

# Vortex generator design for unsteady flow separation control and dynamic stall suppression on pitching thick airfoils

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**Abstract.** This study experimentally investigates the performance of vortex generators (VGs) designed for steady stall control to maximise the lift-to-drag ratio in steady conditions in preventing to prevent unsteady trailing-edge flow separation and dynamic stall during pitch oscillations occurring on inboard and midboard wind turbine blade sections. Surface pressure measurements are conducted in the TU Delft low-speed wind tunnel on a DU-97-W-300 airfoil undergoing pitch oscillations while equipped with VGs of various vane sizes and shapes. In steady conditions, vanes with heights smaller than the local boundary layer thickness optimally balance delaying stall following trailing-edge separation the stall delay with achieving maximum lift-to-drag ratio among the tested triangular vane VGs. However, these same VGs with vane heights smaller than or equal to the steady local boundary layer thickness are insufficient to suppress the onset and upstream progression of a trailing-edge separation front unsteady flow separation in all pitching cycles. VGs whose vane height exceeds the local boundary layer thickness for a larger part of the pitch cycle prevent the onset and upstream progression of the trailing-edge separation front unsteady flow separation and restrict the upstream movement of the stall vortex for a larger percentage of cycles. Contrary to past literature, rectangular vanes yield a higher steady aerodynamic efficiency than triangular vanes. Rectangular vanes also suppress trailing-edge flow separation unsteady flow separation in all pitching cycles at all tested reduced frequencies, indicating more effective boundary layer energisation overall stronger streamwise vortices than triangular vanes, thus and proving to be a better VG shape for steady and unsteady stall suppression on thick airfoils.

## 1 Introduction

Modern wind turbines are following a trend of increasing rotor diameters (IRENA, 2019). Recently deployed offshore wind turbines have blades of more than 100 metres in length, such as the Siemens Gamesa SG 14-222 turbine with a blade length of 108 metres and the Vestas V236 turbine with a blade length of 115 metres. This trend drives blade sections to be made from thicker airfoils to ensure structural integrity and balance the aero-structural loads, as seen in the newest reference wind turbines such as the IEA 15 MW (Gaertner et al., 2020) and 22 MW turbines (Zahle et al., 2024). These thicker airfoils are more prone to flow separation, with the consequent loss of lift decreasing the annual energy production and the fatigue lifetime of the blades (McKenna et al., 2016). The use of Vortex generators (VGs) as passive flow control devices has become a common practice in wind turbine design (Griffin, 1996; Skrzypiński et al., 2014; Bak et al., 2016; Baldacchino et al., 2018). Vortex generators are

25 also being used to mitigate the effects of leading-edge erosion (Gutiérrez et al., 2020; Ravishankara et al., 2020), and being retrofitted on existing turbines to partly restore original performance (Skrzypiński et al., 2020; Manolesos et al., 2024).

Unsteady aerodynamics around the blade sections is becoming increasingly important in the design of large wind turbine blades. The occurrence of cyclic variations in the angle of attack on rotor blades leads to the flow detaching and reattaching on the blade sections as the local angle of attack moves above and below the static stall angle. This phenomenon is referred to as dynamic stall. Early investigations like McCroskey (1972); McCroskey and Fisher (1972); McCroskey (1981); Carr (1988) studied dynamic stall in the context of helicopter rotor blades. In the context of wind turbines, measurements from the NREL Combined Experiment (Butterfield and Nelsen, 1989; Butterfield et al., 1990) ~~were~~ one of the first to show the occurrence of rotating wind turbine blades. Butterfield et al. (1992) showed that dynamic stall occurred on operational wind turbine blades upon cyclic variations of the local angle of attack due to yaw misalignment. Shipley et al. (1995) further investigated the occurrence of dynamic stall on wind turbine blades and pointed to reasons such as yaw misalignment, fluctuating wind speed and direction, and tower shadow for the occurrence of dynamic stall. Dynamic stall on wind turbine blades can lead to cyclic load variations and higher loads on the blade. Shipley et al. (1994) showed that dynamic stall on wind turbine blades increases the chances of fatigue failure and reduces turbine lifetime. Rasmussen et al. (1998) have shown that coupling of pitch motions with structural vibrations can lead to negative aerodynamic damping in the edgewise direction and positive damping in the flapwise direction. Negative damping imparts energy into the structural vibrations, causing uncontrolled growth of the vibrations and rapid failure.

At the airfoil level, the unsteady flow variations leading to dynamic stall are experienced as time-varying motions such as pitching, plunging, etc., which lead to cycles of flow detachment and reattachment. The works of McCroskey (1981); McCroskey et al. (1981); Carr (1988); Leishman and Beddoes (1989) detail the various flow phenomena occurring during dynamic stall. For an airfoil undergoing ~~pitch oscillations~~, McCroskey et al. (1981) list three kinds of stall based on the occurrence and propagation of flow separation during the pitch cycle — leading-edge stall, trailing-edge stall, and mixed stall. Leading-edge stall is said to occur when flow separation first appears near the leading edge and moves towards the trailing edge with increasing angle of attack, while trailing-edge stall is said to occur when the separation front moves from the trailing edge towards the leading edge with increasing angle of attack. Mixed stall usually occurs either when separation fronts originating from both the leading and trailing edge move towards each other and merge somewhere near mid-chord, or when the separation front originates in the middle of the airfoil and moves both in leading-edge and trailing-edge directions. Trailing-edge stall is the most common type of turbulent stall for thick airfoils, typical of inboard and midboard wind turbine blade sections, and is also the type of stall observed on the airfoil section used in this work. ~~When the unsteady trailing edge stall, when dynamic~~ angle of attack exceeds the static stall angle, flow reversal starts at the trailing edge and spreads upstream over much of the airfoil chord. At a certain angle of attack, the separated flow reaches a critical point and a strong vortex called the leading-edge vortex (LEV) forms near the leading edge and starts convecting downstream towards the trailing edge. The lift keeps increasing with increasing angle of attack during this process. Dynamic stall is observed when the LEV convects past the trailing edge into the wake.

Butterfield (1989) shows that dynamic stall causes the integrated aerodynamic forces on a rotating wind turbine blade section to deviate significantly from the static characteristics of the airfoil section. Shipley et al. (1995) show that the local pressure distributions on a wind turbine blade airfoil section differ significantly from the static pressure distributions during dynamic stall. The pressure and flow measurements presented by McCroskey et al. (1981); McAlister et al. (1982); Carr (1988); Choudhry et al. (2014); Gupta and Ansell (2019), among many others, on several airfoils undergoing pitch oscillations show that the changed flow characteristics during dynamic stall lead to significant differences in the steady and unsteady pressure distributions, boundary layer characteristics, and flow separation behaviour. Since VGs control flow separation through energising the boundary layer with streamwise vortices, the difference between steady and unsteady boundary layer characteristics around a pitching airfoil creates the need to investigate the behaviour of VGs in unsteady conditions.

The impact of VGs on the steady aerodynamic performance and flow around wind turbine blade sections has been well-studied in detail in the past. We point readers to the works of Lin (2002) and Zhao et al. (2022) for detailed reviews on the use of VGs for steady flow separation control. Vane-type VGs are the most commonly used VG type for flow separation control on wind turbine blades. On wind turbine blades, VGs are designed to delay the stall onset and increase maximum lift of the airfoil section, while minimising the drag increase caused by the presence of the VGs. The works of Godard and Stanislas (2006); Fouatih et al. (2016); Baldacchino et al. (2018), among others, have investigated a wide range of VG configurations varying different geometric parameters such as vane height, spacing, angle, and chordwise location on the airfoil, studying the impact of these parametric variations on the steady performance using the aforementioned lift, drag, and stall metrics. All these studies concluded that the vane height is the most critical geometrical parameter affecting VG performance. Other parameters like vane spacing, vane inclination, etc. have a significantly smaller impact than vane height. This follows from the fact that the strength of the streamwise vortices that energise the boundary layer and delay flow separation under adverse pressure gradients is proportional to the vane height, as shown by Lin (2002); Ashill et al. (2005) among others. However, larger vane sizes also increase the drag caused by the VGs due to their increased surface area. Thus, designers seeking to optimise VGs designs make a trade-off between using larger vanes to delay stall to a higher angle of attack, and using smaller vanes to limit the drag increase. As solutions to this trade-off, low profile VG designs aiming to reduce drag while maintaining the stall delay benefits have also been proposed in the past by works like Lin (2002); Martínez-Filgueira et al. (2017).

Besides the vane size, literature is also divided on the best vane shape for vane-type VGs. Most literature compares triangular and rectangular vanes. Godard and Stanislas (2006) recommend choosing triangular vanes over rectangular vanes due to their lower drag penalty for the same size. However, Zhen et al. (2011) show that rectangular vanes produce a higher maximum lift and lower skin friction coefficient than triangular vanes of the same size. The lower skin friction coefficient especially should lead to lower drag, and is thus a finding contrary to the work of Godard and Stanislas (2006). Fouatih et al. (2016) also show that rectangular vanes generally produce a higher lift-to-drag ratio, but some configurations may perform poorly due to higher drag. The differences in performance between triangular and rectangular vanes in different studies creates an additional variable leading to uncertainty in the optimal VG design.

The impact of VG designs on unsteady airfoil aerodynamics has been primarily studied through numerical simulations using computational fluid dynamics (CFD). Typically for unsteady studies, VGs have been designed based on steady-state perfor-

mance, with the assumption that the performance in unsteady conditions would be similar. In recent work, Zhu et al. (2020) studied the effect of single and double row VGs on the lift drag and moment characteristics of an NREL S809 airfoil undergoing pitch oscillations using URANS simulations. Zhu et al. (2022) extended the same investigation to combine the effect of leading-edge roughness and VGs using URANS simulations and equivalent sand grain roughness models. Both of these studies based their VG designs on guidelines established through steady investigations from the work of Mueller-Vahl et al. (2012); Baldacchino et al. (2018). Experimental studies focussing on the effect of VGs on unsteady aerodynamic characteristics (Choudhry et al., 2016; Li et al., 2020; De Tavernier et al., 2021; Doosttalab et al., 2025) are challenging to conduct, since they require matching both the high chordwise Reynolds numbers and high degree of unsteadiness at which modern wind turbine blades operate. Representative dynamic stall tests thus require operating at high angles of attack with high wind speeds and high pitching frequencies, which can generate enormous loads, making safe operation of experimental setups a challenge. These experimental studies have also used VGs designed for optimal steady performance due to the limited prior experimental data on unsteady conditions including VGs. The authors of this paper have also based their VG design used in a previous experimental work (Sahoo et al., 2024b) on the optimal VG design proposed by the steady investigations of Baldacchino et al. (2018) with the assumption that the steady optimal VG design will hold true for unsteady investigations as well. This previous investigation focussed on the ability of VGs to counteract the performance loss on a pitching airfoil due to leading edge erosion (simulated via forced transition with a zigzag tape) when the airfoil is passing through various phases of dynamic stall. This paper will instead focus on investigating various VG designs in both steady and unsteady conditions with an objective of verifying the assumption that steady and unsteady performance of all VG designs will be similar. The test conditions in this paper are also different from Sahoo et al. (2024b) to cover a wider range of unsteadiness regimes and ensure transition to turbulence far upstream of the VGs so that the effects discussed in this work can solely be attributed to VG design variation.

The simulations of Zhu et al. (2020) on the NREL S809 airfoil with VGs show that VGs bring about a sharp decrease in the phase-averaged lift coefficient when the airfoil starts to pitch down from the maximum angle of attack and also slow down the reattachment process near the minimum angle of attack. Moreover, the phase-averaged  $C_p$  distributions indicate the presence of a stall vortex that oscillates near the trailing edge. Similar behaviour is also observed in the phase-averaged pressure distributions from the simulations of Zhu et al. (2022) on the same airfoil and VG combinations with forced transition added, and from the experimental results of Wei et al. (2023) on a NACA 0012 airfoil with VGs. These results indicate that the interaction between the stall vortex and the streamwise vortices generated by the VGs may lead to complex unsteady flow separation behaviour that is lost when the results are phase-averaged.

In this work, we conduct wind tunnel experiments on a DU-97-W-300 airfoil section equipped with different VG configurations undergoing pitch oscillations. The DU-97-W-300 airfoil has a maximum thickness-to-chord ratio of 30% and was designed for wind turbine root sections (Timmer and van Rooij, 2003). Several reference wind turbines such as the DTU 10 MW (Bak et al., 2013), AVATAR (Schepers et al., 2018), IEA 15 MW (Gaertner et al., 2020), and IEA 22 MW (Zahle et al., 2024) use an airfoil of 30% thickness to chord ratio for inboard and mid-board sections where the positive stall angle of attack and the aerodynamic efficiency (lift-to-drag ratio) are important design criteria. The tested VGs are thus optimally designed for stall delay and lift-to-drag-ratio for steady conditions.

130 First, we focus on varying the vane height of the VGs to study whether vanes smaller than the local boundary layer height generally recommended by literature for steady applications can prevent unsteady flow separation during pitch oscillations. Secondly, we also compare rectangular and triangular VG vane shapes to investigate which design can better prevent flow separation in unsteady conditions.

## 2 Experiment description

### 2.1 Model and wind tunnel description

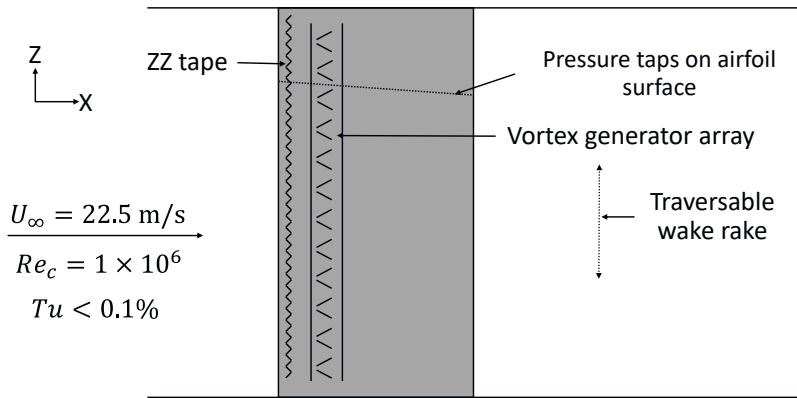
135 The tests were carried out in the closed-loop, low-turbulence tunnel at TU Delft. The octagonal test section has a cross-sectional area of  $1.80 \text{ m} \times 1.25 \text{ m}$  and is 2.60 m long. The tested DU-97-W-300 airfoil section has a maximum thickness-to-chord ratio of 30%. The model has a chord of 0.65 m, a thick trailing edge of 1.7% of the chord, and spans the height of the wind tunnel test section. This gives an aspect ratio of approximately 1.92. The airfoil model with trip tape and VGs installed is shown in Figure 1.

140 The airfoil was designed by Timmer and van Rooij (2003) at TU Delft for inboard sections of wind turbine blades with a high relative thickness for lower structural loads on the turbine shaft and bearings and a relatively high maximum lift to deliver sufficient torque at lower wind speeds. We use 0.5 mm thick zigzag tape to force transition to a turbulent boundary layer at 5% chord-wise location on both sides of the airfoil. As mentioned in Section 1, the forced transition is a key difference from the setup used in previous work by the authors in Sahoo et al. (2024b). The setup of the previous experiment had used 0.2 mm thick  
145 zigzag tape at 5% chord-wise location which proved insufficient to trigger transition to turbulence at the zigzag tape location. Instead, with the thinner zigzag tape, the authors observed the flow transition location varying between the zigzag tape location and the VG location. This caused uncertainty in attributing differences in the pressure distribution between VG and no-VG cases solely to the presence of VGs. Hence, the authors opted for a thicker zigzag tape in this experiment to ensure transition to turbulence at the zigzag tape location and far upstream of the VG location. Throughout the paper, "free" and "forced" are  
150 used to refer to the free or forced transition state of the boundary layer.

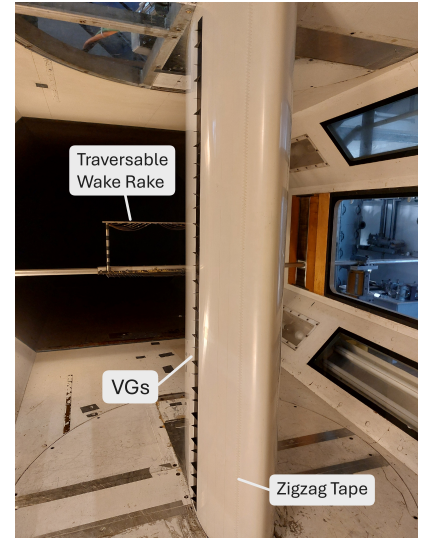
The pitching motion for the dynamic stall tests was imparted using a linear actuator connected to a steel shaft going through the model via a crank mechanism that converted the linear actuation to the rotational motion of the airfoil. The model was clamped at the top and bottom with rotational bearings, leaving a gap of about 1 mm between the model and the tunnel walls. During static tests, this gap was taped off.

### 155 2.2 Vortex Generator design

The symbols used for the various VG array geometry and configuration parameters are shown in Figure 2a. All VGs tested were counter-rotating vanes with a common downwash. Previous steady measurements (Baldacchino et al., 2018) tested VGs between 10%-50% chord-wise location on this airfoil and showed that VGs at 30% chord were the most effective at delaying stall and increasing maximum lift. To simplify the test matrix by fixing the VG placement location, all AH VG arrays were



(a) Schematic (with VG array 3 mounted)

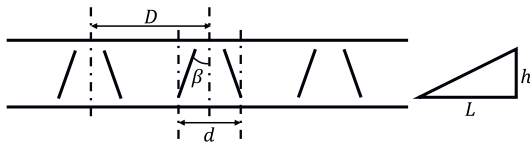


(b) Airfoil model in the test section

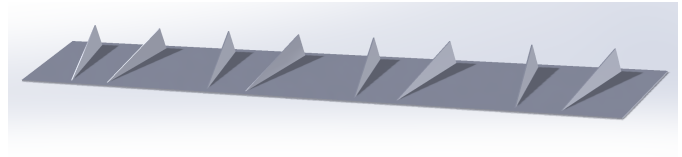
**Figure 1.** Wind tunnel test setup

160 placed at the most effective location of 30% chord ~~-wise location~~ on both sides of the airfoil. The VGs were added across the span of the airfoil model, but leaving a gap of around 100 mm (approximately 8% of the model span) near the tunnel walls (as illustrated in Figure 1a) to avoid interactions between the VGs and the flow near the walls. Thus, the VGs cover around 84% of the airfoil model span. Steady measurements tests from literature (Baldacchino et al., 2018) were reproduced to validate a stall angle of attack difference within  $1^\circ$  of the previous tests.

165 The VG arrays tested in the overall experiment are presented in Table 1. The VG arrays were manufactured via 3D printing. For ease of manufacture and mounting on the airfoil model, a thin mounting strip of 280 mm length and 0.5 mm thickness was included in the VG array designs, as shown in Figure 2b. The height of the VGs was accordingly adjusted to match the total heights mentioned in Table 1. In this work, we compare VG IDs 1 to 3 for the vane size variation and VG4 for the vane shape variation. Henceforth in this paper, arrays 1 to 3 will be referred with their vane height as the 2.5 mm, 5 mm, and 10 mm  
 170 VGs respectively and the array 4 will be referred to as the rectangular VGs. For reference, the heights of the three compared vane sizes with respect to the computed boundary layer height at the VG placement location on the no-VG airfoil are shown in Figure 3 for the whole range of measured angles of attack. At  $0^\circ$  angle of attack, the 2.5 mm VGs are smaller than the local boundary layer thickness, the 5 mm VGs are approximately equal to the local boundary layer thickness, and the 10 mm VGs are larger. The boundary layer height is computed using RFOIL (van Rooij, 1996).

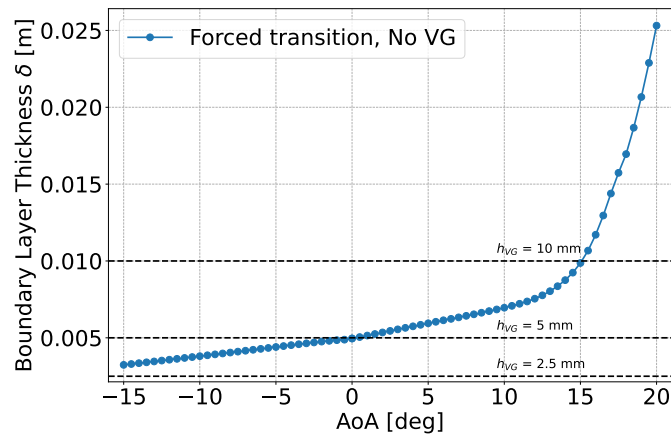


(a) Parameter nomenclature



(b) CAD model with mounting strip for 3D printing.

**Figure 2.** VG arrays used in the wind tunnel tests.



**Figure 3.** Visualising the VG vane height with respect to the boundary layer thickness on the suction side at the VG placement location on the baseline airfoil surface without VGs. Boundary layer height computed using RFOIL (van Rooij, 1996)

## 175 2.3 Test matrix

The test cases presented in this work are part of a larger test matrix presented in Table 2, with the cases discussed in this work highlighted with bold text. The static polars were acquired between  $-15^\circ$  and  $30^\circ$ , capturing the stall region even with VGs. The chord-wise Reynolds numbers were between 0.5 million and 2 million, corresponding to wind speeds between 11.3 m/s to 45.3 m/s. The free-stream turbulence level was well below 0.05%. For the dynamic tests, the Reynolds number of 1 million was chosen. Sinusoidal pitch oscillations of different mean angle and amplitude combinations were applied to make the airfoil experience the various stages of dynamic stall development. The various pitching frequencies (presented dimensionless as the reduced frequency  $k = \frac{\pi c f}{U_\infty}$ ) created unsteady flow around the airfoil that spanned quasi-steady ( $k = 0.045$ ), light unsteadiness ( $k = 0.09$ ), and high unsteadiness ( $k = 0.18$ ) as per the categorisation made by Corke and Thomas (2015) based on the lag between the flow and the airfoil motion due to inertia. The unsteadiness regimes covered in this paper are another key difference between this experiment and the previous experiment described in Sahoo et al. (2024b). Of all the pitching motions tested, we focus on the  $10^\circ \pm 10^\circ$  motion at all tested frequencies in this work. As will be illustrated in Section 3, the airfoil enters and exits

**Table 1.** Overview of VG array geometries tested. The cases presented in this work are highlighted in bold text.

| VG ID    | Vane Shape  | $\beta$ [deg] | L [mm]     | h [mm]     | D [mm]      | d [mm]      | Varying Parameter |
|----------|-------------|---------------|------------|------------|-------------|-------------|-------------------|
| <b>3</b> | <b>Tri</b>  | <b>15</b>     | <b>30</b>  | <b>10</b>  | <b>70</b>   | <b>35</b>   | <b>Baseline</b>   |
| <b>1</b> | <b>Tri</b>  | <b>15</b>     | <b>15</b>  | <b>5</b>   | <b>35</b>   | <b>17.5</b> | <b>Vane size</b>  |
| <b>2</b> | <b>Tri</b>  | <b>15</b>     | <b>7.5</b> | <b>2.5</b> | <b>17.5</b> | <b>8.75</b> |                   |
| <b>4</b> | <b>Rect</b> | <b>15</b>     | <b>30</b>  | <b>10</b>  | <b>70</b>   | <b>35</b>   | <b>Vane shape</b> |
| 5        | Tri         | 15            | 30         | 10         | 70          | 17.5        | Vane spacing      |
| 6        | Tri         | 20            | 30         | 10         | 70          | 35          | Inclination Angle |

the static stall region both with and without VGs with the  $10^\circ \pm 10^\circ$  pitching motion making it a good test case to investigate unsteady flow separation control with VGs.

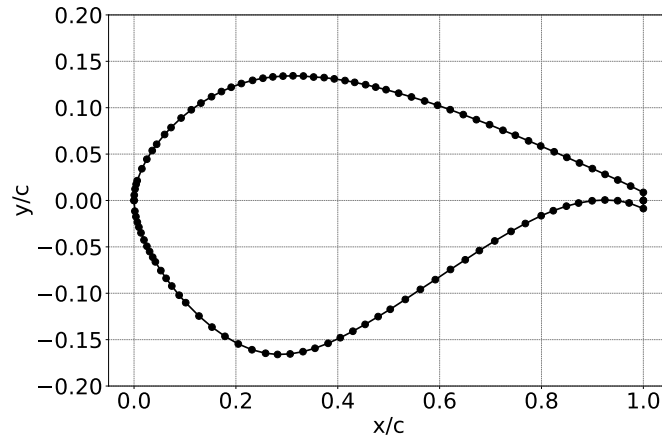
**Table 2.** Overview of all the test cases from the full experiment. The cases presented in this work are highlighted in bold text.

| Reynolds Number<br>Re ( $\times 1E6$ ) | Transition<br>— | VG Array<br>—                       | Mean AoA<br>$\alpha$ [°] | Amplitude<br>A [°] | Frequency<br>f [Hz]  | Reduced Frequency<br>k        |
|--|-----------------|-------------------------------------|--------------------------|--------------------|----------------------|-------------------------------|
| Steady Cases                           |                 |                                     |                          |                    |                      |                               |
| 0.5, 0.75, <b>1.0</b> , 2.0, 3.0       | <b>free</b>     | —                                   | -25 to 40                | —                  | —                    | —                             |
| 0.5, <b>1.0</b> , 2.0                  | <b>forced</b>   | —                                   | -15 to 30                | —                  | —                    | —                             |
| 0.5, <b>1.0</b> , 2.0                  | <b>forced</b>   | <b>VG1, VG2, VG3, VG4, VG5, VG6</b> | -15 to 30                | —                  | —                    | —                             |
| Unsteady Cases                         |                 |                                     |                          |                    |                      |                               |
| 1.0                                    | free            | —                                   | 5, 10                    | 5, 10, 14          | 1.0, 2.0, 2.5        | 0.0902, 0.1805, 0.2255        |
| <b>1.0</b>                             | <b>forced</b>   | —                                   | 5, <b>10</b>             | 5, <b>10</b> , 15  | <b>0.5, 1.0, 2.0</b> | <b>0.0451, 0.0902, 0.1805</b> |
| <b>1.0</b>                             | <b>forced</b>   | <b>VG1, VG2, VG3, VG4, VG5, VG6</b> | 5, <b>10</b>             | 5, <b>10</b> , 15  | <b>0.5, 1.0, 2.0</b> | <b>0.0451, 0.0902, 0.1805</b> |

## 2.4 Instrumentation for data acquisition

190 The normal and tangential forces were calculated from surface pressures on the airfoil measured using a distribution of 102  
 195 pressure ports on the model, including 1 port on the blunt trailing edge (illustrated in Figure 4). The pressure ports are located  
 between approximately 20% to 25% of the span from the top wall at a slight angle with the streamwise direction, as illustrated  
 in Figure 1a. This means the pressure ports span the length of 1 VG pair for the largest 10 mm VGs and 4 pairs for the  
 smallest 2.5 mm VGs. The angled pressure port placement ensures downstream pressure ports are not influenced by upstream  
 disturbances. A traversable wake rake with 67 total pressure and 16 static pressure tubes was used to assess the total drag. The  
 wake rake traversed over a spanwise distance of 140 mm spanning 2 VG pairs for the largest 10 mm VGs and 8 pairs for the

smallest 2.5 mm VGs. Steady measurements were acquired at a rate of 5 Hz for 25 seconds. Unsteady measurements were acquired at a rate of 300 Hz for 150 cycles of pitching motion.



**Figure 4.** Pressure ports distribution on the airfoil model

## 2.5 Data processing

200 The measured pressures were used to calculate the normal force coefficient  $C_n$ , pitching moment coefficient  $C_m$ , lift coefficient  $C_l$ , and drag coefficient  $C_d$ . Drag coefficient from the wake rake pressures was calculated using the method described in Jones (1936). The uncorrected values of these coefficients are presented with a ' symbol throughout the paper. Besides the force and moment coefficients, the location of flow separation is also presented in this paper. Flow over the airfoil surface is considered to have separated when the pressure coefficient plateaus over the airfoil surface ( $\frac{dC_p}{dx} \approx 0$ ). The separation location is determined  
 205 to be the point where the pressure coefficient starts to plateau. An example of flow separation location determined for one steady and one unsteady case is shown in Appendix A.

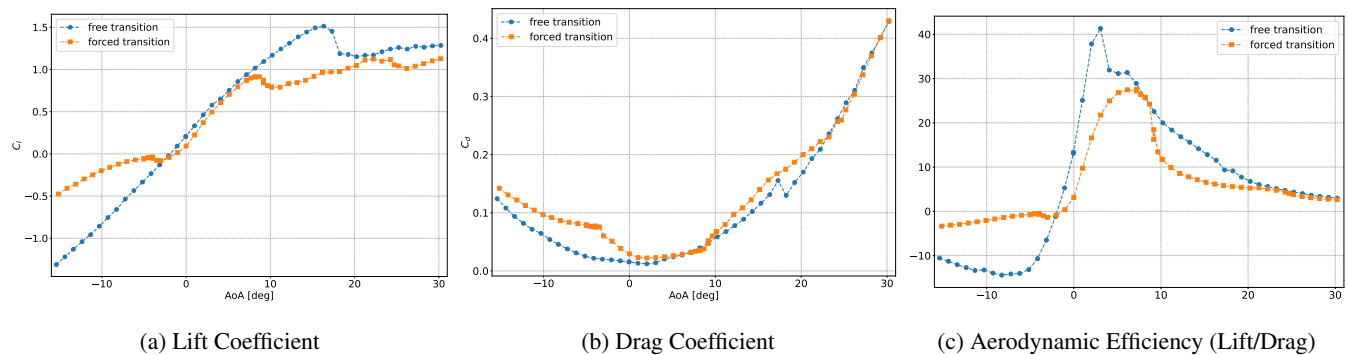
The steady force, moment, and pressure coefficients were corrected for solid and wake blockage using the corrections from Allen and Vincenti (1944), and for wake buoyancy and lift interference (streamline curvature) using the corrections from Garner et al. (1966). The correction procedure is well-documented in literature such as the work of Timmer (2021) and is thus  
 210 left out of this paper for brevity.

The unsteady measurements were corrected for the effects of the tubes connecting the pressure ports to the scanner. The pressure signal at the transducer carries a phase lag and is attenuated in amplitude compared to the pressure signal at the surface of the airfoil due to the air column inside the measurement tubes. The measured pressure signal is corrected for these effects based on the theory of Bergh and Tijdeman (Bergh and Tijdeman, 1965; Boerrigter, 1996) that defines a process to  
 215 determine the response time of a measurement system consisting of pressure tubes and transducers connected in series. It should be noted that the effect of a possibly oscillating air column in the pressure tubes due to the airfoil motion is not included in these corrections. For the current setup, two sets of pressure tubes of diameter 1.8 mm (connected to the model pressure

taps), and diameter 1 mm (connected to the pressure scanner) are used alongside adaptors of inner diameter 0.8 mm to connect both sets of tubes. The larger diameter tubes connected to the model are remnants of the fact that the airfoil model was first  
 220 manufactured for compatibility with an older pressure measurement system that is no longer used in the TU Delft LTT. Both sets of tubes are 90 cm long and the adaptor is 1 cm long. The unsteady measurements could not be corrected for the usual blockage, streamline curvature, and buoyancy effects due to the inability to measure the wake drag during dynamic conditions. The unsteady measurements are thus presented without these corrections.

### 3 Impact of VGs on Steady Behaviour

225 The lift and drag characteristics of the airfoil without VGs in free and fixed transition for a Reynolds number of 1 million are shown in Figure 5. As mentioned in Section 1, the static stall angle of attack, maximum lift coefficient, and lift-to-drag ratio are typically considered the important aerodynamic performance metrics for airfoils used in inboard and mid-board sections of wind turbine blades where VGs are typically placed. In free transition, the airfoil stalls at around  $16^\circ$  angle of attack with a maximum lift coefficient of about 1.6. The aerodynamic efficiency (lift-to-drag ratio) peaks around  $14^\circ$  angle of attack. When  
 230 transition to turbulence is fixed at 5% chord, the airfoil stalls earlier around  $9^\circ$  angle of attack, with the maximum lift coefficient reduced by nearly 40% to 0.95, displaying a strong sensitivity to leading edge roughness.



**Figure 5.** Fixing transition to turbulence with zigzag tape at 5% chord drastically reduces the stall angle and aerodynamic efficiency, indicating the airfoil's strong sensitivity to leading edge roughness.

In the presence of VGs, the lift polars in Figure 6a show VGs delaying stall to a higher angle of attack. As expected from literature (Ashill et al., 2005; Baldacchino et al., 2018), the larger the vane height, the stronger the vortices and the greater the stall delay and maximum lift. The increasing frontal area of the larger VG vanes brings a higher drag penalty due to larger  
 235 vanes even when flow is attached over the airfoil, as seen in Figure 6b. However, since the drag increases drastically when flow separates, the smaller vanes provide a higher peak lift-to-drag ratio but only over a narrow range of angles of attack, while the larger vanes provide a slightly lower peak lift-to-drag ratio but over a wider range of angles of attack, as seen in Figure 6c. Of

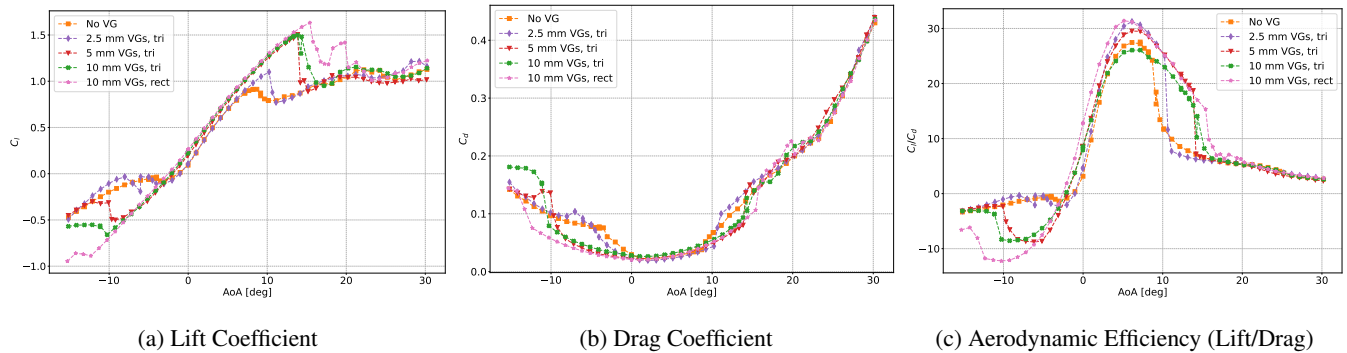
the three sizes of triangular vanes tested, the 5 mm VGs provide the best compromise between significant stall delay from the no-VG case, a high maximum lift, and a lower added drag.

240 Rectangular vanes of 10 mm vane height delayed stall further than triangular vanes of the same size. The rectangular vanes were also observed to generate lower drag when flow is attached. This led to rectangular vanes producing a significantly higher lift-to-drag ratio than triangular vanes of the same size, and even matching the peak lift-to-drag ratio from the smallest triangular vanes. To understand this behaviour, the flow separation characteristics over the suction side of the airfoil was compared for the different vane heights and shapes, by examining the flow separation location (determined as described in Appendix A) with increasing angle of attack in Figure 7. In the no VG case, trailing-edge flow separation gradually progresses upstream towards the leading edge with increasing angle of attack, reaching a chordwise position slightly upstream of 40% chord at the stall angle of attack of  $9^\circ$ . With the addition of VGs, flow separation starts at a higher angle of attack. With the smallest 2.5 mm VGs, separation moves upstream at a slower rate than without VGs until stall at  $10^\circ$  angle of attack, and then at a much faster rate after stall. As the vane height increases, flow separates abruptly as soon as the airfoil stalls, and the separation moves rapidly upstream over the airfoil surface. With the rectangular VGs, separation moves upstream at a slower rate than for triangular VGs of the same size. The rectangular vanes also restrict the flow separation location to be downstream of the VG location ( $x/c = 0.3$ ) for a larger range of angles of attack than the triangular VGs. The airfoil stalls when the separation front reaches slightly upstream of 40% chord. With the addition of VGs, flow separation starts at a higher angle of attack. With the smallest 2.5 mm VGs, the separation front moves upstream at a slower rate than without VGs until the stall angle of attack of 245  $10^\circ$ , indicating energisation of the boundary layer by the streamwise vortices from the VGs. At stall, the separation front moves upstream at a much faster rate, unlike the gradual upstream migration in the no-VG case. Trailing-edge separation appears at a higher angle of attack with VGs of increasing vane height. However, the larger the VG vane, the more abrupt the upstream migration of the trailing-edge separation front leading to stall. The rectangular VGs both delay the appearance of trailing-edge separation and slow down the upstream migration of the separation front than triangular VGs of the same size. The separation front to remains downstream of the VG location ( $x/c = 0.3$ ) up to a higher angle of attack than with the triangular VGs.

The steady measurements indicate that rectangular vanes whose height is larger than the boundary layer height at the VG placement location is the best configuration for both delaying stall and maximising the lift-to-drag ratio. This result is contrary to the conventional recommendations of literature about optimising VG designs that recommend low-profile VG designs with vane heights typically smaller than the local boundary layer thickness for maximising the lift-to-drag ratio. This also goes against the common practice in wind turbine applications of using triangular vanes instead of rectangular vanes due to their perceived lower drag penalty. The superior performance of rectangular vanes in both delaying stall and maximising lift-to-drag ratio indicates that rectangular vanes generate stronger streamwise vortices that energise the boundary layer more effectively than triangular vanes. This hypothesis is supported by the observed slower upstream movement of the flow separation location with increasing angle of attack in presence of rectangular vanes than triangular vanes of the same size. The slower upstream movement of the flow separation location indicates that the boundary layer is more energised and thus better able to withstand a stronger adverse pressure gradient that comes with increasing angle of attack. This result calls for future measurements 270

into airfoil boundary layers at high angles of attack in presence of triangular and rectangular vanes to better understand the differences between the streamwise vortices generated by each vane shape.

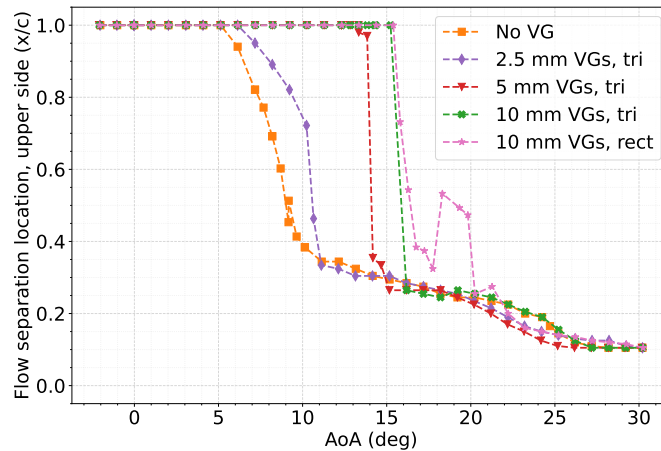
275 The steady measurements indicate that rectangular vanes whose height is larger than the boundary layer height at the VG placement location are the best VGs for delaying both the appearance and the upstream progression of trailing-edge flow separation. As a result, the rectangular vanes provide the largest stall delay, the highest maximum lift, and the highest lift-to-drag ratio before stall among the compared VG configurations. This result is contrary to the conventional recommendation in literature that low-profile VG designs with vane heights smaller than the local boundary-layer thickness provide the best compromise between maximising stall delay and lift-to-drag ratio. The higher lift-to-drag ratio also runs counter to the common  
280 practice in wind turbine applications of using triangular rather than rectangular vanes, due to the perceived lower drag penalty of triangular vanes. The slower upstream progression of trailing-edge separation with rectangular vanes indicates that they energise the boundary layer more effectively than triangular vanes. This result calls for future measurements of airfoil boundary layers at high angles of attack in the presence of triangular and rectangular vanes to better understand the differences in streamwise vortices and turbulent boundary layer interactions for each vane shape.



**Figure 6.** Comparing the stall delay, lift enhancement, drag penalty, and aerodynamic efficiency for different VG heights and shapes.

#### 285 4 Dynamic Stall and VG Effectiveness

For the dynamic cases, we use the normal force coefficient polar and the spatio-temporal evolution of the suction side flow separation location to analyse the unsteady aerodynamic behaviour of the airfoil. Prior works such as McAlister et al. (1982); McAlister et al. investigating the formation and movement of the dynamic stall vortex use the airfoil  $C_p$  distributions and flow separation location as an indicator of dynamic stall vortex location and strength. Following these works, our subsequent analysis of the  
290 dynamic stall vortex evolution on the airfoil surface also uses the spatio-temporal evolution of  $C_p$  and the flow separation location as an indicator of the extent and strength of the stall vortex. Additionally in the presence of VGs, prior works such as Velte and Hansen (2013); Velte and Hansen (2016) have shown that VGs produce streamwise vortices that significantly alter the turbulent boundary layer downstream and prevent flow separation. Thus, in subsequent analysis in this paper, we consider



**Figure 7.** Flow separation location over the suction side of the airfoil with increasing angle of attack for different VG vane heights and shapes. The flow separation location is determined from the pressure distribution over the airfoil surface.

the differences between the spatio-temporal evolution of the flow separation location with and without VGs to be indicative of the energisation of the turbulent boundary layer by the streamwise vortices shed by the VGs, and their impact on the dynamic stall vortex formation and movement.

For the dynamic cases, we use the normal force coefficient polar and the spatio-temporal evolution of the suction side (upper surface) flow separation location to investigate the development of the trailing-edge separation front and the unsteady aerodynamic loading on the airfoil.

#### 4.1 Baseline Airfoil without VGs

The normal force coefficient polar for  $10^\circ \pm 10^\circ$  and all pitching frequencies is shown in Figure 8. The suction side flow separation location for this pitching motion at different phases is shown in Figure 9. Phases 0 to  $\pi$  represent the downstroke motion and phases  $\pi$  to  $2\pi$  represent the upstroke motion. A separation location of  $x/c = 1.0$  implies flow remains attached all over the airfoil upper surface.

The unsteady motion of the airfoil causes the flow around the airfoil to lag behind the instantaneous angle of attack. Trailing edge separation starts around  $7^\circ$  angle of attack during the upstroke motion with  $k = 0.045$  (Figure 9a), close to the steady value of  $6^\circ$  (Figure 7). While the stall vortex is moving upstream (denoted by the flow separation location moving upstream), the airfoil keeps pitching up to higher angles of attack, allowing the normal force coefficient to increase beyond the maximum steady value. Just like the static case, dynamic stall is observed when the flow separation point has moved to  $x/c = 0.4$ , which occurs around  $16^\circ$  angle of attack at  $k = 0.045$ . At  $k = 0.09$ , the faster pitching rate means the stall vortex reaches  $x/c = 0.4$  at an even higher angle of attack of around  $18.5^\circ$  and dynamic stall is delayed further. At  $k = 0.18$ , the flow around the airfoil lags even further behind the airfoil motion, and no flow separation is observed on the airfoil surface throughout the upstroke motion. As the airfoil pitches down, flow starts to reattach and the separation point moves downstream until flow has reattached over

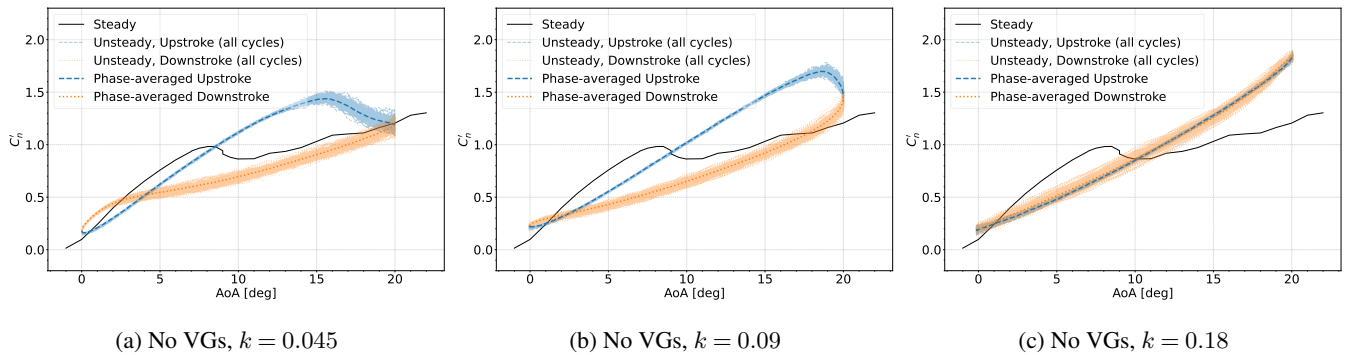
the whole airfoil. Complete reattachment can also be visualised on the normal force coefficient polar when the downstroke curve crosses over the upstroke curve and the downstroke normal coefficient becomes higher than the upstroke value. At  $k = 0.045$ , complete reattachment occurs around  $4^\circ - 3^\circ$  angle of attack. At  $k = 0.09$ , complete reattachment is delayed to around  $3^\circ - 2^\circ$  angle of attack. At  $k = 0.18$ , reattachment never reaches the trailing edge during the downstroke motion, and complete reattachment only occurs close to  $0^\circ - 1^\circ$  angle of attack in the upstroke motion.

The unsteady motion of the airfoil causes the flow around the airfoil to lag behind the instantaneous angle of attack. Trailing-edge separation on the upper surface starts around  $7^\circ$  angle of attack during the upstroke motion with  $k = 0.045$  (Figure 9a), close to the steady value of  $6^\circ$  (Figure 7). While the trailing-edge separation front moves upstream, the airfoil keeps pitching up to higher angles of attack, allowing the normal force coefficient to increase beyond the maximum steady value. Just like the static case, dynamic stall is observed when trailing-edge separation has moved to  $x/c = 0.4$ , which occurs around  $16^\circ$  angle of attack at  $k = 0.045$ . The loss of lift post-stall is gradual as the separation front keeps moving upstream before settling around  $x/c = 0.2$  by  $18^\circ$  angle of attack, where the separation front remains for the rest of the upstroke motion. As the airfoil pitches down, flow starts to reattach and the separation point moves downstream until flow has reattached over the whole airfoil. For  $k = 0.045$ , reattachment starts as soon the downstroke motion begins and complete reattachment occurs around  $4^\circ - 3^\circ$  angle of attack. The downstroke normal force coefficient remains lower than the upstroke value until complete reattachment occurs, after which the downstroke value becomes higher than the upstroke value.

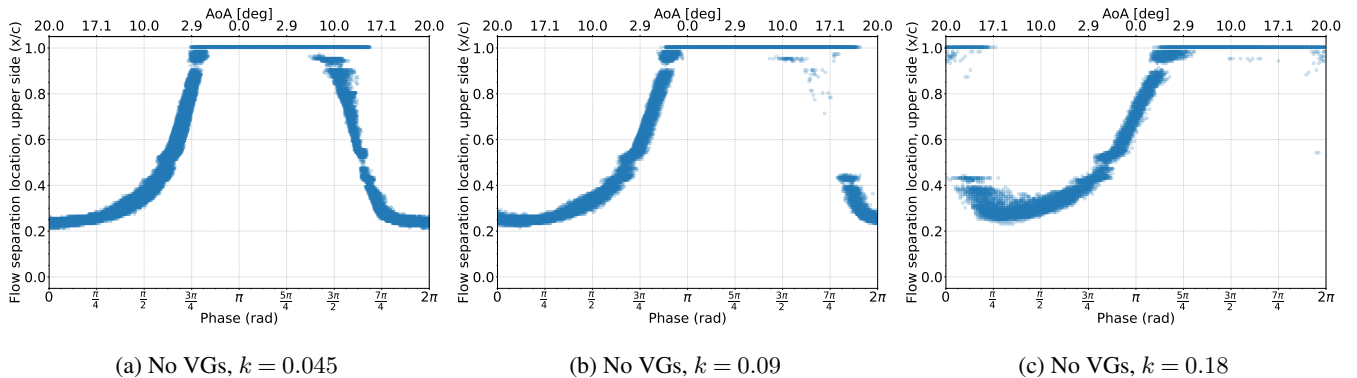
For higher pitching frequencies, the faster pitch rate causes a further lag between the airfoil motion and the flow on the airfoil surface. For  $k = 0.09$ , separation appears abruptly on the airfoil around  $18.5^\circ$  angle of attack and progresses rapidly to  $x/c = 0.4$  by  $19^\circ$  angle of attack. The airfoil already starts to pitch down while the separation front is still moving upstream, and thus the separation front stops slightly upstream of  $x/c = 0.2$  before reattachment starts. For  $k = 0.09$ , reattachment starts only around  $17^\circ$  angle of attack in the downstroke motion, and complete reattachment over the airfoil surface occurs around  $3^\circ - 2^\circ$  angle of attack. For  $k = 0.18$ , the flow around the airfoil lags so far behind the airfoil motion that the trailing-edge separation does not appear during the upstroke motion, but rather during the downstroke motion, around  $17^\circ$  angle of attack. The appearance and upstream progression of the separation front is abrupt and rapid, similar to the  $k = 0.09$  case. Reattachment only starts around  $10^\circ$  angle of attack in downstroke, and complete reattachment only occurs close to  $0^\circ - 1^\circ$  angle of attack upstroke.

#### 4.2 Influence of VGs and effect of vane height variation

To assess the impact of VGs on the unsteady aerodynamic behaviour, we first vary the VG vane height. The normal force coefficient polars for the different vane heights at various pitching frequencies are shown in Figure 10 and the flow separation location over the suction side of the airfoil is shown in Figure 11. For the smallest 2.5 mm VGs ( $h_{VG}/\delta < 1$  at AoA  $0^\circ$ ), the normal force coefficient polars (Figures 10a to 10c) are similar to the baseline case without VGs, with only a slight increase in the maximum normal force coefficient and a small delay in dynamic stall onset by about  $1^\circ$  in the upstroke motion. This is in line with the steady stall trend, which is delayed by about  $1.5^\circ$  when the 2.5 mm VGs are added. Comparing the movement of the stall vortex through the flow separation location (Figures 11a to 11c) shows that the stall vortex advances



**Figure 8.** Normal force coefficient polars for the  $10^\circ \pm 10^\circ$  pitching motion in absence of VGs.



**Figure 9.** Flow separation location on the suction side over 150 pitching cycles of  $10^\circ \pm 10^\circ$  in the absence of VGs.

from the trailing edge to a similar chordwise location as the baseline airfoil case without VGs in the upstroke motion. Due to the presence of VGs, reattachment during the downstroke motion also occurs slightly earlier than the no-VG case. This indicates that the streamwise vortices shed by the 2.5 mm VGs are not strong enough to significantly weaken the stall vortex or prevent its upstream movement once formed. For the slowest pitching frequency  $k = 0.045$ , trailing-edge separation starts around  $12^\circ$  angle of attack (Figure 11a) upstroke as opposed to  $7^\circ$  observed in the steady case. However, the separation front progresses upstream rapidly. As with the no-VG case, the airfoil stalls when the separation front reaches around  $x/c = 0.4$ , which occurs around  $17^\circ$  angle of attack. While the VGs delay the onset of trailing-edge separation, the upstream progression of the separation front is even more rapid than the no-VG case, and hence, dynamic stall is delayed by only about  $1^\circ$  by the 2.5 mm VGs. Reattachment during the downstroke motion starts around  $17^\circ$ , which is later than the no-VG case. But the reattachment progresses faster than the no-VG case and complete reattachment occurs around  $5^\circ - 4^\circ$  angle of attack, which is slightly earlier than the no-VG case. When pitched at higher frequencies of  $k = 0.09$  (Figure 11b) and  $k = 0.18$  (Figure 11c), the onset of trailing-edge separation gets delayed further and the upstream progression of the separation front upstream is even more rapid and abrupt, establishing a similar trend as the no-VG case. The VGs do restrict the ultimate upstream location of

the separation front to around  $x/c = 0.25$ , which is slightly further downstream than the no-VG case where the separation front settles around  $x/c = 0.2$ . Thus, while the smallest VGs energise the boundary layer enough to delay the onset of trailing-edge separation and speed up the reattachment process once started, they are not effective enough to significantly alter the overall unsteady aerodynamic behaviour of the airfoil.

365 The larger 5 mm VGs ( $h_{VG}/\delta \approx 1$  at AoA  $0^\circ$ ) and 10 mm VGs ( $h_{VG}/\delta > 1$  at AoA  $0^\circ$ ) produce stronger vortices in steady conditions and show a more pronounced impact on the unsteady aerodynamic behaviour. From the normal coefficient polars (Figures 10d to 10i) both these VGs suppress dynamic stall in upstroke half of the  $10^\circ \pm 10^\circ$  motion. Examining the flow separation location in the upstroke half (Figures 11d to 11i) shows that the 5 mm VGs restrict the stall vortex to  $x/c \approx 0.7 - 0.6$  at  $k = 0.045$ , and the 10 mm VGs prevent flow separation altogether. At higher reduced frequencies, the lag in the flow response  
370 means that the stall vortex is restricted to even further downstream locations.

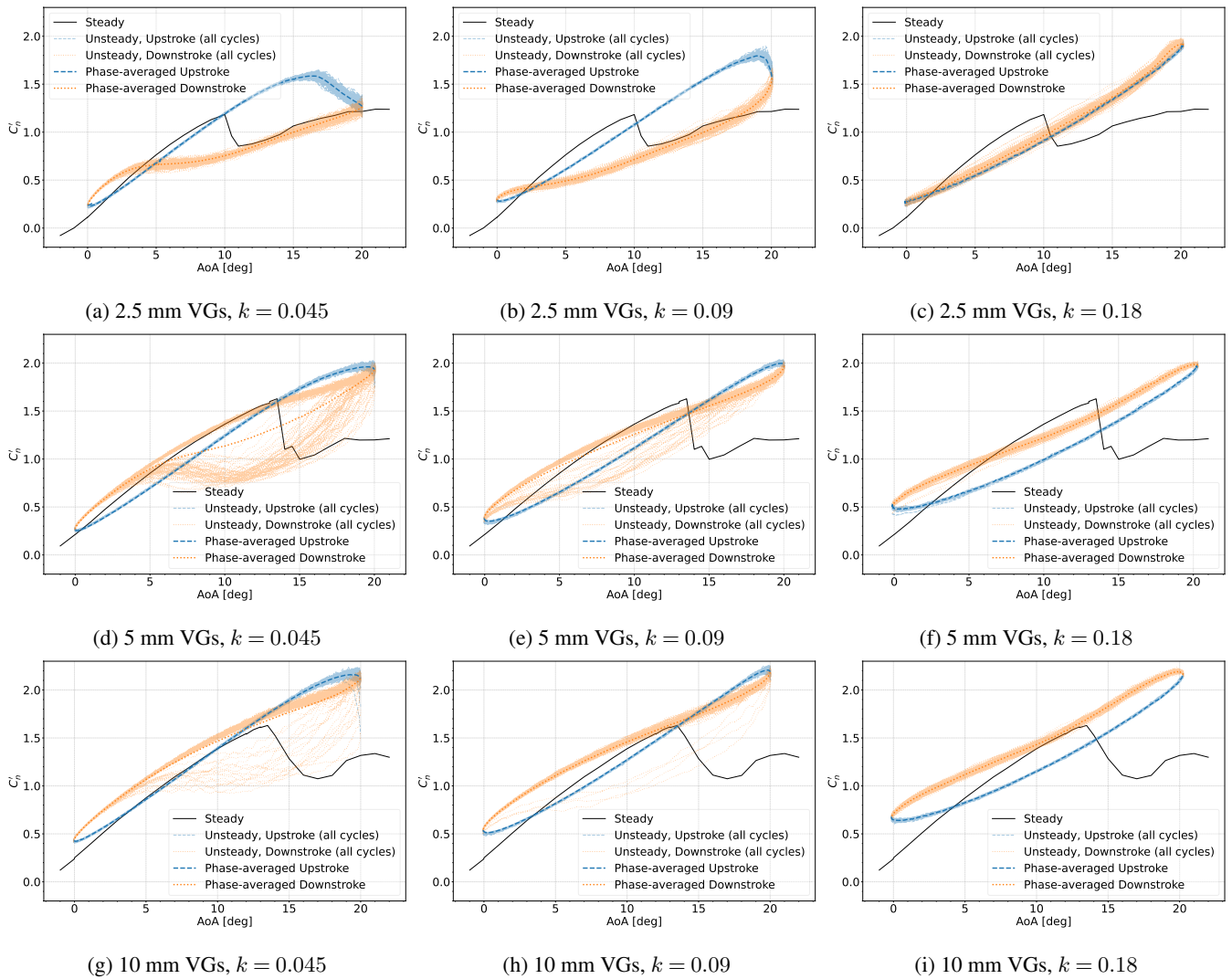
In the downstroke half of the pitching motion, the normal force coefficient polar tends to follow 2 distinct paths moving between an early or a late reattachment. For the 5 mm VGs at  $k = 0.045$  (Figure 10d), flow reattaches either around  $13^\circ - 12^\circ$  in the early reattachment path or around  $8^\circ - 5^\circ$  in the delayed reattachment path. The flow separation location plot (Figure 11d) shows that in the downstroke motion, the stall vortex either moves downstream as the airfoil pitches down, or it first moves  
375 upstream before moving downstream again. For a majority number of cycles, the stall vortex moves from its ultimate upstroke location of  $x/c \approx 0.7 - 0.6$  towards the trailing edge and flow reattaches early. However, in some cycles, the stall vortex continues to move upstream to  $x/c \approx 0.2$  till around  $10^\circ$  angle of attack before moving back downstream towards the trailing edge. Nevertheless, even in the late reattachment path, the reattachment angle  $8^\circ - 5^\circ$  is still higher than the reattachment angle for the no-VG case, which reattaches at  $4^\circ - 3^\circ$ . This provides further evidence towards the interaction between the streamwise  
380 vortices shed by the VGs and the stall vortex, and indicates that the stronger streamwise vortices shed by the 5 mm VGs can weaken the stall vortex more than the 2.5 mm VGs, but are not strong enough to prevent the upstream movement of the stall vortex in some cycles. At a higher reduced frequency of  $k = 0.09$  (Figure 11e), the stall vortex moves upstream of  $x/c \approx 0.6$  during the downstroke motion in a fewer number of cycles. The reattachment angle of attack for the late reattachment path is around  $5^\circ - 4^\circ$ , which is lower than the reattachment angle for  $k = 0.045$  but still higher than the no-VG case, which reattaches  
385 at  $3^\circ - 2^\circ$ . At the highest reduced frequency  $k = 0.18$  (Figure 11f) the stall vortex never moves beyond  $x/c \approx 0.6$  and always moves back downstream from  $x/c \approx 0.6$  towards the trailing edge as the airfoil pitches down. Thus, at the higher reduced frequencies as the airfoil pitches faster, the shed vortices from the VGs have less time to interact with the stall vortex and influence the overall flow around the airfoil, reducing the tendency of flow around the airfoil to separate.

The larger 5 mm VGs ( $h_{VG}/\delta \approx 1$  at AoA  $0^\circ$ ) energise the boundary layer more than the 2.5 mm VGs and hence have a  
390 more pronounced impact on the unsteady aerodynamic behaviour. At the slowest pitching frequency  $k = 0.045$  (Figure 11d), trailing-edge separation only starts around  $15.5^\circ$  angle of attack during the upstroke motion. The upstream progression of the separation front is gradual and not abrupt like the 2.5 mm VGs case. Flow separation only reaches around  $x/c = 0.7 - 0.6$  before the airfoil starts pitching down and stall does not occur (Figure 10d). In the downstroke half of the pitching motion, the normal force coefficient polar and the separation front progression tend to follow 2 distinct paths — either an early reattachment  
395 path or a late reattachment path. In the early reattachment path, the separation front starts moving downstream as the airfoil

400 pitches down. Reattachment is completed around  $14^\circ - 13^\circ$  angle of attack. In the late reattachment path, the separation front first abruptly jumps upstream to  $x/c = 0.4$  and continues to move upstream to around  $x/c = 0.2$  before starting a downstream motion at  $10^\circ$  angle of attack. Reattachment is faster in the the late reattachment path and complete reattachment occurs between  $8^\circ - 5^\circ$  angle of attack. At the higher pitching frequency of  $k = 0.09$  (Figure 11e), trailing-edge separation starts later at around  $17^\circ$  upstroke. The separation front progresses upstream to  $x/c = 0.6$  at nearly the same rate as the  $k = 0.045$  case. This is a departure from the no-VG and 2.5 mm VGs cases, where upstream progression of the separation front became more rapid and abrupt as the pitching frequency increased. The increased lag due to higher frequency means reattachment starts later than the  $k = 0.045$  case. Once again, the separation front and normal force coefficient polar follow either an early reattachment path or a late reattachment path during the downstroke motion. Complete reattachment occurs around  $16^\circ - 14^\circ$  angle of attack in the early reattachment path, and around  $5^\circ - 4^\circ$  angle of attack in the late reattachment path. From the normal force coefficient polar (Figure 10e), fewer number of cycles follow the late reattachment path compared to the  $k = 0.045$  case. This is evident from the mean curve mostly following the early reattachment path for  $k = 0.09$ , while the mean curve lies in between the early and late reattachment paths for  $k = 0.045$ . For the highest frequency  $k = 0.18$ , trailing-edge separation only starts when the airfoil has started to pitch down (Figure 11f) and there are almost zero cycles with late reattachment (Figure 10f). 410 The existence of the late reattachment path and the sudden upstream movement of the separation front in some cycles indicates that the boundary layer energisation provided by the 5 mm VGs is not effective enough. The boundary layer is susceptible to separation in the region around the VGs ( $x_{VG}/c = 0.3$  in this case), particularly at lower pitching frequencies where the flow has more time to react to the change in angle of attack.

415 ~~The larger 10 mm VGs shed stronger vortices that prevent flow separation in the upstroke motion at all reduced frequencies (Figures 11g to 11i). In the downstroke motion, fewer cycles revert to a separated state compared to the 5 mm VGs. The reattachment angle of attack in the separated flow path is approximately  $8^\circ - 5^\circ$ , the same range as the 5 mm VGs. As with the trend noticed for the 5 mm VGs, the number of cycles that revert to a separated state decreases with increasing reduced frequency, disappearing altogether at  $k = 0.18$  (Figure 11i).~~

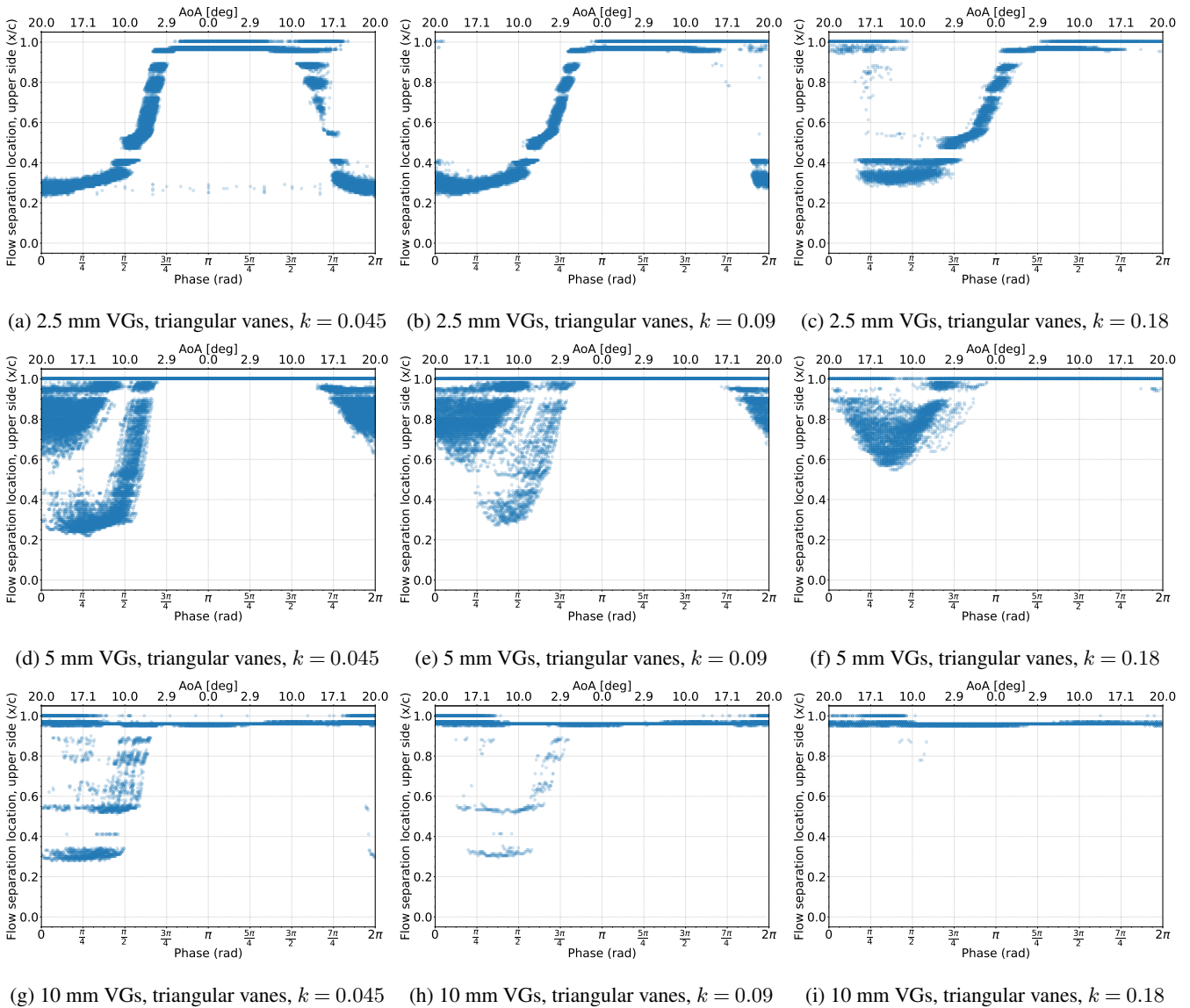
420 With the largest 10 mm VGs ( $h_{VG}/\delta > 1$  at AoA  $0^\circ$ ), trailing-edge separation is greatly reduced due to more effective energisation of the boundary layer by the VGs. With  $k = 0.045$  (Figure 11g), separation only appears in the downstroke phase and is limited to near the trailing edge. Late reattachment cycles where the separation front suddenly moves upstream are far fewer than the 5 mm VGs case. The mean normal force coefficient curve closely follows the early reattachment path (Figure 10g). The angle of attack for complete reattachment in the late reattachment path is around  $8^\circ - 5^\circ$ , the same range as the 5 mm VGs. Trailing-edge separation nearly disappears at  $k = 0.09$ , only observed in pitching cycles which follow the separated flow late reattachment path. At  $k = 0.18$ , trailing-edge separation is completely prevented in all pitching cycles 425 (Figure 11i). In line with the trend observed for the 5 mm VGs, the number of cycles which enter the late reattachment state decreases with increasing reduced frequency, disappearing altogether at  $k = 0.18$  (Figures 10g to 10i).



**Figure 10.** Normal force coefficient polars when the airfoil equipped with triangular VGs of various vane heights is pitching  $10^\circ \pm 10^\circ$ . The polars oscillate between two reattachment curves in the downstroke phase. The number of later reattaching cycles reduces with increasing pitching frequency, and the later reattaching cycles virtually disappear for the highest pitching frequency.

### 4.3 VG Vane Shape: Triangular vs. Rectangular

430 For the steady case in Section 3, rectangular vane VGs proved better than triangular vanes of the same size because they delayed stall further with a higher maximum lift, while also generating lower drag leading to a higher lift-to-drag ratio than the triangular vanes. The rectangular vanes restricted the trailing edge flow separation from moving upstream of the VG location up to a much higher angle of attack, even after stall, than triangular vanes of the same size, indicating **more effective energisation**

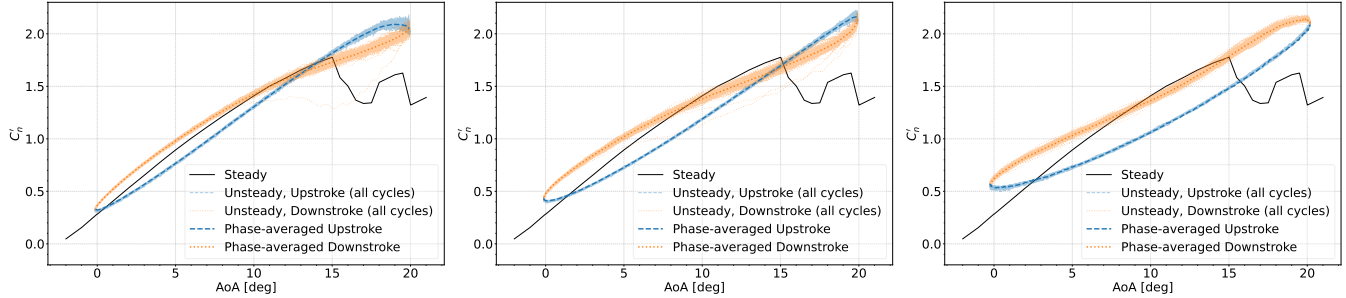


**Figure 11.** Flow separation location on the suction side over 150 pitching cycles of  $10^\circ \pm 10^\circ$  when the airfoil is equipped with triangular vane VGs of three different vane sizes.

of the airfoil boundary layer stronger vortices that persist longer in the airfoil boundary layer at higher pressure gradients. For unsteady conditions, the normal force coefficient polar with rectangular vane VGs for the  $10^\circ \pm 10^\circ$  pitching motion at various pitching frequencies is shown in Figure 12 and the flow separation location over the suction side of the airfoil is shown in Figure 13. The late reattachment cycles observed with the triangular vane VGs in the downstroke motion (Figures 10g and 10h) are virtually absent with the rectangular vane VGs. Besides this, the variation between cycles in the normal force

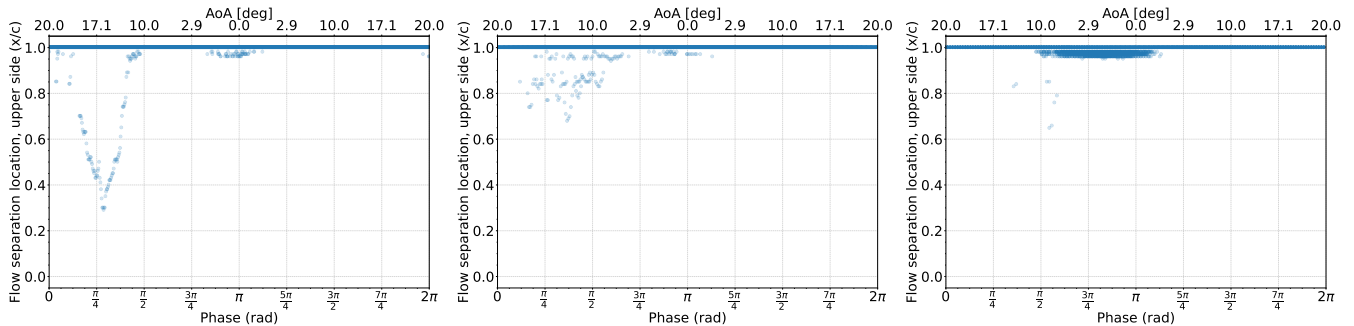
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coefficient polar is also slightly lower for rectangular vanes compared to triangular vanes. Both vane shapes prevent flow separation in the upstroke half of the pitching motion. Unlike triangular vanes where flow separation appears in the downstroke half (Figures 11g and 11h), there is barely any separation observed with rectangular vanes. This reinforces the observation from the steady case that the rectangular vane VGs ~~generate stronger streamwise vortices that~~ are more effective at keeping flow attached to the airfoil surface.



(a) 10 mm VGs, rectangular vanes,  $k = 0.045$  (b) 10 mm VGs, rectangular vanes,  $k = 0.09$  (c) 10 mm VGs, rectangular vanes,  $k = 0.18$

**Figure 12.** Normal force coefficient polars when the airfoil equipped with triangular and rectangular VGs of the same vane size is pitching  $10^\circ \pm 10^\circ$ .



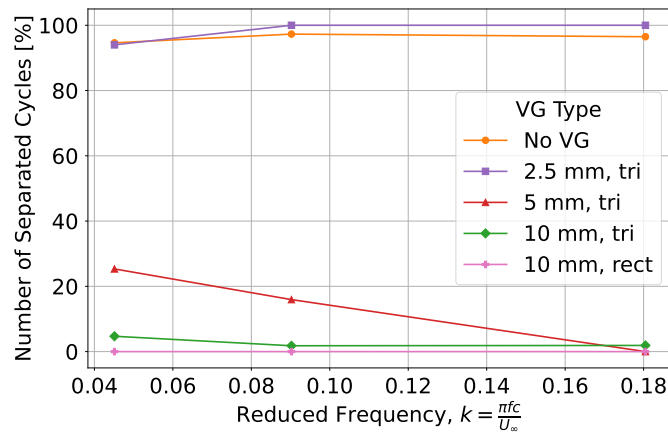
(a) 10 mm VGs, rectangular vanes,  $k = 0.045$  (b) 10 mm VGs, rectangular vanes,  $k = 0.09$  (c) 10 mm VGs, rectangular vanes,  $k = 0.18$

**Figure 13.** Flow separation location on the suction side over 150 pitching cycles of  $10^\circ \pm 10^\circ$  angle of attack when the airfoil is equipped with rectangular vane VGs.

## 5 Outlook on VG design for unsteady flow separation control

To quantify the ability of the different VGs to keep flow attached, we compare the percentage of attached cycles at the mean angle of attack  $10^\circ$  in the downstroke motion of  $10^\circ \pm 10^\circ$  in Figure 14.  $10^\circ$  also lies between the reattachment angles of the early and late reattachment paths for all VGs, making it a suitable angle for this comparison.

The existence of different paths in the normal force coefficient polar and the trailing-edge separation front progression for the 5 mm and 10 mm triangular VGs points to the existence of cycle-to-cycle variations due to insufficient energisation of the boundary layer by the VGs. This insufficient energisation makes the flow around the airfoil susceptible to separation. Not only does this delay reattachment over the airfoil surface lowering the aerodynamic performance, but the constant switching between attached and separated states also lowers the fatigue lifetime of the blade section due to the cycle-to-cycle variance. The number of cycles following the late reattachment path for each VG design is presented in Figure 14. To quantify the number of late reattachment cycles, we calculate the percentage of cycles where flow over the airfoil is separated at  $x/c = 0.5$  at  $10^\circ$  downstroke angle of attack. As we observed in Sections 4.2 and 4.3, it is only in the late reattachment cases that the separation front goes beyond  $x/c = 0.6$ .  $10^\circ$  downstroke lies between the reattachment angles of the early and late reattachment paths for all VGs, making it a suitable angle for this comparison. Note that the early and late reattachment paths are only observed for the 5 mm triangular, 10 mm triangular, and 10 mm rectangular VG cases. Thus, the number of separated cycles for these cases represents the cycles where the VGs fail to prevent upstream propagation of the separation front resulting in the late reattachment path. For the no-VG and 2.5 mm triangular VG cases, the flow separation map and normal force coefficient polar follow only one path, and hence nearly 100% of the cycles are separated. In Sections 5.1 and 5.2 we discuss the implications of the number of cycles with late reattachment for different VG designs for unsteady flow separation and dynamic stall control.



**Figure 14.** Number of ~~separated~~ ~~attached~~ cycles at  $10^\circ$  downstroke when pitching  $10^\circ \pm 10^\circ$  at all tested pitching frequencies with various VGs.

## 5.1 Vane Size

As mentioned in Section 1, past studies have assumed that an optimal VG design in steady conditions will be sufficient for unsteady flow separation control applications. From the steady results of this study (Section 3), using the metric of balancing the delay in stall angle of attack and the increase in maximum lift with a minimal increase in drag, the 5 mm VGs would be the optimal choice among the triangular vane VGs. However, the unsteady results in Section 4.2 showed that the 5 mm

VGs cannot prevent flow separation and upstream movement of the stall vortex in 100% of the cycles of the pitching motion, keeping flow attached for only 75% of the cycles during the downstroke phase at a reduced frequency of  $k = 0.045$ . This led to two distinct reattachment paths in the normal force coefficient polar, increasing the variance of the unsteady aerodynamic forces between cycles. The likelihood of flow separation has a negative impact on the cyclic loading of a wind turbine blade and can lead to early fatigue failure. Despite being less desirable in steady conditions due to their higher drag, the 10 mm VGs were able to keep flow attached for about 95% of the cycles at  $k = 0.045$ , nearly eliminating the likelihood of flow separation and late reattachment. Thus in unsteady conditions, with the goal of preventing flow separation, the larger 10 mm VGs are a better choice than the 5 mm VGs. Smaller low-profile vane designs that are recommended for steady flow separation control in past literature are not sufficient for unsteady separation control. It is known for steady conditions that the greater the vane height, the stronger the streamwise vortices produced by the VGs. Since the unsteady flow separation results are indicative of the location and extent of flow reversal on the airfoil, they can be used to infer the effect of the VG vortices interacting with the upstream spread of flow reversal. Larger vane heights preventing flow separation for a greater percentage of pitching cycles can thus be attributed to the stronger vortices produced by larger vanes keeping the flow reversal in check. Thus, when the airfoil is pitching in and out of the static stall region, the stronger the vortices produced by the VGs, the greater the percentage of cycles where flow separation is prevented.

At higher frequencies, both the 5 mm and 10 mm VGs tend towards a larger percentage of attached flow pitching cycles, while the 2.5 mm VGs cannot prevent flow separation at all. This is attributed to a pitching rate effect which is well known in literature, rather than a VG effect. When the pitching rate is increased to higher reduced frequencies, the flow around the airfoil becomes less likely to separate since the angle of attack changes faster than the flow around the airfoil can react. Even if flow separation does appear at the trailing edge, the flow still lags far behind the motion of the airfoil and is forced to reattach quicker as the angle of attack decreases. Thus, if a wind turbine blade designer expects faster changes in angle of attack, then the objective of keeping flow attached is less sensitive to a careful choice of VG vane height due to the inherent tendency of the flow to remain attached at higher pitching frequencies.

In Section 4.2, we observed that the 2.5 mm VGs only energise the boundary layer enough to delay the onset of trailing-edge separation by a few degrees compared to the no-VG case, but cannot restrict the upstream movement of the separation front after stall. The 5 mm VGs can both delay the onset of trailing-edge separation and restrict the upstream movement of the separation front to about 60% chord once it appears, but not for 100% of the pitching cycles. The boundary layer is still prone to separation and the separation front can make a sudden upstream movement in some pitching cycles, settling at about 20% chord. This tendency to separate in some cycles creates early and late reattachment paths, increasing the variance of aerodynamic forces over pitching cycles. At the lowest frequency  $k = 0.045$  when the flow has the most time to react to the airfoil motion, the 5 mm VGs only restrict the separation front for 75% of the pitching cycles i.e. 25% cycles follow the late reattachment path (Figure 14). As the flow response time decreases with increasing pitching frequency, the airfoil boundary layer becomes less prone to separation. The separation front gets restricted for 85% of the cycles at  $k = 0.09$  and 100% of the cycles at  $k = 0.18$ . The 10 mm VGs restrict the separation front for 95% of the cycles at  $k = 0.045$  and nearly 100% of the cycles at  $k = 0.09$  and  $k = 0.18$ .

Based on the expected rate of change in angle of attack on the blade, the choice of VG vane height to prevent flow separation in unsteady conditions becomes more or less critical. For slower changes in angle of attack, VGs with larger vane heights would be prevent flow separation for a greater percentage of the pitching cycles. For faster changes in angle of attack, the choice of VG vane height is less critical because the flow around the airfoil is less prone to separation. Of the three vane heights tested in this work, choosing a suitable vane height based on steady criteria would have yielded the 5 mm VGs as the optimal choice because they optimise the stall delay and maximum lift increase with a lower drag increase. However, neither the 2.5 mm VGs nor the 5 mm VGs would be a suitable choice in unsteady conditions since they cannot sufficiently energise the boundary layer to prevent trailing-edge separation for a significant percentage of pitching cycles.

To aid wind turbine blade designers in selecting a suitable vane height for unsteady flow separation control, we use the boundary layer thickness at the VG location as a reference length scale to compare the vane heights. In Figure 3, we calculated the steady boundary layer thickness at the VG location ( $x/c = 0.3$ ) using RFOIL. Note that the cycles of flow separation and reattachment due to the pitching motion can cause the instantaneous local boundary layer thickness and its evolution to vary slightly between pitching cycles and deviate from the steady value. Nevertheless, the ease of calculating the steady boundary layer thickness still makes it a useful reference length scale for preliminary VG vane height selection. Comparison of vane height with the boundary layer thickness also helps to translate the results of this study to other chordwise placement locations not tested in this study. Assuming that the incoming boundary layer upstream of the VG location does not change significantly between the no-VG and VG cases, we can divide the range of angles of attack covered in the  $10^\circ \pm 10^\circ$  pitching motion into two regions based on whether the vane height is larger or smaller than the incoming boundary layer thickness. From Figure 3, the 10 mm vanes are larger than the steady boundary layer thickness till  $15^\circ$  angle of attack, the 5 mm vanes till  $1^\circ$ , and the 2.5 mm vanes are always smaller than the boundary layer thickness within the calculated angle of attack range. The flow separation results show that the greater the percentage of the pitching cycle where the vane height is higher than the incoming boundary layer height, the greater the likelihood of preventing flow separation during the pitching cycle. If a wind turbine blade designer desires to keep flow attached in all pitching cycles during unsteady conditions with VGs, the vane height should be designed to be larger than the local steady boundary layer thickness for as much of the operating angle of attack range as possible.

## 5.2 Vane Shape

As mentioned in Section 1, the choice of an optimal VG vane shape between triangular and rectangular vanes is still an open question in literature. Some literature recommended the use of triangular vanes over rectangular vanes due to the expected higher drag of rectangular vanes in steady conditions. The steady results of this study in Section 3 showed that rectangular vane VGs are already a better choice than triangular vanes of the same size in steady conditions energise the boundary layer more effectively than triangular vane VGs in steady conditions, delaying the onset of trailing-edge separation and slowing down the upstream progression of the separation front with increasing angle of attack. Rectangular vanes are were both able to delay static stall to a higher angle of attack with a higher maximum lift, while also generating lower drag leading to a higher lift-to-drag ratio than the triangular vanes. The slower upstream movement of the trailing edge flow separation with

535 ~~rectangular vanes in steady conditions indicated that they produced stronger vortices that persisted in the airfoil boundary layer at higher pressure gradients.~~

The outperformance of rectangular vane VGs over triangular vane VGs continued in unsteady conditions. Rectangular vane VGs kept the flow attached for 100% of the cycles at all the tested pitching frequencies, virtually eliminating the likelihood of separated flow during the  $10^\circ \pm 10^\circ$  pitching motion. The near absence of flow separation with rectangular vanes throughout the pitching cycle further reinforces the inference from the steady results that rectangular vanes ~~energise the boundary layer more effectively produce stronger streamwise vortices~~ than triangular vanes of the same size. ~~Combining the results from the VG vane height and vane shape comparisons, for~~ For a wind turbine blade designer aiming to prevent flow separation in unsteady conditions, rectangular vane VGs with height larger than the local boundary layer thickness would be the optimal choice among the VG designs described in this work.

## 545 **6 Sources of uncertainty**

One of the central recommendations of this paper is that VGs selected for unsteady flow control during pitching motions should have a vane height larger than the local boundary layer thickness for as much of the pitching angle of attack range as possible. The reference used for this is the steady no-VG boundary layer thickness at the VG chordwise location calculated using RFOIL. While RFOIL calculations come with their own uncertainties quantified in literature (van Rooij, 1996; Sahoo et al., 2024a), using the steady no-VG boundary layer thickness as a reference for preliminary VG vane height selection also comes with limitations. During pitching motions, the flow around the airfoil depends on various factors like the phase of motion (upstroke or downstroke) and the pitching frequency which leads how the flow responds to the motion. Cycles of flow separation and reattachment due to the pitching motion can cause the instantaneous boundary layer thickness and its unsteady characteristics to deviate from the steady characteristics calculated from RFOIL. This can cause the exact range of angles of attack in the pitching cycle where the vane height is larger than the local boundary layer thickness can deviate from the range presented in this work. In an attempt to provide practical VG design recommendations while overcoming this limitation, our analysis is statistical in nature. We base our comparisons of VG vane height and shape on their impact on the percentage of separated and attached flow cycles. The greater the range of angles of attack in the pitching cycle where the vane height is larger than the local boundary layer thickness, the greater the likelihood of preventing flow separation during the pitching cycle. Overall, the recommendation of this paper is to use larger rectangular VGs considering the need for unsteady flow separation control even when smaller triangular VGs may prove sufficient for steady flow control.

Some other uncertainties in the data arise from the measurement setup itself. Particularly for the unsteady results, we base our analysis on quasi-2D chordwise pressure coefficient distributions. The angled placement of the pressure ports (described in Section 2.4), which covers the spanwise length of at least 1 VG pair for every VG design tested, can average over the spanwise periodic flow variations caused by the vortices from the counter-rotating VGs. However, unsteady trailing-edge separation is 3D and the spanwise variation in flow due to separation cannot be covered by the pressure ports. This can lead to some uncertainty in predicting the exact chordwise location of the separation front from the measured pressure data. The relatively

low aspect ratio of the wing section means that the boundary layer growing on the top wall of the wind tunnel can also introduce spanwise variation in the flow, affecting the pressure measurements. These sources of uncertainty mean that the conclusions of this work should rather be interpreted in context of the general trends in the flow separation behaviour and aerodynamic polars in presence of different VG designs.

## 7 Conclusions

Past literature and industrial practice on designing vortex generators for wind turbine blades have assumed that the optimal VG designs for steady conditions will also perform optimally in unsteady conditions. This paper presents arguments against that hypothesis by showing that VGs that prevent steady flow separation can still allow unsteady flow separation in a significant portion of the pitching cycles. Variations in the onset and progression of separation lead to significant variations in aerodynamic loads between cycles, which can reduce the fatigue lifetime of the blade section and detrimentally impact the aerodynamic damping on structural vibrations. To demonstrate this, we use wind tunnel measurements in the TU Delft Low Speed Tunnel on a DU-97-W-300 airfoil section, a typical representative in terms of aerodynamic performance of mid-board and inboard sections of modern wind turbines, equipped with various VG array designs. The airfoil is subjected to pitching motions that pitch the airfoil above and below into and out of the static stall angle of attack region in presence of VGs with various pitching frequencies for 150 pitching cycles. Transition to turbulence is fixed using zigzag tape close to the leading edge to simulate the effect of leading edge erosion often experienced in wind turbine blades where VGs are used. The forces on the airfoil are calculated using surface pressure measurements (and wake rake measurements for the steady cases). The VGs were fixed at 30% chordwise location to simplify the test matrix, and also owing to the fact that 30% chord has been shown to be the most effective VG location for this airfoil. The results of VG design selection are contextualised with local steady boundary layer development with increasing angle of attack to translate the results to other VG placement locations not covered by this study. Primarily, the VG vane size and vane shape have been varied to investigate their impact on steady and unsteady flow separation control and the onset of static and dynamic stall.

In steady conditions, the rectangular vane VGs of the largest vane size proved to be the optimal choice for both delaying static stall and maximising the lift-to-drag ratio. This is in contrast to the recommendations from literature to opt for low-profile VGs that need to balance the delayed stall with the drag penalty to maximise the lift-to-drag ratio. While the recommendations from literature held true for triangular vane VGs, the rectangular vane VGs produced both a delayed stall and a smaller drag penalty than their triangular counterparts with the same vane size. Tracing the onset of flow separation from the surface pressure distributions indicated that rectangular vanes caused a slower upstream movement of the trailing edge flow separation than triangular vanes, which could be inferred as the rectangular vanes generating stronger streamwise vortices that energise the boundary layer more effectively to withstand stronger adverse pressure gradients.

In steady conditions, triangular vane VGs followed the expected trend from literature, where both the angle of attack of trailing-edge separation onset and the added drag simultaneously increase with vane height, resulting in the selection of an optimal vane height to balance the trade-off between delayed stall and a high lift-to-drag ratio. In this study, the VGs with

vane height approximately equal to the local boundary layer thickness at  $0^\circ$  angle of attack (i.e. the 5 mm vanes) provided this optimal balance. However, when considering both vane height and vane shape, rectangular vane VGs whose vane height is larger than the local boundary layer thickness at  $0^\circ$  angle of attack (i.e. the 10 mm vanes) outperformed all other VG designs by both delaying trailing-edge separation onset (and hence static stall too) and producing a smaller drag penalty than even the smallest triangular VGs tested. This is contrary to recommendations from literature to opt for low-profile triangular VGs, and indicates that rectangular vane VGs overall energise the boundary layer more effectively than triangular vane VGs.

When pitching, the baseline airfoil without VGs encounters dynamic stall when the stall vortex moves to about 40% chord from the leading edge, indicated by a sharp drop in the normal force coefficient. The presence of VGs delays dynamic stall, but only significantly prevents flow separation when VGs of vane height equal to or greater than the local boundary layer thickness at the minimum angle of attack of the pitching motion (i.e. the 5 mm and 10 mm vanes in this study) are used. The 5 mm vanes can only prevent the upstream propagation of the stall vortex for 75% of the cycles at the lowest pitching frequency, resulting in two distinct early reattachment and late reattachment modes in the downstroke phase depending on whether the flow remains attached or separates. The number of late reattachment cycles significantly affects the mean normal coefficient and brings large variations in the loads between consecutive cycles. These load variations can detrimentally impact the aerodynamic damping on structural vibrations and reduce the fatigue lifetime of the blade section. The larger 10 mm vanes prevent flow separation for 95% of the cycles for the same pitching motion, reducing the chances of load variations on the wind turbine blade section. The overall results show that the greater the chance that the vane height exceeds the local boundary layer thickness during the oscillation cycle, the more likely the VGs are at preventing unsteady flow separation. Tracing the movement of unsteady flow separation over the airfoil surface indicates that the larger VGs are more effective at restricting the upstream movement of separated flow, which was inferred to be due to the stronger streamwise vortices generated by the larger VGs. Thus, low-profile triangular vane VG designs recommended for steady conditions due to their optimal lift-to-drag ratio can be insufficient to suppress unsteady flow separation in all pitching cycles. At faster pitching motions, flow around the airfoil has a lower tendency to separate and the objective of preventing flow separation becomes less sensitive to the VG vane size.

In unsteady cases too, rectangular vanes of equal height performed better than triangular vanes, yielding a full suppression of flow separation at all tested pitching frequencies. Not only did the rectangular vanes prevent unsteady flow separation for all cycles, they also produced a slightly lesser variation in the normal coefficient between consecutive attached cycles than the triangular vanes. While literature has often focused on triangular vane shapes for wind turbine applications, the superior performance of rectangular vanes in this study warrants further investigation and adoption for wind turbine applications.

When pitching, only VGs whose vane height exceeds the local boundary layer thickness for a significant portion of the pitching cycle (i.e. the 10 mm vanes in this study) energised the boundary layer enough to significantly delay the onset of trailing-edge flow separation and prevent upstream propagation of the separation front (thus preventing dynamic stall) for more than 90% of the pitching cycles at all pitching frequencies. The smaller 5 mm vanes, whose boundary layer energisation was considered sufficient in steady conditions to optimally balance static stall delay with lift-to-drag ratio, could only prevent flow separation for 75% of the cycles at the lowest pitching frequency, resulting in two distinct flow separation maps and two distinct

paths of early and late reattachment in the normal force coefficient polars. For 25% of the pitching cycles, flow separated over a significant portion of the airfoil surface to cause a large drop in the normal force coefficient. These large variations between cycles can detrimentally impact the aerodynamic damping on structural vibrations and reduce the fatigue lifetime of the blade section. The overall results show that the greater the chance that the vane height exceeds the local boundary layer thickness during the oscillation cycle, the more effective the boundary layer energisation and the more likely that trailing edge separation and large variations in aerodynamic loads can be prevented. Rectangular vanes proved the best at preventing trailing-edge separation at all pitching frequencies, and were the only VG design to prevent flow separation for all pitching cycles regardless of pitching frequency. This indicates that rectangular vanes overall energise the boundary layer more effectively than triangular vane VGs. Finally, motions of faster pitching frequencies were less sensitive to the choice of VG vane size, since the larger lag between flow and airfoil motion ensured a lower tendency for flow separation and higher tendency for faster reattachment if flow does separate.

Overall, the conclusions of investigations in this paper highlight the importance of designing VGs keeping unsteady flow conditions under consideration. The importance of longer measurement durations spanning numerous pitching cycles to capture the significant variations between cycles is also emphasised. The findings of this paper can serve as a basis for choosing more optimal VG designs to prevent unsteady flow separation for wind turbine blades facing dynamic stall. The presented results also motivate the need for further researching the interaction of streamwise vortices generated by VGs of different geometries with the trailing-edge separation front and the dynamic stall vortex through flow field measurements that can resolve these the complex interactions between the VG vortices and the dynamic stall vortex. Finally, the dataset associated with this paper and the larger experiment is also intended to aid with the validation and development of numerical models for airfoils with VGs undergoing dynamic stall. A deeper understanding of the impact of VGs on the unsteady aerodynamic characteristics of wind turbine blade sections and the underlying flow interactions will help create more accurate numerical models to aid in the optimal design of VGs for modern wind turbines. This will lead to smarter deployment of these flow control devices for improved performance and lifetime of wind turbine blades.

*Data availability.* The data supporting this paper's findings is available in the 4TU.ResearchData repository at <https://doi.org/10.4121/374c2baa-aca1-487e-8463-6ef167569be7>.

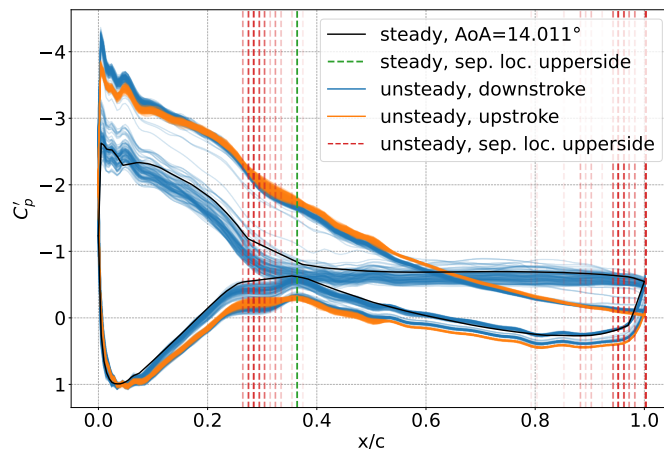
*Author contributions.* **AS:** Conceptualisation, Methodology, Formal Analysis, Writing - Original Draft, **WY:** Writing - Review & Editing, Supervision, **DR:** Writing - Review & Editing, Supervision

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## Appendix A: Determining the flow separation location

The flow separation location is determined by analysing the surface pressure coefficient ( $C_p$ ) distribution along the airfoil chord. As mentioned in Section 2.5 flow is assumed to have separated when the pressure coefficient plateaus over the airfoil surface ( $\frac{dC_p}{dx} \approx 0$ ) and the flow separation location is determined to be the point where this plateau begins. An example of this calculation is shown in Figure A1 for both the steady and unsteady cases at an angle of attack of  $14^\circ$  when the airfoil is equipped with the 5 mm VGs. Both cases are at a chordwise Reynolds number is 1 million and transition to turbulence is fixed with zigzag tape at  $x/c = 0.05$  on both sides of the airfoil. For the unsteady case, the pitching motion is  $10^\circ \pm 10^\circ$  at a frequency of 0.5 Hz corresponding to a reduced frequency of  $k = 0.045$ . The steady flow separation location is  $x/c \approx 0.36$ . As discussed in Section 4.2, the unsteady downstroke cases show two different flow separation locations — either around  $x/c \approx 0.25 - 0.4$ , or around  $x/c > 0.85$  — depending on whether the flow around the airfoil takes the early reattachment or late reattachment path respectively. Note that a separation location of  $x/c = 1.0$  implies that the flow is fully attached over the airfoil surface.



**Figure A1.** Example of determining the flow separation location from the surface pressure coefficient distribution for both steady and unsteady cases at  $\alpha = 14^\circ$ ,  $Re_c = 1$  million with 5 mm VGs and transition fixed at  $x/c = 0.05$  with zigzag tape.

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## List of changes

|     |   |    |
|-----|---|----|
|     | Replaced: for steady stall control . . . . .  | 1  |
| 800 | Replaced: in preventing . . . . .   | 1  |
|     | Added: trailing-edge . . . . .  | 1  |
|     | Added: and dynamic stall during pitch oscillations occurring on inboard and [...] . . . . .         | 1  |
|     | Replaced: delaying stall following trailing-edge separation . . . . .                               | 1  |
|     | Added: achieving . . . . .  | 1  |
| 805 | Replaced: the onset and upstream progression of a trailing-edge separation front . . . . .          | 1  |
|     | Replaced: the onset and upstream progression of the trailing-edge separation front . . . . .        | 1  |
|     | Replaced: trailing-edge flow separation . . . . .   | 1  |
|     | Replaced: more effective boundary layer energisation . . . . .                                      | 1  |
|     | Replaced: , thus . . . . .  | 1  |
| 810 | Replaced: were . . . . .  | 2  |
|     | Replaced: pitch oscillations, McCroskey et al. (1981) list three kinds of stall bas [...] . . . . . | 2  |
|     | Added: s . . . . .  | 2  |
|     | Added: s . . . . .  | 3  |
|     | Replaced: energising . . . . .  | 3  |
| 815 | Added: . . . . .  | 3  |
|     | Replaced: to . . . . .  | 3  |
|     | Added: - . . . . .  | 3  |
|     | Deleted: s . . . . .  | 3  |
|     | Replaced: attack . . . . .  | 4  |
| 820 | Added: Previous steady measurements (Baldacchino et al., 2018) tested VGs [...] . . . . .           | 5  |
|     | Replaced: To simplify the test matrix by fixing the VG placement location, all . . . . .            | 5  |
|     | Added: (with VG array 3 mounted) . . . . .  | 6  |
|     | Added: the most effective location of . . . . .   | 6  |
|     | Deleted: -wise location . . . . .   | 6  |
| 825 | Added: (approximately 8% of the model span) . . . . .   | 6  |
|     | Added: (as illustrated in Figure 1a) . . . . .  | 6  |
|     | Added: Thus, the VGs cover around 84% of the airfoil model span. . . . .                            | 6  |
|     | Replaced: measurements . . . . .  | 6  |
|     | Added: The pressure ports are located between approximately 20% to 25% of [...] . . . . .           | 8  |
| 830 | Deleted: , reaching a chordwise position slightly upstream of 40% chord at the [...] . . . . .      | 11 |
|     | Added: The airfoil stalls when the separation front reaches slightly upstream [...] . . . . .       | 11 |

|     |   |    |
|-----|---|----|
|     | Deleted: The steady measurements indicate that rectangular vanes whose height [...]                   | 12 |
|     | Added: The steady measurements indicate that rectangular vanes whose height [...]                     | 12 |
|     | Deleted: For the dynamic cases, we use the normal force coefficient polar and [...]                   | 13 |
| 835 | Added: For the dynamic cases, we use the normal force coefficient polar and [...]                     | 13 |
|     | Deleted: The unsteady motion of the airfoil causes the flow around the airfoil to [...]               | 14 |
|     | Added: The unsteady motion of the airfoil causes the flow around the airfoil to [...]                 | 14 |
|     | Added: For higher pitching frequencies, the faster pitch rate causes a further [...]                  | 14 |
|     | Deleted: , with only a slight increase in the maximum normal force coefficient [...]                  | 15 |
| 840 | Added: For the slowest pitching frequency $k = 0.045$ , trailing-edge separation [...]                | 16 |
|     | Deleted: The larger 5 mm VGs ( $h_{VG}/\delta \approx 1$ at AoA $0^\circ$ ) and 10 mm VGs [...]       | 16 |
|     | Deleted: In the downstroke half of the pitching motion, the normal force coeffi [...]                 | 16 |
|     | Added: The larger 5 mm VGs ( $h_{VG}/\delta \approx 1$ at AoA $0^\circ$ ) energise the boundary [...] | 17 |
|     | Deleted: The larger 10 mm VGs shed stronger vortices that prevent flow separa [...]                   | 17 |
| 845 | Added: With the largest 10 mm VGs ( $h_{VG}/\delta > 1$ at AoA $0^\circ$ ), trailing-edge [...]       | 17 |
|     | Replaced: more effective energisation of the airfoil boundary layer                                   | 19 |
|     | Deleted: generate stronger streamwise vortices that   | 20 |
|     | Deleted: To quantify the ability of the different VGs to keep flow attached, we [...]                 | 20 |
|     | Added: The existence of different paths in the normal force coefficient polar [...]                   | 21 |
| 850 | Replaced: separated   | 21 |
|     | Deleted: As mentioned in Section 1, past studies have assumed that an optimal [...]                   | 22 |
|     | Deleted: At higher frequencies, both the 5 mm and 10 mm VGs tend towards a [...]                      | 22 |
|     | Added: In Section 4.2, we observed that the 2.5 mm VGs only energise the [...]                        | 22 |
|     | Added: Based on the expected rate of change in angle of attack on the blade, [...]                    | 23 |
| 855 | Added: To aid wind turbine blade designers in selecting a suitable vane height [...]                  | 23 |
|     | Added: range of   | 23 |
|     | Added: steady   | 23 |
|     | Replaced: triangular  | 23 |
|     | Deleted: are already a better choice than triangular vanes of the same size in [...]                  | 23 |
| 860 | Added: energise the boundary layer more effectively than triangular vane VGs [...]                    | 23 |
|     | Replaced: are   | 23 |
|     | Deleted: The slower upstream movement of the trailing edge flow separation [...]                      | 24 |
|     | Replaced: energise the boundary layer more effectively  | 24 |
|     | Replaced: Combining the results from the VG vane height and vane shape comp [...]                     | 24 |
| 865 | Added: Sources of uncertainty   | 24 |
|     | Added: One of the central recommendations of this paper is that VGs selected [...]                    | 24 |

|     |   |    |
|-----|---|----|
|     | Added: Some other uncertainties in the data arise from the measurement setup [...]      | 25 |
|     | Replaced: by showing that VGs that prevent steady flow separation can still allow [...] | 25 |
|     | Replaced: pitch   | 25 |
| 870 | Replaced: above and below   | 25 |
|     | Replaced: angle of attack   | 25 |
|     | Added: where VGs are used   | 25 |
|     | Added: The VGs were fixed at 30% chordwise location to simplify the test [...]          | 25 |
|     | Replaced: have been   | 25 |
| 875 | Deleted: In steady conditions, the rectangular vane VGs of the largest vane size [...]  | 25 |
|     | Added: In steady conditions, triangular vane VGs followed the expected trend [...]      | 26 |
|     | Deleted: When pitching, the baseline airfoil without VGs encounters dynamic [...]       | 26 |
|     | Deleted: In unsteady cases too, rectangular vanes of equal height performed be [...]    | 26 |
|     | Added: When pitching, only VGs whose vane height exceeds the local bound [...]          | 27 |
| 880 | Replaced: conclusions of  | 27 |
|     | Added: the trailing-edge separation front and   | 27 |
|     | Deleted: d  | 27 |
|     | Replaced: these   | 27 |
|     | Deleted: between the VG vortices and the dynamic stall vortex                           | 27 |