



Wake steering under inflow wind direction uncertainty: an LES study

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Abstract.

Wake steering through static yaw control is a promising wind farm flow control strategy, however full scale implementation in real wind farms is hampered by uncertainties not typically present in a simulation environment. The most notable of these are bias and variability in inflow wind direction - which are both inherent in the atmosphere and introduced through imperfect measurements. To investigate the impact of these uncertainties, LES is conducted on a row of four turbines in a conventionally neutral boundary layer, using three yaw configurations (an unyawed baseline, the leading turbine yawed and the first three turbines yawed) under different inflow wind directions $\in [-5, 8]^\circ$. The impact of the applied yaw strategy and mean wind direction offset is first studied, considering the asymmetry introduced by veer, mean wake shape, changes in local inflow angle and individual turbine power and loads. Considering mean wind farm power output, the inflow wind direction standard deviation in the current study ($\sigma_{WD} = 2.3^\circ$) results in a beneficial window for wake steering of $8.5^\circ (\in [-1.5, 7.0]^\circ)$ with peak total power gains of 23% and 7.5% for the two yaw strategies, respectively. Extrapolating to an uncertainty of $\sigma_{WD} = 4.5^\circ$ using a Gaussian convolution reduces the beneficial ranges to 8° and 6.5° respectively, with peak gains of 7.5% and 2%. While exact numbers depend on turbine spacing, the substantial decrease in peak power and narrow range of power gains signify that wake steering is highly sensitive to wind direction uncertainty and small biases in mean inflow wind direction. Therefore, accurate measurement of these quantities and inclusion of them in prediction models is essential.

1 Introduction

Wake effects - namely lower mean velocity and higher turbulence intensity - cause power losses and fatigue increases in wind farms, when wind turbines operate in the wakes of those upstream. Wind farm flow control (WFFC) involves altering the operation of individual turbines in order to reduce wake-induced losses in a wind farm, and hence improve overall metrics such as total power production (Meyers et al., 2022). Static yaw control is a WFFC technique that consists of applying a constant yaw misalignment angle to a turbine nacelle relative to the incoming flow. This produces the effect of wake steering, in which the asymmetry in the rotor loads imparts forces on the flow which lead to deflection of the mean wake centreline in the crosswind direction. Therefore, in aligned or nearly-aligned flow scenarios with significant wake effects, wake steering could be applied to redirect the wakes of upstream turbines and hence increase the mean inflow velocity and power output of



25 downstream turbines (Jiménez et al., 2010). However, static yaw results in a power output and fatigue penalty for the turbines
it is applied to (Hulsman et al., 2020; Debusscher et al., 2022), and hence identifying exactly when, where and how to utilise
wake steering WFFC is in reality non-trivial.

This is in particular due to the complex, 3-dimensional and dynamic nature of wind turbine wake behaviour and wind farm
flows. Wake recovery - and hence the effectiveness of applying wake steering - is significantly impacted by ambient turbulence
30 intensity (Wu and Porté-Agel, 2012; Churchfield et al., 2012), veer (van der Laan and Sørensen, 2017) and turbulence integral
length scale (Du et al., 2021; Hodgson et al., 2023a), which are driven by atmospheric stability. Wind farm flows also include
interactions with the size and layout of the wind farm (Cortina et al., 2016; VerHulst and Meneveau, 2014; Andersen et al.,
2017), and with the atmospheric boundary layer (Allaerts and Meyers, 2017; Abkar and Porté-Agel, 2015). The asymmetry
introduced by yawing further complicates wake physics, by introducing a counter-rotating vortex pair which deflects the wake
35 and modifies the mean wake shape to a curled (or ‘kidney’) shape (Mikkelsen, 2004; Howland et al., 2016). This leads to
further interactions with wake rotation and veer which lead to anticlockwise yaw (as seen from above) being more effective in
the northern hemisphere (Fleming et al., 2018; Archer and Vasel-Be-Hagh, 2019; Narasimhan et al., 2022).

Even once appropriate conditions for applying static yaw control have been identified in a theoretical, quasi-static sense - a
wind farm with relatively close spacing, aligned mean inflow wind direction, below rated velocity and low ambient turbulence
40 intensity - significant challenges remain when implementing yaw control in a practical context. Sources of uncertainty exist
in both the application of the intended control strategy and the measurement of inflow conditions which the strategy relies
on. Concerning the former, imperfect response to a control input can occur due to time lag and low speed of yaw actuation,
and large deadband zones in individual turbine yaw controllers leading to imprecise tracking of the mean inflow angle. Yaw
position uncertainty has been reported both as a Laplacian distribution with scale factor $\nu = 6.16^\circ$ (Quick et al., 2020), and
45 Gaussian-distributed with standard deviation 1.75° (Simley et al., 2020). Regarding the latter, measuring the inflow conditions
e.g. using nacelle anemometers and wind vanes can introduce bias and uncertainty due to sensor drift and error, which are
exacerbated in yawed conditions due to calibration issues and flow distortion around the nacelle. Additionally, inflow conditions
have an inherent uncertainty due to turbulence and inhomogeneity of background flow conditions over the extent of a wind
farm. Reported values of wind direction uncertainty (the short-term variability within 1-10 min periods) typically range from
50 $2.5^\circ - 6^\circ$: 2.7° from 10-minute sonic anemometer data from an offshore wind farm (Gaumond et al., 2014), 3.6° predicted
from 10-min turbine sensor data (Mittelmeier et al., 2017), 5.15° and 5.2° using 1-min averages for two different onshore
locations (both a combination of yaw position and wind direction uncertainty), with much larger values for wind speeds of
less than 8ms^{-1} (Simley et al., 2020, 2021). Spatial variability in mean values can also be significant; the difference in wind
direction (without wind farms present) was found to have quartiles of -1.5° and 1.3° on intra-cluster scale ($\sim 10\text{km}$), and
55 -3.8° and 5.0° on inter-cluster scale ($\sim 50\text{km}$) using New Europe Wind Atlas (NEWA) data in Von Brandis et al. (2023).

The range of inflow wind directions over which yaw control is predicted to be beneficial varies between setups, depending
on turbine spacing and the flow model used in prediction. In field experiments, yaw predictions are typically made using
engineering models, such as implemented in FLORIS (Gebraad et al., 2016) or PyWake (Mads M. Pedersen and Réthoré, 2023).
Typical ranges over which yaw is applied are $\sim [0, 25]^\circ$ if only one yaw direction is considered (Fleming et al. (2019, 2020)) or



60 $\sim [-20, 20]^\circ$ for both directions (Doekemeijer et al. (2021)), with large yaw angles (e.g. $> 15^\circ$) occurring in a smaller range
($\sim [0, 10]^\circ$ or $\sim [-10, 10]^\circ$). When attempting to evaluate the impact of the applied strategy, results are binned by wind speed
and direction and the inactive and active control periods are compared within each bin. In order to ensure enough data per bin,
and not to over-resolve relative to measurement uncertainties, wind direction bin widths are typically $3 - 5^\circ$ (Göçmen et al.,
2022; Fleming et al., 2020; Doekemeijer et al., 2021). This is relatively large in comparison to the predicted beneficial wind
65 direction window for wake steering. Additionally, optimal yaw setpoint predictions often display a discontinuous change in
yaw misalignment with wind direction (e.g. through a change in sign) around fully aligned conditions, as the models predict
a ‘breaking point’ where it is optimal to yaw the turbine in the opposite direction (Rott et al., 2018). This leads to a very high
sensitivity in the desired yaw position at exactly the area where potential gains (and potential losses if incorrect control is
applied) are highest.

70 Rott et al. (2018) attempts to address both the issues related to discontinuities in yaw setpoint and wind direction uncertainty
by proposing applying a Gaussian convolution to the predicted setpoints from engineering models, which both reduces the
high gradients around fully aligned conditions and the magnitude of predicted yaw angles. Simley et al. (2020) used a similar
approach in reverse to achieve a better fit with experimental data by proposing that the achieved yaw offsets were a convolution
of the Gaussian yaw error distribution and the intended yaw setpoints. Kanev (2020) suggests a hysteresis-based approach to
75 reduce the turbine yaw duty due to sign changes in optimal angle. In Quick et al. (2020), the impact of five sources of uncertainty
on yaw optimisations were studied; yaw position, wind direction, wind speed, turbulence intensity and shear, with the former
two found to be the most impactful. The largest overall impact was that of wind direction uncertainty, with larger values leading
to a greater spread in the possible wake area, therefore increasing baseline (unyawed) power production and decreasing the
optimal yaw setpoint. However, assessing uncertainties only using engineering wake models has some drawbacks. Engineering
80 models generally only include the impact of turbulence implicitly through wake expansion coefficients (Peña et al., 2016), and
so do not capture the effect of wake dynamics such as far-wake meandering (Larsen et al., 2008; Medici and Alfredsson, 2006).
Many models do not include the curled mean shape of a yawed wake, and can also struggle to correctly capture wake deflection
(Steiner et al., 2025). Additionally, the asymmetry between effectiveness of anticlockwise and clockwise yaw angles, and the
interaction of the wake with veer, are not modelled. All of these factors may affect how wind direction uncertainty is predicted
85 to impact the wind farm flow and total power output.

Therefore, this work aims to address the issue of wake steering under inflow wind direction uncertainty using Large-eddy
simulations (LES). By utilising a conventionally neutral boundary layer (CNBL) inflow, and an aero-servo-elastic coupled
actuator disc for turbine modelling, the wakes, wind farm flow, power and loads can be studied while including the effect of
dynamic wake behaviour and turbulent inflow, and interaction with shear and veer. However, while LES allows atmospheric
90 boundary layers to be used as inflow, these do not include the impact of meso-scale variations and instead typically use a
constant geostrophic wind to drive the flow, resulting in less variability in inflow velocity and direction than in field experiments.
Hence, a number of inflow wind directions are simulated in order to study both the impact of bias (e.g. an error between the
assumed and actual mean wind direction) and uncertainty (e.g. short-term variability) in inflow wind direction. Rotating the
wind farm coordinates means that different wind directions can be simulated using an identical inflow, and hence the effect



of the incoming wind direction can be isolated. A row of four turbines is simulated with three different yaw configurations: a baseline with no yaw; the leading turbine yawed anticlockwise by 20° ; and the first three turbines yawed anticlockwise by 20° . Six different inflow wind directions are simulated: $[-5, -3, 0, 3, 5, 8]^\circ$. First, the flow is studied: wake deflection, wake shape, local inflow angle, and their development through the turbine row. Then, the individual turbine power and loads are addressed, and finally the total wind farm power output and impact of wind direction bias and uncertainty are examined.

2 Methodology

2.1 Flow Solver

All simulations are conducted using EllipSys3D, a general purpose multi-block Navier-Stokes solver developed at DTU (Sørensen, 1995; Michelsen, 1992, 1994). Ellipsys3D solves the incompressible governing equations with a finite volume method in general curvilinear coordinates using a collocated grid. The potential temperature transport equation is also solved, as a conventionally neutral boundary layer (CNBL) is utilised as inflow and hence temperature effects are included in simulations. An extended SIMPLEC algorithm solves the pressure correction equation (Shen et al., 2003; Kobayashi and Pereira, 1991) with Rhie/Chow interpolation, and time advancement is performed with a second-order accurate three-level implicit method including sub-iterations in each time step. A fourth-order central differencing scheme discretises the convective terms, with a fourth-order dissipation term to reduce numerical instabilities (Wit and van Rhee, 2013). Turbulence modelling is achieved using Large Eddy Simulations (LES) with the AMD subgrid scale model (Abkar et al., 2016). Log law is applied at the lowest grid cell to calculate the instantaneous shear stress.

2.2 Wind Turbine Modelling

The IEA22MW reference wind turbine is used in this work, which has a diameter of $D = 284\text{m}$ and a rated power of 22MW (Zahle et al., 2024). Wind turbines are modelled in LES using the actuator disc (AD) method (Mikkelsen, 2004), which is coupled to the aero-servo-elastic solver HAWC2 (Larsen and Hansen, 2007) through the open-source python coupling framework Dynamiks (Steiner et al., 2025). Dynamiks extracts the velocity components along the positions of the three rotating blades from EllipSys3D and passes them to HAWC2, which calculates loads and deflections using a Blade-Element Momentum (BEM) approach based on tabulated aerofoil data. HAWC2 has a multi-body formulation based on Timoshenko beam elements and is able to account for non-linear effects of large deflections. The calculated loads and deflections of each blade are transferred back to EllipSys3D and used to set the position and magnitude of the body forces which make up the actuator disc. These AD body forces are applied to the computational grid in three overlapping 240° sections, in which the forcing decreases linearly from a maximum at the blade location to zero at the neighbouring blades. A 1-dimensional Gaussian smearing is also applied in the streamwise direction. This AD formulation, built from three overlapping sectors each representing a single blade, allows non-uniform loading to be captured. The two-way nature of the coupling means that the interaction between loading, deflections and flow is represented (Hodgson et al., 2021). Additionally, HAWC2 uses the DTU Wind Energy



Controller (Hansen and Henriksen, 2013), meaning that the turbine exhibits realistic changes in rotational speed and pitch in response to the turbine operation and loading.

2.3 Atmospheric Boundary Layer Precursor

One inflow is used for all simulations, consisting of 5100 s of a conventionally neutral boundary layer (CNBL). The CNBL is generated using a precursor simulation in LES, using a domain size of $16640 \times 16640 \times 3000$ m (in streamwise, spanwise, vertical respectively) with periodic boundary conditions applied on lateral and streamwise faces and a grid resolution of $dx = dy = 2dz = 20$ m. Rayleigh damping is applied above a height of 2000 m (Klemp and Lilly, 1978). The precursor is initialised with the following conditions: temperature profile $dT_0/dz = 288.15$ K until 600 m height with perturbations up to 100 m height to encourage breakdown into turbulence, then a linear gradient of $dT_0/dz = 1$ K/km above; geostrophic wind values $U_G = 9.48 \text{ ms}^{-1}$ and $V_G = -0.59 \text{ ms}^{-1}$; velocity profiles based on a log-law with a 600 m boundary layer height (Allaerts and Meyers, 2015). Conditions constant throughout the precursor are the Coriolis parameter $f_c = 1.1947 \times 10^{-4} \text{ s}^{-1}$; wall roughness $z_0 = 0.001$ m, wall temperature $T_{wall} = 288.15$ K; geostrophic wind magnitude $\sqrt{(U_G^2 + V_G^2)} = 9.5 \text{ ms}^{-1}$. A wind direction controller is also active, which alters the geostrophic wind components in order to obtain a fully aligned flow (0°) at the turbine hub height of 170 m. The precursor is spun up over a flow time of 28 hrs, over which the boundary layer and turbulence develops. Then, another 5100 s of flow time is run, over which the three velocity components and temperature are extracted over a streamwise plane spanning the entire domain in vertical and lateral extent. This data is then used as the inflow to the successor simulation containing the turbines. Figure 1 shows the horizontally- and time-averaged profiles of the CNBL over the 5100 s used as inflow to the successor simulation. The achieved inflow has below rated velocity, is fully aligned (mean wind direction of -0.05°) at hub height and has a relatively low hub height TI of 3.8%, hence representing atmospheric conditions ideal for the application of wake steering.

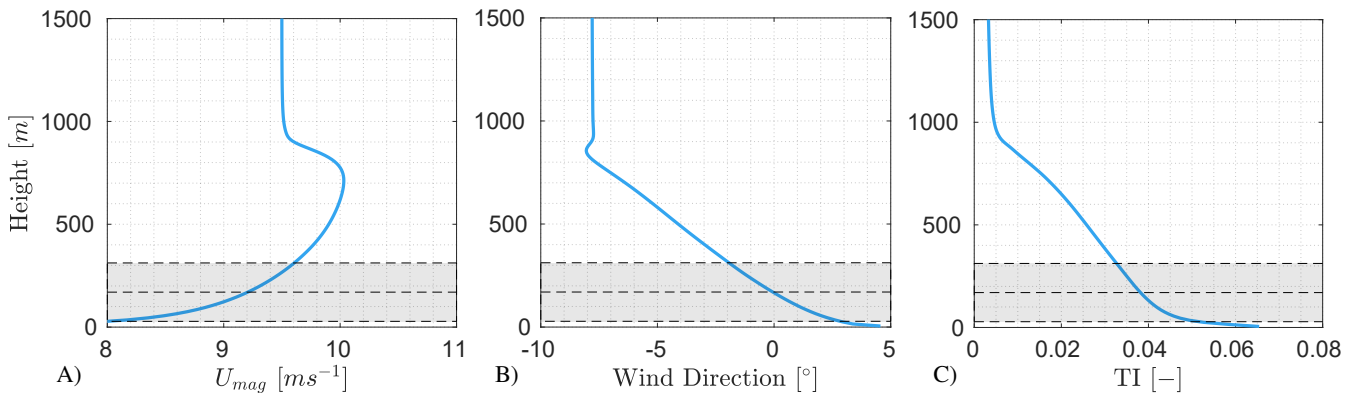


Figure 1. Horizontally- and time-averaged profiles of the CNBL precursor inflow: A) Velocity magnitude U_{mag} (ms^{-1}); B) Wind direction ($^\circ$); C) Turbulence intensity (TI) based on hub height mean velocity. Area marked in grey represents the turbine rotor extent.



2.4 Simulation Setup

All successor simulations utilise the same computational domain, which has dimensions of $13490 \times 4970 \times 3000$ m ($47.5D \times 17.5D \times 10.5D$) and a refined region extending from the inlet to 9940 m ($35D$) downstream, with lateral extent of 2840 m ($10D$) centred on the domain centreline and extending vertically from the ground to a height of 1136 m ($4D$). Inside the refined region,
150 the grid resolution is $dx = dy = dz = 32/D$, a resolution sufficient to converge both the turbine thrust coefficient and wake behaviour (Hodgson et al., 2021, 2023b). Outside of the refined region, the cell sizes are stretched to the domain boundaries. The simulated wind farm consists of a row of 4 turbines spaced $7D$ apart, with the leading turbine placed $3.5D$ from the inlet and hence the final turbine being placed $11.5D$ (1.5 times the turbine spacing) before the end of the refined region. All simulations are run for 5100 s of flow time, in which the first 1500 s are used as spin up in which the flow and wakes develop,
155 and the last 3600 s are used for analysis.

In order to examine wake steering wind farm flow control, three different yaw configurations are examined: the first a baseline case where no yaw is applied; secondly a single-turbine yaw case where the upstream turbine is yawed -20° ; and thirdly a multi-turbine yaw case where the first three turbines are yawed -20° . Note that a negative yaw direction in this context refers to the turbine rotating anticlockwise when seen from above, and hence is the direction which produces more beneficial wake
160 steering in the northern hemisphere due to the interaction between turbine yaw, wake rotation and veer (Fleming et al., 2018; Archer and Vassel-Be-Hagh, 2019). This work investigates both mean wind direction bias (a constant offset, which is what is simulated) and standard deviation (both included and extrapolated to larger values from the obtained results). As the mean wind direction is unaltered in the LES, the wind farm coordinates are rotated to achieve a change in wind direction relative to the wind turbine row. Note that the wind turbines still face directly into the incoming wind, and hence this simulates a situation
165 with no error in the individual turbine yaw controllers. Six different inflow wind directions (hence coordinate rotations of the wind farm) are studied: $[-5, -3, 0, 3, 5, 8]^\circ$. Consistent with the yaw rotation definition, a positive wind direction indicates a clockwise rotation of the incoming wind relative to a fully aligned inflow.

In order to achieve a fair comparison the available power outputs and inflow angles at each of the turbine locations (e.g. in each coordinate configuration) should be identical, so that results can be attributed to the simulated inflow wind direction rather than the turbine locations. Therefore, initial simulations were run - one set without turbines present and another with only the
170 first turbine present - to assess the dependency of inflow angle, wind speed and first turbine power output on location. Mean velocity matched to 0.1% between each turbine location in the empty domain, and power output for the first turbine changed less than 0.5% - hence this defines the minimum level of power change that can be judged as significant in the results. For the inflow angle, across all turbine locations in the empty domain the hub height values are between -0.15° and 0.15° (the
175 mean horizontally-averaged value during the last 5100s of the precursor was -0.05°). This minimal variation around 0.0° was judged as sufficient to say that the six desired wind directions ($[-5, -3, 0, 3, 5, 8]^\circ$) are achieved by the coordinate rotations.



3 Results

3.1 Wind Farm Flow

The impact of the different inflow wind directions on the wind farm flow is first qualitatively examined, by comparing the mean
 180 flows across a horizontal plane at hub height for all wind directions and all yaw configurations, shown in Figure 2.

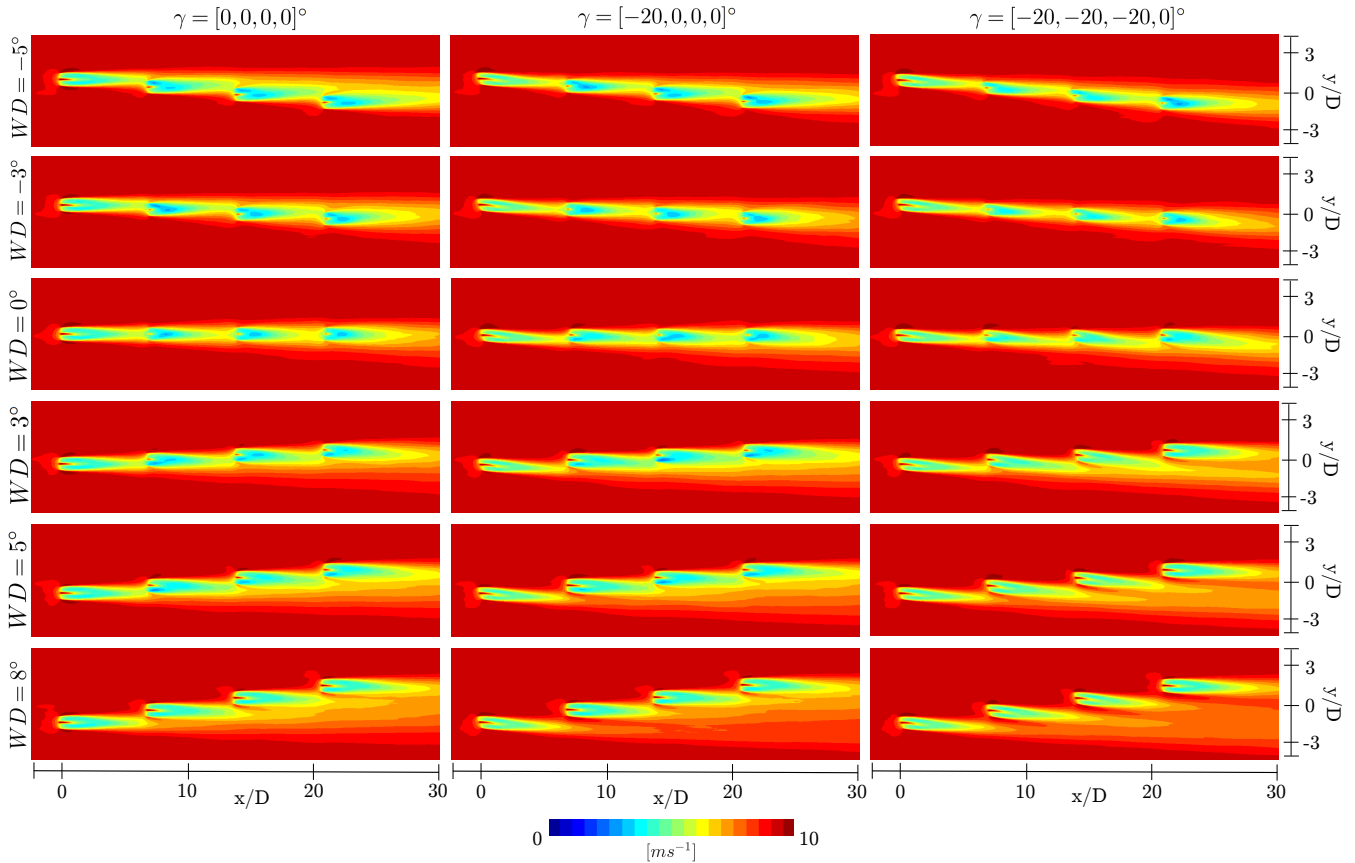


Figure 2. Contour plots using horizontal plane at turbine hub height of U_{mag} (ms^{-1}) for all wind directions, showing baseline case with no yaw (left); yawed case with first turbine yawed -20° (middle) and yawed case in which the first 3 turbines are yawed -20° (right). From top to bottom: -5° , -3° , 0° , 3° , 5° , 8° .

Figure 2 demonstrates how the coordinate rotations of the wind farm allow different inflow wind directions to be simulated. The third row, first column simulation ($WD = 0^\circ, \gamma = [0, 0, 0, 0]^\circ$) shows the baseline case in which the wind direction is fully aligned with the turbine row and no yaw is applied. There is already flow turning through the farm in this case, due to the interaction of the wakes with the inflow veer (van der Laan and Sørensen, 2017). As shown in Figure 1, the veer is $\sim 4.5^\circ$ over
 185 the rotor area and the boundary layer height is around 900 m. This veer is relatively low compared to stable times of day with lower boundary layer heights (e.g. as simulated in a diurnal cycle inflow in Hodgson et al. (2025a) or a CNBL in Ivanell et al.



(2025)) and hence even stronger effects could be present with other inflow conditions. Wind directions of $WD = [-5, -3, 3, 5]^\circ$ represent partial wake cases, where in the unyawed configuration the mean wake from each turbine impinges on the rotor area of the following. By comparing the unyawed configurations of $WD = -5^\circ$ and 5° , and -3° and 3° , the asymmetry of the wind farm flow introduced by the veer can be seen, as the negative inflow wind directions lead to greater wake impingement, due to the flow turning through the row. The largest wind direction offset $WD = 8^\circ$ shows very little wake impingement on downstream turbines in the unyawed configuration (this of course depends on the turbine spacing in addition to the angle). It is therefore likely that with this large a bias in wind direction, the yawed configurations at $WD = 8^\circ$ will give a total power loss due to the power reduction for yawed turbines. It is also apparent that the yawed configurations in cases $WD = -5^\circ$ and $WD = -3^\circ$ will result in a loss, as the applied yaw acts to steer the wakes into the downstream turbines, turning a partial wake case into a full wake.

To examine the mean wake shapes and wake deflection, Figures 3 and 4 show the mean normalised wake deficit at $0.5D$ upstream from the second turbine location (Figure 3) and the fourth turbine location (Figure 4), with mean wake centres and standard deviations marked, calculated using a centre-of-mass approach (Andersen, 2014). Only the four most relevant wind directions are shown, $WD = [-3, 0, 3, 5]^\circ$. It should be noted that Figure 3 only shows one of the two yawed configurations as the second turbine inflow is effectively identical in these cases.

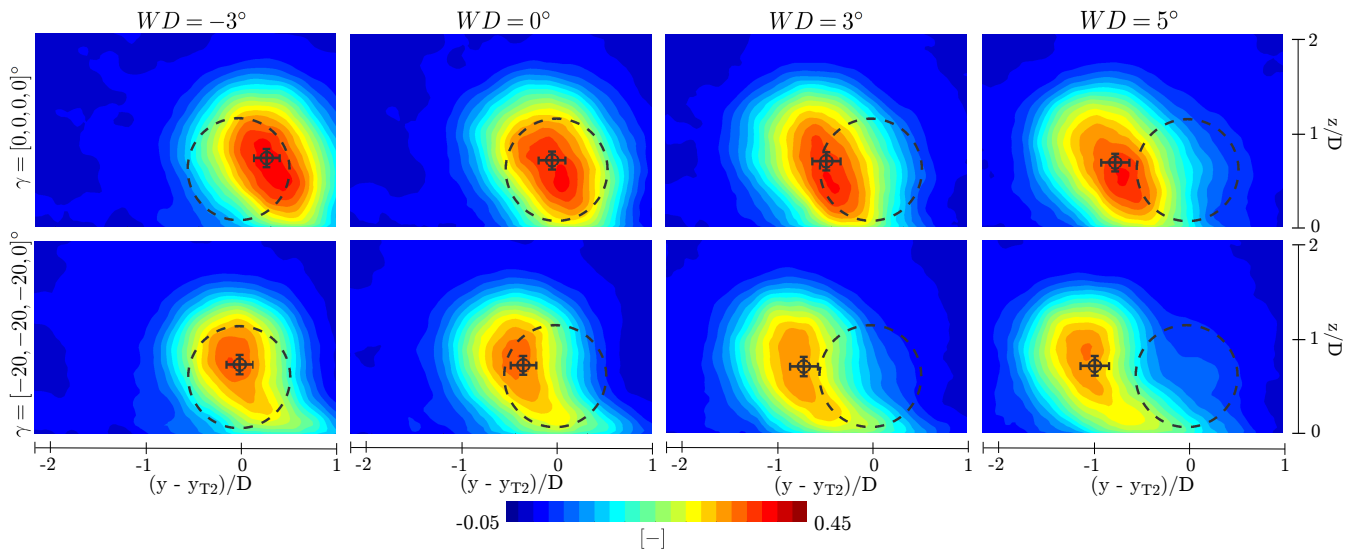


Figure 3. Contour plots using cross-stream plane at $1R$ in front of Turbine 2, showing mean normalised velocity deficit, $U(z)_{in} - U/U(z)_{in}$ velocity. Mean wake centre position and error bars showing standard deviation of wake centre in black. Dashed circle represents the rotor position and area of Turbine 2. Top row: baseline cases without yaw; bottom row: first three turbines yawed. From left to right: wind directions of $-3^\circ, 0^\circ, 3^\circ, 5^\circ$. Planes oriented as seen from behind.

The impact of both veer and yaw on the mean wake shapes can be clearly seen in the inflow to Turbine 2 (Figure 3). For the unyawed configurations (top row), a skewed mean wake deficit is visible, while the yawed configurations (bottom row) display

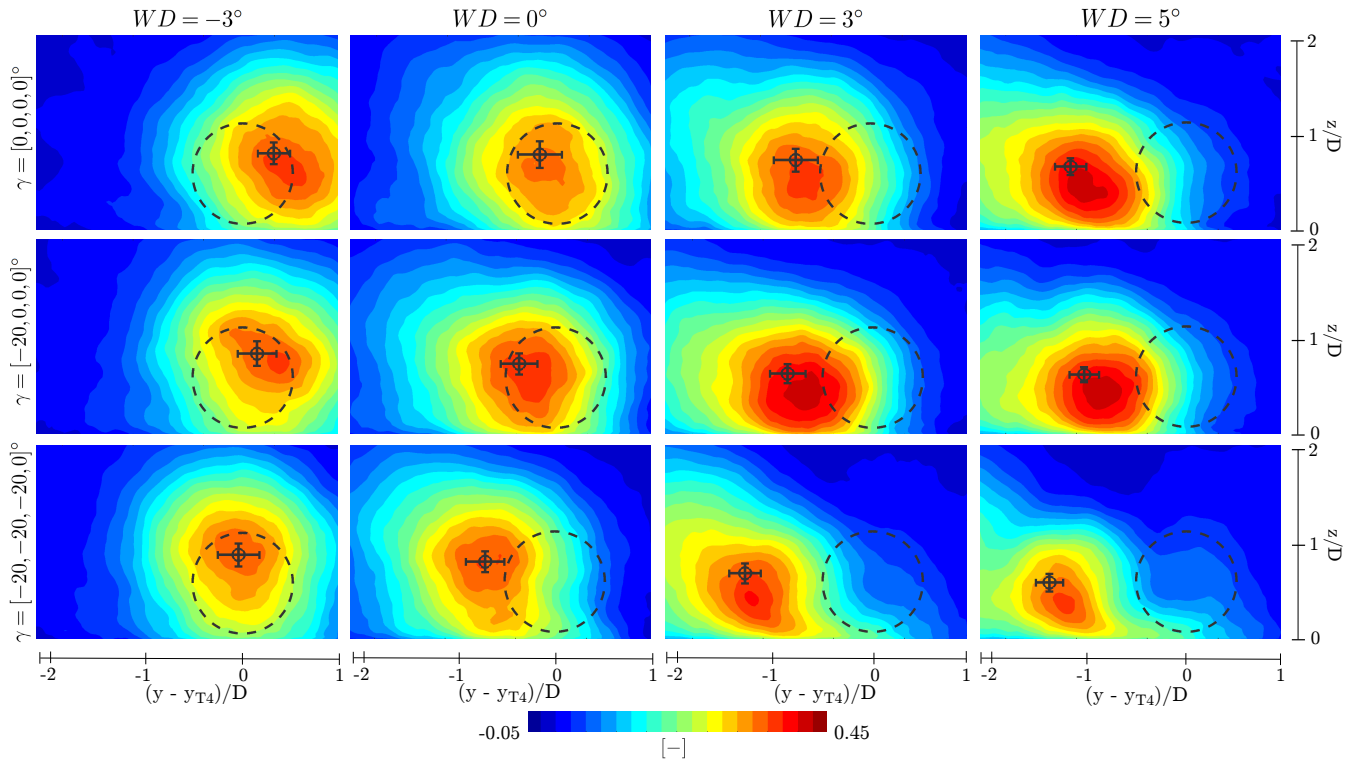


Figure 4. Contour plots using cross-stream plane at $1R$ in front of Turbine 4, showing mean normalised velocity deficit, $U(z)_{in} - U / U(z)_{in}$ velocity. Mean wake centre position and error bars showing standard deviation of wake centre in black. Dashed circle represents the rotor position and area of Turbine 4. Top row: baseline cases without yaw; middle row: first turbine yawed; bottom row: first three turbines yawed. From left to right: wind directions of -3° , 0° , 3° , 5° . Planes oriented as seen from behind.

a mean wake deficit which is both skewed and curled, as well as having a deflected mean centre position. As expected, the wake centre standard deviation due to wake meandering is larger in the lateral direction than the vertical (España et al., 2012). There is little noticeable difference between the standard deviations in the unyawed and yawed configurations, suggesting similar wake meandering for both. The yaw applied to the leading turbine deflects the wake centre by around $0.25D$ by the second turbine location in all cases.

In Figure 4 the mean inflows contain a much broader area of velocity deficit than in Figure 3, as these inflows are formed from the combined wakes of three turbines rather than one. The wake centre standard deviations are also larger than in Figure 3, as the interaction of multiple wakes leads to larger and more chaotic motions. Additionally, there is little evidence of the skewed and curled mean shapes that are present for the first wake. As a turbine wake has additional turbulence and a velocity deficit, it changes the shear and veer profiles at the inflow to downstream turbines, meaning that their wakes do not display the same strong veer interaction as the leading wake. This also demonstrates that beyond the entry region of a wind farm, it is the characteristics of the wakes and wind farm rather than the ambient conditions that can begin to dominate the flow, as seen for



turbulent spectra in Hodgson et al. (2025b) and Andersen et al. (2017). This is particularly the case for the more aligned wake cases, while for $WD = 3^\circ$ and $WD = 5^\circ$ cases the curled shape can be seen when all three turbines are yawed (the rightmost two of the bottom row in Figure 4) only because the wakes of the other turbines are already sufficiently deflected that the third turbine wake behaves closer to what is seen for freestream conditions.

220 After qualitatively analysing the mean wakes and the mean local inflows, the local wind direction at each turbine is assessed. Figure 5 shows area-normalised histograms of the local wind direction calculated from a point velocity sampled at hub height $0.5D$ in front of each turbine, after applying a 60 s moving mean on the 1 Hz signal. Note that $0.5D$ in front (or upstream) means a point in negative x-direction relative to each turbine, rather than relative to the rotated centreline of the wind farm.

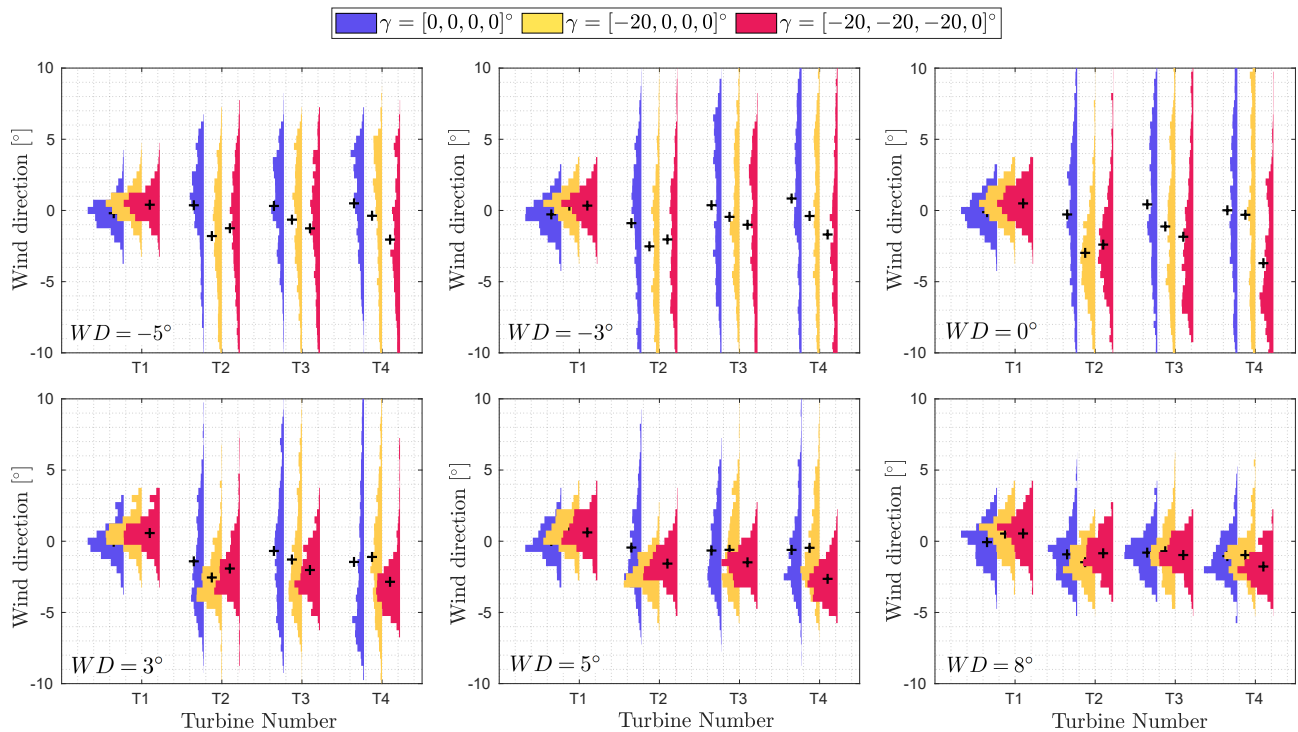


Figure 5. Area-normalised histograms of wind direction measured $1R$ upstream of each turbine location for all yaw scenarios and for each inflow wind direction. Black crosses indicate the mean of each distribution.

For all wind directions, the leading turbine in the baseline unyawed case has a wind direction with a mean at 0° and a relatively Gaussian distribution, as expected. There is a slight positive offset in the mean for all of the leading turbines in yawed configurations, presumably due to asymmetry introduced in the induction zone due to the yaw. The standard deviation of this freestream inflow distribution (using a 60 s moving mean) is $\sigma_{WD} = 1.2^\circ$. The 1 min and 10 min standard deviations of the raw data are 2.4° and 2.3° respectively.

It is clear that the distribution of inflow wind direction experienced by the first turbine is substantially different to that of downstream turbines that operate in wake. Particularly visible for the most aligned wake cases, $WD = -3^\circ$ and $WD = 0^\circ$,



the standard deviation of the wind inflow direction is substantially increased by the presence of wakes, with a spread greater than $\pm 10^\circ$, while the spread of the inflow distribution is $\pm 3^\circ$. Therefore, the presence of wakes generates large uncertainty in inflow wind direction for waked turbines, regardless of the uncertainty present in the ambient flow, as also shown in Andersen et al. (2015). The distributions of inflow wind direction also clearly demonstrate that for $WD = 8^\circ$ there is very little wake impingement on the downstream turbines, as all distributions are similar in shape to that at the inflow to the first turbine.

The yaw misalignment also leads to a mean local wind direction offset at the turbine immediately downstream, due to not only deflecting the mean wake centre but also leading to a local redirection of the flow. For example for $WD = 0^\circ$, a difference in mean local wind direction of 3° is present at the second turbine; similar trends are reflected for all other wind directions. Additionally, when only the leading turbine is yawed (the yellow distributions), the local wind direction distribution tends back to the unyawed baseline by the end of the turbine row, while the largest difference in mean local wind direction occurs at the fourth turbine, in the configurations where three turbines are yawed.

3.2 Individual Turbine Response

After examining the flow and local wind directions, the response of the individual turbines - in terms of power output and loading - can be examined. Figure 6 and Figure 7 show the mean and standard deviation of power output and damage equivalent loads (DELs) of the flapwise blade root bending moment of each turbine in the row, for all yaw configurations and all inflow wind directions. Damage equivalent loading is calculated from data at frequency 1 Hz over 10 minute periods, staggered by 5 minutes, in order to generate 11 samples for the 1 hour time period. The mean and standard deviation in Figure 7 are of those 11 samples. The power output mean and standard deviations are likewise calculated from 10-min means of the raw 1 Hz data.

As expected, the leading turbine has the highest power output and the lowest damage equivalent loads, as it experiences the freestream inflow with higher velocity and lower turbulence intensity than the flow within the turbine row. Generally, after the first turbine the individual turbine power output decreases and the DELs increase, depending on the degree of waked inflow. For the first turbine, yawing increases the flapwise DELs and reduces the power output. Similar to the mean local wind direction offset induced by wake redirection, the power output of the one-turbine yaw configuration tends back to that of the baseline through the row, which agrees with the conclusions of Archer and Vassel-Be-Hagh (2019) that yawing only the leading turbine is insufficient to achieve changes past 2-3 turbines downstream. In the three-turbine yaw configuration, for wind directions $WD = 0^\circ$ and $WD = 3^\circ$, the most significant power gains compared to the baseline occur at the last turbine, showing the importance of the cumulative gains.

The trends in power output confirm the qualitative conclusions from the mean flow plots in Figure 2; that for negative wind directions yawing causes a power loss as it enhances rather than mitigates wake effects, and that for a wind direction offset of 8° there is very little wake interaction. For $WD = 8^\circ$, the downstream turbines in the baseline case have a higher power output than the yawed leading turbine in the yawed configurations. This case clearly exists past the boundary for beneficial application of wake steering for this wind farm, as the losses due to the power-yaw relation exceed the wake losses present in the baseline. The exponent α in the power-yaw relation has a value of 3 according to momentum theory, but in reality varies between 1 – 3 for different turbines and waked states (Liew et al., 2020). Fitting the power-yaw relation to the first turbine loss at $WD = 0^\circ$

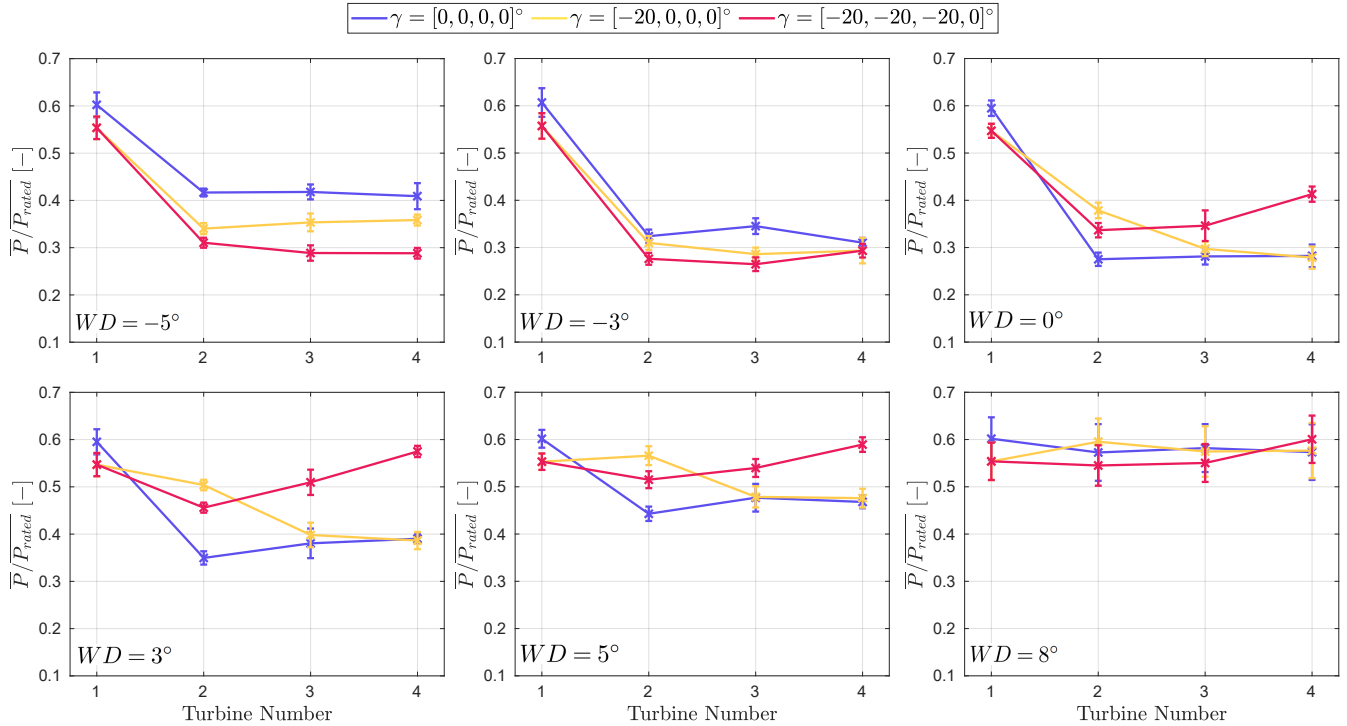


Figure 6. Mean and standard deviation of individual turbine power output across each turbine row, for all yaw scenarios. Each plot shows a different inflow wind direction (as labelled).

265 (so based on $\gamma = 0^\circ$ and $\gamma = -20^\circ$) gives an exponent of $\alpha = 1.35$, a low exponent which leads to a relatively small penalty for yawing compared to other turbines and the assumptions made in engineering wake models.

The DEL plots in Figure 7 show that the maximum flapwise DELs occur in partial wake cases; for the unyawed configurations at $WD = -3^\circ$, $WD = 3^\circ$ and the yawed configurations for $WD = 0^\circ$. While yawing increases the flapwise DELs for an individual turbine, there are several wind directions in which the yaw strategy leads to reductions in total DELs over the turbine row: $WD = -3^\circ$, $WD = 3^\circ$, $WD = 5^\circ$ and $WD = 8^\circ$. The DEL reduction for $WD = -3^\circ$ is due to moving from a partial wake to a full wake state which is therefore accompanied by an undesirable power loss; while for $WD = 3^\circ$, $WD = 5^\circ$ and $WD = 8^\circ$, the load reduction occurs through mitigation of the partial wake state by steering the wakes further away from downstream turbines. These results are aligned with Bartl et al. (2018), in which yaw moment reductions were observed when partial wake states were mitigated. This is particularly interesting for $WD = 8^\circ$, where DEL decreases are present for the three-turbine yaw scenario despite it resulting in total power losses. This decrease in flapwise DELs by mitigation of partial wake can be seen in the local inflow wind direction plots of Figure 5, as the high spread of local wind direction for downstream turbines present in the unyawed configurations is significantly reduced in the yawed configurations.

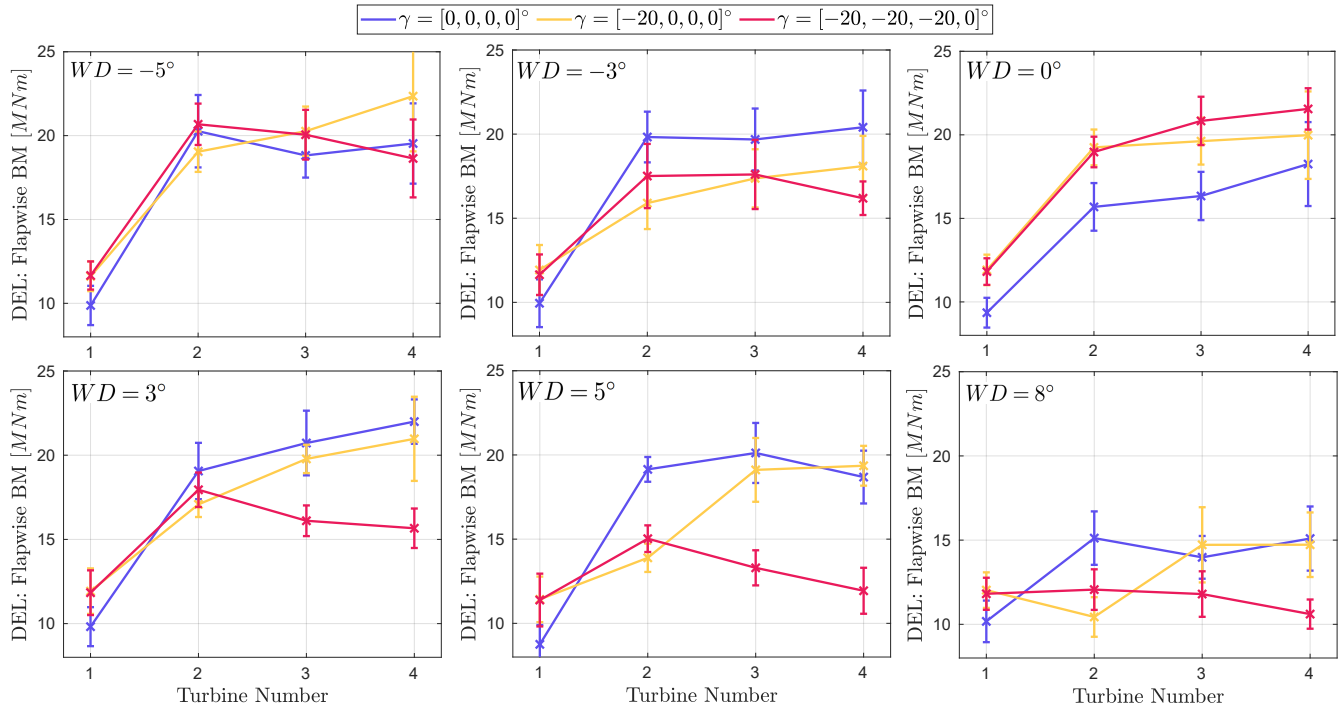


Figure 7. Mean and standard deviation of 10 minute damage equivalent loads for flapwise bending moment for individual turbines across each turbine row, for all yaw scenarios. Each plot shows a different inflow wind direction (as labelled).

3.3 Wind Farm Power Output

Examining the wind farm power output allows the effect of applying wake steering and its sensitivity to inflow wind direction uncertainty to be established. Figure 8 shows the mean wind farm power output for all configurations, grouped by inflow wind direction. Error bars show the standard deviation of the instantaneous (1 Hz) wind farm power.

As expected, the lowest wind farm power output of any unyawed configuration occurs at the fully aligned inflow conditions of $WD = 0^\circ$, with increases in power output at both positive and negative wind directions due to the offset in inflow wind direction reducing the wake losses in the turbine row. The difference in power output between the unyawed configurations at $WD = -3^\circ$ and $WD = 3^\circ$ (2.8 MW, around 8%), and $WD = -5^\circ$ and $WD = 5^\circ$ (3.2 MW, also around 8%) shows the asymmetry introduced due to the wake interaction with veer, as otherwise the two pairs of cases are mirror images of one another.

To clarify the power changes between yaw configurations and wind directions, Figure 9 shows the difference in mean wind farm power output. Figure 9A shows the power change between the yawed and unyawed configurations (e.g. the power change due to applying wake steering) for all wind directions; Figure 9B shows the power change between the non-zero inflow wind directions and the fully aligned case (e.g. the power change due to the offset in inflow wind direction) for all yaw configurations. Including both plots is important because it is interesting to note the relative size of the power output change caused by the two

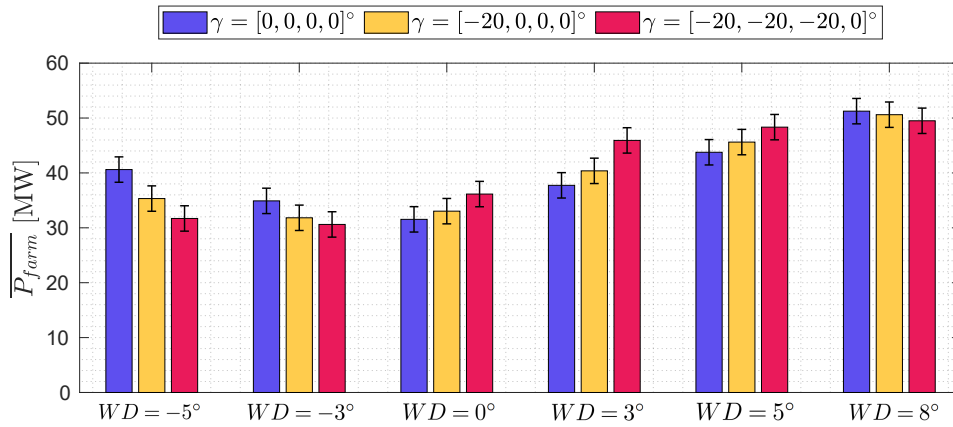


Figure 8. Mean wind farm power output for all cases. Error bars represent standard deviation of instantaneous (1 Hz) power.

effects. Error bars on both plots show the standard deviation of the instantaneous (1 Hz) difference between cases, therefore representing the 16th and 84th percentiles of the distributions (which are Gaussian in shape).

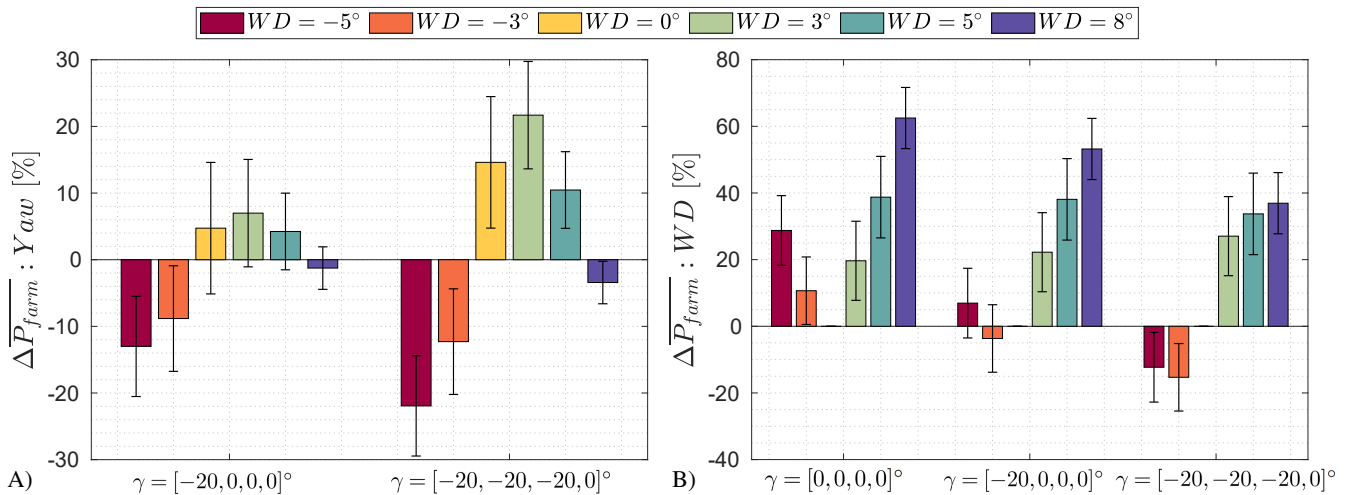


Figure 9. Differences in mean wind farm power output: A) Power difference due to yawing (e.g. difference relative to unyawed baseline case); B) power difference due to wind direction offset (e.g. difference relative to $WD = 0^\circ$ case). Error bars represent the standard deviation of the instantaneous (1 Hz) power difference.

295 Figure 9A shows that yawing either the first turbine, or the first three turbines, leads to wind farm power gains for wind directions $WD = 0^\circ, 3^\circ$ and 5° , and losses for $WD = -5^\circ, -3^\circ$ and 8° . Peak power gains occur at a mean wind direction of 3° . Yawing three turbines rather than one leads to greater potential power output gains at beneficial inflow wind directions, but



also greater losses at disadvantageous ones. However, the ratio between losses and gains (e.g. between power gain at $WD = 3^\circ$ and power loss at $WD = -3^\circ$) is better when yawing three turbines, and hence this yaw configuration is more promising despite the higher sensitivity to inflow wind direction. Additionally, the high standard deviation of the instantaneous power change indicates that if power losses should be avoided, then even the maximum gain in the one-turbine yaw configuration is insufficient to ensure this. Whereas for the three turbine yaw case, within one standard deviation of the mean a power gain is still predicted for $WD = 0^\circ$, $WD = 3^\circ$ and $WD = 5^\circ$. The standard deviation is largest for $WD = 0^\circ$ in both yaw configurations, and decreases with increasing wind direction as the wake effects within the turbine row decrease.

The maximum percentage gain in wind farm power output due to yaw is 22%, achieved by yawing the first three turbines when the inflow wind direction angle is 3° . This percentage increase is similar to the impact of around a $2 - 3^\circ$ change in inflow wind direction, as shown in Figure 9B. For the unyawed configuration, there is a change in wind farm power output of 20% between inflow wind directions of 0° and 3° , and an additional 18% between 3° and 5° . This underlines two somewhat competing conclusions: firstly, the significant power losses due to wake effects in an exactly fully aligned case, and hence the importance of mitigating such losses; and secondly, the high degree of certainty that is required about the mean wind direction if wake steering is to be applied. It is a relatively small range of wind directions that result in significant wake losses for this wind farm (and hence large power gains from wake steering), and the wind farm power output in an unyawed state increases regardless of yaw when a small wind direction offset is present.

Finally, using the mean wind farm power output results from different wind directions, the sensitivity of power output to inflow wind direction uncertainty can be established. This is achieved by firstly fitting a spline to each of the mean wind farm power output to inflow wind direction relationships, for each yaw configuration (the data points in Figure 8). In order to improve the spline gradients at the extreme points, $WD = -5^\circ$ and $WD = 8^\circ$, additional data points are added at $WD = -12^\circ$ and $WD = 10^\circ$, at which the turbines are assumed to operate completely in freestream and hence the farm has a total power which can be calculated from summing the mean powers of the unyawed and/or yawed states of the leading turbine. The splines exactly pass through each LES data point. These splines (one for each yaw configuration) represent the wind farm power output response under an inflow wind direction uncertainty of $\sigma_{WD,LES} = 2.3^\circ$, which is the standard deviation of the freestream wind direction at the inflow to the first turbine. This value is inherent in the LES, arising due to the turbulent variations in the simulated atmospheric boundary layer. However, the purpose of simulating many wind directions is to expand the conclusions to the larger values of wind direction uncertainty present at real wind farms, with values reported in literature between $2.5^\circ - 6^\circ$ (Gaumond et al., 2014; Mittelmeier et al., 2017; Simley et al., 2020, 2021). Therefore, the impact of larger inflow wind direction standard deviations σ_{WD} is simulated by applying Gaussian convolutions with different standard deviations to the original splines (Rott et al., 2018; Simley et al., 2020). As the un-convoluted results (e.g. the original splines) already include the inherent $\sigma_{WD} = 2.3^\circ$ from LES, the total σ_{WD} shown is calculated as $\sigma_{WD} = \sqrt{\sigma_{WD,LES}^2 + \sigma_{WD,ADDED}^2}$, where $\sigma_{WD,LES} = 2.3^\circ$. These results are shown in Figure 10A, and show the expected value of mean wind farm power output for different yaw configurations and different wind direction uncertainties: the x-axis represents the mean of the inflow wind direction (the bias), each line style represents a different standard deviation (the uncertainty), and each colour a different yaw configuration. Figure



10B shows the percentage difference in wind farm power output between the yawed and unyawed configurations for each wind direction uncertainty.

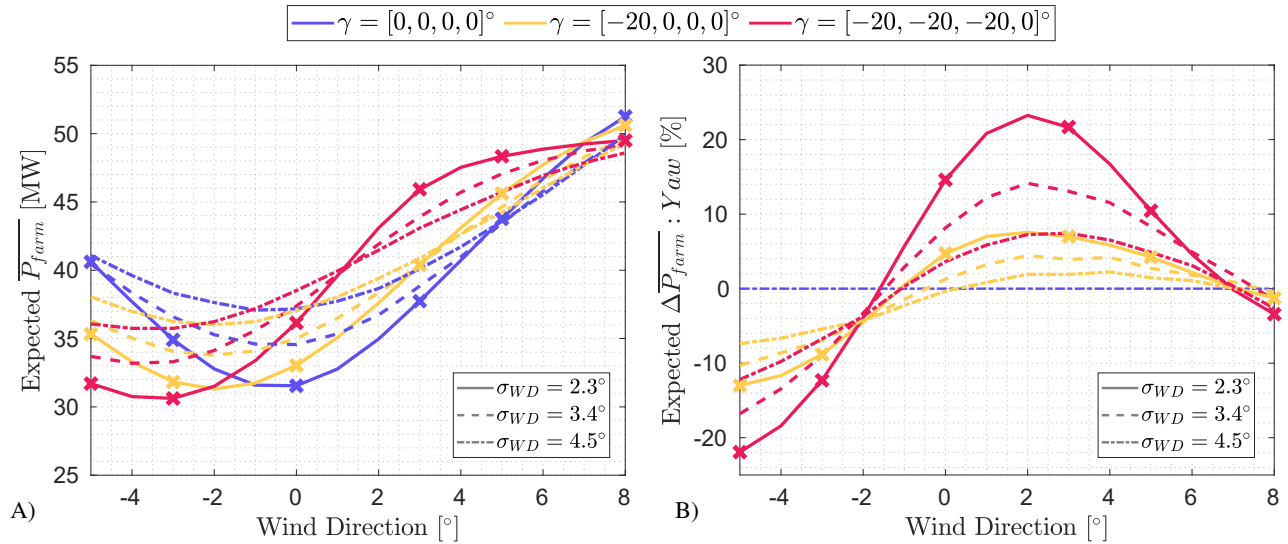


Figure 10. Impact of inflow wind direction uncertainty on wind farm power output: A) Mean wind farm power output under different wind direction uncertainties and yaw configurations, with crosses indicating LES data points (from Figure 8), solid lines showing a fitted spline through the LES results, and dashed lines giving predicted results from different wind direction standard deviations; B) Percentage difference in mean wind farm power output for each wind direction uncertainty, with crosses showing LES data points (from Figure 9A), solid lines showing a spline fit to the LES results and dashed lines giving predicted results under different wind direction standard deviations.

The solid lines and crosses in Figure 10A are simply splines fitted to the LES results from Figure 8, and hence show the same results. However, trends within each yaw configuration are demonstrated more clearly; that the unyawed configuration has a minimum power output at fully aligned conditions, while for the yawed configurations the minimum is essentially shifted by -1.5° or -3° respectively - the amount of row misalignment equivalent to the achieved wake redirection. The inclusion of larger values of wind direction uncertainty leads to the flattening of the trends; for the unyawed baseline, wind direction uncertainty increases the expected power output at $WD = 0^\circ$, as the contribution from the most aligned wind direction is decreased. Expected wind farm power output is also increased in the minima of the curves for the yawed configurations, but the gradient of power increase and the peak values are reduced.

Figure 10B shows the percentage difference between the yawed and unyawed configurations under different wind direction uncertainties. Therefore, this also represents the application of a Gaussian convolution to the wind farm power difference plots in Figure 9. Again, the crosses show the LES results and hence the solid lines represent a spline fit to those values. Considering only the inherent $\sigma_{WD} = 2.3^\circ$ present in the LES, the predicted peak gain is 23% at a mean wind direction of 2° for the 3-turbine yaw case, and 7.5% also at a mean wind direction of 2° for the 1-turbine yaw case. The range of inflow wind directions at which these wake steering regimes are beneficial are $\in [-1.5^\circ, 7^\circ]$ and $\in [-1^\circ, 7^\circ]$ respectively. However, with larger values



of wind direction uncertainty, the expected power gains and range over which they are achieved decrease. Examination of Figure 10A explains why this is the case: the expected power of the baseline unyawed configuration significantly increases with larger wind direction uncertainties, and therefore there is less to gain from wake steering. Additionally, the smoothing of the gradient in the yawed configurations due to the Gaussian convolution reduces the peak expected power, therefore further diminishing the difference between yawed and unyawed setups. The maximum expected power change decreases from 23% and 7.5% respectively for the two yawed configurations at $\sigma_{WD} = 2.3^\circ$, to 7.5% and 2.0% respectively at $\sigma_{WD} = 4.5^\circ$. The range of positive power change is reduced to $\in [-1^\circ, 7^\circ]$ for the 3 turbine yaw configuration, and to $\in [0.5^\circ, 7^\circ]$ for the 1 turbine yaw configuration. In addition to changing the size of the peak power change, the ratio between losses and gains is also detrimentally affected. While the peak is reduced from 23% to 7.5% in the 3-turbine yaw case, the power losses outside of the beneficial range do not decrease as much, changing from -22% to -12% at $WD = -5^\circ$ and from -3.5% to -3% at $WD = 8^\circ$. Therefore, the potential gains are decreased due to the uncertainty of the full-wake state actually occurring, while the losses incurred by individual turbines when yawing are relatively unaffected.

4 Discussion

This work investigates the impact of inflow wind direction uncertainty (both in mean bias and standard deviation) on wake steering wind farm flow control using LES simulations of a row of four turbines in a conventionally neutral atmospheric boundary layer. The veer included in the inflow induces flow turning through the turbine row, such that under the otherwise mirrored mean wind directions $WD = [-3^\circ, 3^\circ]$ and $WD = [-5^\circ, 5^\circ]$ there is a 8% change in the baseline wind farm power output. This large difference in power output, and the skewed wake visible behind the first turbine, emphasises the need for lower fidelity models to include the impact of veer (even before adding its interaction with wake steering), as they may over- or under-estimate the impact of control strategies by incorrectly predicting the baseline flow and wind farm performance.

Although the inflow to the second turbine clearly exhibited skewed and curled mean wake shapes due to veer and yaw, further into the turbine row there was a broader and more self-similar mean deficit, with higher wake centre standard deviation and less evidence of skew or curl. Within the turbine row in deep wake cases, it is therefore the wake-generated turbulence and velocity that begin to dominate the behaviour, as seen for turbulent spectra in Hodgson et al. (2025b). Studying the distributions of local wind direction at each turbine showed that the standard deviation and spread increase significantly when in wake flow, in comparison to the freestream. The distribution spread was also linked to the turbine damage equivalent loads, particularly visible for the wind direction $WD = 8^\circ$ where yawing led to a total power decrease but also a significant decrease in fatigue loads. In fact, all the partial wake cases (which experienced the highest baseline loads) saw load reductions on the waked turbines when yaw control was applied, suggesting that from a loads perspective there could be advantages in yawing to mitigate partial wake states (Bartl et al., 2018).

Examining wind farm power output showed that regarding both the peak power gains and the ratio of gains to losses under unfavourable wind directions, yawing the first three turbines was more promising than yawing only the first. Operationally applying wake steering may also rely on ensuring no risk of instantaneous power losses, in addition to simply a mean gain. In



that case, the standard deviations of instantaneous power difference showed that yawing only the first turbine was unable to meet this requirement, while yawing three turbines did ensure this under mean wind directions $\in [0^\circ, 5^\circ]$.

However, this work demonstrates that potential power gains from applying wake steering rely on precise knowledge of the mean and standard deviation of inflow wind direction. The maximum range of wind directions where a mean power gain is predicted is $\leq 8.5^\circ$, and peak gains decreased significantly for higher wind direction uncertainties. Although the range would occur twice over the entire 360° of possible wind directions due to symmetry, or even up to four times if positive yaw angles were considered (although wake redirection and potential power gains would be lower for these scenarios, and many field experiments only apply a single yaw direction), the challenge is fundamentally in the narrowness of the range. Although wake steering is clearly beneficial in LES with perfect knowledge and controllability over simulation parameters, this work shows that relatively small bias in mean wind direction ($\pm 3 - 4^\circ$ for this case) or an increase in uncertainty could remove any potential gain. Mean biases could be introduced in a operational context by applying a single mean wind direction over an entire large wind farm extent, especially when considering complex atmospheric boundary layer inflows (Ivanell et al., 2025). Even without wind farms present Von Brandis et al. (2023) shows spatial variability in mean wind direction of $\sim \pm 2^\circ$ on $\sim 10\text{km}$ scale and $\sim \pm 4^\circ$ in $\sim 50\text{km}$ scale, suggesting that $\pm 3^\circ$ is entirely possible for certain atmospheric conditions. In field experiments, an overall mean wind direction has been determined either through measurements using nacelle-mounted lidars or anemometers (Simley et al., 2021; Doekemeijer et al., 2021), or nearby lidars and sodars (Simley et al., 2020). Although the difference in mean wind direction may be low in small farms such as these, the present work suggests that using a single ‘global’ mean wind direction in yaw angle optimisation could be problematic for large farms, if the atmospheric conditions or terrain lead to spatial mean wind direction variations of even a few degrees. However, locally measuring the wind direction using wind vanes and anemometers also presents challenges, due to measurement drift and particularly due to calibration issues and flow distortion when yawing. Larger values of wind direction or yaw error uncertainty are both inherent in the ambient flow and introduced through imprecise measurements or servos. The significant decrease in the peak power gain due to wind direction uncertainty arguably suggests that even if the mean wind direction was precisely known, wind direction uncertainties of $> 4^\circ$ may result in wake steering not being worthwhile for this case. In addition, the decision to apply wake steering in reality would require a higher expected power gain (e.g. not just above zero) due to trade-offs with loading or other risks. Therefore, the maximum allowable wind direction uncertainty would likely be even smaller.

The exact range of wind directions over which wake steering is beneficial is dependent on the turbine spacing, as that determines the effective ‘wake overlap’ between downstream turbines at a given mean wind direction. In order to provide a first estimation at a generalisation of the results in this work, the contour plot in Figure 11 shows the percentage area overlap between turbine rotor areas (only the rotor, not considering wake expansion) for different spacings and wind directions, with lines at constant area overlaps equal to that at the wind directions of zero-crossings in Figure 10B. This approach does not consider the change in wake deficit or the non-linear increase in wake deflection with downstream distance. Although highly simplified, this demonstrates a basic trend in the relationship; that shorter spacings will be more robust to wind direction uncertainty as a larger mean angle is required for no wake effects to be present. For comparison, predictions using ‘robust’ optimal yaw angles from Rott et al. (2018) and spacing of $4D$ showed a 12° range of mean wind directions which resulted



in a positive power change; and in field experiments Simley et al. (2020) saw ranges with positive power change of $\sim 10^\circ$ and $\sim 18^\circ$ for spacings of $5.04D$ and $2.89D$ respectively, suggesting that the highly simplified approach in Figure 11 slightly overestimates the range for shorter spacings (by $2^\circ - 3^\circ$ for these examples).

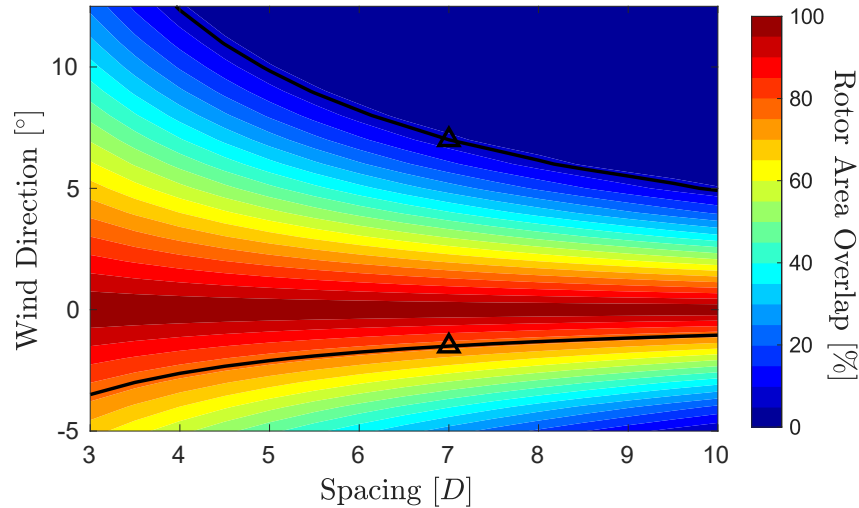


Figure 11. Percentage overlap of two aligned row turbine rotor areas at different spacings and for different wind directions. Marker shows the zero crossing of $\Delta \overline{P_{arm}}$ as predicted in Figure 10B, for the spacing $7D$ simulated here. Lines show a constant rotor overlap percentage calculated for each marker point.

4.1 Limitations and Further Work

420 In the present work, a single yaw setpoint is applied which remains unchanged across wind directions (as the impact of both bias and uncertainty are investigated), rather than finding optimal yaw angles for each wind direction and then applying a Gaussian convolution, thereby assuming no error in the mean, as in Rott et al. (2018). It could be the case that a ‘robust’ yaw angle optimisation for this case would result in smaller yaw angles. This would likely decrease the peak power gain, and may not extend the beneficial range of wind directions (Rott et al., 2018). Fundamentally, the issue remains the same: the range

425 of mean wind direction angles over which wake steering can be successfully applied stretches between on one side a small opposing angle, beyond which the yaw control acts to steer the wakes into the subsequent turbines rather than away from them; and on the other side an angle large enough to have relatively minimal wake interaction anyway, and hence the power losses incurred by yawing are larger than any possible benefit of wake steering. Then, any wind direction uncertainty will act to shrink this range further.

430 One limitation of both the current work and others considering the impact of wind direction uncertainty is exactly what type of uncertainty is simulated, and how, compared to what occurs in the real atmosphere. It is well reported that short-term wind direction variability can be modelled with a Gaussian distribution, for statistics taken over 5 min or 10 min periods (Gaumond



et al., 2014), and that this is a more significant contributor to the total uncertainty than yaw position uncertainty (Quick et al., 2020). Yaw position uncertainty applied to each turbine individually would result in all turbines having small random offsets
435 relative to the local wind direction. Whereas, this work assumes the turbines exactly face the incoming wind direction, and the bias is introduced e.g. through the wind farm controller using a different direction to what is locally present. This therefore represents a best case scenario, particularly regarding short-time variability, as in reality the turbines would not be exactly aligned with the wind direction.

Perhaps the biggest limitation of the results is applying a Gaussian convolution across a range of wind directions in order
440 to extrapolate the impact of wind direction uncertainty. If short-term variability is being simulated, then a single fluctuation of the inflow wind direction is unlikely to have a length scale equivalent to the downstream farm extent, and hence representing the effect of that fluctuation by rotating the entire wind farm coordinates by a certain value is perhaps an overestimate of the impact. This is emphasised by the additional gains achieved by yawing three turbines instead of only one, despite the very high local wind direction variability seen within the turbine row (e.g. it is still possible to achieve a gain from wake steering under
445 a very high local inflow uncertainty). In the scenario studied here, with a spacing of $7D$ and diameter 284 m, the flow-through time of the turbine row is 650 s at freestream velocity or 930 s assuming a wake velocity of $0.7U_0$, greater than the 600 s time period length used to define σ_{WD} . Therefore, estimation of the impact of wind direction uncertainty greater than the inherent 2.3° may represent an upper bound. However, this does not apply to the impact of bias, and additionally the beneficial impact of assuming perfect relative alignment of the turbines may counteract any overestimation of the detrimental impact of wind
450 direction uncertainty.

As this work has shown that the potential gains from wake steering are sensitive to bias and uncertainty in wind direction, the obvious next question is: are there other wind farm control strategies that would perform better? Approaches such as derating (Annoni et al., 2016) or helix control (Frederik et al., 2020) act to reduce the wake deficit rather than redirect the wake, and therefore could be more robust to uncertainties. Further work could also clarify the impact on using clockwise yaw angles
455 rather than anticlockwise, as although they are known to be less beneficial, their use is often not penalised in engineering models. Considering the sensitivity seen here even for anticlockwise yaw angles, it could be that there are almost no scenarios in which clockwise yaw is beneficial, when taking into account realistic wind direction uncertainty.

5 Conclusions

This work investigates the impact of bias and uncertainty in inflow wind direction on wake steering wind farm flow control, by
460 conducting LES on a row of four turbines with $7D$ spacing using a conventionally neutral boundary layer inflow. Coordinate rotations are applied to the wind farm to simulate inflow wind directions of $[-5, -3, 0, 3, 5, 8]^\circ$. Three yaw configurations are compared: a baseline with no yaw; the first turbine yawed anticlockwise by 20° , and the first three turbines yawed anticlockwise by 20° . When studying both flow and power output, the impact of veer interaction is significant; leading to a 8% difference in power output between unyawed configurations for both pairs $WD = [-3, 3]^\circ$ and $WD = [-5, 5]^\circ$. The wake of the first
465 turbine exhibits a skewed and/or curled mean wake shape due to veer and yaw, but after the second turbine this becomes



much less apparent in aligned row cases, as the wake properties begin to dominate the flow. The local inflow wind direction standard deviation significantly increases between the leading turbine and those that experience waked inflows, highlighting the increased uncertainty that is present in deep wake cases. When studying flapwise blade root bending moment damage equivalent loads, partial wake cases show the highest loading, and applying wake steering causes load reductions for these cases.

For the wind direction uncertainty inherent in the LES ($\sigma_{WD} = 2.3^\circ$), the peak wind farm power change due to yawing occurs at a mean wind direction of 2° , with increases of 23% and 7.5% respectively for the three turbine and one turbine yaw configurations. Positive power changes occur over a range of mean wind directions $[-1.5^\circ, 7.0^\circ]$. The peak gain, 23%, is roughly equivalent to the power increase caused by a $2 - 3^\circ$ change in mean wind direction in the unyawed baseline. When investigating a wind direction uncertainty of $\sigma_{WD} = 4.5^\circ$ by applying a Gaussian convolution to the results from different wind directions, the peak power gains reduce to 7.5%, over a range of $[-1^\circ, 7^\circ]$, and 2.0%, over a range of $[0.5^\circ, 7^\circ]$, respectively. Both the significant decrease of expected power peak with increased wind direction uncertainty, and the relatively small range of inflow wind directions over which positive power changes are predicted regardless of uncertainty, demonstrate the challenges with applying wake steering operationally. Even if the mean inflow direction is precisely known, this study shows that it arguably still might not be worthwhile to apply wake steering when the uncertainty is high. And conversely if the wind direction standard deviation could be accurately measured and known to be low, then even a $\pm 3 - 4^\circ$ bias in the mean wind direction measurement (which could occur e.g. due to measurement error or by assuming a single value across an entire large wind farm) is enough to remove the predicted gains for this wind farm spacing ($7D$). Therefore, it is important that robust and accurate wind direction measurements are available locally at each turbine, to help reduce the impact of mean wind direction bias. It may also be advisable to specify a minimum range of wind directions for predicted gains to occur over before considering wake steering, such that expected levels of uncertainty cannot accidentally lead to losses.

Code and data availability. EllipSys3D and HAWC2 are proprietary codes developed at DTU, for which a license can be bought. The coupling framework Dynamiks is open source and available on Github. All simulation data is available upon request.

Author contributions. Both ELH and SJA formulated the idea for the paper. ELH generated the results, performed the analysis, and wrote, revised and edited the manuscript. SJA helped with analysis, supervision and the revision and editing of the manuscript.

Competing interests. The authors declare no competing interests.



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