervals provides additional insights. The findings indicated that larger time averaging intervals result in greater percentage decreases in power and that rising turbulence intensity show a decrease in power at 7 m/s wind speed. At the 'knee' of the power curve, at 11 m/s, smaller time intervals of 30 and 60 seconds pulled up the power curve, where shorter time

420 intervals of 1 second and 120 seconds having a more neutral effect. Longer time intervals of 300 and 600 seconds pulled down the power curve. Thus, at 11 m/s, different time intervals can have both increasing and decreasing effects on power output.

This research contributes valuable insights into the multifaceted effects of turbulence intensity, blade roughness and time averaging on wind turbine performance. Crucially, it highlights how data analysis techniques can either mask or reveal the subtle effects of erosion and turbulence. Emphasising the necessity for a holistic approach in assessing turbine efficiency, taking into account various factors that influence power output and energy production. Furthermore, the study demonstrates

that the choice of time averaging intervals can significantly distort the perceived performance of wind turbines, particularly in the detection of subtle changes in aerodynamic efficiency due to factors like blade surface conditions.

Future research should broaden the scope to investigate how leading edge roughness, turbulence intensity, wind shear, yaw misalignment and other factors such as operations and maintenance events collectively influence annual energy production. This research should focus on the long-term implications of these combined effects and lead to the development of optimised

430 This research should focus on the long-term implications of these combined effects and lead to the development of optimised maintenance and operational strategies. While seemingly small, the hidden losses due to erosion can add up to a significant drain on renewable energy resources. Accurate quantification of these losses is essential for evidence-based optimisation of wind turbine operations.

Author contributions. Tahir H. Malik was the primary researcher, responsible for the conception of the study, all experimental work, data
 collection and analysis and the drafting of the manuscript. Christian Bak, as the PhD supervisor, provided oversight, theoretical support and guidance in refining the research methodology and helped shape the direction of the work.

Competing interests. The author Tahir H. Malik has received his PhD funding and is by employed by Vattenfall.





Acknowledgements. We gratefully acknowledge the support of Vattenfall, particularly for financing this study and providing access to vital wind turbine resources. We also thank the AI language model by OpenAI (2023) for its assistance in refining the manuscript.





References 440

- Abolude, A. T. and Zhou, W.: Assessment and Performance Evaluation of a Wind Turbine Power Output, Energies, 11, https://doi.org/10.3390/en11081992, 2018.
- Badihi, H., Zhang, Y., Jiang, B., Pillay, P., and Rakheja, S.: A comprehensive review on signal-based and model-based condition monitoring of wind turbines: Fault diagnosis and lifetime prognosis, Proceedings of the IEEE, 110, 754-806, 2022.
- Bak, C., Skrzypiński, W., Gaunaa, M., Villanueva, H., Brønnum, N. F., and Kruse, E. K.: Full scale wind turbine test of vortex generators 445 mounted on the entire blade, in: Journal of Physics: Conference Series, vol. 753, p. 022001, IOP Publishing, https://doi.org/10.1088/1742-6596/753/2/022001, 2016.
 - Bak, C., Forsting, A. M., and Sorensen, N. N.: The influence of leading edge roughness, rotor control and wind climate on the loss in energy production, in: Journal of Physics: Conference Series, vol. 1618, p. 052050, IOP Publishing, https://doi.org/10.1088/1742-
- 450
- 6596/1618/5/052050, 2020.
 - Bak, C., Olsen, A., Forsting, A., Bjerge, M., Handberg, M., and Shkalov, H.: Wind tunnel test of airfoil with erosion and leading edge protection, Journal of Physics: Conference Series, 2507, 2023.
 - Barthelmie, R. J. and Jensen, L.: Evaluation of wind farm efficiency and wind turbine wakes at the Nysted offshore wind farm, Wind Energy, 13, 573–586, 2010.
- 455 Ding, Y., Barber, S., and Hammer, F.: Data-Driven wind turbine performance assessment and quantification using SCADA data and field measurements, Frontiers in Energy Research, 10, 1050 342, 2022.
 - Do, M.-T. and Berthaut-Gerentes, J.: Optimal time step of SCADA data for the power curve of wind turbine, Journal of Physics: Conference Series, 1102, 012 025, https://doi.org/10.1088/1742-6596/1102/1/012025, 2018.

Ehrmann, R. S., Wilcox, B., White, E. B., and Maniaci, D. C.: Effect of surface roughness on wind turbine performance, Tech. rep., Sandia 460 National Lab.(SNL-NM), Albuquerque, NM (United States), 2017.

- Elliott, D. and Infield, D.: An assessment of the impact of reduced averaging time on small wind turbine power curves, energy capture predictions and turbulence intensity measurements, Wind Energy, 17, 337-342, https://doi.org/https://doi.org/10.1002/we.1579. EMD International A/S: WindPRO Software for Wind Energy Analysis, https://www.emd.dk/windpro/, accessed: 2023-06-01, 2023.
- Gaudern, N.: A practical study of the aerodynamic impact of wind turbine blade leading edge erosion, in: Journal of Physics: Conference 465 Series, vol. 524, p. 012031, IOP Publishing, 2014.
 - Gonzalez, E., Stephen, B., Infield, D., and Melero, J. J.: On the use of high-frequency SCADA data for improved wind turbine performance monitoring, Journal of Physics: Conference Series, 926, 012 009, https://doi.org/10.1088/1742-6596/926/1/012009, 2017.
 - Gonzalez, E., Stephen, B., Infield, D., and Melero, J. J.: Using high-frequency SCADA data for wind turbine performance monitoring: A sensitivity study, Renewable energy, 131, 841-853, 2019.
- 470 Han, W., Kim, J., and Kim, B.: Effects of contamination and erosion at the leading edge of blade tip airfoils on the annual energy production of wind turbines, Renewable energy, 115, 817-823, 2018.

Hansen, M. O.: Aerodynamics of wind turbines. Earthscan, James & James, 8, 14, 2008.

- International Electrotechnical Commission (IEC): Wind turbines Part 1: Wind turbine generators General requirements, Tech. rep., Geneva, Switzerland, 2019.
- 475 Kim, D.-Y., Kim, Y.-H., and Kim, B.-S.: Changes in wind turbine power characteristics and annual energy production due to atmospheric stability, turbulence intensity, and wind shear, Energy, 214, 119 051, https://doi.org/https://doi.org/10.1016/j.energy.2020.119051, 2021.





Krog Kruse, E., Bak, C., and Olsen, A. S.: Wind tunnel experiments on a NACA 633-418 airfoil with different types of leading edge roughness, Wind Energy, 24, 1263–1274, 2021.

Kruse, E.: A Method for Quantifying Wind Turbine Leading Edge Roughness and its Influence on Energy Production: LER2AEP, Phd, DTU

480 Wind Energy, Roskilde, Denmark, (DTU Wind Energy PhD), 2019.

- Larsen, T. J. and Hansen, A. M.: How 2 HAWC2, the user's manual, Risø National Laboratory, 2007.
- Maniaci, D., White, E., Wilcox, B., Langel, C., van Dam, C., and Paquette, J.: Experimental Measurement and CFD Model Development of Thick Wind Turbine Airfoils with Leading Edge Erosion, in: Journal of Physics: Conference Series, vol. 753, p. 022013, IOP Publishing, https://doi.org/10.1088/1742-6596/1618/5/052050, 2016.
- Mann, J.: The spatial structure of neutral atmospheric surface-layer turbulence, Journal of fluid mechanics, 273, 141–168, 1994.
 OpenAI: ChatGPT: Optimizing Language Models for Dialogue, https://openai.com/chatgpt/, 2023.

Saint-Drenan, Y.-M., Besseau, R., Jansen, M., Staffell, I., Troccoli, A., Dubus, L., Schmidt, J., Gruber, K., Simões, S. G., and Heier, S.: A parametric model for wind turbine power curves incorporating environmental conditions, Renewable Energy, 157, 754–768, 2020.

- St. Martin, C. M., Lundquist, J. K., Clifton, A., Poulos, G. S., and Schreck, S. J.: Wind turbine power production and annual energy production
 depend on atmospheric stability and turbulence, Wind Energy Science, 1, 221–236, https://doi.org/10.5194/wes-1-221-2016, 2016.
 - Wagner, R., Courtney, M., Larsen, T. J., and Paulsen, U. S.: Simulation of shear and turbulence impact on wind turbine performance, Danmarks Tekniske Universitet, Risø Nationallaboratoriet for Bæredygtig Energi, 2010.
 - Wharton, S. and Lundquist, J. K.: Atmospheric stability affects wind turbine power collection, Environmental Research Letters, 7, 014 005, https://doi.org/10.1088/1748-9326/7/1/014005, 2012.